# Package 'MPCR'

November 26, 2023

Type Package

Title Multi Precision Computing
Version 1.0
<b>Date</b> 2023-11-12
<b>Author</b> David Helmy [aut, cph], Sameh Abdulah [cre, cph], KAUST King Abdullah University of Science and Technology [fnd, cph], Brightskies [cph]
Maintainer Sameh Abdulah <sameh.abdulah@kaust.edu.sa></sameh.abdulah@kaust.edu.sa>
<b>Description</b> Provides new data-structure support for multi- and mixed-precision for R users. The package supports 16-bit, 32-bit, and 64-bit operations. To the best of our knowledge, 'MPCR' differs from the currently available packages in the following: 'MPCR' introduces a new data structure that supports three different precisions (16-bit, 32-bit, and 64-bit), allowing for optimized memory allocation based on the desired precision. This feature offers significant advantages in-memory optimization. 'MPCR' extends support to all basic linear algebra methods across different precisions. 'MPCR' maintains a consistent interface with normal R functions, allowing for seamless code integration and a user-friendly experience.
License GPL (>= 3)
Imports methods, Rcpp (>= 1.0.9)
<b>Depends</b> R (>= 3.6.0)
RoxygenNote 7.2.3
SystemRequirements CMake (>=3.20), C++ (>= 11)
NeedsCompilation yes
OS_type unix
<pre>URL https://github.com/stsds/MPCR</pre>
R topics documented:
01-MPCR       2         02-Converters       4         03-Arithmetic       5         04-Comparison       6         05-Copy       7
1

2 01-MPCR

n_1_1	MPCR MPCR S4 Class	
Index		36
	39-MPCR TRSM	. 34
	38-MPCR GEMM	
	37-Back/Forward solve	
	36-Singular value decomposition	
	35-Solve	
	34-Reciprocal condition	
	33-QR decomposition	
	32-Norm	. 28
	31-Symmetric	. 27
	30-Eigen decomposition	
	29-Crossprod	
	28-Cholesky inverse	
	27-Cholesky decomposition	
	26-Print	
	25-Metadata	
	24-Check precision	
	23-Transpose	
	22-Hyperbolic	
	21-Trig	
	20-Special Math	
	19-Sweep	
	18-Scale	
	17-Round	
	16-Replicate	
	15-NA's	
	14-Miscmath	
	13-Mathis	
	12-Log	
	11-Extremes	
	10-Diagonal	
	09-Bind	
	08-Concatenate	
	07-Extract-Replace	
	06-Dimensions	. 8

# Description

MPCR is a multi-precision vector/matrix, that enables the creation of vector/matrix with three different precisions (16-bit (half), 32-bit(single), and 64-bit(double)).

# Value

MPCR object (constructor - accessors - methods)

01-MPCR 3

#### Constructor

```
new Creates a new instance of zero values of the MPCR class. new (MPCR, size, "precision") size The total number of values for which memory needs to be allocated.

precision String to indicate the precision of MPCR object ("half", "single", or "double").
```

#### Accessors

The following accessors can be used to get the values of the slots:

```
IsMatrix Boolean to indicate whether the MPCR object is a vector or matrix.
```

Size Total number of elements inside the object, (row\*col) in the case of matrix, and number of elements in the case of vector.

Row Number of rows.

Col Number of cols.

#### Methods

The following methods are available for objects of class MPCR:

**PrintValues:** PrintValues (): Prints all the values stored in the matrix or vector, along with metadata about the object.

**ToMatrix:** ToMatrix (row, col): Changes the object representation to match the new dimensions, no memory overhead.

**ToVector:** ToVector(): Changes the MPCR matrix to vector, no memory overhead.

```
# Example usage of the class and its methods
library(MPCR)
MPCR_object <- new(MPCR,50,"single")

MPCR_object$ToMatrix(5,10)
MPCR_object$Row #5
MPCR_object$Col #10
MPCR_object$Size #50
MPCR_object$IsMatrix #TRUE

MPCR_object$PrintValues()
MPCR_object$ToVector()</pre>
```

4 02-Converters

02-Converters

Converters

#### **Description**

Converters from R to MPCR objects and vice-versa.

#### Value

An MPCR or R numeric vector/matrix.

#### **MPCR Converter**

Convert R object to MPCR object.

#### **MPCR** converters:

```
as.MPCR(data, nrow = 0, ncol = 0, precision): Converts R object to MPCR object.
```

data R matrix/vector.

nrow Number of rows of the new MPCR matrix, **default = zero** which means a vector will be created.

ncol Number of cols of the new MPCR matrix, **default = zero** which means a vector will be created.

precision String indicates the precision of the new MPCR object (half, single, or double).

#### **R** Converter

Convert an MPCR object to R object.

#### R vector converter:

 ${\tt MPCR.ToNumericVector}\,({\tt x}): Converts \ an \ MPCR \ object \ to \ a \ numeric \ R \ vector.$ 

x MPCR object.

#### R matrix converter:

MPCR.ToNumericMatrix(x): Converts an MPCR object to a numeric R matrix.

x MPCR object.

```
# Example usage of the class and its methods
library(MPCR)
a <- matrix(1:36, 6, 6)
MPCR_matrix <- as.MPCR(a,nrow=6,ncol=6,precision="single")
r_vector <- MPCR.ToNumericVector(MPCR_matrix)
r_vector
r_matrix <- MPCR.ToNumericMatrix(MPCR_matrix)
r_matrix</pre>
```

03-Arithmetic 5

03-Arithmetic

Binary arithmetic numeric/MPCR objects.

## **Description**

Binary arithmetic for numeric/MPCR objects.

## Usage

```
## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 + e2

## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 - e2

## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 * e2

## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 / e2

## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 ^ e2

## S4 method for signature 'Rcpp_MPCR,Rcpp_MPCR'
e1 ^ e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 + e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 * e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 - e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 / e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 / e2

## S4 method for signature 'Rcpp_MPCR,BaseLinAlg'
e1 / e2
```

#### **Arguments**

e1, e2 Numeric/MPCR objects.

#### Value

An MPCR object, matching the data type of the highest precision input.

6 04-Comparison

#### **Examples**

```
library(MPCR)
s1 <- as.MPCR(1:20,nrow=2,ncol=10,"single")
s2 <- as.MPCR(21:40,nrow=2,ncol=10,"double")

x <- s1 + s2
typeof(x) # A 64-bit precision (double) MPCR matrix.

s3 <- as.MPCR(1:20,nrow=2,ncol=10,"single")
x <- s1 + s3
typeof(x) # A 32-bit precision (single) MPCR matrix.</pre>
```

04-Comparison

Binary comparison operators for numeric/MPCR objects.

# Description

Binary comparison operators for numeric/MPCR objects.

#### Usage

```
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 < e2
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 <= e2
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 == e2
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 != e2
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 > e2
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
e1 >= e2
## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
e1 < e2
## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
e1 == e2
```

05-Copy 7

```
## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
e1 != e2

## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
e1 > e2

## S4 method for signature 'Rcpp_MPCR, BaseLinAlg'
e1 >= e2
```

#### **Arguments**

e1, e2 Numeric/MPCR objects.

#### Value

A vector/matrix of logicals.

## **Examples**

```
library(MPCR)
s1 <- as.MPCR(1:20,nrow=2,ncol=10,"single")
s2 <- as.MPCR(21:40,nrow=2,ncol=10,"double")
x <- s1 > s2
```

05-Copy

copy

# Description

Functions for copying MPCR objects.

#### Value

An MPCR copy from the input object.

# MPCR deep copy

Create a copy of an MPCR object. Typically, using 'equal' creates a new pointer for the object, resulting in any modifications made to object one affecting object two as well.

#### copy

```
\label{eq:mpcr} \begin{split} & \texttt{MPCR.copy}\,(\texttt{x}) : \textbf{Create a new copy of an MPCR object.} \\ & \texttt{x MPCR object.} \end{split}
```

8 06-Dimensions

## **Examples**

```
library (MPCR)
# Example usage of the class and its methods
a <- matrix(1:36, 6, 6)
MPCR_matrix <- as.MPCR(a,nrow=6,ncol=6,precision="single")</pre>
# Normal equal '=' will create a new pointer of the object, so any change in object A
# will affect object B
temp_MPCR_matrix = MPCR_matrix
temp_MPCR_matrix[2,2] <- 500</pre>
MPCR_matrix[2,2]
MPCR_matrix_copy <- MPCR.copy(MPCR_matrix)</pre>
MPCR_matrix[2,2] < -100
MPCR_matrix_copy[2,2] <- 200
MPCR_matrix[2,2]
                            #100
MPCR_matrix_copy[2,2]
                            #200
```

06-Dimensions

dimensions

## **Description**

Returns the number of rows or cols in an MPCR object.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
nrow(x)

## S4 method for signature 'Rcpp_MPCR'
ncol(x)
```

#### Arguments

X

An MPCR object.

## Value

The number of rows/cols in an MPCR object.

07-Extract-Replace 9

#### **Examples**

```
library(MPCR)
x <- as.MPCR(1:16,4,4,"single")
y <- as.MPCR(1:20,4,5,"double")
rows_x <- nrow(x)
cols_y <- ncol(y)</pre>
```

07-Extract-Replace Extract or replace elements from an MPCR object.

## **Description**

Extract or replace elements from an MPCR object using the '[', '[[', '[<-', and '[[<-' operators. When extracting values, they will be converted to double precision. However, if you update a single object, the double value will be cast down to match the precision. If the MPCR object is a matrix and you access it using the 'i' index, the operation is assumed to be performed in column-major order, or using 'i' and 'j' index.

#### Usage

```
## S4 method for signature 'Rcpp_MPCR'
x[i, j, drop = TRUE]
  ## S4 replacement method for signature 'Rcpp_MPCR'
x[i, j, ...] <- value
  ## S4 method for signature 'Rcpp_MPCR'
x[i, drop = TRUE]]
  ## S4 replacement method for signature 'Rcpp_MPCR'
x[i, ...]] <- value</pre>
```

#### **Arguments**

```
x An MPCR object.
i Row index or indices.
j Column index or indices.
... ignored.
drop ignored.
value A value to replace the selected elements with.
```

```
library(MPCR)
  x <-as.MPCR(1:50,precision="single")
  ext <- x[5]
  x[5] <- 0
  x$ToMatrix(5,10)
  x[2,5]
  x[3,5] <- 100</pre>
```

10 *09-Bind* 

08-Concatenate

concatenate

#### **Description**

c () function for MPCR objects.

#### Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.Concatenate(x)
```

#### **Arguments**

Х

List of MPCR objects.

#### Value

MPCR object containing values from all objects in the list.

# **Examples**

```
library(MPCR)
x <- as.MPCR(1:20,precision="single")
y <- as.MPCR(1:20,precision="single")
list <- c(x,y)
new_obj <- MPCR.Concatenate(list)</pre>
```

09-Bind

bind

## **Description**

```
rbind() and cbind() for MPCR objects.
```

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.rbind(x,y)

## S4 method for signature 'Rcpp_MPCR'
MPCR.cbind(x,y)
```

# Arguments

```
x An MPCR object.
y An MPCR object.
```

10-Diagonal

# Value

An MPCR object, matching the data type of the highest precision input.

## **Examples**

```
library(MPCR)
# create 2 MPCR matrix a,b
a <- as.MPCR(1:20,nrow=2,ncol=10,"single")
b <- as.MPCR(21:40,nrow=2,ncol=10,"double")

x <- MPCR.rbind(a,b)
y <- MPCR.cbind(a,b)</pre>
```

10-Diagonal

diag

# Description

Returns the diagonal of an MPCR matrix.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
diag(x)
```

# Arguments

Х

An MPCR matrix.

#### Value

An MPCR vector contains the main diagonal of the matrix.

```
library(MPCR)
x <- as.MPCR(1:16,4,4,"single")
diag_vals <- diag(x)</pre>
```

12-Log

11-Extremes

Min-Max Functions

# Description

Min-Max functions for MPCR objects values and indices, all NA values are disregarded.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
min(x)

## S4 method for signature 'Rcpp_MPCR'
max(x)

## S4 method for signature 'Rcpp_MPCR'
which.min(x)

## S4 method for signature 'Rcpp_MPCR'
which.max(x)
```

## **Arguments**

Х

An MPCR object.

#### Value

Min/max value/index.

# **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
min <-min(x)
min_idx <-which.min(x)</pre>
```

12-Log

Logarithms and Exponentials

# Description

exp/log functions.

13-Mathis

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
exp(x)

## S4 method for signature 'Rcpp_MPCR'
expm1(x)

## S4 method for signature 'Rcpp_MPCR'
log(x, base = 1)

## S4 method for signature 'Rcpp_MPCR'
log10(x)

## S4 method for signature 'Rcpp_MPCR'
log2(x)
```

## Arguments

x An MPCR object.

base The logarithm base. If base = 1, exp(1) is assumed, only base 1,2, and 10 avail-

able.

## Value

An MPCR object of the same dimensions as the input.

## **Examples**

```
library(MPCR)
x <- as.MPCR(1:20,precision="double")
log(x)</pre>
```

13-Mathis

Finite, infinite, and NaNs

# Description

Finite, infinite, and NaNs.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
is.finite(x)
## S4 method for signature 'Rcpp_MPCR'
```

14 14-Miscmath

```
is.infinite(x)
## S4 method for signature 'Rcpp_MPCR'
is.nan(x)
```

# Arguments

Х

An MPCR object.

#### Value

A bool vector/matrix of the same dimensions as the input.

# **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
is.nan(sqrt(x))</pre>
```

14-Miscmath

Miscellaneous mathematical functions

## **Description**

Miscellaneous mathematical functions.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
abs(x)

## S4 method for signature 'Rcpp_MPCR'
sqrt(x)
```

# Arguments

Х

An MPCR object.

#### Value

An MPCR object of the same dimensions as the input.

15-NA's

#### **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
sqrt(x)</pre>
```

15-NA's

NA's

# Description

```
is.na(), na.omit(), and na.exclude() for MPCR objects.
```

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.is.na(object,index=-1)
## S4 method for signature 'Rcpp_MPCR'
MPCR.na.exclude(object,value)
## S4 method for signature 'Rcpp_MPCR'
MPCR.na.omit(object)
```

#### **Arguments**

object MPCR object.

index If a particular index in the MPCR matrix/vector is specified, it will be checked.

If no index is provided, all elements will be checked.

value Value to replace all NAN with.

## Value

MPCR.is.na will return matrix/vector/bool according to input of the function. MPCR.na.exclude & MPCR.na.omit will not return anything.

```
library(MPCR)
x <- as.MPCR(1:20,precision="single")
x[1] <- NAN
MPCR.is.na(x,index=1) #TRUE
MPCR.na.exclude(x,50)
x[1] #50</pre>
```

16 17-Round

16-Replicate

replicate

# Description

Replicates the given input number of times according to count/len, only one should be set at a time, and in case both values are given, only the len value will have effect.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
rep(x,count=0,len=0)
```

# Arguments

x An MPCR object.

count Value to determine how many times the input value will be replicated.

Value to determine the required output size, the input will be replicated until it

matches the output len size.

## Value

MPCR vector containing the replicated values.

## **Examples**

```
library(MPCR)
x <- as.MPCR(1:16,4,4,"single")
rep_vals_1 <- rep(x,count=2) #output size will be 16*2
rep_vals_2 <- rep(x,len=2) #output size will be 2</pre>
```

17-Round

Rounding functions

# Description

Rounding functions.

18-Scale 17

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
ceiling(x)

## S4 method for signature 'Rcpp_MPCR'
floor(x)

## S4 method for signature 'Rcpp_MPCR'
trunc(x)

## S4 method for signature 'Rcpp_MPCR'
round(x, digits = 0)
```

## **Arguments**

x An MPCR object.digits The number of digits to use in rounding.

#### Value

An MPCR object of the same dimensions as the input.

## **Examples**

```
library(MPCR)
input <- runif(20,-1,1)
x <- as.MPCR(input,precision="double")
floor(x)</pre>
```

18-Scale scale

# Description

Center or scale an MPCR object.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
scale(x, center, scale)
```

# Arguments

```
{\tt x} An MPCR object. center, scale Logical or MPCR objects.
```

19-Sweep

## Value

An MPCR matrix.

# **Examples**

```
library(MPCR)
  input <-as.MPCR(1:50,precision="single")
  x$ToMatrix(5, 10)
  temp_center_scale <- new(1:10,precision="double")
  z <- scale(x=input, center=FALSE, scale=temp_center_scale)</pre>
```

19-Sweep

sweep

## **Description**

Sweep an MPCR vector through an MPCR matrix.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
sweep(x,stat,margin,FUN)
```

#### **Arguments**

x An MPCR object.

stat MPCR vector containing the value(s) that should be used in the operation.

margin 1 means row; otherwise means column.

FUN Sweeping function; must be one of "+", "-", "\*", "/", or "^".

## Value

An MPCR matrix of the same type as the highest precision input.

```
library(MPCR)
x <- as.MPCR(1:20,10,2,"single")
y <- as.MPCR(1:5,precision="double")
sweep_out <- sweep(x, stat=y, margin=1, FUN="+")
MPCR.is.double(sweep_out) #TRUE</pre>
```

20-Special Math

```
20-Special Math Special mathematical functions.
```

# Description

Special mathematical functions.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
gamma(x)

## S4 method for signature 'Rcpp_MPCR'
lgamma(x)
```

#### **Arguments**

Х

An MPCR object.

#### Value

An MPCR object of the same dimensions as the input.

## **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
lgamma(x)</pre>
```

21-Trig

Trigonometric functions

# Description

Basic trig functions.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
sin(x)

## S4 method for signature 'Rcpp_MPCR'
cos(x)
```

20 22-Hyperbolic

```
## S4 method for signature 'Rcpp_MPCR'
tan(x)

## S4 method for signature 'Rcpp_MPCR'
asin(x)

## S4 method for signature 'Rcpp_MPCR'
acos(x)

## S4 method for signature 'Rcpp_MPCR'
atan(x)
```

## Arguments

Х

An MPCR object.

#### Value

An MPCR object of the same dimensions as the input.

#### **Examples**

```
library(MPCR)

mpcr_matrix <- as.MPCR(1:20,nrow=2,ncol=10,"single")
x <- sin(mpcr_matrix)</pre>
```

22-Hyperbolic

Hyperbolic functions

#### **Description**

These functions give the obvious hyperbolic functions. They respectively compute the hyperbolic cosine, sine, tangent, and their inverses, arc-cosine, arc-tangent (or 'area cosine', etc).

#### Usage

```
## S4 method for signature 'Rcpp_MPCR'
sinh(x)
## S4 method for signature 'Rcpp_MPCR'
cosh(x)
## S4 method for signature 'Rcpp_MPCR'
tanh(x)
## S4 method for signature 'Rcpp_MPCR'
asinh(x)
## S4 method for signature 'Rcpp_MPCR'
acosh(x)
```

23-Transpose 21

```
## S4 method for signature 'Rcpp_MPCR'
atanh(x)
```

## **Arguments**

Х

An MPCR object.

## Value

An MPCR object of the same dimensions as the input.

# **Examples**

```
library(MPCR)

mpcr_matrix <- as.MPCR(1:20,nrow=2,ncol=10,precision="single")
x <- sinh(mpcr_matrix)</pre>
```

23-Transpose

transpose

# Description

Transpose an MPCR object.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
t(x)
```

## **Arguments**

Х

An MPCR object.

## Value

An MPCR object.

```
library(MPCR)
a <- matrix(1:20, nrow = 2)
a_MPCR <- as.MPCR(a,2,10,"double")
a_MPCR_transpose <- t(a_MPCR)</pre>
```

22 25-Metadata

```
24-Check precision Metadata functions
```

## **Description**

Checks the precision of a given MPCR object.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.is.single(x)
## S4 method for signature 'Rcpp_MPCR'
MPCR.is.half(x)
## S4 method for signature 'Rcpp_MPCR'
MPCR.is.double(x)
## S4 method for signature 'Rcpp_MPCR'
MPCR.is.float(x)
```

# Arguments

v

An MPCR object.

#### Value

Boolean indicates the precision of the object according to the used function.

# **Examples**

```
library(MPCR)
x <- as.MPCR(1:20,precision="double")
MPCR.is.double(x) #TRUE
MPCR.is.single(x) #FALSE</pre>
```

25-Metadata

Metadata functions

## **Description**

Metadata functions.

26-Print 23

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
storage.mode(x)
## S4 method for signature 'Rcpp_MPCR'
typeof(x)
## S4 method for signature 'Rcpp_MPCR'
MPCR.object.size(x)
## S4 method for signature 'Rcpp_MPCR'
MPCR.ChangePrecision(x,precision)
```

## **Arguments**

x An MPCR object.precision String with the required precision.

#### Value

Prints/change metadata about an MPCR object.

#### **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
typeof(x)
MPCR.ChangePrecision(x,"single")
MPCR.is.single(x) #True</pre>
```

26-Print *print* 

# Description

Prints the precision and type of the object, and print will print the meta data of the object without printing the values. Function x\$PrintValues() should be used to print the values."

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
print(x)

## S4 method for signature 'Rcpp_MPCR'
show(object)
```

#### **Arguments**

```
x, object An MPCR objects.
```

#### Details

Prints metadata about the object and some values.

## Value

A string containing the metadata of the MPCR object.

# **Examples**

```
library(MPCR)
x <- as.MPCR(1:16,4,4,"single")
y <- as.MPCR(1:20,4,5,"double")
x
print(y)</pre>
```

```
27-Cholesky decomposition cholesky decomposition
```

# Description

Performs the Cholesky factorization of a positive definite MPCR matrix x.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
chol(x,upper_triangle=TRUE)
```

# Arguments

```
x An MPCR matrix.

upper_triangle

Boolean to check on which triangle the cholesky decomposition should be applied.
```

#### Value

An MPCR matrix.

28-Cholesky inverse 25

#### **Examples**

```
28-Cholesky inverse
```

cholesky inverse

## **Description**

Performs the inverse of the original matrix using the Cholesky factorization of an MPCR matrix x.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
chol2inv(x, size = NCOL(x))
```

# Arguments

x An MPCR object.

size The number of columns to use.

#### Value

An MPCR object.

26 29-Crossprod

29-Crossprod crossprod

## **Description**

Calculates the cross product of two MPCR matrices. It uses BLAS routine gemm() for  $A \times B$  operations and syrk() for  $A \times A^T$  operations.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
crossprod(x, y = NULL)

## S4 method for signature 'Rcpp_MPCR'
tcrossprod(x, y = NULL)
```

#### **Arguments**

x An MPCR object.

y Either NULL, or an MPCR matrix.

#### **Details**

Calculates cross product of two MPCR matrices performs:

```
x \%*\% y, t(x) \%*\% x
```

This function uses blas routine gemm() for **A** X **B** operations & syrk() for **A** X **A**^T operations.

## Value

An MPCR matrix.

```
library(MPCR)
x <- as.MPCR(1:16,4,4,"single")
y <- as.MPCR(1:20,4,5,"double")

z <- crossprod(x)  # t(x) x
z <- tcrossprod(x)  # x t(x)
z <- crossprod(x,y)  # x y
z <- x %*% y  # x y</pre>
```

```
30-Eigen decomposition eigen decomposition
```

# Description

Solves a system of equations or invert an MPCR matrix, using lapack routine syevr ()

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
eigen(x, only.values = FALSE)
```

## **Arguments**

```
x An MPCR object. only.values (TRUE/FALSE)?
```

#### Value

A list contains MPCR objects describing the values and optionally vectors.

## **Examples**

```
library(MPCR)
s <- runif(10, 3)
cross_prod <- crossprod(s)
x <- as.MPCR(cross_prod, nrow(cross_prod), nrow(cross_prod), precision)
y <- eigen(x)</pre>
```

31-Symmetric

isSymmetric

#### **Description**

Check if a given MPCR matrix is symmetric.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
isSymmetric(object, ...)
```

## **Arguments**

```
object An MPCR matrix.
... Ignored.
```

28 32-Norm

## Value

A logical value.

# **Examples**

```
library(MPCR)

x <- as.MPCR(1:50,25,2,"Single")
isSymmetric(x) #false

crossprod_output<-crossprod(x)
isSymmetric(crossprod_output) #true</pre>
```

32-Norm

norm

# Description

Compute norm.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
norm(x, type = "0")
```

# Arguments

x An MPCR object.

type "O"-ne, "I"-nfinity, "F"-robenius, "M"-ax modulus, and "1" norms.

## Value

An MPCR object.

```
library(MPCR)

x <- as.MPCR(1:20,precision="double")
norm(x, type="0")</pre>
```

33-QR decomposition 29

```
33-QR decomposition
```

QR decomposition

#### **Description**

QR factorization and related functions.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
qr(x, tol = 1e-07)

## S4 method for signature 'ANY'
qr.Q(qr, complete = FALSE, Dvec)

## S4 method for signature 'ANY'
qr.R(qr, complete = FALSE)
```

#### **Arguments**

x An MPCR matrix.

qr QR decomposition MPCR object.

The tolerance for determining numerical column rank.

complete Should the complete or truncated factor be returned?

Dvec Vector of diagonals to use when re-constructing Q (default is 1's).

#### **Details**

The factorization is performed by the LAPACK routine geqp3 (). This should be similar to calling qr () on an ordinary R matrix with the argument LAPACK=TRUE.

## Value

```
qr Output of qr().
```

```
library(MPCR)

qr_input <-as.MPCR( c(1, 2, 3, 2, 4, 6, 3, 3, 3),3,3,"single")
qr_out <- qr(qr_input)
qr_out
qr_out[["qr"]]$PrintValues()</pre>
```

```
qr_out[["qraux"]]$PrintValues()
qr_out[["pivot"]]$PrintValues()
qr_out[["rank"]]$PrintValues()
qr_q <- qr.Q(qr_out)
qr_q</pre>
```

```
34-Reciprocal condition {\it reciprocal\ condition}
```

# Description

Compute matrix norm.

## Usage

```
## S4 method for signature 'Rcpp_MPCR'
rcond(x, norm = "O", useInv = FALSE)
```

# Arguments

x An MPCR object.
norm "O"-ne or "I"-nfinity norm.
useInv TRUE to use the lower triangle only.

## Value

An MPCR Object.

```
library(MPCR)
x <- as.MPCR(1:20,precision="double")
rcond(x)</pre>
```

35-Solve 31

35-Solve solve

# Description

Solve a system of equations or invert an MPCR matrix.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
solve(a, b = NULL, ...)
```

## **Arguments**

```
a, b An MPCR objects.... Ignored.
```

#### Value

Solves the equation AX=B .and if B=NULL t(A) will be used.

## **Examples**

```
library(MPCR)

x <- as.MPCR(1:20,4,5,"double")
y <- crossprod(x)
solve(y)</pre>
```

```
36-Singular value decomposition SVD
```

## **Description**

SVD factorization.

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
La.svd(x, nu = min(n, p), nv = min(n, p))
## S4 method for signature 'Rcpp_MPCR'
svd(x, nu = min(n, p), nv = min(n, p))
```

32 37-Back/Forward solve

## Arguments

```
x An MPCR matrix.

nu, nv The number of left/right singular vectors to return.
```

#### **Details**

The factorization is performed by the LAPACK routine gesdd().

#### Value

The SVD decomposition of the MPCR matrix.

## **Examples**

```
37-Back/Forward solve
```

Back/Forward solve

## Description

Solves a system of linear equations where the coefficient matrix is upper or lower triangular. The function solves the equation A X = B, where A is the coefficient matrix, X is the solution vector, and B is the right-hand side vector.

# Usage

```
## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
backsolve(r, x, k = ncol(r), upper.tri = TRUE, transpose = FALSE)

## S4 method for signature 'Rcpp_MPCR, Rcpp_MPCR'
forwardsolve(l, x, k = ncol(l), upper.tri = FALSE, transpose = FALSE)
```

38-MPCR GEMM 33

## **Arguments**

1	An MPCR object.
r	An MPCR object.
X	An MPCR object whose columns give the right-hand sides for the equations.
k	The number of columns of r and rows of x to use.
upper.tri	logical; if TRUE, the upper triangular part of r is used. Otherwise, the lower one.
transpose	logical; if TRUE, solve for $t(1, r)$ %*% output == x.

#### Value

An MPCR object represents the solution to the system of linear equations.

## **Examples**

```
library(MPCR)
a <- matrix(c(2, 0, 0, 3), nrow = 2)
b <- matrix(c(1, 2), nrow = 2)
a_MPCR <- as.MPCR(a,2,2,"single")
b_MPCR <- as.MPCR(b,2,1,"double")
x <- forwardsolve(a_MPCR, b_MPCR)
x</pre>
```

38-MPCR GEMM

MPCR GEMM (Matrix-Matrix Multiplication)

## **Description**

```
Performs matrix-matrix multiplication of two given MPCR matrices to performs: C = alpha \ A * B + beta \ C

C = alpha \ A \ A^T + beta \ C
```

1

# Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.gemm(a,b = NULL,c,transpose_a= FALSE,transpose_b=FALSE,alpha=1,beta=0)
```

# Arguments

```
    a An MPCR matrix A.
    b An MPCR matrix B, if NULL, the function will perform syrk operation from blas.
    c Input/Output MPCR matrix C.
```

34 39-MPCR TRSM

transpose\_a A flag to indicate whether transpose matrix A should be used, if B is NULL and

transpose\_a =TRUE

The function will perform the following operation:

C=alphaA^TXA+betaC.

transpose\_b A flag to indicate whether transpose matrix B should be used.

alpha Specifies the scalar alpha. beta Specifies the scalar beta.

#### Value

An MPCR matrix.

#### **Examples**

```
library(MPCR)
# create 3 MPCR matrices a,b,c
print(c)
MPCR.gemm(a,b,c,transpose_a=false,transpose_b=TRUE,alpha=1,beta=1)
print(c)
```

39-MPCR TRSM

MPCR TRSM (Triangular Solve)

#### **Description**

```
Solves a triangular matrix equation. performs: op(A)*X=alpha*B
X*op(A)=alpha*B
```

#### Usage

```
## S4 method for signature 'Rcpp_MPCR'
MPCR.trsm(a,b,upper_triangle,transpose,side = 'L',alpha =1)
```

#### Arguments

a MPCR Matrix A. b MPCR Matrix B.

upper\_triangle

If the value is TRUE, the referenced part of matrix A corresponds to the upper

triangle, with the opposite triangle assumed to contain zeros.

transpose If TRUE, the transpose of A is used. side 'R for Right side, 'L' for Left side.

alpha Factor used for A, If alpha is zero, A is not accessed.

39-MPCR TRSM 35

# Value

An MPCR Matrix.

# **Index**

!=,Rcpp_MPCR,BaseLinAlg-method	(04-Comparison), 6
(04-Comparison), 6	>=, Rcpp_MPCR, Rcpp_MPCR-method
!=,Rcpp_MPCR,Rcpp_MPCR-method	(04-Comparison), 6
(04-Comparison), 6	[,Rcpp_MPCR-method
*Topic <b>S4 class</b>	(07-Extract-Replace), 9
01-MPCR, 2	[<-, Rcpp_MPCR-method
*,Rcpp_MPCR,BaseLinAlg-method	(07-Extract-Replace), 9
(03-Arithmetic), 5	[[,Rcpp_MPCR-method
*, Rcpp_MPCR, Rcpp_MPCR-method	(07-Extract-Replace), 9
(03-Arithmetic), 5	[[<-,Rcpp_MPCR-method
+,Rcpp_MPCR,BaseLinAlg-method	(07-Extract-Replace), 9
(03-Arithmetic), 5	^,Rcpp_MPCR,BaseLinAlg-method
+, Rcpp_MPCR, Rcpp_MPCR-method	(03-Arithmetic), 5
(03-Arithmetic), 5	^,Rcpp_MPCR,Rcpp_MPCR-method
-,Rcpp_MPCR,BaseLinAlg-method	(03-Arithmetic), 5
(03-Arithmetic), 5	01-MPCR, 2
-, Rcpp_MPCR, Rcpp_MPCR-method	02-Converters,4
(03-Arithmetic), 5	03-Arithmetic, 5
/,Rcpp_MPCR,BaseLinAlg-method	04-Comparison, $6$
(03-Arithmetic), 5	05-Copy, <b>7</b>
/,Rcpp_MPCR,Rcpp_MPCR-method	06-Dimensions, 8
(03-Arithmetic),5	07-Extract-Replace,9
<pre>&lt;,Rcpp_MPCR,BaseLinAlg-method</pre>	08-Concatenate, 10
(04-Comparison), 6	09-Bind, 10
<pre>&lt;,Rcpp_MPCR,Rcpp_MPCR-method</pre>	10-Diagonal, 11
(04-Comparison),6	11-Extremes, 12
<=,Rcpp_MPCR,BaseLinAlg-method	12-Log, <mark>12</mark>
(04-Comparison), $6$	13-Mathis, <b>13</b>
<=,Rcpp_MPCR,Rcpp_MPCR-method	14-Miscmath, 14
(04-Comparison), 6	15-NA's, 15
==,Rcpp_MPCR,BaseLinAlg-method	16-Replicate, 16
(04-Comparison), 6	17-Round, <b>16</b>
==,Rcpp_MPCR,Rcpp_MPCR-method	18-Scale, <mark>17</mark>
(04-Comparison), 6	19-Sweep, <b>18</b>
>,Rcpp_MPCR,BaseLinAlg-method	20-Special Math, 19
(04-Comparison), 6	21-Trig, <mark>19</mark>
>,Rcpp_MPCR,Rcpp_MPCR-method	22-Hyperbolic, 20
(04-Comparison), 6	23-Transpose, 21
>=,Rcpp MPCR,BaseLinAlg-method	24-Check precision. 22

25-Metadata, 22	comparison(04-Comparison),6
26-Print, <b>23</b>	concatenate (08-Concatenate), 10
27-Cholesky decomposition, 24	Converters (02-Converters), 4
28-Cholesky inverse, 25	copy (05-Copy), 7
29-Crossprod, 26	cos, Rcpp_MPCR-method(21-Trig), 19
30-Eigen decomposition, 27	cosh, Rcpp_MPCR-method
31-Symmetric, 27	(22-Hyperbolic), $20$
32-Norm, 28	crossprod (29-Crossprod), 26
33-QR decomposition, 29	crossprod, Rcpp_MPCR-method
34-Reciprocal condition, 30	(29-Crossprod), <mark>26</mark>
35-Solve, 31	
36-Singular value decomposition,	diag(10-Diagonal),11
31	diag, Rcpp_MPCR-method
37-Back/Forward solve, 32	(10-Diagonal), <b>11</b>
38-MPCR GEMM, <b>33</b>	dimensions (06-Dimensions), 8
39-MPCR TRSM, <b>34</b>	
	eigen(30-Eigen decomposition),27
abs, Rcpp_MPCR-method	eigen, Rcpp_MPCR-method(30-Eigen
(14-Miscmath), <b>14</b>	decomposition),27
acos, Rcpp_MPCR-method(21-Trig),	exp, Rcpp_MPCR-method $(12-Log)$ , $12$
19	expm1, Rcpp_MPCR-method(12-Log),
acosh, Rcpp_MPCR-method	12
(22-Hyperbolic), 20	extremes (11-Extremes), 12
arithmetic (03-Arithmetic), 5	
as.MPCR(02-Converters), 4	floor, Rcpp_MPCR-method
asin, Rcpp_MPCR-method (21-Trig),	(17–Round), <mark>16</mark>
19	forwardsolve, Rcpp_MPCR, Rcpp_MPCR-method
asinh, Rcpp_MPCR-method	(37-Back/Forward solve), 32
(22-Hyperbolic), 20	
atan, Rcpp_MPCR-method (21-Trig),	gamma, Rcpp_MPCR-method
19	(20-Special Math), 19
atanh, Rcpp_MPCR-method	hyperbolic(22-Hyperbolic), 20
(22-Hyperbolic), 20	nipersorie (22 nipersorie), 20
, 12	is.finite,Rcpp_MPCR-method
backsolve, Rcpp_MPCR, Rcpp_MPCR-method	(13-Mathis), 13
(37-Back/Forward solve), 32	is.infinite, Rcpp_MPCR-method
	(13-Mathis), 13
ceiling, Rcpp_MPCR-method	is.nan,Rcpp_MPCR-method
(17-Round), <mark>16</mark>	(13-Mathis), 13
Check Precision (24-Check	isSymmetric(31-Symmetric), 27
precision), 22	isSymmetric, Rcpp_MPCR-method
chol (27-Cholesky decomposition),	(31-Symmetric), 27
24	(======================================
chol, Rcpp_MPCR-method	La.svd, Rcpp_MPCR-method
(27-Cholesky	(36-Singular value
decomposition), 24	decomposition), 31
chol2inv(28-Cholesky inverse), 25	lgamma, Rcpp_MPCR-method
chol2inv, Rcpp_MPCR-method	(20-Special Math), 19
(28-Cholesky inverse).25	log (12-Log), 12

$log, Rcpp\_MPCR-method(12-Log), I2$	MPCR.exp(12-Log), 12
log10, Rcpp_MPCR-method(12-Log),	MPCR.expm1 $(12-Log)$ , 12
12	MPCR.floor $(17-Round)$ , 16
log2, Rcpp_MPCR-method (12-Log), 12	MPCR.forwardsolve
	(37-Back/Forward solve), 32
mathis (13-Mathis), 13	MPCR.gamma (20-Special Math), 19
max, Rcpp_MPCR-method	MPCR.gemm (38-MPCR GEMM), 33
(11-Extremes), 12	MPCR.gemm, Rcpp_MPCR-method
metadata (25-Metadata), 22	
min, Rcpp_MPCR-method	(38-MPCR GEMM), 33
(11-Extremes), 12	MPCR.is.double(24-Check
miscmath (14-Miscmath), 14	precision), 22
MPCR (01-MPCR), 2	MPCR.is.double, Rcpp_MPCR-method
MPCR GEMM (38-MPCR GEMM), 33	(24-Check precision), 22
MPCR TRSM (39-MPCR TRSM), 34	MPCR.is.finite(13-Mathis),13
	MPCR.is.float(24-Check
MPCR.abs (14-Miscmath), 14	precision), 22
MPCR.acos (21-Trig), 19	MPCR.is.float, Rcpp_MPCR-method
MPCR.acosh (22-Hyperbolic), 20	(24-Check precision), 22
MPCR.Add(03-Arithmetic),5	MPCR.is.half(24-Check
MPCR.asin (21-Trig), 19	precision), 22
MPCR.asinh (22-Hyperbolic), 20	MPCR.is.half,Rcpp_MPCR-method
MPCR.atan $(21-Trig)$ , 19	(24-Check precision), 22
MPCR.atanh (22-Hyperbolic), $20$	MPCR.is.infinite(13-Mathis), 13
MPCR.backsolve(37-Back/Forward	MPCR.is.na (15-NA's), 15
solve), 32	MPCR.is.na, Rcpp_MPCR-method
MPCR.cbind(09-Bind), 10	
MPCR.cbind, Rcpp_MPCR-method	(15-NA's), 15
(09-Bind), 10	MPCR.is.nan (13-Mathis), 13
MPCR.ceiling(17-Round), 16	MPCR.is.single(24-Check
MPCR.ChangePrecision	precision), 22
(25-Metadata), <mark>22</mark>	MPCR.is.single, Rcpp_MPCR-method
MPCR.ChangePrecision, Rcpp_MPCR-metho	d (24-Check precision), 22
(25-Metadata), <mark>22</mark>	MPCR.isSymmetric(31-Symmetric),
MPCR.chol(27-Cholesky	27
decomposition), 24	MPCR.La.svd(36-Singular value
MPCR.chol2inv(28-Cholesky	decomposition), 31
inverse), 25	MPCR.lgamma(20-Special Math), 19
MPCR.Concatenate	MPCR.log $(12-Log)$ , 12
(08-Concatenate), 10	MPCR.log10 (12-Log), 12
MPCR.Concatenate, Rcpp_MPCR-method	MPCR.log2 (12-Log), 12
(08-Concatenate), 10	MPCR.max(11-Extremes), 12
MPCR.copy (05-Copy), 7	MPCR.min(11-Extremes), 12
= = : = = :	MPCR.Multiply(03-Arithmetic), 5
MPCR.cos (21-Trig), 19	
MPCR.cosh (22-Hyperbolic), 20	MPCR.na.exclude (15-NA's), 15
MPCR.crossprod (29-Crossprod), 26	MPCR.na.exclude, Rcpp_MPCR-method
MPCR.diag(10-Diagonal), 11	(15-NA's), 15
MPCR.Divide (03-Arithmetic), 5	MPCR.na.omit (15-NA's), 15
MPCR.eigen(30-Eigen	MPCR.na.omit, Rcpp_MPCR-method
decomposition), 27	(15-NA's), 15

MPCR.ncol (06-Dimensions), 8	norm (32-Norm), 28
MPCR.norm (32-Norm), 28	norm, Rcpp_MPCR-method (32-Norm),
MPCR.nrow(06-Dimensions), 8	28
MPCR.object.size(25-Metadata), 22	nrow, Rcpp_MPCR-method
MPCR.object.size, Rcpp_MPCR-method	(06-Dimensions),8
(25-Metadata), <mark>22</mark>	
MPCR.Power (03-Arithmetic), 5	print (26-Print), 23
MPCR.print (26-Print), 23	print,Rcpp_MPCR-method
MPCR.qr(33-QR decomposition), 29	(26-Print), <mark>23</mark>
MPCR.rbind(09-Bind), 10	
MPCR.rbind, Rcpp_MPCR-method	qr(33-QR decomposition),29
(09-Bind), 10	qr, Rcpp_MPCR-method( $33$ -QR
MPCR.rcond(34-Reciprocal	decomposition), 29
condition), 30	qr.Q, ANY-method (33-QR
MPCR.rep(16-Replicate), 16	decomposition), 29
MPCR.round (17-Round), 16	qr.R, ANY-method (33-QR
MPCR.scale (18-Scale), 17	decomposition), 29
MPCR.show (26-Print), 23	
MPCR.sin (21-Trig), 19	rcond(34-Reciprocal condition),
MPCR.sinh (22-Hyperbolic), 20	30
MPCR.solve(35-Solve), 31	rcond, Rcpp_MPCR-method
MPCR.sqrt (14-Miscmath), 14	(34-Reciprocal condition)
MPCR.storage.mode(25-Metadata),	30
22	Rcpp_MPCR-class(01-MPCR), $2$
MPCR.str(26-Print), 23	rep,Rcpp_MPCR-method
MPCR.Subtract (03-Arithmetic), 5	(16-Replicate), <mark>16</mark>
MPCR.svd(36-Singular value	replicate(16-Replicate),16
decomposition), 31	round (17-Round), <mark>16</mark>
MPCR.sweep (19-Sweep), 18	round, Rcpp_MPCR-method
MPCR.t (23-Transpose), 21	(17-Round), <mark>16</mark>
MPCR.tan (21-Trig), 19	
MPCR.tanh(22-Hyperbolic), 20	scale (18-Scale), <b>17</b>
MPCR.tcrossprod(29-Crossprod), 26	scale, Rcpp_MPCR-method
MPCR.ToNumericMatrix	(18-Scale), <b>17</b>
(02-Converters),4	show, Rcpp_MPCR-method (26-Print),
MPCR.ToNumericVector	23
(02-Converters),4	$sin, Rcpp\_MPCR-method(21-Trig), 19$
MPCR.trsm (39-MPCR TRSM), 34	sinh, Rcpp_MPCR-method
MPCR.trsm, Rcpp_MPCR-method	(22-Hyperbolic), 20
(39-MPCR TRSM), 34	solve (35-Solve), 31
MPCR.trunc(17-Round), 16	solve, Rcpp_MPCR-method
MPCR.typeof(25-Metadata), 22	(35-Solve), 31
MPCR.which.max(11-Extremes), 12	specialmath(20-Special Math),19
MPCR.which.min(11-Extremes), 12	sqrt, Rcpp_MPCR-method
	(14-Miscmath), <b>14</b>
NA's (15-NA's), 15	storage.mode, Rcpp_MPCR-method
ncol, Rcpp_MPCR-method	(25-Metadata), <mark>22</mark>
(06-Dimensions),8	svd(36-Singular value
new, 3	decomposition), 31

```
svd, Rcpp_MPCR-method
       (36-Singular value
       decomposition), 31
sweep (19-Sweep), 18
sweep,Rcpp_MPCR-method
       (19-Sweep), 18
t, Rcpp_MPCR-method
       (23-Transpose), 21
tan, Rcpp_MPCR-method (21-Trig), 19
tanh, Rcpp_MPCR-method
       (22-Hyperbolic), 20
tcrossprod, Rcpp_MPCR-method
       (29-Crossprod), 26
transpose (23-Transpose), 21
trig(21-Trig), 19
trunc, Rcpp_MPCR-method
       (17-Round), 16
typeof, Rcpp_MPCR-method
       (25-Metadata), 22
which.max, Rcpp_MPCR-method
       (11-Extremes), 12
which.min, Rcpp_MPCR-method
       (11-Extremes), 12
```