

Physics 30 – Lesson 7

Optics – Curved Mirrors

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Practice problems

1) $h_o = 5.0\text{cm}$
 $d_o = 14\text{cm}$
 $R = 10\text{cm} \rightarrow f = 5\text{cm}$

a) $\frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o}$
 $\frac{1}{d_i} = \frac{1}{5\text{cm}} - \frac{1}{14\text{cm}}$
 $\frac{1}{d_i} = 0.129$
 $d_i = 7.78\text{cm}$

b) inverted, real, smaller

c) $\frac{h_i}{h_o} = \frac{-d_i}{d_o}$
 $h_i = \frac{-(7.78\text{cm})(5.0\text{cm})}{14\text{cm}}$
 $h_i = -2.78\text{cm}$

2) $h_o = 5.0\text{cm}$
 $d_o = 14\text{cm}$
 $R = -10\text{cm} \rightarrow f = -5\text{cm}$

Note that f is $(-)$ for a diverging/convex mirror

a) $\frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o}$
 $\frac{1}{d_i} = \frac{1}{-5\text{cm}} - \frac{1}{14\text{cm}}$
 $\frac{1}{d_i} = -0.271$
 $d_i = -3.68\text{cm}$

b) inverted, real, smaller

c) $\frac{h_i}{h_o} = \frac{-d_i}{d_o}$
 $h_i = \frac{-(-3.68\text{cm})(5.0\text{cm})}{14\text{cm}}$
 $h_i = 1.32\text{cm}$

3) $m = -0.25$
 $d_o = 30\text{cm}$

a) The only mirror that can produce an inverted (i.e. real) image is a **converging** or **concave** mirror. In addition, note that the focal length calculation below yields a positive answer (i.e. converging mirror).

b) $m = \frac{h_i}{h_o} = \frac{-d_i}{d_o}$
 $-0.25 = \frac{-d_i}{30\text{cm}}$
 $d_i = 7.5\text{cm}$

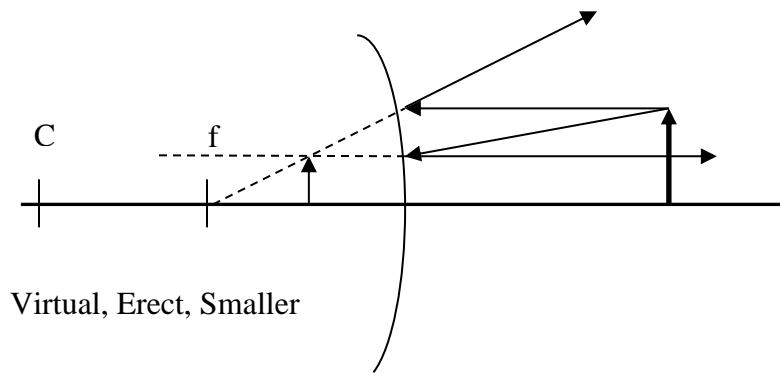
$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$
 $\frac{1}{f} = \frac{1}{7.5\text{cm}} + \frac{1}{30\text{cm}}$
 $\frac{1}{f} = 0.167$
 $f = 6.0\text{cm}$

Assignment

1)

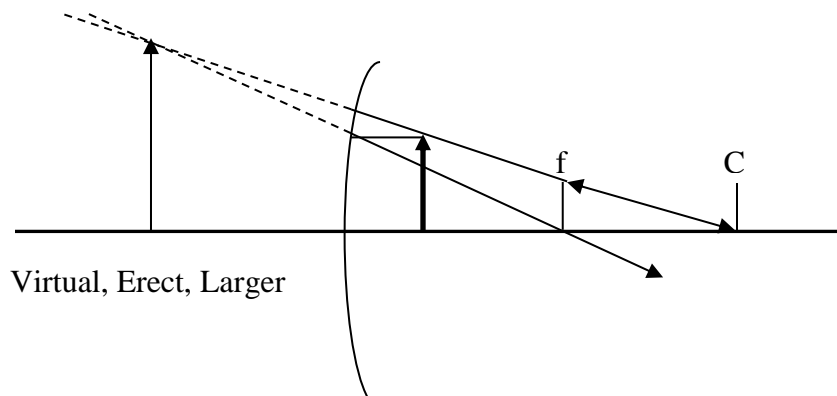
A)

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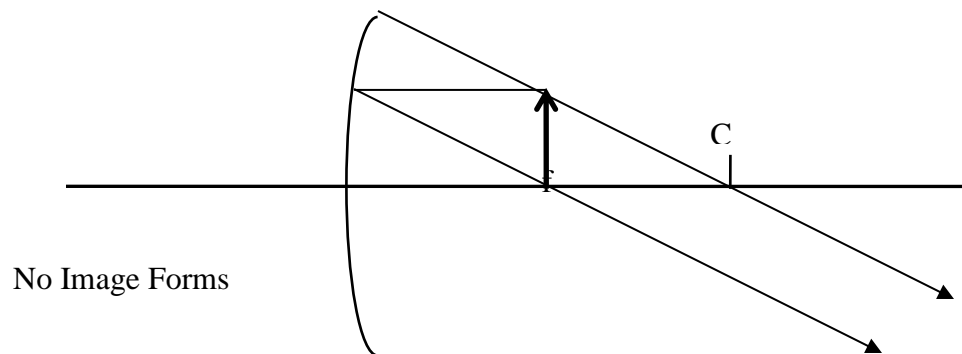
B)

/2



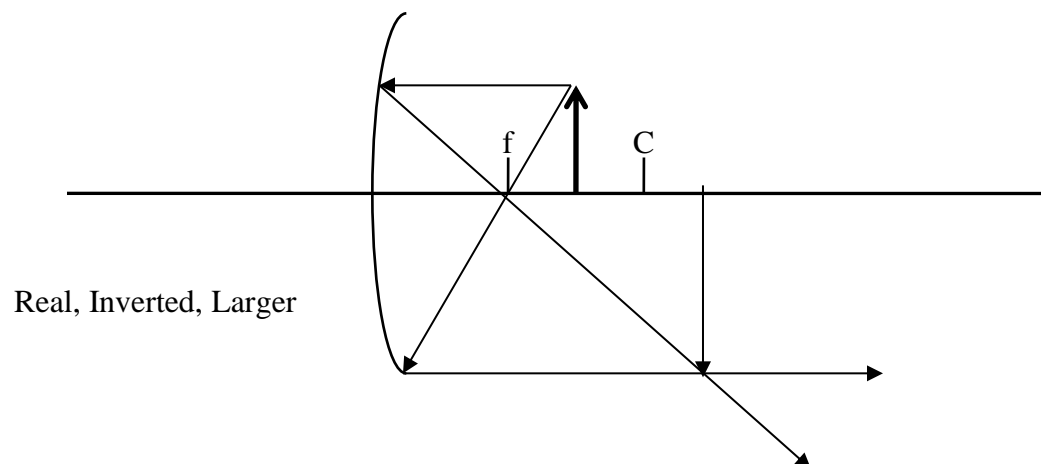
C)

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D)

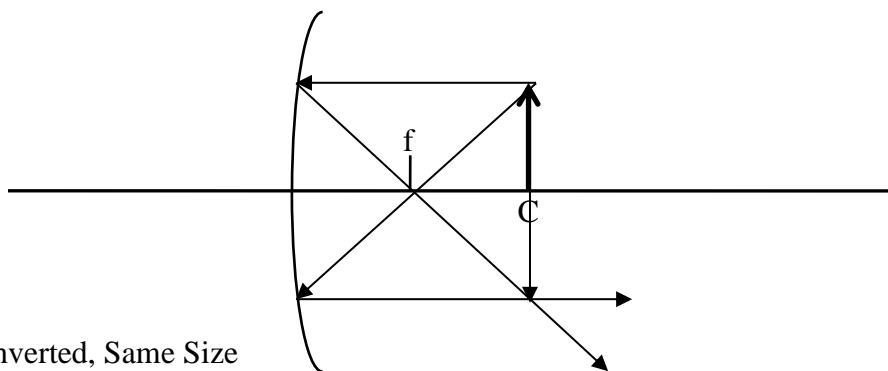
/2



E)

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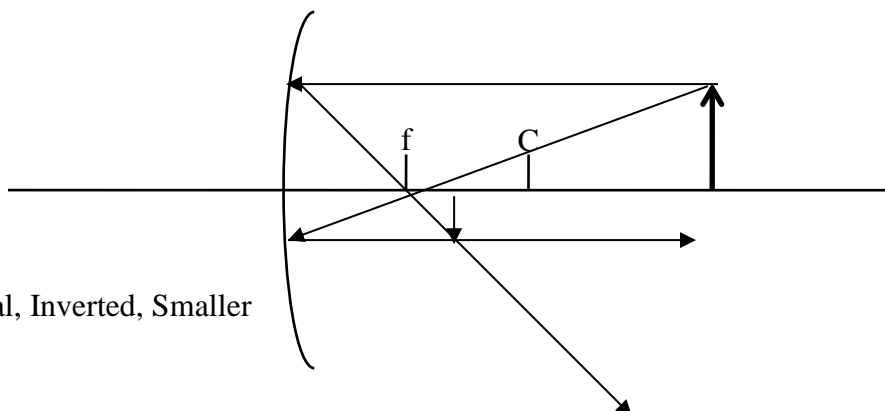
Real, Inverted, Same Size



F)

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Real, Inverted, Smaller



2)

$$h_o = 6.0\text{cm}$$

$$d_o = 40\text{cm}$$

$$R = 60\text{cm} \rightarrow f = 30\text{cm}$$

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$$\text{a) } \frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o}$$

$$\frac{1}{d_i} = \frac{1}{30\text{cm}} - \frac{1}{40\text{cm}}$$

$$\boxed{d_i = 120\text{cm}}$$

c) inverted, real, larger

$$\text{b) } \frac{h_i}{h_o} = \frac{-d_i}{d_o}$$

$$h_i = \frac{-(120\text{cm})(6.0\text{cm})}{40\text{cm}}$$

$$\boxed{h = -18\text{cm}}$$

3)

$$h_o = 6.0\text{cm}$$

$$d_o = 40\text{cm}$$

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$$R = -60\text{cm} \rightarrow f = -30\text{cm}$$

$$\text{a) } \frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o}$$

$$\frac{1}{d_i} = \frac{1}{-30\text{cm}} - \frac{1}{40\text{cm}}$$

$$\boxed{d_i = -17\text{cm}}$$

c) erect, virtual, smaller

$$\text{b) } h_i = \frac{-d_i h_o}{d_o}$$

$$h_i = \frac{-(-17\text{cm})(6.0\text{cm})}{40\text{cm}}$$

$$\boxed{h = 2.66\text{cm}}$$

4)

$$d_o = 40\text{cm}$$

$$d_i = -80\text{cm}$$

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erect \therefore virtual $\therefore (-)$

a)

b) concave (f is positive)

$$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$$

$$\frac{1}{f} = \frac{-1}{80\text{cm}} + \frac{1}{40\text{cm}}$$

$$f = 80\text{cm}$$

$$R = 2f = 2 \times 80\text{cm}$$

$$\boxed{R = 160\text{cm}}$$

5)

$$d_o = 40\text{cm}$$

$$d_i = +120\text{cm}$$

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inverted \therefore virtual $\therefore (+)$

a)

b) concave (f is positive)

$$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$$

$$\frac{1}{f} = \frac{1}{120\text{cm}} + \frac{1}{40\text{cm}}$$

$$f = 30\text{cm}$$

$$R = 2f = 2 \times 30\text{cm}$$

$$\boxed{R = 60\text{cm}}$$

6)

$$d_o = 40\text{cm}$$

$$d_i = -20\text{cm}$$

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erect $\therefore (-)$

a)

b) convex (f is negative)

$$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$$

$$\frac{1}{f} = \frac{1}{-20\text{cm}} + \frac{1}{40\text{cm}}$$

$$f = -40\text{cm}$$

$$R = 2f = 2 \times (-40\text{cm})$$

$$\boxed{R = -80\text{cm}}$$

7) $h_o = 20\text{cm}$
 $d_o = 30\text{cm}$
 $h_i = +10$
erect $\therefore (+)$

/8 $d_o = 30\text{cm} + 60\text{cm} = 90\text{cm}$

a. $\frac{-d_i}{d_o} = \frac{h_i}{h_o}$
 $d_i = \frac{-h_i d_o}{h_o}$
 $d_i = \frac{-10\text{cm}(30\text{cm})}{20\text{cm}}$
 $d_i = -15\text{cm}$

b. $\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$
 $\frac{1}{f} = \frac{-1}{15\text{cm}} + \frac{1}{30\text{cm}}$
 $f = -30\text{cm}$

c. $\frac{1}{d_i} = \frac{1}{f} - \frac{1}{d_o}$
 $\frac{1}{d_o} = \frac{-1}{30\text{cm}} - \frac{1}{90\text{cm}}$
 $d_i = -22.5\text{cm}$

d. $h_i = \frac{-d_i h_o}{d_o}$
 $h_i = \frac{-(-22.5\text{cm})(20\text{cm})}{90\text{cm}}$
 $h_i = 5.0\text{cm}$

8) $R = 80\text{cm} \rightarrow f = 40\text{cm}$
 $h_i = -3h_o \rightarrow d_i = 3d_o$
 d_i is positive because it is
inverted / real

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$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$
 $\frac{1}{40\text{cm}} = \frac{1}{3d_o} + \frac{1}{d_o}$
 $\frac{1}{40\text{cm}} = \frac{1}{3d_o} + \frac{3}{3d_o}$
 $\frac{1}{40\text{cm}} = \frac{4}{3d_o}$
 $3d_o = 160\text{cm}$
 $d_o = \frac{160\text{cm}}{3}$
 $d_o = 53\text{cm}$

9) $R = 180\text{cm} \rightarrow f = 90\text{cm}$
 $h_i = +2h_o \rightarrow d_i = -2d_o$
 d_i is negative because it is
erect / virtual

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$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$
 $\frac{1}{90\text{cm}} = \frac{1}{-2d_o} + \frac{1}{d_o}$
 $\frac{1}{90\text{cm}} = \frac{-1}{2d_o} + \frac{2}{2d_o}$
 $\frac{1}{90\text{cm}} = \frac{1}{2d_o}$
 $2d_o = 90\text{cm}$
 $d_o = \frac{90\text{cm}}{2}$
 $d_o = 45\text{cm}$

10)

$$f = -60cm$$

(-) because convex mirror

$$\frac{1}{f} = \frac{1}{d_i} + \frac{1}{d_o}$$

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$$h_i = \frac{h_o}{6} \rightarrow d_i = \frac{-d_o}{6}$$

(-) because virtual

$$\frac{-1}{60cm} = \frac{-1}{\frac{d_o}{6}} + \frac{1}{d_o}$$

$$\frac{-1}{60cm} = \frac{-6}{d_o} + \frac{1}{d_o}$$

$$\frac{-1}{60cm} = \frac{-5}{d_o}$$

$$-d_o = -5(60cm)$$

$$\boxed{d_o = 300cm}$$