

The chain rule and the extended power rule

3.7.1

a. 
$$\frac{dy}{dx} = \frac{1}{2\sqrt{x^2+\sqrt{x}}} \left( 2x + \frac{1}{2\sqrt{x}} \right)$$

b. 
$$\frac{dy}{dx} = 30 \left( \frac{2x-1}{\sqrt{1-x}} + x \right)^{29} \cdot \left( \frac{2\sqrt{1-x} - (2x-1)\frac{-1}{2\sqrt{1-x}}}{1-x} + 1 \right)$$

3.7.2 Applying the chain rule at every step, we have

$$(f(g(h(p(x)))))' = f'(g(h(p(x))))(g(h(p(x))))' = f'(g(h(p(x))))g'(h(p(x)))(h(p(x)))'$$

which leads to the answer.