Chemistry 20 – Lesson 26 pH and pOH

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1.
$$\left[H_{(aq)}^{+}\right] \times \left[OH_{(aq)}^{-}\right] = K_{w}$$

$$\left[OH_{(aq)}^{-}\right] = \frac{K_{w}}{\left[H_{(aq)}^{+}\right]}$$

$$\left[OH_{(aq)}^{-}\right] = \frac{1.0 \times 10^{-14} \, (m_{(aq)})^{-3} \, r_{(aq)}^{-3}}{4.40 \times 10^{-3} \, r_{(aq)}^{-3}}$$

$$\begin{bmatrix}
OH_{(aq)}^{-} \end{bmatrix} = \frac{1.0 \times 10^{-14} \text{ (mol/L)}^{2}}{4.40 \times 10^{-3} \text{ mol/L}}$$

$$\begin{bmatrix}
OH_{(aq)}^{-} \end{bmatrix} = 2.27 \times 10^{-12} \text{ mol/L}$$

3.
$$n_{HCI} = \frac{0.37 \text{ g}}{36.46 \frac{\text{g}}{\text{mol}}} = 0.010148 \text{mol}$$
$$\left[HCl_{(aq)} \right] = \frac{0.010148 \text{mol}}{0.250 \text{ L}} = 0.040592 \frac{\text{mol}}{\text{L}}$$

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$$HCl_{(aq)} \xrightarrow{100\%} H^{+}_{(aq)} + Cl^{-}_{(aq)}$$

$$\left[H^{+}_{(aq)}\right] = \left[HCl_{(aq)}\right] = 0.040592 \, \frac{\text{mol}}{L}$$

$$\begin{array}{c} Ca(OH)_{2(aq)} \longrightarrow Ca_{(aq)}^{2+} + 2OH_{(aq)}^{-} \\ \\ \left[OH_{(aq)}^{-}\right] = 2 \times \left[Ca(OH)_{2(aq)}\right] \\ \\ \left[OH_{(aq)}^{-}\right] = 2 \times \left[6.9 \times 10^{-3} \text{ mol/L}\right] \\ \\ \left[OH_{(aq)}^{-}\right] = 1.38 \times 10^{-2} \text{ mol/L} \end{array}$$

$$\begin{split} & \left[H_{(aq)}^{+} \right] \times \left[OH_{(aq)}^{-} \right] = K_{w} \\ & \left[OH_{(aq)}^{-} \right] = \frac{K_{w}}{\left[H_{(aq)}^{+} \right]} \\ & \left[OH_{(aq)}^{-} \right] = \frac{1.0 \times 10^{-14} \, \binom{\text{mol}}{\text{L}}^{2}}{0.040592 \, \frac{\text{mol}}{\text{L}}} \\ & \left[OH_{(aq)}^{-} \right] = 2.46 \times 10^{-13} \, \frac{\text{mol}}{\text{L}} \end{split}$$

$$\begin{split} & \left[H_{(aq)}^{+} \right] \times \left[OH_{(aq)}^{-} \right] = K_{w} \\ & \left[H_{(aq)}^{+} \right] = \frac{K_{w}}{\left[OH_{(aq)}^{-} \right]} \\ & \left[H_{(aq)}^{+} \right] = \frac{1.0 \times 10^{-14} \, \binom{\text{mol/L}}{2}}{1.38 \times 10^{-2} \, \frac{\text{mol/L}}{2}} \\ & \left[H_{(aq)}^{+} \right] = 7.25 \times 10^{-13} \, \frac{\text{mol/L}}{2} \end{split}$$

4.

$$n_{KOH} = \frac{20.0 \,\mathrm{g}}{56.11^{\mathrm{g}}/_{\mathrm{mol}}} = 0.35644 \,\mathrm{mol}$$
$$\left[KOH_{(aq)} \right] = \frac{0.35644 \,\mathrm{mol}}{0.500 L} = 0.7128854 \,\mathrm{mol}/_{L}$$

$$\begin{bmatrix} H_{(aq)}^{+} \end{bmatrix} \times \begin{bmatrix} OH_{(aq)}^{-} \end{bmatrix} = K_{w}$$

$$\begin{bmatrix} H_{(aq)}^{+} \end{bmatrix} = \frac{K_{w}}{\begin{bmatrix} OH_{(aq)}^{-} \end{bmatrix}}$$

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$$KOH_{(s)} \longrightarrow K_{(aq)}^{+} + OH_{(aq)}^{-}$$

$$\left[OH_{(aq)}^{-} \right] = \left[KOH_{(aq)} \right] = 0.7128854 \, \text{mol/L}$$

$$\left[H_{(aq)}^{+}\right] = \frac{1.0 \times 10^{-14} \, \binom{\text{mol}_{L}}{2}}{0.7128854 \, \frac{\text{mol}_{L}}{2}}$$

$$\boxed{ \left[H_{\rm (aq)}^+ \right] \! = \! 1.403 \! \times \! 10^{-14} \, \frac{\text{mol}}{\text{L}} }$$

6.

(a)

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Food	$\begin{matrix} [\mathbf{H}^+_{(\mathbf{aq})}] \\ (\mathbf{mol/L}) \end{matrix}$	[OH ⁻ (aq)] (mol/L)	pН	рОН
oranges	5.5×10^{-3}	1.8×10^{-12}	2.26	11.74
asparagus	4×10^{-9}	3×10^{-6}	8.4	5.6
olives	5.0×10^{-4}	2.0×10^{-11}	3.30	10.70
blackberries	4.0×10^{-4}	2.5×10^{-11}	3.40	10.60

(b) Oranges would taste most sour.

$$n_{\text{NaOH}} = \frac{26\,\text{g}}{40.00\,\text{g}_{\text{mol}}^{\text{g}}} = 0.65\text{mol}$$

$$[NaOH_{(aq)}] = \frac{0.65mol}{0.150L} = 4.33 \frac{mol}{L}$$

$$pOH = -\log[OH^{-}]$$

$$pOH = -log[4.33\,\text{mol}/\text{L}]$$

$$pOH = -0.64$$

Note that negative values for pH and pOH are possible. Further, a negative pH or pOH indicates a very concentrated acidic or basic solution.

$$NaOH_{(s)} \longrightarrow Na_{(aq)} + OH_{(aq)}$$

 $OH_{(aq)} = NaOH_{(aq)} = 4.33 \,\text{mol/L}$

$$pH + pOH = 14$$

$$pH = 14 - pOH = 14 - (-0.64)$$

$$pH = 14.64$$

$$pH + pOH = 14$$

$$pOH = 14 - pH = 14 - (11.50)$$

$$pOH = 2.50$$

$$n_{KOH} = 3.2 \times 10^{-3} \text{ mol/L} (0.500 \text{L})$$

$$n_{you} = 1.6 \times 10^{-3} \text{ mol}$$

$$[OH_{(aq)}^{-}] = 10^{-pOH}$$

$$[OH_{(aq)}^{-}] = 10^{-2.50}$$

$$[OH_{(aq)}^{-}] = 3.2 \times 10^{-3} \text{ mol/L}$$

$$n_{KOH} = 3.2 \times 10^{-3} \text{ mol/L} (0.500 L)$$

$$n_{KOH} = 1.6 \times 10^{-3} \text{ mol}$$

$$m_{KOH} = 1.6 \times 10^{-3} \, mol(56.11 \, {}_{mol}^{g})$$

$$m_{KOH} = 0.089 \, g$$

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(a) neutral?
$$[\mathbf{H}^+] = [\mathbf{OH}^-]$$

(b) acidic?
$$[\mathbf{H}^+] > [\mathbf{OH}^-]$$

(c) basic?
$$[\mathbf{H}^+] < [\mathbf{OH}^-]$$

10.

$$\begin{bmatrix} H_{(aq)}^{+} \end{bmatrix} = \frac{K_{w}}{\begin{bmatrix} OH_{(aq)}^{-} \end{bmatrix}}$$

$$[H_{(aq)}^{+}] = \frac{1.0 \times 10^{-14} (\frac{mol}{L})^{2}}{2.5 \times 10^{-7} \frac{mol}{L}}$$

$$\begin{bmatrix} H_{(aq)}^{+} \end{bmatrix} = 4.0 \times 10^{-8} \frac{mol}{L}$$

$$pH = -\log[H^+]$$

$$pH = -log[4.0 \times 10^{-8} \text{ mol/L}]$$

$$\boxed{pH = 7.40}$$

$$pH = 7.40$$

11.

$$[H_{(aq)}^+] = 10^{-pH}$$

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 $[H_{(aq)}^+] = 10^{-5.6}$

$$\label{eq:Hamiltonian} \boxed{ \left[H_{(aq)}^+ \right] = 2.5 \times 10^{-6} \; \frac{\text{mol}}{\text{L}} }$$

12.

/2If the pH decreases by 1, the concentration has increased by a factor of 10. Therefore, a change of 3 pH units is equivalent to a 1000 fold change in concentration.

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$$[H_{(aq)}^+] = 10^{-pH}$$

 $[H_{(aq)}^+] = 10^{-1.57}$

$$[H^{+}] = 2.7 \times 10^{-2} \text{ mol}$$

$$[H_{(aq)}^+] = 2.7 \times 10^{-2} \text{ mol/L}$$

$$n_{HCl} = 2.7 \times 10^{-2} \frac{\text{mol}}{L} (0.250 L)$$

$$n_{HCl} = 0.0067288 mol$$

 $m_{HCl} = 0.0067288 mol(36.46 \, {}^g\!\!/_{mol})$

$$m_{\rm HCl} = 0.25\,g$$

14.

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$$n_{\text{CH}_3\text{COOH}} = \frac{60.0 \,\text{kg}}{60.06 \,\text{g/mol}} = 0.999 \,\text{kmol}$$

$$0.999 \,\text{kmol} = 0.7002 \,\text{rel}$$

$$\[HCl_{(aq)}\] = \frac{0.999 \, kmol}{1.25 \, kL} = 0.7992 \, \frac{mol}{L}$$

$$pH = -\log[H^+]$$

$$pH = -\log[0.0103896 \, \frac{\text{mol}}{1}]$$

$$pH = 1.98$$

$$CH_3COOH_{(aq)} \xrightarrow{\quad 1.3\% \quad} H_{(aq)}^+ \quad + \quad CH_3COO_{(aq)}^-$$

$$\left[H_{(aq)}^{+} \right] = 0.013 \left[0.7992 \right] = 0.0103896 \, \text{mol}_{L}^{\prime}$$

$$pH + pOH = 14$$

$$pOH = 14 - pH = 14 - 1.98$$

$$pOH = 12.02$$

15.
$$pH + pOH = 14$$
$$pOH = 14 - pH = 14 - 10.35$$
$$pOH = 3.65$$

$$\begin{split} &n_{NaOH}^{} = 2.24 \! \times \! 10^{-4} \, \text{mol/}_{L}^{}(2.00 L) \\ &n_{NaOH}^{} = 4.48 \! \times \! 10^{-4} \, \text{mol} \end{split}$$

$$\begin{split} & [OH^-_{(aq)}] = 10^{-pOH} \\ & [OH^-_{(aq)}] = 10^{-3.65} \\ & [OH^-_{(aq)}] = 2.24 \times 10^{-4} \ \text{mol/L} \end{split}$$

$$m_{NaOH} = 4.48 \times 10^{-4} \, mol(40.00 \, g_{mol}^{g})$$

$$\boxed{m_{\text{NaOH}} = 0.018\,\text{g}}$$