



Borgnakke Sonntag

Fundamentals of
Thermodynamics

SOLUTION MANUAL
CHAPTER 4

8e

Updated June 2013

CONTENT CHAPTER 4

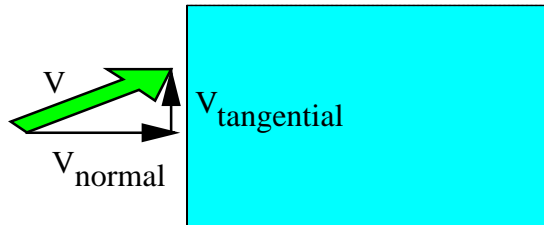
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In-Text Concept Questions

4.a

A mass flow rate into a control volume requires a normal velocity component. Why?

The tangential velocity component does not bring any substance across the control volume surface as it flows parallel to it, the normal component of velocity brings substance in or out of the control volume according to its sign. The normal component must be into the control volume to bring mass in, just like when you enter a bus (it does not help that you run parallel with the bus side).

**4.b**

Can a steady state device have boundary work?

No. Any change in size of the control volume would require either a change in mass inside or a change in state inside, neither of which is possible in a steady-state process.

4.c

Can you say something about changes in \dot{m} and \dot{V} through a steady flow device?

The continuity equation expresses the conservation of mass, so the total amount of \dot{m} entering must be equal to the total amount leaving. For a single flow device the mass flow rate is constant through it, so you have the same mass flow rate across any total cross-section of the device from the inlet to the exit.

The volume flow rate is related to the mass flow rate as

$$\dot{V} = v \dot{m}$$

so it can vary if the state changes (then v changes) for a constant mass flow rate.

This also means that the velocity can change (influenced by the area as $\dot{V} = \mathbf{V}A$) and the flow can experience an acceleration (like in a nozzle) or a deceleration (as in a diffuser).

4.d

In a multiple device flow system, I want to determine a state property. Where should I be looking for information—upstream or downstream?

Generally flow is affected more by what happened to it which is upstream than what is in front of it. Only the pressure information can travel upstream and give rise to accelerations (nozzle) or decelerations (stagnation type flow). Heat transfer that can heat or cool a flow can not travel very fast and is easily overpowered by the convection. If the flow velocity exceeds the speed of sound even the pressure information can not travel upstream.

4.e

How does a nozzle or sprayhead generate kinetic energy?

By accelerating the fluid from a high pressure towards the lower pressure, which is outside the nozzle. The higher pressure pushes harder than the lower pressure so there is a net force on any mass element to accelerate it.



4.f

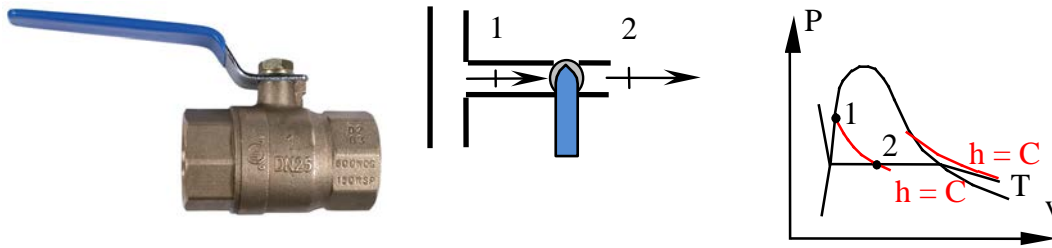
What is the difference between a nozzle flow and a throttle process?

In both processes a flow moves from a higher to a lower pressure. In the nozzle the pressure drop generates kinetic energy, whereas that does not take place in the throttle process. The pressure drop in the throttle is due to a flow restriction and represents a loss.

4.g

If you throttle a saturated liquid what happens to the fluid state? What if this is done to an ideal gas?

The throttle process is approximated as a constant enthalpy process. Changing the state from saturated liquid to a lower pressure with the same h gives a two-phase state so some of the liquid will vaporize and it becomes colder.

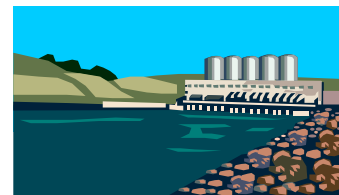
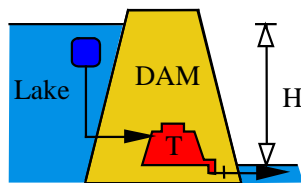


If the same process happens in an ideal gas then same h gives the same temperature (h a function of T only) at the lower pressure.

4.h

A turbine at the bottom of a dam has a flow of liquid water through it. How does that produce power? Which terms in the energy equation are important if the CV is the turbine only? If the CV is the turbine plus the upstream flow up to the top of the lake, which terms in the energy equation are then important?

The water at the bottom of the dam in the turbine inlet is at a high pressure. It runs through a nozzle generating kinetic energy as the pressure drops. This high kinetic energy flow impacts a set of rotating blades or buckets, which converts the kinetic energy to power on the shaft and the flow leaves at low pressure and low velocity.

**CV Turbine only.**

The high P in and the low P out shows up in the $(h = u + Pv)$ flow terms of the energy equation giving the difference in the flow work terms Pv in and out.

CV Turbine plus upstream flow.

For this CV the pressures in and out are the same (1 atm) so the difference is in the potential energy terms (gz) included in h_{tot} .

4.i

If you compress air the temperature goes up, why? When the hot air, high P flows in long pipes it eventually cools to ambient T. How does that change the flow?

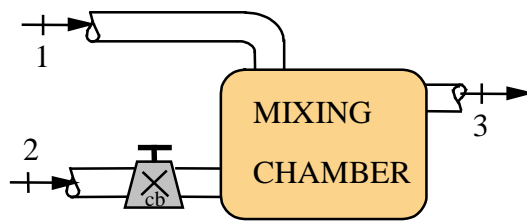
As the air is compressed, volume decreases so work is done on a mass element, its energy and hence temperature goes up. If it flows at nearly constant P and cools, its density increases (v decreases) so it slows down for same mass flow rate ($\dot{m} = \rho A \mathbf{V}$) and flow area.

4.j

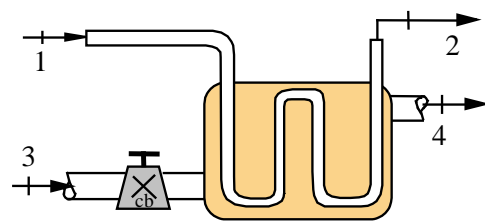
A mixing chamber has all flows at the same P , neglecting losses. A heat exchanger has separate flows exchanging energy, but they do not mix. Why have both kinds?

You might allow mixing when you can use the resulting output mixture, say it is the same substance. You may also allow it if you definitely want the outgoing mixture, like water out of a faucet where you mix hot and cold water. Even if it is different substances it may be desirable, say you add water to dry air to make it more moist, typical for a winter time air-conditioning set-up.

In other cases it is different substances that flow at different pressures with one flow heating or cooling the other flow. This could be hot combustion gases heating a flow of water or a primary fluid flow around a nuclear reactor heating a transfer fluid flow. Here the fluid being heated should stay pure so it does not absorb gases or radioactive particles and becomes contaminated. Even when the two flows have the same substance there may be a reason to keep them at separate pressures.



An open mixing chamber



A closed tube in shell heat exchanger.

4.k

An initially empty cylinder is filled with air from 20°C, 100 kPa until it is full. Assuming no heat transfer is the final temperature larger, equal to or smaller than 20°C? Does the final T depend on the size of the cylinder?

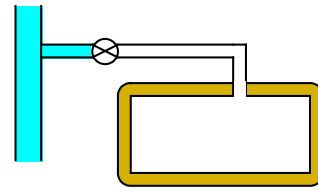
This is a transient problem with no heat transfer and no work. The balance equations for the tank as C.V. become

$$\text{Continuity Eq.:} \quad m_2 - 0 = m_i$$

$$\text{Energy Eq.:} \quad m_2 u_2 - 0 = m_i h_i + Q - W = m_i h_i + 0 - 0$$

$$\text{Final state:} \quad u_2 = h_i = u_i + P_i v_i \quad \& \quad P_2 = P_i$$

$T_2 > T_i$ and it does not depend on V



Concept-Study Guide Problems

4.1

A temperature difference drives a heat transfer. Does a similar concept apply to \dot{m} ?

Yes. A pressure difference drives the flow. The fluid is accelerated in the direction of a lower pressure as it is being pushed harder behind it than in front of it. This also means a higher pressure in front can decelerate the flow to a lower velocity which happens at a stagnation point on a wall.



4.2

What kind of effect can be felt upstream in a flow?

Only the pressure can be felt upstream in a subsonic flow. In a supersonic flow no information can travel upstream. The temperature information travels by conduction and even small velocities overpowers the conduction with the convection of energy so the temperature at a given location is mainly given by the upstream conditions and influenced very little by the downstream conditions.

4.3

Which one of the properties (P , v , T) can be controlled in a flow? How?

Since the flow is not contained there is no direct control over the volume and thus no control of v . The pressure can be controlled by installation of a pump or compressor if you want to increase it or use a turbine, nozzle or valve through which the pressure will decrease. The temperature can be controlled by heating or cooling the flow in a heat exchanger.

4.4

Air at 500 kPa is expanded to 100 kPa in two steady flow cases. Case one is a nozzle and case two is a turbine, the exit state is the same for both cases. What can you say about the specific turbine work relative to the specific kinetic energy in the exit flow of the nozzle?

For these single flow devices let us assume they are adiabatic and that the turbine does not have any exit kinetic energy then the energy equations become:

$$\text{Energy Eq.4.13 nozzle: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Energy Eq.4.13 turbine: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + gZ_2 + w_T$$

Comparing the two we get $\frac{1}{2} \mathbf{V}_2^2 = w_T$ so the result is that the nozzle delivers kinetic energy of the same amount as the turbine delivers shaft work.

4.5

Pipes that carry a hot fluid like steam in a power plant, exhaust pipe for a diesel engine in a ship etc. are often insulated. Is that to reduce the heat loss or is there another purpose?

You definitely want to insulate pipes that carry hot steam from the boiler to the turbines in a power plant and pipes that flows hot water from one location to another. Even if the energy in the flow is unwanted the pipes should be insulated for safety. Any place that people could touch a hot surface (or very cold surface) there is a risk of a burn and that should be avoided.

4.6

A windmill takes a fraction of the wind kinetic energy out as power on a shaft. In what manner does the temperature and wind velocity influence the power? Hint: write the power as mass flow rate times specific work.

The work as a fraction f of the flow of kinetic energy becomes

$$\dot{W} = \dot{m} w = \dot{m} f \frac{1}{2} \mathbf{V}_{\text{in}}^2 = \rho A \mathbf{V}_{\text{in}} f \frac{1}{2} \mathbf{V}_{\text{in}}^2$$

so the power is proportional to the velocity cubed. The temperature enters through the density, so assuming air is ideal gas

$$\rho = 1/v = P/RT$$

and the power is inversely proportional to temperature.



A windmill farm west of Denmark in the North Sea.

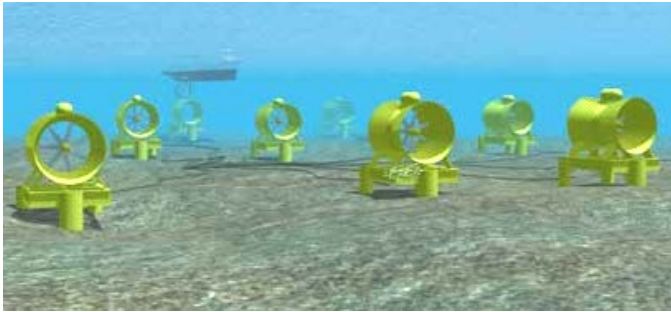
4.7

An underwater turbine extracts a fraction of the kinetic energy from the ocean current. In what manner does the temperature and water velocity influence the power? Hint: write the power as mass flow rate times specific work.

The work as a fraction f of the flow of kinetic energy becomes

$$\dot{W} = \dot{m} w = \dot{m} f \frac{1}{2} \mathbf{V}_{\text{in}}^2 = \rho A \mathbf{V}_{\text{in}} f \frac{1}{2} \mathbf{V}_{\text{in}}^2$$

so the power is proportional to the velocity cubed. The temperature enters through the density, so assuming water is incompressible density is constant and the power does not vary with the temperature.



A proposed underwater tidal flow turbine farm. Each turbine is for 1 MW with a diameter of 11.5 m mounted on the seafloor.

4.8

A liquid water turbine in the bottom of a dam takes energy out as power on a shaft. Which term(s) in the energy equation are changing and important?

The water at the bottom of the dam in the turbine inlet is at a high pressure. In a standard turbine it runs through blade passages like a propeller. In this case the inlet high pressure is used directly to generate the force on the moving blades.

For a Pelton turbine the water runs through a nozzle generating kinetic energy as the pressure drops. The high kinetic energy flow impacts a set of rotating buckets and converts the flow kinetic energy to power on the shaft so the flow leaves at low pressure and low velocity.



From Environmental Energy Technologies Division of the Lawrence Berkeley National Laboratory, and the U.S. Department of Energy

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4.9

You blow a balloon up with air. What kind of work terms including flow work do you see in that case? Where is the energy stored?

As the balloon is blown up mass flow in has flow work associated with it. Also as the balloon grows there is a boundary work done by the inside gas and a smaller boundary work from the outside of the balloon to the atmosphere. The difference between the latter two work terms goes into stretching the balloon material and thus becomes internal energy (or you may call that potential energy) of the balloon material. The work term to the atmosphere is stored in the atmosphere and the part of the flow work that stays in the gas is stored as the gas internal energy.



4.10

A storage tank for natural gas (NG) has a top dome that can move up or down as gas is added or subtracted from the tank maintaining 110 kPa, 290 K inside. A pipeline at 110 kPa, 290 K now supplies some NG to the tank. Does it change state during the filling process? What happens to the flow work?

As the pressure inside the storage tank is the same as in the pipeline the state does not change. However the tank volume goes up and work is done on the moving boundary at the 110 kPa so this work equals the flow work. The net effect is the flow work goes into raising the dome.



Continuity equation and flow rates

4.11

A large brewery has a pipe of cross sectional area 0.2 m^2 flowing carbon dioxide at 400 kPa , 10°C with a volume flow rate of $0.3 \text{ m}^3/\text{s}$. Find the velocity and the mass flow rate.

$$\dot{m} = A\mathbf{V}/v = \dot{V}/v$$

$$v = RT/P = 0.1889 \text{ kJ/kg-K} \times 283.15 \text{ K} / 400 \text{ kPa} = 0.1337 \text{ m}^3/\text{kg}$$

$$\dot{m} = \dot{V}/v = (0.3 \text{ m}^3/\text{s}) / (0.1337 \text{ m}^3/\text{kg}) = \mathbf{2.24 \text{ kg/s}}$$

$$\mathbf{V} = \dot{V} / A = 0.1337 \text{ (m}^3/\text{s}) / 0.2 \text{ m}^2 = \mathbf{0.67 \text{ m/s}}$$

4.12

Air at 35°C, 105 kPa, flows in a 100 mm × 150 mm rectangular duct in a heating system. The mass flow rate is 0.015 kg/s. What are the velocity of the air flowing in the duct and the volume flow rate?

Solution:

Assume a constant velocity across the duct area with

$$A = 100 \times 150 \times 10^{-6} \text{ m}^2 = 0.015 \text{ m}^2$$

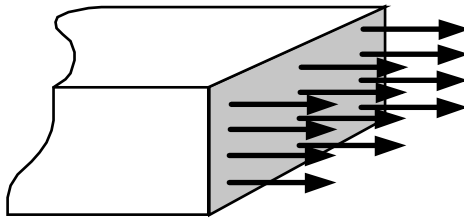
Ideal gas so:

$$v = \frac{RT}{P} = \frac{0.287 \text{ kJ/kg-K} \times 308.2 \text{ K}}{105 \text{ kPa}} = 0.8424 \text{ m}^3/\text{kg}$$

and the volumetric flow rate from Eq. 4.3,

$$\dot{V} = \dot{m}v = A\mathbf{V} = 0.015 \text{ kg/s} \times 0.8424 \text{ m}^3/\text{kg} = \mathbf{0.01264 \text{ m}^3/\text{s}}$$

$$\mathbf{V} = \frac{\dot{V}}{A} = \frac{0.01264 \text{ m}^3/\text{s}}{0.015 \text{ m}^2} = \mathbf{0.84 \text{ m/s}}$$



4.13

A pool is to be filled with 60 m^3 water from a garden hose of 2.5 cm diameter flowing water at 2 m/s. Find the mass flow rate of water and the time it takes to fill the pool.

Solution:

With constant velocity we have

$$\dot{V} = \dot{m}v = A\mathbf{V} = \pi \times (0.025 \text{ m})^2 \times 2 \text{ m/s} = 0.003927 \text{ m}^3/\text{s}$$

$$\Delta t = V / \dot{V} = 60 \text{ m}^3 / (0.003927 \text{ m}^3/\text{s}) = 15279 \text{ s} = \mathbf{4 \text{ h } 14 \text{ min } 39 \text{ s}}$$

From table A.3 we get the water density

$$\dot{m} = \dot{V} / v = \rho \dot{V} = 997 \text{ kg/m}^3 \times 0.003927 \text{ m}^3/\text{s} = \mathbf{3.9 \text{ kg/s}}$$

4.14

An empty bathtub has its drain closed and is being filled with water from the faucet at a rate of 10 kg/min. After 10 minutes the drain is opened and 4 kg/min flows out and at the same time the inlet flow is reduced to 2 kg/min. Plot the mass of the water in the bathtub versus time and determine the time from the very beginning when the tub will be empty.

Solution:

During the first 10 minutes we have

$$\frac{dm_{cv}}{dt} = \dot{m}_i = 10 \text{ kg/min}, \quad \Delta m = \dot{m} \Delta t_1 = 10 \times 10 = 100 \text{ kg}$$

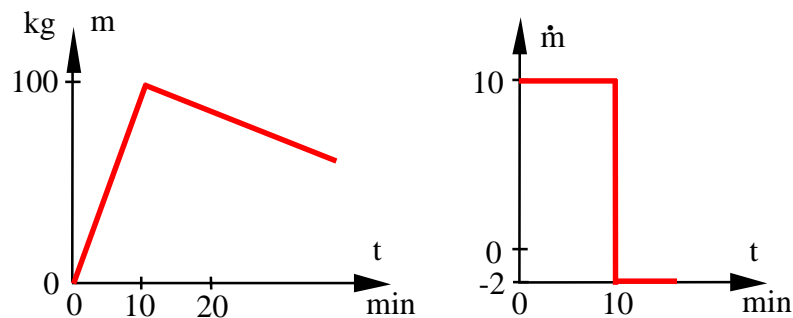
So we end up with 100 kg after 10 min. For the remaining period we have

$$\frac{dm_{cv}}{dt} = \dot{m}_i - \dot{m}_e = 2 - 4 = -2 \text{ kg/min}$$

$$\Delta m_2 = \dot{m}_{net} \Delta t_2 \rightarrow \Delta t_2 = \frac{\Delta m}{\dot{m}_{net}} = -100/-2 = 50 \text{ min.}$$

So it will take an additional 50 min. to empty

$$\Delta t_{tot} = \Delta t_1 + \Delta t_2 = 10 + 50 = \mathbf{60 \text{ min.}}$$



4.15

A flat channel of depth 1 m has a fully developed laminar flow of air at P_o , T_o with a velocity profile as: $V = 4V_c x(H - x)/H^2$, where V_c is the velocity on the center-line and x is the distance across the channel as shown in Fig. P4.15. Find the total mass flow rate and the average velocity both as functions of V_c and H .

$$\dot{m} = AV/v = \dot{V}/v$$

Since the velocity is distributed we need to integrate over the area. From Eq.4.2

$$\dot{V} = \int V_{\text{local}} dA = \int V(x) W dx$$

where W is the depth. Substituting the velocity we get

$$\begin{aligned}\dot{V} &= \int 4V_c (x/H) (1 - x/H) W dx \\ &= 4 V_c WH \int_0^1 z (1 - z) dz \quad (z = x/H) \\ &= 4 V_c WH \left(\frac{1}{2} z^2 - \frac{1}{3} z^3 \right) \Big|_0^1 = \frac{2}{3} V_c WH = \frac{2}{3} V_c A\end{aligned}$$

Average velocity: $V = \dot{V}/A = \frac{2}{3} V_c$

Mass flow rate: $\dot{m} = \dot{V}/v = \frac{2}{3} V_c WH/v$

4.16

Nitrogen gas flowing in a 50-mm diameter pipe at 15°C, 200 kPa, at the rate of 0.05 kg/s, encounters a partially closed valve. If there is a pressure drop of 30 kPa across the valve and essentially no temperature change, what are the velocities upstream and downstream of the valve?

Solution:

Same inlet and exit area: $A = \frac{\pi}{4} (0.050)^2 = 0.001963 \text{ m}^2$

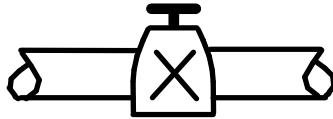
Ideal gas: $v_i = \frac{RT_i}{P_i} = \frac{0.2968 \text{ kJ/kg-K} \times 288.2 \text{ K}}{200 \text{ kPa}} = 0.4277 \text{ m}^3/\text{kg}$

From Eq.6.3,

$$V_i = \frac{\dot{m}v_i}{A} = \frac{0.05 \text{ kg/s} \times 0.4277 \text{ m}^3/\text{kg}}{0.001963 \text{ m}^2} = \mathbf{10.9 \text{ m/s}}$$

Ideal gas: $v_e = \frac{RT_e}{P_e} = \frac{0.2968 \text{ kJ/kg-K} \times 288.2 \text{ K}}{170 \text{ kPa}} = 0.5032 \text{ m}^3/\text{kg}$

$$V_e = \frac{\dot{m}v_e}{A} = \frac{0.05 \text{ kg/s} \times 0.5032 \text{ m}^3/\text{kg}}{0.001963 \text{ m}^2} = \mathbf{12.8 \text{ m/s}}$$



4.17

A boiler receives a constant flow of 5000 kg/h liquid water at 5 MPa, 20°C and it heats the flow such that the exit state is 450°C with a pressure of 4.5 MPa. Determine the necessary minimum pipe flow area in both the inlet and exit pipe(s) if there should be no velocities larger than 20 m/s.

Solution:

Mass flow rate from Eq. 4.3, both $\mathbf{V} \leq 20$ m/s

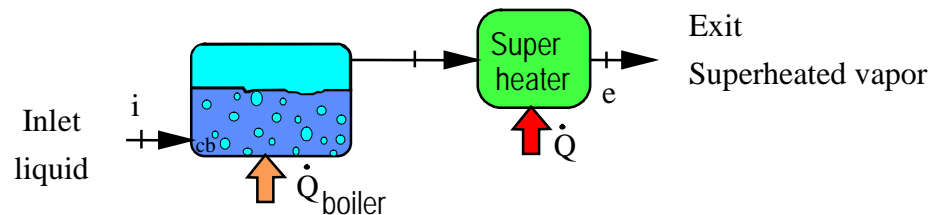
$$\dot{m}_i = \dot{m}_e = (A\mathbf{V}/v)_i = (A\mathbf{V}/v)_e = 5000 \frac{1}{3600} \text{ kg/s}$$

Table B.1.4 $v_i = 0.001 \text{ m}^3/\text{kg},$

Table B.1.3 $v_e = (0.08003 + 0.0633)/2 = 0.07166 \text{ m}^3/\text{kg},$

$$\begin{aligned} A_i &\geq v_i \dot{m}/\mathbf{V}_i = 0.001 \text{ m}^3/\text{kg} \times \frac{5000}{3600} \text{ kg/s} / 20 \text{ m/s} \\ &= 6.94 \times 10^{-5} \text{ m}^2 = \mathbf{0.69 \text{ cm}^2} \end{aligned}$$

$$\begin{aligned} A_e &\geq v_e \dot{m}/\mathbf{V}_e = 0.07166 \text{ m}^3/\text{kg} \times \frac{5000}{3600} \text{ kg/s} / 20 \text{ m/s} \\ &= 4.98 \times 10^{-3} \text{ m}^2 = \mathbf{50 \text{ cm}^2} \end{aligned}$$



4.18

A 0.6 m diameter household fan takes air in at 98 kPa, 20°C and delivers it at 105 kPa, 21°C with a velocity of 1.5 m/s. What are the mass flow rate (kg/s), the inlet velocity and the outgoing volume flow rate in m³/s?

Solution:

$$\begin{array}{ll} \text{Continuity Eq.} & \dot{m}_i = \dot{m}_e = A\mathbf{V}/v \\ \text{Ideal gas} & v = RT/P \end{array}$$

$$\text{Area : } A = \frac{\pi}{4} D^2 = \frac{\pi}{4} \times 0.6^2 = 0.2827 \text{ m}^2$$

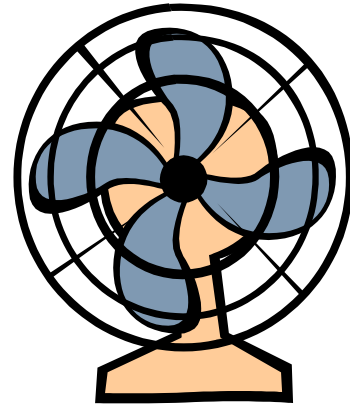
$$\dot{V}_e = A\mathbf{V}_e = 0.2827 \times 1.5 = \mathbf{0.4241 \text{ m}^3/\text{s}}$$

$$v_e = \frac{RT_e}{P_e} = \frac{0.287 \times (21 + 273)}{105} = 0.8036 \text{ m}^3/\text{kg}$$

$$\dot{m}_i = \dot{V}_e/v_e = 0.4241/0.8036 = \mathbf{0.528 \text{ kg/s}}$$

$$A\mathbf{V}_i/v_i = \dot{m}_i = A\mathbf{V}_e/v_e$$

$$\mathbf{V}_i = \mathbf{V}_e \times (v_i/v_e) = \mathbf{V}_e \times \frac{RT_i}{P_i v_e} = 1.5 \times \frac{0.287 \text{ kJ/kg-K} \times (20 + 273) \text{ K}}{98 \text{ kPa} \times 0.8036 \text{ m}^3/\text{kg}} = \mathbf{1.6 \text{ m/s}}$$



4.19

An airport ventilation system takes $2.5 \text{ m}^3/\text{s}$ air at 100 kPa , 17°C into a furnace and heats it to 52°C and delivers the flow to a duct with cross-sectional area 0.4 m^2 at 110 kPa . Find the mass flow rate and the velocity in the duct?

Solution:

The inflow flow is given by a \dot{m}_i

Continuity Eq.: $\dot{m}_i = \dot{V}_i / v_i = \dot{m}_e = A_e \mathbf{V}_e / v_e$

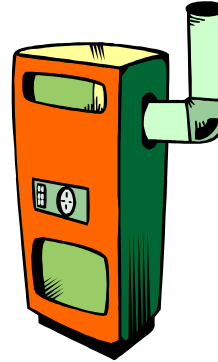
$$\text{Ideal gas: } v_i = \frac{RT_i}{P_i} = \frac{0.287 \times 290}{100} = 0.8323 \frac{\text{m}^3}{\text{kg}}$$

$$v_e = \frac{RT_e}{P_e} = \frac{0.287 \times (52 + 273)}{110}$$

$$= 0.8479 \text{ m}^3/\text{kg}$$

$$\dot{m}_i = \dot{V}_i / v_i = 2.5 (\text{m}^3/\text{s}) / 0.8323 (\text{m}^3/\text{kg}) = 3.004 \text{ kg/s}$$

$$\mathbf{V}_e = \dot{m} v_e / A_e = \frac{3.004 \times 0.8479}{0.4} \frac{\text{m}^3/\text{s}}{\text{m}^2} = \mathbf{6.37 \text{ m/s}}$$



Single flow single device processes

Nozzles, diffusers

4.20

Liquid water at 15°C flows out of a nozzle straight up 15 m. What is nozzle \mathbf{V}_{exit} ?

$$\text{Energy Eq.4.13: } h_{\text{exit}} + \frac{1}{2} \mathbf{V}_{\text{exit}}^2 + gH_{\text{exit}} = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gH_2$$

If the water can flow 15 m up it has specific potential energy of gH_2 which must equal the specific kinetic energy out of the nozzle $\mathbf{V}_{\text{exit}}^2/2$. The water does not change P or T so h is the same.

$$\begin{aligned} \mathbf{V}_{\text{exit}}^2/2 &= g(H_2 - H_{\text{exit}}) = gH \Rightarrow \\ \mathbf{V}_{\text{exit}} &= \sqrt{2gH} = \sqrt{2 \times 9.807 \times 15 \text{ m}^2/\text{s}^2} = \mathbf{17.15 \text{ m/s}} \end{aligned}$$



4.21

A nozzle receives an ideal gas flow with a velocity of 25 m/s, and the exit is at 100 kPa, 300 K with a velocity of 250 m/s. Determine the inlet temperature if the gas is argon, helium or nitrogen.

Solution:

C.V. Nozzle: $\dot{m}_i = \dot{m}_e$ & assume no heat transfer \Rightarrow

Energy Eq.4.13: $h_i + \frac{1}{2} \mathbf{V}_i^2 = \frac{1}{2} \mathbf{V}_e^2 + h_e \Rightarrow h_i = h_e + \frac{1}{2} \mathbf{V}_e^2 - \frac{1}{2} \mathbf{V}_i^2$

$$h_i - h_e \approx C_p (T_i - T_e) = \frac{1}{2} (\mathbf{V}_e^2 - \mathbf{V}_i^2) = \frac{1}{2} (250^2 - 25^2) \text{ m}^2/\text{s}^2$$

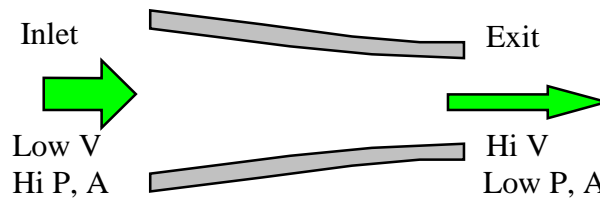
$$= 30937.5 \text{ J/kg} = 30.938 \text{ kJ/kg}$$

Specific heats for ideal gases are from table A.5

Argon $C_p = 0.52 \text{ kJ/kg K}$; $\Delta T = \frac{30.938}{0.52} = 59.5$ **$T_i = 359.5 \text{ K}$**

Helium $C_p = 5.193 \text{ kJ/kg K}$; $\Delta T = \frac{30.938}{5.193} = 5.96$ **$T_i = 306 \text{ K}$**

Nitrogen $C_p = 1.042 \text{ kJ/kg K}$; $\Delta T = \frac{30.938}{1.042} = 29.7$ **$T_i = 330 \text{ K}$**



4.22

A diffuser receives 0.1 kg/s steam at 500 kPa, 350°C. The exit is at 1 MPa, 400°C with negligible kinetic energy and the flow is adiabatic. Find the diffuser inlet velocity and the inlet area.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process: } Z_1 = Z_2$$

$$\text{State 1: Table B.1.3 } h_1 = 3167.65 \text{ kJ/kg, } v_1 = 0.57012 \text{ m}^3/\text{kg}$$

$$\text{State 2: } \mathbf{V}_2 = 0, \text{ Table B.1.3 } h_2 = 3263.88 \text{ kJ/kg}$$

Then from the energy equation

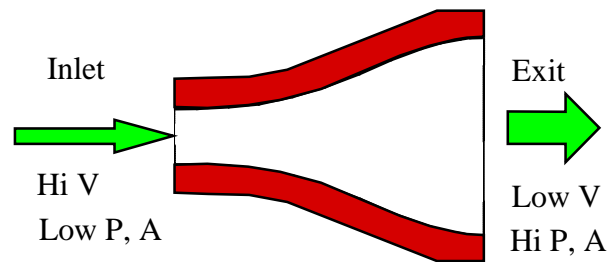
$$\frac{1}{2} \mathbf{V}_1^2 = h_2 - h_1 = 3263.88 - 3167.65 = 96.23 \text{ kJ/kg}$$

$$\mathbf{V}_1 = \sqrt{2(h_2 - h_1)} = \sqrt{2 \times 96.23 \times 1000} = \mathbf{438.7 \text{ m/s}}$$

The mass flow rate from Eq.4.3

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V} / v$$

$$A = \dot{m} v / \mathbf{V} = 0.1 \text{ kg/s} \times 0.57012 \text{ m}^3/\text{kg} / 438.7 \text{ m/s} = 0.00013 \text{ m}^2 = \mathbf{1.3 \text{ cm}^2}$$



4.23

In a jet engine a flow of air at 1000 K, 200 kPa and 30 m/s enters a nozzle, as shown in Fig. P4.23, where the air exits at 850 K, 90 kPa. What is the exit velocity assuming no heat loss?

Solution:

C.V. nozzle. No work, no heat transfer

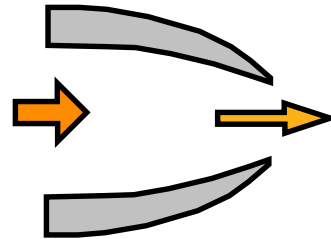
$$\text{Continuity} \quad \dot{m}_i = \dot{m}_e = \dot{m}$$

$$\text{Energy :} \quad \dot{m} (h_i + \frac{1}{2} \mathbf{V}_i^2) = \dot{m} (h_e + \frac{1}{2} \mathbf{V}_e^2)$$

Due to high T take h from table A.7.1

$$\begin{aligned} \frac{1}{2} \mathbf{V}_e^2 &= \frac{1}{2} \mathbf{V}_i^2 + h_i - h_e \\ &= \frac{1}{2000} (30)^2 + 1046.22 - 877.4 \\ &= 0.45 + 168.82 = 169.27 \text{ kJ/kg} \end{aligned}$$

$$\mathbf{V}_e = (2000 \times 169.27)^{1/2} = \mathbf{581.8 \text{ m/s}}$$



4.24

In a jet engine a flow of air at 1000 K, 200 kPa and 40 m/s enters a nozzle where the air exits at 500 m/s, 90 kPa. What is the exit temperature assuming no heat loss?

Solution:

C.V. nozzle, no work, no heat transfer

Continuity $\dot{m}_i = \dot{m}_e = \dot{m}$

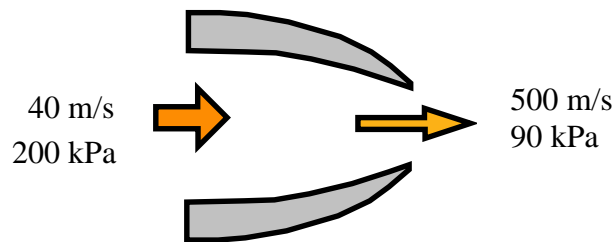
Energy : $\dot{m} (h_i + \frac{1}{2} \mathbf{V}_i^2) = \dot{m} (h_e + \frac{1}{2} \mathbf{V}_e^2)$

Due to the high T we take the h value from Table A.7.1

$$\begin{aligned} h_e &= h_i + \frac{1}{2} \mathbf{V}_i^2 - \frac{1}{2} \mathbf{V}_e^2 \\ &= 1046.22 \text{ kJ/kg} + 0.5 \times (40^2 - 500^2) \text{ m}^2/\text{s}^2 \times (1/1000) \text{ kJ/J} \\ &= 1046.22 - 124.2 = 922.02 \text{ kJ/kg} \end{aligned}$$

Interpolation in Table A.7.1

$$T_e = 850 + 50 \frac{922.02 - 877.4}{933.15 - 877.4} = \mathbf{890 \text{ K}}$$



4.25

Superheated vapor ammonia enters an insulated nozzle at 30°C, 1000 kPa, shown in Fig. P4.25, with a low velocity and at the steady rate of 0.01 kg/s. The ammonia exits at 300 kPa with a velocity of 450 m/s. Determine the temperature (or quality, if saturated) and the exit area of the nozzle.

Solution:

C.V. Nozzle, steady state, 1 inlet and 1 exit flow, insulated so no heat transfer.

$$\text{Energy Eq.4.13: } q + h_i + \mathbf{V}_i^2/2 = h_e + \mathbf{V}_e^2/2,$$

$$\text{Process: } q = 0, \quad \mathbf{V}_i = 0$$

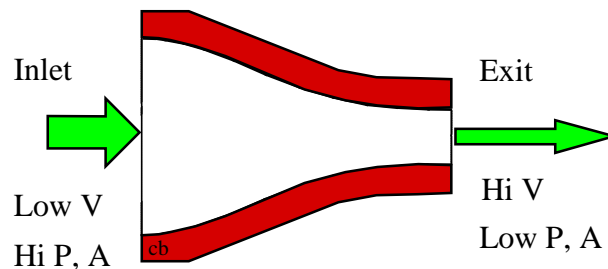
$$\text{Table B.2.2: } h_i = 1479.1 = h_e + 450^2/(2 \times 1000) \Rightarrow h_e = 1377.85 \text{ kJ/kg}$$

$$\text{Table B.2.1: } P_e = 300 \text{ kPa Sat. state at } -9.24^\circ\text{C} :$$

$$h_e = 1377.85 = 137.89 + x_e \times 1293.82,$$

$$\Rightarrow x_e = \mathbf{0.9584}, \quad v_e = 0.001536 + x_e \times 0.40566 = 0.3903 \text{ m}^3/\text{kg}$$

$$A_e = \dot{m}_e v_e / \mathbf{V}_e = 0.01 \times 0.3903 / 450 = \mathbf{8.67 \times 10^{-6} \text{ m}^2}$$



4.26

The wind is blowing horizontally at 30 m/s in a storm at P_0 , 20°C toward a wall, where it comes to a stop (stagnation) and leaves with negligible velocity similar to a diffuser with a very large exit area. Find the stagnation temperature from the energy equation.

Solution:

$$\text{Energy Eq.:} \quad h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process:} \quad Z_1 = Z_2 \quad \text{and} \quad V_2 = 0$$

$$h_2 = h_1 + \frac{1}{2} \mathbf{V}_1^2$$

$$\begin{aligned} T_2 &= T_1 + \frac{1}{2} \times (\mathbf{V}_1^2 / C_p) \\ &= 293 \text{ K} + \frac{1}{2} \times (30 \text{ m/s})^2 / (1.004 \text{ kJ/kg-K} \times 1000 \text{ J/kJ}) \\ &= \mathbf{293.45 \text{ K}} \end{aligned}$$

4.27

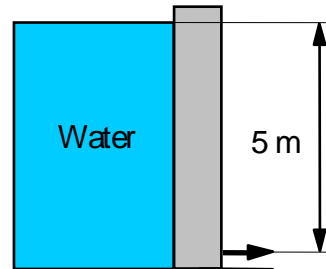
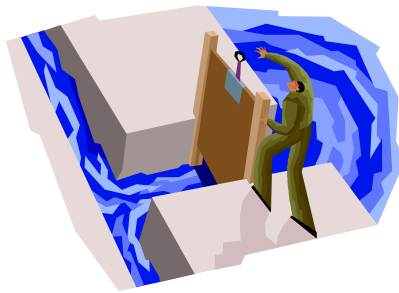
A sluice gate dams water up 5 m. There is a small hole at the bottom of the gate so liquid water at 20°C comes out of a 1 cm diameter hole. Neglect any changes in internal energy and find the exit velocity and mass flow rate.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process: } h_1 = h_2 \quad \text{both at } P = 1 \text{ atm}$$

$$V_1 = 0 \quad Z_1 = Z_2 + 5 \text{ m}$$



$$\frac{1}{2} \mathbf{V}_2^2 = g (Z_1 - Z_2)$$

$$\mathbf{V}_2 = \sqrt{2g(Z_1 - Z_2)} = \sqrt{2 \times 9.806 \times 5} = \mathbf{9.902 \text{ m/s}}$$

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V} / v = \frac{\pi}{4} D^2 \times (\mathbf{V}_2 / v)$$

$$= \frac{\pi}{4} \times (0.01)^2 \text{ m}^2 \times (9.902 \text{ m/s}) / (0.001002 \text{ m}^3/\text{kg}) = \mathbf{0.776 \text{ kg/s}}$$

4.28

A diffuser, shown in Fig. P4.28, has air entering at 100 kPa, 300 K, with a velocity of 200 m/s. The inlet cross-sectional area of the diffuser is 100 mm². At the exit, the area is 860 mm², and the exit velocity is 20 m/s. Determine the exit pressure and temperature of the air.

Solution:

$$\text{Continuity Eq. 4.3:} \quad \dot{m}_i = A_i \mathbf{V}_i / v_i = \dot{m}_e = A_e \mathbf{V}_e / v_e,$$

$$\text{Energy Eq. (per unit mass flow) 4.13:} \quad h_i + \frac{1}{2} \mathbf{V}_i^2 = h_e + \frac{1}{2} \mathbf{V}_e^2$$

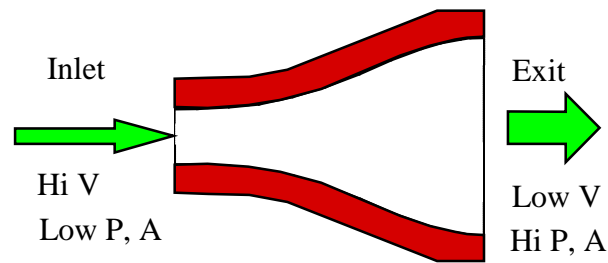
$$h_e - h_i = \frac{1}{2} \times 200^2 / 1000 - \frac{1}{2} \times 20^2 / 1000 = 19.8 \text{ kJ/kg}$$

$$T_e = T_i + (h_e - h_i) / C_p = 300 + \frac{19.8 \text{ kJ/kg}}{1.004 \text{ kJ/kg-K}} = \mathbf{319.72 \text{ K}}$$

Now use the continuity equation and the ideal gas law

$$v_e = v_i \left(\frac{A_e \mathbf{V}_e}{A_i \mathbf{V}_i} \right) = (RT_i / P_i) \left(\frac{A_e \mathbf{V}_e}{A_i \mathbf{V}_i} \right) = RT_e / P_e$$

$$P_e = P_i \left(\frac{T_e}{T_i} \right) \left(\frac{A_i \mathbf{V}_i}{A_e \mathbf{V}_e} \right) = 100 \text{ kPa} \left(\frac{319.72}{300} \right) \left(\frac{100 \times 200}{860 \times 20} \right) = \mathbf{123.92 \text{ kPa}}$$



4.29

A meteorite hits the upper atmosphere at 3000 m/s, where the pressure is 0.1 atm and the temperature is -40°C . How hot does the air become right in front of the meteorite assuming no heat transfer in this adiabatic stagnation process?

Solution:

$$\text{Energy Eq.: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$h_2 = h_1 + \frac{1}{2} \mathbf{V}_1^2$$

$$T_2 = T_1 + \frac{1}{2} \times (\mathbf{V}_1^2 / C_p) = 233 + \frac{1}{2} \times \frac{3000^2}{1.004 \times 1000} = \mathbf{4715 \text{ K}}$$

At this high temperature we cannot assume constant specific heats, so use A.7

$$h_2 = h_1 + \frac{1}{2} \mathbf{V}_1^2 = 233.3 + \frac{1}{2} \times \frac{3000^2}{1000} = 4733.3 \text{ kJ/kg}$$

Table A.7 is listed to 3000 K so we have to extrapolate to get

$$T_2 = 3000 + 50 \frac{4733.3 - 3525.36}{3525.36 - 3460.73} = \mathbf{3935 \text{ K}}$$

The value of C_p over 3000 K is 1.293 kJ/kgK from the last two table entries. At this temperature there will be some chemical reactions that should be considered to have a more realistic temperature.

4.30

The front of a jet engine acts similar to a diffuser, receiving air at 900 km/h, -5°C , 50 kPa, bringing it to 80 m/s relative to the engine before entering the compressor. If the flow area is increased to 120% of the inlet area, find the temperature and pressure in the compressor inlet.

Solution:

C.V. Diffuser, Steady state, 1 inlet, 1 exit flow, no q, no w.

$$\text{Continuity Eq.4.3: } \dot{m}_i = \dot{m}_e = (A\mathbf{V}/v)$$

$$\text{Energy Eq.4.12: } \dot{m} \left(h_i + \frac{1}{2} \mathbf{V}_i^2 \right) = \dot{m} \left(\frac{1}{2} \mathbf{V}_e^2 + h_e \right)$$

$$\begin{aligned} h_e - h_i &= C_p (T_e - T_i) = \frac{1}{2} \mathbf{V}_i^2 - \frac{1}{2} \mathbf{V}_e^2 = \frac{1}{2} \left(\frac{900 \times 1000}{3600} \right)^2 - \frac{1}{2} (80)^2 \\ &= \frac{1}{2} (250)^2 - \frac{1}{2} (80)^2 = 28050 \text{ J/kg} = 28.05 \text{ kJ/kg} \end{aligned}$$

$$\Delta T = 28.05/1.004 = 27.9 \Rightarrow T_e = -5 + 27.9 = \mathbf{22.9^{\circ}\text{C}}$$

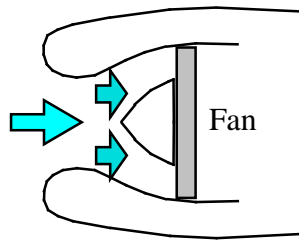
Now use the continuity eq.:

$$A_i \mathbf{V}_i / v_i = A_e \mathbf{V}_e / v_e \Rightarrow v_e = v_i \left(\frac{A_e \mathbf{V}_e}{A_i \mathbf{V}_i} \right)$$

$$v_e = v_i \times \frac{1.2 \times 80}{1 \times 250} = v_i \times 0.384$$

$$\text{Ideal gas: } Pv = RT \Rightarrow v_e = RT_e/P_e = RT_i \times 0.384/P_i$$

$$P_e = P_i (T_e/T_i)/0.384 = 50 \text{ kPa} \times 296/(268 \times 0.384) = \mathbf{143.8 \text{ kPa}}$$



Throttle flow

4.31

R-410A at -5°C , 700 kPa is throttled, so it becomes cold at -40°C . What is the exit P?

C.V. Throttle. Steady state,

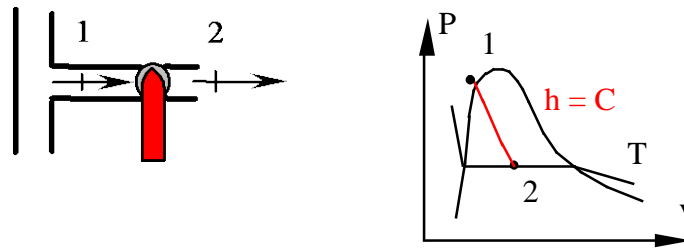
Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

Energy Eq.4.13: $h_i = h_e$,

Inlet state: Table B.4.1 $h_i = 50.22 \text{ kJ/kg}$ (slightly compressed liquid)

Exit state: Table B.4.1 since $h < h_g = 262.83 \text{ kJ/kg}$ it is two-phase

$P = P_{\text{sat}} = \mathbf{175 \text{ kPa}}$



4.32

Carbon dioxide is throttled from 20°C, 2 MPa to 800 kPa. Find the exit temperature assuming ideal gas behavior and repeat for real-gas behavior.

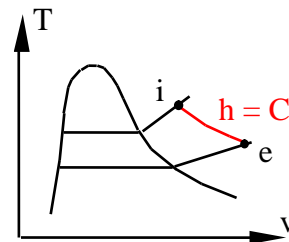
C.V. Throttle (valve, restriction), Steady flow, 1 inlet and exit, no q , w

Energy Eq.4.13: $h_i = h_e$

Ideal gas: same h gives $T_i = T_e = 20^\circ\text{C}$

Real gas : $\left. \begin{array}{l} h_i = h_e = 368.42 \text{ kJ/kg} \\ P_e = 0.8 \text{ MPa} \end{array} \right\} \begin{array}{l} \text{Table B.3.2} \\ T_e = 5.3^\circ\text{C} (= 278 \text{ K}) \end{array}$

Comment: As you go towards lower P it becomes closer to ideal gas and the constant h curve bends to become horizontal (h becomes fct of T only)



4.33

Saturated liquid R-134a at 25°C is throttled to 300 kPa in a refrigerator. What is the exit temperature? Find the percent increase in the volume flow rate.

Solution:

Steady throttle flow. Assume no heat transfer and no change in kinetic or potential energy.

$$h_e = h_i = h_{f\ 25^\circ\text{C}} = 234.59\ \text{kJ/kg} = h_{f\ e} + x_e h_{fg\ e} \quad \text{at 300 kPa}$$

From table B.5.1 we get $T_e = T_{\text{sat}}(300\ \text{kPa}) = \mathbf{0.56^\circ\text{C}}$

Let's use 0°C for the following (we could interpolate to get at 0.56°C)

$$x_e = \frac{h_e - h_{f\ e}}{h_{fg\ e}} = \frac{234.59 - 200}{198.36} = 0.1744$$

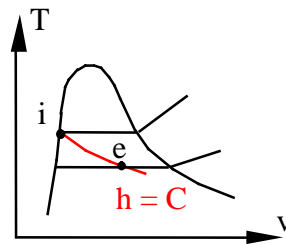
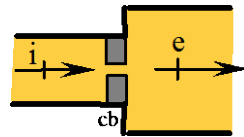
$$v_e = v_f + x_e v_{fg} = 0.000773 + x_e 0.06842 = 0.0127\ \text{m}^3/\text{kg}$$

$$v_i = v_{f\ 25^\circ\text{C}} = 0.000829\ \text{m}^3/\text{kg}$$

$\dot{V} = \dot{m}v$ so the ratio becomes

$$\frac{\dot{V}_e}{\dot{V}_i} = \frac{\dot{m}v_e}{\dot{m}v_i} = \frac{v_e}{v_i} = \frac{0.0127}{0.000829} = \mathbf{15.32}$$

So the increase is 14.32 times or **1432 %**



4.34

A supply line has a steady flow of R-410A at 1000 kPa, 60°C from which a flow is taken out through a throttle with an exit flow at 300 kPa. Find the exit temperature.

C.V. Throttle. Steady state,

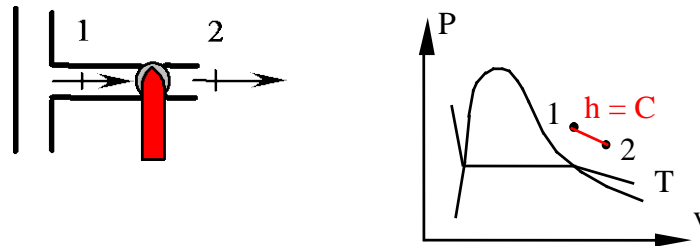
Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

Energy Eq.4.13: $h_i = h_e$,

Inlet state: Table B.4.2 $h_i = 335.75 \text{ kJ/kg}$

Exit state: Table B.4.2 since $h > h_g$

Interpolate: $T = 40 + 20 \frac{335.75 - 327.22}{344.81 - 327.22} = 49.7^\circ\text{C}$,



4.35

Carbon dioxide used as a natural refrigerant flows out of a cooler at 10 MPa, 40°C after which it is throttled to 1.4 MPa. Find the state (T, x) for the exit flow.

C.V. Throttle. Steady state,

Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

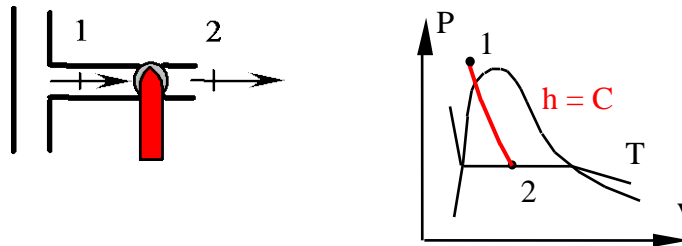
Energy Eq.4.13: $h_i = h_e$,

Inlet state: Table B.3.2 $h_i = 200.14$ kJ/kg

Exit state: Table B.3.1 since $h < h_g = 323.87$ kJ/kg

Interpolate: $T = -30.6^\circ\text{C}$, $h_f = 19.2$ kJ/kg, $h_{fg} = 304.67$ kJ/kg

$$x = (200.14 - 19.2) / 304.67 = \mathbf{0.594}$$



4.36

Liquid water at 180°C, 2000 kPa is throttled into a flash evaporator chamber having a pressure of 500 kPa. Neglect any change in the kinetic energy. What is the fraction of liquid and vapor in the chamber?

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

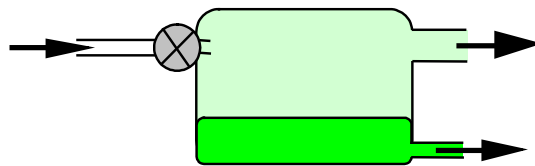
$$\begin{aligned} \text{Process: } Z_1 &= Z_2 \quad \text{and} \quad \mathbf{V}_2 = \mathbf{V}_1 \\ \Rightarrow h_2 &= h_1 = 763.71 \text{ kJ/kg} \quad \text{from Table B.1.4} \end{aligned}$$

$$\text{State 2: } P_2 \text{ \& } h_2 \Rightarrow 2\text{-phase}$$

$$h_2 = h_f + x_2 h_{fg}$$

$$x_2 = (h_2 - h_f) / h_{fg} = \frac{763.71 - 640.21}{2108.47} = 0.0586$$

Fraction of	Vapor: $x_2 = 0.0586$	(5.86 %)
	Liquid: $1 - x_2 = 0.941$	(94.1 %)



Two-phase out of the valve. The liquid drops to the bottom.

4.37

Helium is throttled from 1.2 MPa, 20°C, to a pressure of 100 kPa. The diameter of the exit pipe is so much larger than the inlet pipe that the inlet and exit velocities are equal. Find the exit temperature of the helium and the ratio of the pipe diameters.

Solution:

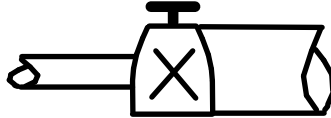
C.V. Throttle. Steady state,

Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

Energy Eq.4.13: $h_i = h_e$, Ideal gas $\Rightarrow T_i = T_e = 20^\circ\text{C}$

$$\dot{m} = \frac{A V}{R T / P} \quad \text{But } \dot{m}, V, T \text{ are constant} \Rightarrow P_i A_i = P_e A_e$$

$$\Rightarrow \frac{D_e}{D_i} = \left(\frac{P_i}{P_e} \right)^{1/2} = \left(\frac{1.2}{0.1} \right)^{1/2} = 3.464$$



4.38

Methane at 1 MPa, 300 K is throttled through a valve to 100 kPa. Assume no change in the kinetic energy. What is the exit temperature?

Solution:

Energy Eq. 4.13: $h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$

Process: $Z_1 = Z_2$ and $\mathbf{V}_2 = \mathbf{V}_1$

State 1, Table B.7.2: $h_1 = 618.76 \text{ kJ/kg}$

Use energy eq.: $\Rightarrow h_2 = h_1 = 618.76 \text{ kJ/kg}$

State 2: $P_2 \text{ \& } h_2 \Rightarrow \text{look in B.7.2 : Superheated vapor}$

$$T_2 = 275 + 25 \frac{618.76 - 572.36}{627.58 - 572.36} = \mathbf{296 \text{ K}}$$

Notice if it had been ideal gas then $T_2 = T_1$

4.39

R-134a is throttled in a line flowing at 25°C, 750 kPa with negligible kinetic energy to a pressure of 165 kPa. Find the exit temperature and the ratio of exit pipe diameter to that of the inlet pipe ($D_{\text{ex}}/D_{\text{in}}$) so the velocity stays constant.

Solution:

Energy Eq.4.13: $h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$

Process: $Z_1 = Z_2$ and $\mathbf{V}_2 = \mathbf{V}_1$

State 1, Table B.5.1: $h_1 = 234.59 \text{ kJ/kg}$, $v_1 = v_f = 0.000829 \text{ m}^3/\text{kg}$

Use energy eq.: $\Rightarrow h_2 = h_1 = 234.59 \text{ kJ/kg}$

State 2: $P_2 \text{ \& } h_2 \Rightarrow 2\text{-phase}$ and $T_2 = T_{\text{sat}}(165 \text{ kPa}) = \mathbf{-15^\circ\text{C}}$

$$h_2 = h_f + x_2 h_{fg} = 234.59 \text{ kJ/kg}$$

$$x_2 = (h_2 - h_f) / h_{fg} = (234.59 - 180.19) / 209 = 0.2603$$

$$v_2 = v_f + x_2 \times v_{fg} = 0.000746 + 0.2603 \times 0.11932 = 0.0318 \text{ m}^3/\text{kg}$$

Now the continuity equation with $\mathbf{V}_2 = \mathbf{V}_1$ gives, from Eq.4.3,

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V} / v = A_1 \mathbf{V}_1 / v_1 = (A_2 \mathbf{V}_1) / v_2$$

$$(A_2 / A_1) = v_2 / v_1 = (D_2 / D_1)^2$$

$$(D_2 / D_1) = (v_2 / v_1)^{0.5} = (0.0318 / 0.000829)^{0.5} = \mathbf{6.19}$$

Turbines, Expanders

4.40

A steam turbine has an inlet of 3 kg/s water at 1200 kPa, 350°C and velocity of 15 m/s. The exit is at 100 kPa, 150°C and very low velocity. Find the specific work and the power produced.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$$

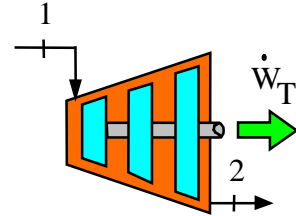
$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$\text{Table B.1.3: } h_1 = 3153.59 \text{ kJ/kg}, \quad h_2 = 2776.38 \text{ kJ/kg}$$

$$w_T = h_1 + \frac{1}{2} \mathbf{V}_1^2 - h_2 = 3153.59 + \frac{15^2}{2000} - 2776.38 = \mathbf{377.3 \text{ kJ/kg}}$$

(remember to convert $\text{m}^2/\text{s}^2 = \text{J/kg}$ to kJ/kg by dividing with 1000)

$$\begin{aligned} \dot{W}_T &= \dot{m} \times w_T = 3 \text{ kg/s} \times 377.3 \text{ kJ/kg} \\ &= \mathbf{1132 \text{ kW}} \end{aligned}$$



4.41

Air at 20 m/s, 1500 K, 875 kPa with 5 kg/s flows into a turbine and it flows out at 25 m/s, 850 K, 105 kPa. Find the power output using constant specific heats.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$$

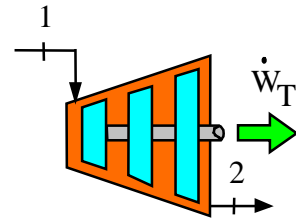
$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$\text{Table A.5: } C_p = 1.004 \text{ kJ/kg-K}$$

$$\begin{aligned} w_T &= h_1 + \frac{1}{2} \mathbf{V}_1^2 - h_2 - \frac{1}{2} \mathbf{V}_2^2 = C_p(T_1 - T_2) + \frac{1}{2} \mathbf{V}_1^2 - \frac{1}{2} \mathbf{V}_2^2 \\ &= 1.004 \text{ kJ/kg-K} \times (1500 - 850) \text{ K} + \frac{20^2 - 25^2}{2000} (\text{m}^2/\text{s}^2) \times (\text{kJ/J}) \\ &= \mathbf{652.5 \text{ kJ/kg}} \end{aligned}$$

(remember to convert $\text{m}^2/\text{s}^2 = \text{J/kg}$ to kJ/kg by dividing with 1000)

$$\begin{aligned} \dot{W}_T &= \dot{m} \times w_T = 5 \text{ kg/s} \times 652.5 \text{ kJ/kg} \\ &= \mathbf{3263 \text{ kW}} \end{aligned}$$



4.42

Solve the previous problem using Table A.7.

Air at 20 m/s, 1500 K, 875 kPa with 5 kg/s flows into a turbine and it flows out at 25 m/s, 850 K, 105 kPa. Find the power output using constant specific heats.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$$

$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$\text{Table A.7.1: } h_1 = 1635.8 \text{ kJ/kg}, \quad h_2 = 877.4 \text{ kJ/kg}$$

$$w_T = h_1 - h_2 + \frac{1}{2} \mathbf{V}_1^2 - \frac{1}{2} \mathbf{V}_2^2$$

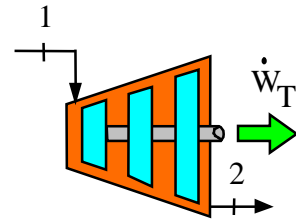
$$= (1635.8 - 877.4) \text{ kJ/kg} + \frac{20^2 - 25^2}{2000} (\text{m}^2/\text{s}^2) \times (\text{kJ/J})$$

$$= \mathbf{758.3 \text{ kJ/kg}}$$

(remember to convert $\text{m}^2/\text{s}^2 = \text{J/kg}$ to kJ/kg by dividing with 1000)

$$\dot{W}_T = \dot{m} \times w_T = 5 \text{ kg/s} \times 758.3 \text{ kJ/kg}$$

$$= \mathbf{3792 \text{ kW}}$$



4.43

A windmill with rotor diameter of 20 m takes 40% of the kinetic energy out as shaft work on a day with 20°C and wind speed of 35 km/h. What power is produced?

Solution:

Continuity Eq. $\dot{m}_i = \dot{m}_e = \dot{m}$

Energy $\dot{m} (h_i + \frac{1}{2} \mathbf{V}_i^2 + gZ_i) = \dot{m} (h_e + \frac{1}{2} \mathbf{V}_e^2 + gZ_e) + \dot{W}$

Process information: $\dot{W} = \dot{m} \frac{1}{2} \mathbf{V}_i^2 \times 0.4$

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V}_i / v_i$$

$$A = \frac{\pi}{4} D^2 = \frac{\pi}{4} 20^2 = 314.16 \text{ m}^2$$

$$v_i = RT_i / P_i = \frac{0.287 \times 293}{101.3} = 0.8301 \text{ m}^3/\text{kg}$$

$$\mathbf{V}_i = 35 \text{ km/h} = \frac{35 \times 1000}{3600} = 9.7222 \text{ m/s}$$

$$\dot{m} = A \mathbf{V}_i / v_i = \frac{314.16 \times 9.7222}{0.8301} = 3679.5 \text{ kg/s}$$

$$\frac{1}{2} \mathbf{V}_i^2 = \frac{1}{2} 9.7222^2 \text{ m}^2/\text{s}^2 = 47.26 \text{ J/kg}$$

$$\begin{aligned} \dot{W} &= 0.4 \dot{m} \frac{1}{2} \mathbf{V}_i^2 = 0.4 \times 3679.5 \text{ kg/s} \times 47.26 \text{ J/kg} = 69\,557 \text{ W} \\ &= \mathbf{69.56 \text{ kW}} \end{aligned}$$



4.44

A liquid water turbine receives 2 kg/s water at 2000 kPa, 20°C and velocity of 15 m/s. The exit is at 100 kPa, 20°C and very low velocity. Find the specific work and the power produced.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$$

$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$\text{State 1: } \text{Table B.1.4} \quad h_1 = 85.82 \text{ kJ/kg}$$

$$\text{State 2: } \text{Table B.1.1} \quad h_2 = 83.94 \quad (\text{which is at 2.3 kPa so we should add } \Delta P_v = 97.7 \times 0.001 \text{ to this})$$

$$w_T = h_1 + \frac{1}{2} \mathbf{V}_1^2 - h_2 = 85.82 + 15^2/2000 - 83.94 = \mathbf{1.9925 \text{ kJ/kg}}$$

$$\dot{W}_T = \dot{m} \times w_T = 2 \text{ kg/s} \times 1.9925 \text{ kJ/kg} = \mathbf{3.985 \text{ kW}}$$

Notice how insignificant the specific kinetic energy is.

4.45

What is the specific work one can expect from the dam in Problem 4.27?

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$$

$$\text{Process: } \mathbf{V}_2 = \mathbf{V}_1; \quad P_1 = P_2 = P_0; \quad h_1 = h_2$$

Same velocity if same flow area (incompressible flow) and the water temperature does not change significantly. The specific potential energy difference can be extracted

$$w_T = gZ_1 - gZ_2 = 9.806 \text{ m/s}^2 \times (5 - 0) \text{ m} = 49 \text{ m}^2/\text{s}^2 = \mathbf{49 \text{ J/kg}}$$

This is a very small amount of specific work.

4.46

A small, high-speed turbine operating on compressed air produces a power output of 100 W. The inlet state is 400 kPa, 50°C, and the exit state is 150 kPa, -30°C. Assuming the velocities to be low and the process to be adiabatic, find the required mass flow rate of air through the turbine.

Solution:

C.V. Turbine, no heat transfer, no ΔKE , no ΔPE

Energy Eq.4.13: $h_{in} = h_{ex} + w_T$

Ideal gas so use constant specific heat from Table A.5

$$\begin{aligned} w_T &= h_{in} - h_{ex} \cong C_p(T_{in} - T_{ex}) \\ &= 1.004 \text{ (kJ/kg-K)} [50 - (-30)] \text{ K} = 80.3 \text{ kJ/kg} \end{aligned}$$

$$\dot{W} = \dot{m} w_T \quad \Rightarrow \quad \dot{m} = \dot{W} / w_T = 0.1 \text{ kW} / 80.3 \text{ kJ/kg} = \mathbf{0.00125 \text{ kg/s}}$$

The dentist's drill has a small air flow and is not really adiabatic.

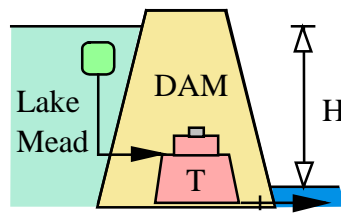


4.47

Hoover Dam across the Colorado River dams up Lake Mead 200 m higher than the river downstream. The electric generators driven by water-powered turbines deliver 1300 MW of power. If the water is 17.5°C, find the minimum amount of water running through the turbines.

Solution:

C.V.: H₂O pipe + turbines,



Continuity: $\dot{m}_{\text{in}} = \dot{m}_{\text{ex}}$;

Energy Eq.4.13: $(h + \mathbf{V}^2/2 + gz)_{\text{in}} = (h + \mathbf{V}^2/2 + gz)_{\text{ex}} + w_T$

Water states: $h_{\text{in}} \cong h_{\text{ex}}$; $v_{\text{in}} \cong v_{\text{ex}}$

Now the specific turbine work becomes

$$w_T = gz_{\text{in}} - gz_{\text{ex}} = 9.807 \times 200/1000 = 1.961 \text{ kJ/kg}$$

$$\dot{m} = \dot{W}_T / w_T = \frac{1300 \times 10^3 \text{ kW}}{1.961 \text{ kJ/kg}} = 6.63 \times 10^5 \text{ kg/s}$$

$$\dot{V} = \dot{m}v = 6.63 \times 10^5 \text{ kg/s} \times 0.001001 \text{ m}^3/\text{kg} = \mathbf{664 \text{ m}^3/\text{s}}$$

4.48

A small turbine, shown in Fig. P 4.48, is operated at part load by throttling a 0.25 kg/s steam supply at 1.4 MPa, 250°C down to 1.1 MPa before it enters the turbine and the exhaust is at 10 kPa. If the turbine produces 110 kW, find the exhaust temperature (and quality if saturated).

Solution:

C.V. Throttle, Steady, $q = 0$ and $w = 0$. No change in kinetic or potential energy. The energy equation then reduces to

Energy Eq.4.13: $h_1 = h_2 = 2927.2 \text{ kJ/kg}$ from Table B.1.3

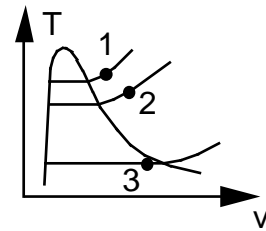
C.V. Turbine, Steady, no heat transfer, specific work: $w = \frac{110}{0.25} = 440 \text{ kJ/kg}$

Energy Eq.: $h_1 = h_2 = h_3 + w = 2927.2 \text{ kJ/kg}$

$$\Rightarrow h_3 = 2927.2 - 440 = 2487.2 \text{ kJ/kg}$$

State 3: (P, h) Table B.1.2 $h < h_g$
 $2487.2 = 191.83 + x_3 \times 2392.8$

$$\Rightarrow T = 45.8^\circ\text{C}, \quad x_3 = 0.959$$



4.49

A small expander (a turbine with heat transfer) has 0.05 kg/s helium entering at 1000 kPa, 550 K and it leaves at 250 kPa, 300 K. The power output on the shaft is measured to 55 kW. Find the rate of heat transfer neglecting kinetic energies.

Solution:

C.V. Expander. Steady operation

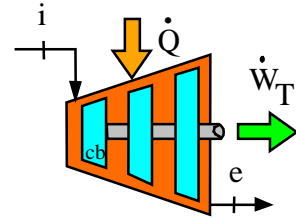
Cont. $\dot{m}_i = \dot{m}_e = \dot{m}$

Energy $\dot{m}h_i + \dot{Q} = \dot{m}h_e + \dot{W}$

$$\dot{Q} = \dot{m} (h_e - h_i) + \dot{W}$$

Use specific heat from Table A.5: $C_{p, \text{He}} = 5.193 \text{ kJ/kg} \cdot \text{K}$

$$\begin{aligned}\dot{Q} &= \dot{m} C_p (T_e - T_i) + \dot{W} \\ &= 0.05 \text{ kg/s} \times 5.193 \text{ kJ/kg} \cdot \text{K} \times (300 - 550) \text{ K} + 55 \text{ kW} \\ &= -64.91 + 55 = \mathbf{-9.9 \text{ kW}}\end{aligned}$$



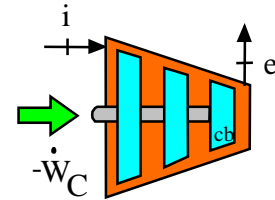
Compressors, fans

4.50

A compressor in a commercial refrigerator receives R-410A at -25°C , $x = 1$. The exit is at 1000 kPa, 40°C . Neglect kinetic energies and find the specific work.

Solution:

C.V. Compressor, steady state, single inlet and exit flow. For this device we also assume no heat transfer and $Z_i = Z_e$



From Table B.4.1 : $h_i = 269.77 \text{ kJ/kg}$

From Table B.4.2 : $h_e = 316.05 \text{ kJ/kg}$

Energy Eq.4.13 reduces to

$$w_c = h_i - h_e = (269.77 - 316.05) \text{ kJ/kg} = \mathbf{-46.28 \text{ kJ/kg}}$$

4.51

A compressor brings nitrogen from 100 kPa, 290 K to 2000 kPa. The process has a specific work input of 450 kJ/kg and the exit temperature is 450 K. Find the specific heat transfer using constant specific heats.

Solution:

C.V. Compressor. Not adiabatic, neglect kinetic and potential energy changes.

$$\text{Energy Eq.4.13: } q + h_i + \mathbf{V}_i^2/2 + gZ_i = h_e + \mathbf{V}_e^2/2 + w + gZ_e$$

$$\text{Process: } Z_i = Z_e ; \quad \mathbf{V}_i^2/2 = \mathbf{V}_e^2/2$$

Solve for the heat transfer

$$\begin{aligned} q &= h_e + w - h_i = C_p (T_e - T_i) + w \\ &= 1.042 \text{ kJ/kg-K} \times (450 - 290) \text{ K} - 450 \text{ kJ/kg} = \mathbf{-283.3 \text{ kJ/kg}} \end{aligned}$$

Recall standard sign notation is work positive out.

4.52

A portable fan blows 0.3 kg/s room air with a velocity of 15 m/s (see Fig. P4.18). What is the minimum power electric motor that can drive it? Hint: Are there any changes in P or T?

Solution:

C.V. Fan plus space out to near stagnant inlet room air.

$$\text{Energy Eq.4.13:} \quad q + h_i + \mathbf{V}_i^2/2 = h_e + \mathbf{V}_e^2/2 + w$$

Here $q \cong 0$, $\mathbf{V}_i \cong 0$ and $h_i = h_e$ same P and T

$$-w = \mathbf{V}_e^2/2 = (15^2/2) \text{ (m/s)}^2 = 112.5 \text{ J/kg} = 0.1125 \text{ kJ/kg}$$

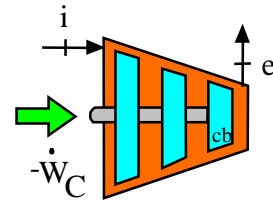
$$-\dot{W} = -\dot{m}w = 0.3 \text{ kg/s} \times 0.1125 \text{ kJ/kg} = \mathbf{0.034 \text{ kW}}$$

4.53

A refrigerator uses the natural refrigerant carbon dioxide where the compressor brings 0.02 kg/s from 1 MPa, -20°C to 6 MPa using 2 kW of power. Find the compressor exit temperature.

Solution:

C.V. Compressor, steady state, single inlet and exit flow. For this device we also assume no heat transfer and $Z_i = Z_e$



From Table B.3.2 : $h_i = 342.31 \text{ kJ/kg}$

Energy Eq.4.13 reduces to

$$\dot{W} = \dot{m}w_C = \dot{m} (h_i - h_e) \Rightarrow h_e = h_i - \dot{W}/\dot{m}$$

$$h_e = 342.31 \text{ kJ/kg} - [-2 \text{ kW}] / (0.02 \text{ kg/s}) = 442.31 \text{ kJ/kg}$$

From Table B.3.2 :

$$T_e = 100 + 20 (442.31 - 421.69)/(445.02 - 421.69) = \mathbf{117.7^{\circ}\text{C}}$$

4.54

An air compressor takes in air at 100 kPa, 17°C and delivers it at 1 MPa, 600 K to a constant-pressure cooler, which it exits at 300 K. Find the specific compressor work and the specific heat transfer in the cooler.

Solution

C.V. air compressor $q = 0$

Continuity Eq.: $\dot{m}_2 = \dot{m}_1$

Energy Eq.4.13: $0 = h_1 + w_c \text{ in} - h_2$

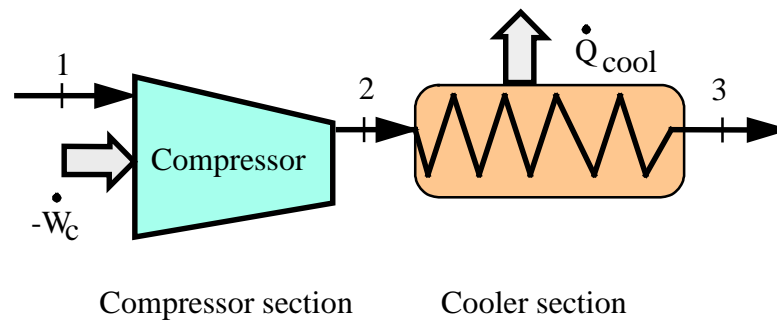


Table A.7: $h_1 = 290.19 \text{ kJ/kg}$, $h_2 = 607.32 \text{ kJ/kg}$, $h_3 = 300.47 \text{ kJ/kg}$

$$w_c \text{ in} = h_2 - h_1 = 607.32 - 290.19 = \mathbf{317.13 \text{ kJ/kg}}$$

C.V. cooler $w = 0$

Continuity Eq.: $\dot{m}_3 = \dot{m}_1$

Energy Eq.4.13: $0 = h_2 - q_{\text{out}} - h_3$

$$q_{\text{out}} = h_2 - h_3 = 607.32 - 300.47 = \mathbf{306.85 \text{ kJ/kg}}$$

Comment: For these temperatures we could have used constant specific heats from A.5

4.55

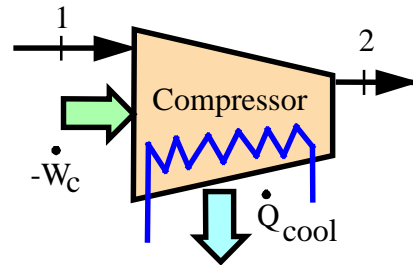
A compressor brings R-134a from 150 kPa, -10°C to 1200 kPa, 50°C . It is water cooled with a heat loss estimated as 40 kW and the shaft work input is measured to be 150 kW. How much is the mass flow rate through the compressor?

Solution:

C.V Compressor. Steady flow.
Neglect kinetic and potential energies.

$$\text{Energy : } \dot{m} h_i + \dot{Q} = \dot{m} h_e + \dot{W}$$

$$\dot{m} = (\dot{Q} - \dot{W}) / (h_e - h_i)$$



Look in table B.5.2

$$h_i = 393.84 \text{ kJ/kg}, \quad h_e = 426.84 \text{ kJ/kg}$$

$$\dot{m} = \frac{-40 - (-150)}{426.84 - 393.84} \frac{\text{kW}}{\text{kJ/kg}} = \mathbf{3.333 \text{ kg/s}}$$

4.56

The compressor of a large gas turbine receives air from the ambient at 95 kPa, 20°C, with a low velocity. At the compressor discharge, air exits at 1.52 MPa, 430°C, with velocity of 90 m/s. The power input to the compressor is 5000 kW. Determine the mass flow rate of air through the unit.

Solution:

C.V. Compressor, steady state, single inlet and exit flow.

$$\text{Energy Eq.4.13: } q + h_i + \mathbf{V}_i^2/2 = h_e + \mathbf{V}_e^2/2 + w$$

Here we assume $q \cong 0$ and $\mathbf{V}_i \cong 0$ so using constant C_{p0} from A.5

$$-w = C_{p0}(T_e - T_i) + \mathbf{V}_e^2/2 = 1.004(430 - 20) + \frac{(90)^2}{2 \times 1000} = 415.5 \text{ kJ/kg}$$

Notice the kinetic energy is 1% of the work and can be neglected in most cases. The mass flow rate is then from the power and the specific work

$$\dot{m} = \frac{\dot{W}_c}{-w} = \frac{5000 \text{ kW}}{415.5 \text{ kJ/kg}} = \mathbf{12.0 \text{ kg/s}}$$

4.57

How much power is needed to run the fan in Problem 4.18?

A household fan of diameter 0.6 m takes air in at 98 kPa, 20°C and delivers it at 105 kPa, 21°C with a velocity of 1.5 m/s. What are the mass flow rate (kg/s), the inlet velocity and the outgoing volume flow rate in m³/s?

Solution:

$$\begin{array}{ll} \text{Continuity Eq.} & \dot{m}_i = \dot{m}_e = A\mathbf{V}/v \\ \text{Ideal gas} & v = RT/P \end{array}$$

$$\text{Area: } A = \frac{\pi}{4} D^2 = \frac{\pi}{4} \times 0.6^2 = 0.2827 \text{ m}^2$$

$$\dot{V}_e = A\mathbf{V}_e = 0.2827 \times 1.5 = 0.4241 \text{ m}^3/\text{s}$$

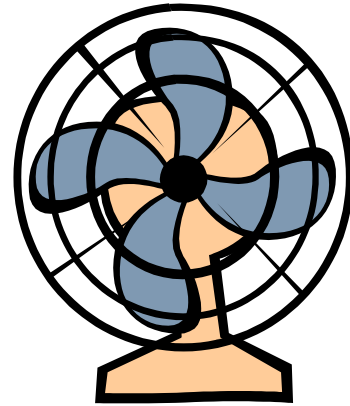
$$v_e = \frac{RT_e}{P_e} = \frac{0.287 \times (21 + 273)}{105} = 0.8036 \text{ m}^3/\text{kg}$$

$$\dot{m}_i = \dot{V}_e/v_e = 0.4241/0.8036 = 0.528 \text{ kg/s}$$

$$A\mathbf{V}_i/v_i = \dot{m}_i = A\mathbf{V}_e/v_e$$

$$\mathbf{V}_i = \mathbf{V}_e \times (v_i/v_e) = \mathbf{V}_e \times \frac{RT_i}{P_i v_e} = 1.5 \times \frac{0.287 \text{ kJ/kg-K} \times (20 + 273) \text{ K}}{98 \text{ kPa} \times 0.8036 \text{ m}^3/\text{kg}} = 1.6 \text{ m/s}$$

$$\begin{aligned} \dot{W} &= \dot{m}(h_i + \frac{1}{2}V_i^2 - h_e - \frac{1}{2}V_e^2) = \dot{m} [C_p (T_i - T_e) + \frac{1}{2} V_i^2 - \frac{1}{2} V_e^2] \\ &= 0.528 [1.004 (-1) + \frac{1.6^2 - 1.5^2}{2000}] = 0.528 [-1.004 + 0.000155] \\ &= -0.53 \text{ kW} \end{aligned}$$



4.58

A compressor in an industrial air-conditioner compresses ammonia from a state of saturated vapor at 200 kPa to a pressure of 1000 kPa. At the exit the temperature is measured to be 100°C and the mass flow rate is 0.5 kg/s. What is the required motor size (kW) for this compressor?

Solution:

C.V. Compressor. Assume adiabatic and neglect kinetic energies.

Energy Eq.4.13: $w_C = h_1 - h_2$

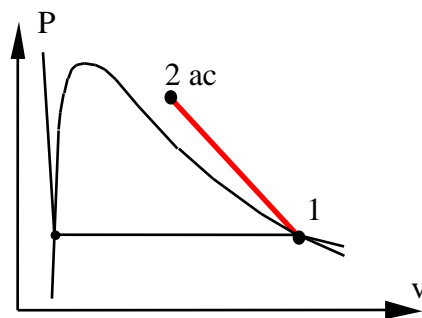
States: 1: B.2.2: $h_1 = 1419.6 \text{ kJ/kg}$

2: B.2.2 $h_{2,AC} = 1664.3 \text{ kJ/kg}$

Energy equation:

$$-w_C = h_2 - h_1 = 1664.3 - 1419.6 = 244.7 \text{ kJ/kg}$$

$$\dot{W} = 0.5 \text{ kg/s} \times 244.7 \text{ kJ/kg} = \mathbf{122 \text{ kW}}$$



4.59

An exhaust fan in a building should be able to move 3 kg/s air atmospheric pressure air at 25°C through a 0.5 m diameter vent hole. How high a velocity must it generate and how much power is required to do that?

Solution:

C.V. Fan and vent hole. Steady state with uniform velocity out.

$$\text{Continuity Eq.: } \dot{m} = \text{constant} = \rho A \mathbf{V} = A \mathbf{V} / v = A \mathbf{V} P / RT$$

$$\text{Ideal gas : } P v = RT, \quad \text{and area is } A = \frac{\pi}{4} D^2$$

Now the velocity is found

$$\begin{aligned} \mathbf{V} &= \dot{m} RT / \left(\frac{\pi}{4} D^2 P \right) \\ &= 3 \text{ kg/s} \times 0.287 \text{ kJ/kg-K} \times 293.15 \text{ K} / \left(\frac{\pi}{4} \times 0.5^2 \text{ m}^2 \times 101 \text{ kPa} \right) \\ &= \mathbf{12.7 \text{ m/s}} \end{aligned}$$

The kinetic energy out is

$$\frac{1}{2} \mathbf{V}_2^2 = \frac{1}{2} \times 12.7^2 / 1000 = 0.08065 \text{ kJ/kg}$$

which is provided by the work (only two terms in energy equation that does not cancel, we assume $\mathbf{V}_1 = 0$)

$$\dot{W}_{\text{in}} = \dot{m} \frac{1}{2} \mathbf{V}_2^2 = 3 \text{ kg/s} \times 0.08065 \text{ kJ/kg} = \mathbf{0.242 \text{ kW}}$$

4.60

A compressor receives R-410A as saturated vapor R-410A at 400 kPa and brings it to 2000 kPa, 60°C. Then a cooler brings it to saturated liquid at 2000 kPa (see Fig. P4.54). Find the specific compressor work and the specific heat transfer in the cooler?

C.V. Compressor. Assume adiabatic and neglect kinetic, potential energies.

Energy Eq.4.13: $w = h_1 - h_2$

States: 1: B.4.2 $h_1 = 271.9 \text{ kJ/kg}$

2: B.4.2 $h_2 = 320.62 \text{ kJ/kg}$

3: B.4.1 $h_3 = 106.14 + \frac{2.31}{5} (114.95 - 106.14) = 110.2 \text{ kJ/kg}$

$-w_C = h_2 - h_1 = 320.62 - 271.9 = \mathbf{48.72 \text{ kJ/kg}}$

C.V. Cooler. No work, neglect kinetic, potential energies.

Energy Eq. 4.13: $q = h_3 - h_2 = 110.2 - 320.62 = \mathbf{-210.4 \text{ kJ/kg}}$



The compressor is inside the unit to the left that also houses a fan and the heat exchanger.



4.61

An air flow is brought from 20°C, 100 kPa to 1000 kPa, 330°C by an adiabatic compressor driven by a 50-kW motor. What are the mass flow rate and the exit volume flow rate of air?

C.V. Compressor. Assume adiabatic and neglect kinetic, potential energies.

Energy Eq.4.13: $w = h_1 - h_2$

$$\begin{aligned} -w_C = h_2 - h_1 &\approx C_P (T_2 - T_1) = 1.004 \text{ kJ/kg-K} \times (330 - 20) \text{ K} \\ &= 311.2 \text{ kJ/kg} \end{aligned}$$

The mass flow rate scale the work term so

$$\dot{m} = \dot{W} / -w_C = \frac{50 \text{ kW}}{311.2 \text{ kJ/kg}} = \mathbf{0.1606 \text{ kg/s}}$$

$$\begin{aligned} \dot{V} = \dot{m} v &= \dot{m} \frac{RT}{P} = 0.1606 \text{ kg/s} \frac{0.287 \times (330 + 273) \text{ kJ/kg}}{1000 \text{ kPa}} \\ &= \mathbf{0.0278 \text{ m}^3/\text{s}} \end{aligned}$$

Heaters/Coolers

4.62

The air conditioner in a house or a car has a cooler that brings atmospheric air from 30°C to 10°C both states at 101 kPa. If the flow rate is 0.75 kg/s find the rate of heat transfer.

Solution:

CV. Cooler. Steady state single flow with heat transfer.

Neglect changes in kinetic and potential energy and no work term.

Energy Eq. 4.13: $q_{\text{out}} = h_i - h_e$

Use constant specific heat from Table A.5 (T is around 300 K)

$$\begin{aligned} q_{\text{out}} &= h_i - h_e = C_P (T_i - T_e) \\ &= 1.004 \frac{\text{kJ}}{\text{kg K}} \times (30 - 10) \text{ K} = 20.1 \text{ kJ/kg} \end{aligned}$$

$$\dot{Q}_{\text{out}} = \dot{m} q_{\text{out}} = 0.75 \times 20.1 = \mathbf{15 \text{ kW}}$$

4.63

A boiler section boils 3 kg/s saturated liquid water at 2000 kPa to saturated vapor in a reversible constant-pressure process. Find the specific heat transfer in the process.

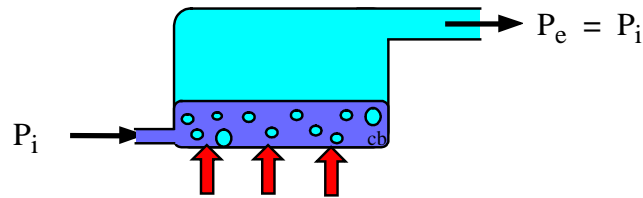
C.V. Boiler. Steady state single inlet and exit flow, neglect potential energy and since velocities are low we neglect kinetic energies.

Energy Eq. 4.13: $q + h_i = h_e$

From Table B.1.2: $h_i = 908.77 \text{ kJ/kg}$

Table B.1.3: $h_e = 2799.51 \text{ kJ/kg}$

$$q = h_e - h_i = 2799.51 - 908.77 = \mathbf{1890.74 \text{ kJ/kg}}$$



4.64

A condenser (cooler) receives 0.05 kg/s R-410A at 2000 kPa, 80°C and cools it to 10°C. Assume the exit properties are as for saturated liquid with the same T. What cooling capacity (kW) must the condenser have?

Solution:

C.V. R-410A condenser. Steady state single flow, heat transfer out and no work.

$$\text{Energy Eq. 4.12:} \quad \dot{m} h_1 = \dot{m} h_2 + \dot{Q}_{\text{out}}$$

$$\text{Inlet state: Table B.4.2} \quad h_1 = 343.22 \text{ kJ/kg,}$$

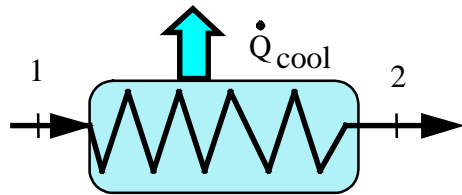
$$\text{Exit state: Table B.4.1} \quad h_2 = 73.21 \text{ kJ/kg (compressed liquid)}$$

To be more accurate we could have added $(P - P_{\text{sat}})v$ to the h_2 .

Process: Neglect kinetic and potential energy changes.

Cooling capacity is taken as the heat transfer out i.e. positive out so

$$\begin{aligned} \dot{Q}_{\text{out}} &= \dot{m} (h_1 - h_2) = 0.05 \text{ kg/s} \times (343.22 - 73.21) \text{ kJ/kg} \\ &= \mathbf{13.5 \text{ kW}} \end{aligned}$$



4.65

Carbon dioxide enters a steady-state, steady-flow heater at 300 kPa, 300 K, and exits at 275 kPa, 1500 K, as shown in Fig. P4.65. Changes in kinetic and potential energies are negligible. Calculate the required heat transfer per kilogram of carbon dioxide flowing through the heater.

Solution:

C.V. Heater Steady state single inlet and exit flow.

Energy Eq. 4.13: $q + h_i = h_e$

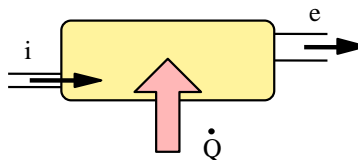


Table A.8: $q = h_e - h_i = 1614.9 - 214.4 = \mathbf{1400.5 \text{ kJ/kg}}$

[If we use C_{p0} from A.5 then $q \cong 0.842 \text{ kJ/kg-K} \times (1500 - 300)\text{K} = 1010.4 \text{ kJ/kg}$]

Too large ΔT , T_{ave} to use C_{p0} at room temperature.

4.66

Find the heat transfer in Problem 4.17

A boiler receives a constant flow of 5000 kg/h liquid water at 5 MPa, 20°C and it heats the flow such that the exit state is 450°C with a pressure of 4.5 MPa. Determine the necessary minimum pipe flow area in both the inlet and exit pipe(s) if there should be no velocities larger than 20 m/s.

Solution:

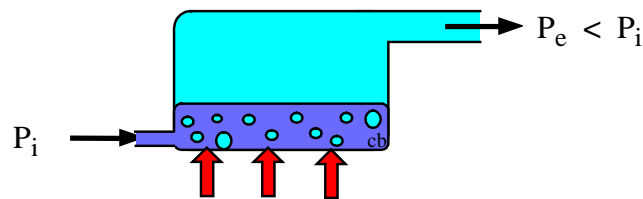
C.V. Heater. Steady state single inlet and exit flow, neglect potential energy and since velocities are low we neglect kinetic energies.

Energy Eq. 4.13: $q + h_i = h_e$

From Table B.1.4: $h_i = 88.64 \text{ kJ/kg}$

Table B.1.3: $h_e = (3330.23 + 3316.15)/2 = 3323.19 \text{ kJ/kg}$

$$q = h_e - h_i = 3323.19 - 88.64 = \mathbf{3234.6 \text{ kJ/kg}}$$



4.67

A chiller cools liquid water for air-conditioning purposes. Assume 2.5 kg/s water at 20°C, 100 kPa is cooled to 5°C in a chiller. How much heat transfer (kW) is needed?

Solution:

C.V. Chiller. Steady state single flow with heat transfer. Neglect changes in kinetic and potential energy and no work term.

Energy Eq. 4.13: $q_{\text{out}} = h_i - h_e$

Properties from Table B.1.1:

$$h_i = 83.94 \text{ kJ/kg} \quad \text{and} \quad h_e = 20.98 \text{ kJ/kg}$$

Now the energy equation gives

$$q_{\text{out}} = 83.94 - 20.98 = 62.96 \text{ kJ/kg}$$

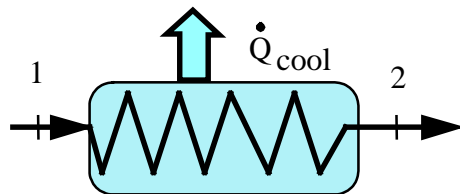
$$\dot{Q}_{\text{out}} = \dot{m} q_{\text{out}} = 2.5 \times 62.96 = \mathbf{157.4 \text{ kW}}$$

Alternative property treatment since single phase and small ΔT

If we take constant specific heat for the liquid from Table A.4

$$\begin{aligned} q_{\text{out}} &= h_i - h_e \cong C_p (T_i - T_e) \\ &= 4.18 \text{ kJ/kg-K} \times (20 - 5) \text{ K} = 62.7 \text{ kJ/kg} \end{aligned}$$

$$\dot{Q}_{\text{out}} = \dot{m} q_{\text{out}} = 2.5 \text{ kg/s} \times 62.7 \text{ kJ/kg} = \mathbf{156.75 \text{ kW}}$$



4.68

Saturated liquid nitrogen at 600 kPa enters a boiler at a rate of 0.008 kg/s and exits as saturated vapor, see Fig. P4.68. It then flows into a super heater also at 600 kPa where it exits at 600 kPa, 280 K. Find the rate of heat transfer in the boiler and the super heater.

Solution:

C.V.: boiler steady single inlet and exit flow, neglect KE, PE energies in flow

Continuity Eq.: $\dot{m}_1 = \dot{m}_2 = \dot{m}_3$

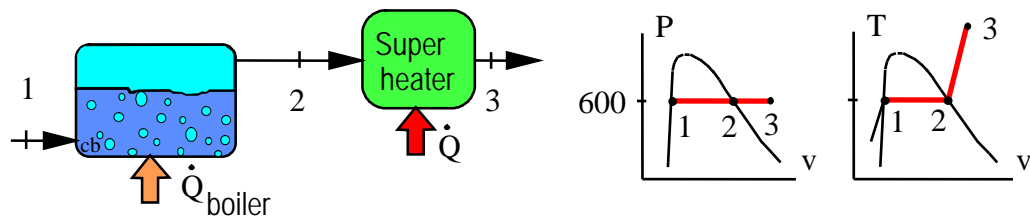


Table B.6.1: $h_1 = -81.469$ kJ/kg, $h_2 = 86.85$ kJ/kg,

Table B.6.2: $h_3 = 289.05$ kJ/kg

Energy Eq. 4.13: $q_{\text{boiler}} = h_2 - h_1 = 86.85 - (-81.469) = 168.32$ kJ/kg

$$\dot{Q}_{\text{boiler}} = \dot{m}_1 q_{\text{boiler}} = 0.008 \text{ kg/s} \times 168.32 \text{ kJ/kg} = \mathbf{1.346 \text{ kW}}$$

C.V. Superheater (same approximations as for boiler)

Energy Eq. 4.13: $q_{\text{sup heater}} = h_3 - h_2 = 289.05 - 86.85 = 202.2$ kJ/kg

$$\dot{Q}_{\text{sup heater}} = \dot{m}_2 q_{\text{sup heater}} = 0.008 \text{ kg/s} \times 202.2 \text{ kJ/kg} = \mathbf{1.62 \text{ kW}}$$

4.69

Carbon dioxide used as a natural refrigerant flows through a cooler at 10 MPa, which is supercritical so no condensation occurs. The inlet is at 220°C and the exit is at 50°C. Find the specific heat transfer.

C.V. Cooler. Steady state single flow with heat transfer. Neglect changes in kinetic and potential energy and no work term.

Energy Eq. 4.13: $0 = h_i - h_e + q$

Properties from Table B.3.2:

$$h_i = 542.91 \text{ kJ/kg} \quad \text{and}$$

$$h_e = (200.14 + 312.11)/2 = 256.13 \text{ kJ/kg}$$

Now the energy equation gives

$$q = 256.13 - 542.91 = \mathbf{-286.79 \text{ kJ/kg}}$$

4.70

In a steam generator, compressed liquid water at 10 MPa, 30°C, enters a 30-mm diameter tube at the rate of 3 L/s. Steam at 9 MPa, 400°C exits the tube. Find the rate of heat transfer to the water.

Solution:

C.V. Steam generator. Steady state single inlet and exit flow.

Constant diameter tube: $A_i = A_e = \frac{\pi}{4} (0.03)^2 = 0.0007068 \text{ m}^2$

Table B.1.4 $\dot{m} = \dot{V}_i/v_i = 0.003/0.0010003 = 3.0 \text{ kg/s}$

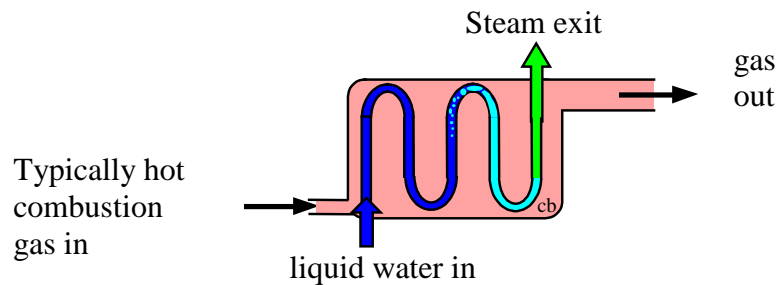
$$V_i = \dot{V}_i/A_i = 0.003/0.0007068 = 4.24 \text{ m/s}$$

Exit state properties from Table B.1.3

$$V_e = V_i \times v_e/v_i = 4.24 \times 0.02993/0.0010003 = 126.86 \text{ m/s}$$

The energy equation Eq. 4.12 is solved for the heat transfer as

$$\begin{aligned} \dot{Q} &= \dot{m} \left[(h_e - h_i) + (V_e^2 - V_i^2)/2 \right] \\ &= 3.0 \text{ kg/s} \times \left[3117.8 - 134.86 + \frac{126.86^2 - 4.24^2}{2 \times 1000} \right] \text{ kJ/kg} = \mathbf{8973 \text{ kW}} \end{aligned}$$



4.71

An oven has five radiant heaters; each one is rated at 15 kW. It should heat some 2-kg steel plates from 20°C to 800 K. How many of these plates per minute can it heat?

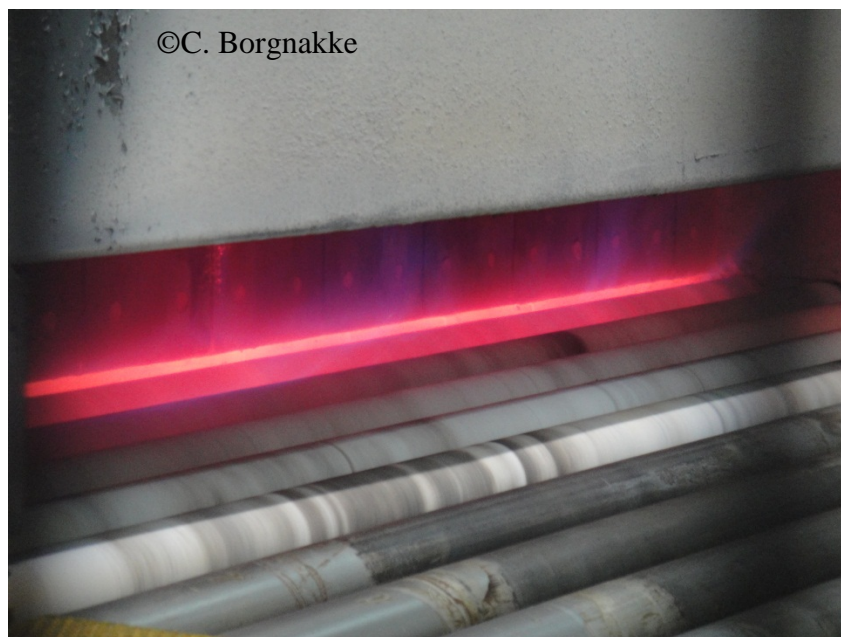
C.V. Oven, steady state operation. A flow of plates in (represents an \dot{m})

Energy Eq.: $0 = \dot{m} (h_i - h_e) + \dot{Q}$

$$\dot{Q} = \dot{m} (h_e - h_i) = \dot{m} C (T_e - T_i)$$

$$\dot{m} = \dot{Q} / C (T_e - T_i) = \frac{5 \times 15 \text{ kW}}{0.46 (800 - 293) \text{ kJ/kg}} = 0.322 \text{ kg/s}$$

$$N = \dot{m}/m = (0.322 / 2) \text{ 1/s} = 0.161 \text{ 1/s} = \mathbf{9.65 \text{ per min}}$$



Front end of oven with steel rollers to bring the plates in
a skirt hangs down to limit heat losses.

4.72

A cryogenic fluid as liquid nitrogen at 90 K, 400 kPa flows into a probe used in cryogenic surgery. In the return line the nitrogen is then at 160 K, 400 kPa. Find the specific heat transfer to the nitrogen. If the return line has a cross sectional area 100 times larger than the inlet line what is the ratio of the return velocity to the inlet velocity?

Solution:

C.V line with nitrogen. No kinetic or potential energy changes

$$\text{Continuity Eq.:} \quad \dot{m} = \text{constant} = \dot{m}_e = \dot{m}_i = A_e \mathbf{V}_e / v_e = A_i \mathbf{V}_i / v_i$$

$$\text{Energy Eq. 4.13:} \quad q = h_e - h_i$$

$$\text{State i, Table B.6.1: } h_i = -95.58 \text{ kJ/kg, } v_i = 0.001343 \text{ m}^3/\text{kg}$$

$$\text{State e, Table B.6.2: } h_e = 162.96 \text{ kJ/kg, } v_e = 0.11647 \text{ m}^3/\text{kg}$$

From the energy equation

$$q = h_e - h_i = 162.96 - (-95.58) = \mathbf{258.5 \text{ kJ/kg}}$$

From the continuity equation

$$\mathbf{V_e/V_i} = A_i/A_e (v_e/v_i) = \frac{1}{100} \frac{0.11647}{0.001343} = \mathbf{0.867}$$

4.73

An evaporator has R-410A at -20°C and quality 20% flowing in, with the exit flow being saturated vapor at -20°C . Knowing that there is no work, find the specific heat transfer.

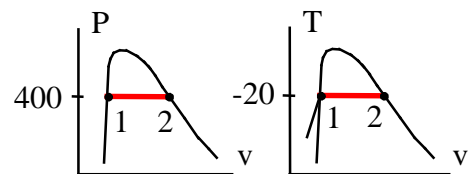
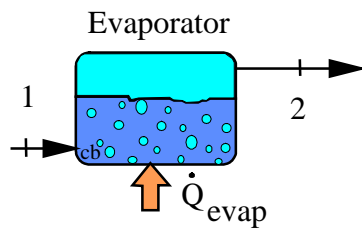
C.V. Heater Steady state single inlet and exit flow.

Energy Eq.4.13: $0 = q + h_1 - h_2$

Table B.4: $h_1 = 28.24 + 0.2 \times 243.65 = 76.97 \text{ kJ/kg}$

$h_2 = 271.89 \text{ kJ/kg}$

$q = h_2 - h_1 = 271.89 - 76.97 = \mathbf{194.92 \text{ kJ/kg}}$



4.74

A flow of liquid glycerine flows around an engine, cooling it as it absorbs energy. The glycerine enters the engine at 60°C and receives 19 kW of heat transfer. What is the required mass flow rate if the glycerine should come out at maximum 95°C?

Solution:

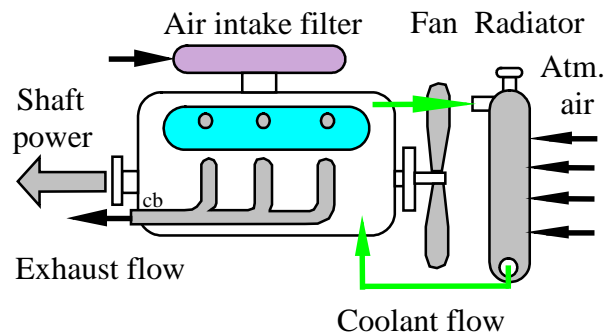
C.V. Liquid flow (glycerine is the coolant), steady flow. no work.

$$\text{Energy Eq.: } \dot{m}h_i + \dot{Q} = \dot{m}h_e$$

$$\dot{m} = \dot{Q} / (h_e - h_i) = \frac{\dot{Q}}{C_{\text{gly}} (T_e - T_i)}$$

From table A.4 $C_{\text{gly}} = 2.42 \text{ kJ/kg}\cdot\text{K}$

$$\dot{m} = \frac{19}{2.42 (95 - 60)} \frac{\text{kW}}{\text{kJ/kg}} = \mathbf{0.224 \text{ kg/s}}$$



Pumps, pipe and channel flows

4.75

An irrigation pump takes water from a river at 10°C, 100 kPa and pumps it up to an open canal, where it flows out 100 m higher at 10°C. The pipe diameter in and out of the pump is 0.1 m and the motor driving the unit is 5 hp. What is the flow rate neglecting kinetic energy and losses?

C.V. Pump plus pipe to canal.

This is a single steady flow device with atmospheric pressure in and out.

$$\begin{aligned}\text{Energy Eq.: } 0 &= h_i + 0 + gZ_i + w_{p \text{ in}} - h_e - 0 - gZ_e \\ w_{p \text{ in}} &= g(Z_e - Z_i) = 9.81 \text{ m/s}^2 \times 100 \text{ (m/s)}^2 = 0.981 \text{ kJ/kg} \\ \dot{W}_{p \text{ in}} &= 5 \text{ hp} = 5 \text{ hp} \times 0.746 \text{ kW/hp} = 3.73 \text{ kW}\end{aligned}$$

Find the flow rate from the work

$$\dot{m} = \dot{W}_{p \text{ in}} / w_{p \text{ in}} = 3.73 \text{ kW} / 0.981 \text{ kJ/kg} = \mathbf{3.8 \text{ kg/s}}$$

4.76

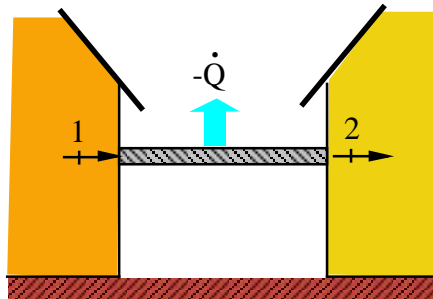
A pipe flows water at 15°C from one building to another. In the winter time the pipe loses an estimated 500 W of heat transfer. What is the minimum required mass flow rate that will ensure that the water does not freeze (i.e. reach 0°C)?

Solution:

Energy Eq.: $\dot{m}h_i + \dot{Q} = \dot{m}h_e$

Assume saturated liquid at given T from table B.1.1

$$\dot{m} = \frac{\dot{Q}}{h_e - h_i} = \frac{-500 \times 10^{-3} \text{ kW}}{0 - 62.98 \text{ kJ/kg}} = \frac{0.5}{62.98} \text{ kg/s} = \mathbf{0.00794 \text{ kg/s}}$$



4.77

A river flowing at 0.5 m/s across a 1-m-high and 10-m-wide area has a dam that creates an elevation difference of 2 m. How much energy could a turbine deliver per day if 80% of the potential energy can be extracted as work?

CV Dam from upstream to downstream 2 m lower elevation

Continuity Eq.: $\dot{m} = \text{constant} = \dot{m}_e = \dot{m}_i = A_e \mathbf{V}_e / v_e = A_i \mathbf{V}_i / v_i$

Find the mass flow rate

$$\dot{m} = A \mathbf{V}_i / v = \rho A \mathbf{V}_i = 997 \text{ kg/m}^3 \times (1 \times 10) \text{ m}^2 \times 0.5 \text{ m/s} = 4985 \text{ kg/s}$$

Energy Eq.: $0 = \dot{m} (h_i + 0.5 \mathbf{V}_i^2 + gZ_i) - \dot{m} (h_e + 0.5 \mathbf{V}_e^2 + gZ_e) - \dot{W}$

The velocity in and out is the same assuming same flow area and the two enthalpies are also the same since same T and $P = P_0$.

$$\begin{aligned} \dot{W} &= 0.8 \dot{m} g(Z_i - Z_e) = 0.8 \times 4985 \text{ kg/s} \times 9.807 \text{ m/s}^2 \times 2 \text{ m} \\ &= 78\,221 \text{ J/s} = 78\,221 \text{ W} = 78.2 \text{ kW} \end{aligned}$$

$$W = \dot{W} \Delta t = 78.2 \text{ (kJ/s)} \times 24 \times 60 \times 60 \text{ s} = \mathbf{6.76 \text{ GJ}}$$

4.78

A steam pipe for a 300-m tall building receives superheated steam at 200 kPa at ground level. At the top floor the pressure is 125 kPa and the heat loss in the pipe is 110 kJ/kg. What should the inlet temperature be so that no water will condense inside the pipe?

Solution:

C.V. Pipe from 0 to 300 m, no ΔKE , steady state, single inlet and exit flow.

Neglect any changes in kinetic energy.

Energy Eq. 4.13: $q + h_i = h_e + gZ_e$

No condensation means: Table B.1.2, $h_e = h_g$ at 125 kPa = 2685.4 kJ/kg

$$h_i = h_e + gZ_e - q = 2685.4 + \frac{9.807 \times 300}{1000} - (-110) = 2810.1 \text{ kJ/kg}$$

At 200 kPa: $T \sim 170^\circ\text{C}$ Table B.1.3

4.79

Consider a water pump that receives liquid water at 25°C, 100 kPa and delivers it to a same diameter short pipe having a nozzle with exit diameter of 2 cm (0.02 m) to the atmosphere 100 kPa. Neglect the kinetic energy in the pipes and assume constant u for the water. Find the exit velocity and the mass flow rate if the pump draws a power of 1 kW.

Solution:

$$\text{Continuity Eq.: } \dot{m}_i = \dot{m}_e = A\mathbf{V}/v; \quad A = \frac{\pi}{4}D_e^2 = \frac{\pi}{4} \times 0.02^2 = 3.1416 \times 10^{-4} \text{ m}^2$$

$$\text{Energy Eq. 4.13: } h_i + \frac{1}{2}\mathbf{V}_i^2 + gZ_i = h_e + \frac{1}{2}\mathbf{V}_e^2 + gZ_e + w$$

$$\text{Properties: } h_i = u_i + P_i v_i = h_e = u_e + P_e v_e; \quad P_i = P_e; \quad v_i = v_e$$

$$w = -\frac{1}{2}\mathbf{V}_e^2 \quad \Rightarrow \quad -\dot{W} = \dot{m} \left(\frac{1}{2}\mathbf{V}_e^2 \right) = A \times \frac{1}{2}\mathbf{V}_e^3/v_e$$

$$\mathbf{V}_e = \left(\frac{-2\dot{W}v_e}{A} \right)^{1/3} = \left(\frac{2 \times 1000 \times 0.001003}{3.1416 \times 10^{-4}} \right)^{1/3} = \mathbf{18.55 \text{ m/s}}$$

$$\dot{m} = A\mathbf{V}_e/v_e = 3.1416 \times 10^{-4} \times 18.55 / 0.001003 = \mathbf{5.81 \text{ kg/s}}$$

4.80

A small water pump is used in an irrigation system. The pump takes water in from a river at 10°C, 100 kPa at a rate of 5 kg/s. The exit line enters a pipe that goes up to an elevation 20 m above the pump and river, where the water runs into an open channel. Assume the process is adiabatic and that the water stays at 10°C. Find the required pump work.

Solution:

C.V. pump + pipe. Steady state, 1 inlet, 1 exit flow. Assume same velocity in and out, no heat transfer.

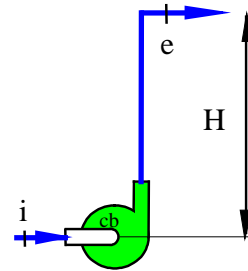
Continuity Eq.: $\dot{m}_{in} = \dot{m}_{ex} = \dot{m}$

Energy Eq. 4.12:

$$\dot{m}(h_{in} + (1/2)V_{in}^2 + gz_{in}) =$$

$$\dot{m}(h_{ex} + (1/2)V_{ex}^2 + gz_{ex}) + \dot{W}$$

States: $h_{in} = h_{ex}$ same (T, P)



$$\begin{aligned}\dot{W} &= \dot{m} g(z_{in} - z_{ex}) = 5 \text{ kg/s} \times 9.807 \text{ m/s}^2 \times (0 - 20) \text{ m} / (1000 \text{ J/kJ}) \\ &= \mathbf{-0.98 \text{ kW}}\end{aligned}$$

I.E. 0.98 kW required input

4.81

A small stream with water at 15°C runs out over a cliff creating a 50 m tall waterfall. Estimate the downstream temperature when you neglect the horizontal flow velocities upstream and downstream from the waterfall. How fast was the water dropping just before it splashed into the pool at the bottom of the waterfall?

Solution:

CV. Waterfall, steady state. Assume no \dot{Q} nor \dot{W}

Energy Eq. 4.13: $h + \frac{1}{2}V^2 + gZ = \text{const.}$

State 1: At the top zero velocity $Z_1 = 100 \text{ m}$

State 2: At the bottom just before impact, $Z_2 = 0$

State 3: At the bottom after impact in the pool.

$$h_1 + 0 + gZ_1 = h_2 + \frac{1}{2}V_2^2 + 0 = h_3 + 0 + 0$$

Properties: $h_1 \cong h_2$ same T, P

$$\Rightarrow \frac{1}{2}V_2^2 = gZ_1$$

$$V_2 = \sqrt{2gZ_1} = \sqrt{2 \times 9.806 \text{ m/s}^2 \times 50 \text{ m}} = \mathbf{31.3 \text{ m/s}}$$

Energy equation from state 1 to state 3

$$h_3 = h_1 + gZ_1$$

use $\Delta h = C_p \Delta T$ with value from Table A.4 (liquid water)

$$\begin{aligned} T_3 &= T_1 + gZ_1 / C_p \\ &= 20 + 9.806 \text{ m/s}^2 \times 50 \text{ m} / (4180 \text{ J/kg-K}) = \mathbf{20.12 \text{ }^\circ\text{C}} \end{aligned}$$

4.82

A cutting tool uses a nozzle that generates a high speed jet of liquid water.

Assume an exit velocity of 500 m/s of 20°C liquid water with a jet diameter of 2 mm (0.002 m). How much mass flow rate is this? What size (power) pump is needed to generate this from a steady supply of 20°C liquid water at 200 kPa?

Solution:

C.V. Nozzle. Steady state, single flow.

Continuity equation with a uniform velocity across A

$$\dot{m} = A \mathbf{V} / v = \frac{\pi}{4} D^2 \mathbf{V} / v = \frac{\pi}{4} 0.002^2 \times 500 / 0.001002 = \mathbf{1.568 \text{ kg/s}}$$

Assume $Z_i = Z_e = \emptyset$, $u_e = u_i$ and $\mathbf{V}_i = 0$ $P_e = 100 \text{ kPa}$ (atmospheric)

Energy Eq.4.13:
$$h_i + \emptyset + \emptyset = h_e + \frac{1}{2} \mathbf{V}_e^2 + \emptyset + w$$

$$\begin{aligned} w &= h_i - h_e - \frac{1}{2} \mathbf{V}_e^2 = u_i - u_e + P_i v_i - P_e v_e - \frac{1}{2} \mathbf{V}_e^2 \\ &= (P_i - P_e) v_i - \frac{1}{2} \mathbf{V}_e^2 \\ &= 0.001002 \text{ m}^3/\text{kg} \times (200 - 100) \text{ kPa} - 0.5 \times \frac{500^2 \text{ m}^2/\text{s}^2}{1000 \text{ J/kJ}} \\ &= 0.1002 - 125 \cong -125 \text{ kJ/kg} \end{aligned}$$

$$\dot{W} = \dot{m} w = 1.568 \text{ kg/s} \times (-125 \text{ kJ/kg}) = \mathbf{-196 \text{ kW}}$$

4.83

The main waterline into a tall building has a pressure of 600 kPa at 5 m below ground level. A pump brings the pressure up so the water can be delivered at 200 kPa at the top floor 100 m above ground level. Assume a flow rate of 10 kg/s liquid water at 10°C and neglect any difference in kinetic energy and internal energy u . Find the pump work.

Solution:

C.V. Pipe from inlet at -5 m up to exit at +100 m, 200 kPa.

$$\text{Energy Eq.4.13: } h_i + \frac{1}{2}V_i^2 + gZ_i = h_e + \frac{1}{2}V_e^2 + gZ_e + w$$

With the same u the difference in h 's are the Pv terms

$$\begin{aligned} w &= h_i - h_e + \frac{1}{2}(V_i^2 - V_e^2) + g(Z_i - Z_e) \\ &= P_i v_i - P_e v_e + g(Z_i - Z_e) \\ &= 600 \times 0.001 - 200 \times 0.001 + 9.806 \times (-5 - 100)/1000 \\ &= 0.4 - 1.03 = -0.63 \text{ kJ/kg} \end{aligned}$$

$$\dot{W} = \dot{m}w = 10 \times (-0.63) = \mathbf{-6.3 \text{ kW}}$$

Multiple flow single device processes

Turbines, Compressors, Expanders

4.84

An adiabatic steam turbine in a power plant receives 5 kg/s steam at 3000 kPa, 500°C. Twenty percent of the flow is extracted at 1000 kPa, 350°C to a feedwater heater, and the remainder flows out at 200 kPa, 200°C (see Fig. P4.84). Find the turbine power output.

C.V. Turbine Steady state, 1 inlet and 2 exit flows.

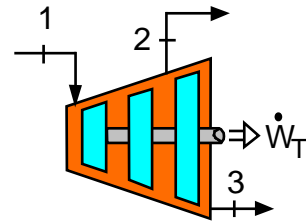
$$\text{Continuity Eq. 4.9: } \dot{m}_1 = \dot{m}_2 + \dot{m}_3 ; \Rightarrow \dot{m}_3 = \dot{m}_1 - \dot{m}_2 = 150 \text{ lbm/s}$$

$$\text{Energy Eq. 4.10: } \dot{m}_1 h_1 = \dot{W}_T + \dot{m}_2 h_2 + \dot{m}_3 h_3$$

$$\text{Table B.1.2 } h_1 = 3456.48 \text{ kJ/kg,}$$

$$h_2 = 3157.65 \text{ kJ/kg}$$

$$\text{Table B.1.1 : } h_3 = 2870.46 \text{ kJ/kg}$$



From the energy equation, Eq. 4.10

$$\begin{aligned} \dot{W}_T &= \dot{m}_1 h_1 - \dot{m}_2 h_2 - \dot{m}_3 h_3 = (5 \times 3456.48 - 1 \times 3157.65 - 4 \times 2870.46) \text{ kJ/s} \\ &= \mathbf{2643 \text{ kW}} \end{aligned}$$

4.85

A compressor receives 0.05 kg/s R-410A at 200 kPa, -20°C and 0.1 kg/s R-410A at 400 kPa, 0°C . The exit flow is at 1000 kPa, 60°C as shown in Fig. P4.85. Assume it is adiabatic, neglect kinetic energies and find the required power input.

C.V. whole compressor steady, 2 inlets, 1 exit, no heat transfer $\dot{Q} = 0$

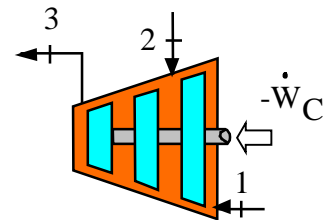
Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3 = 0.05 + 0.1 = 0.15 \text{ kg/s}$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 - \dot{W}_C = \dot{m}_3 h_3$

Table B.3.2: $h_1 = 278.72 \text{ kJ/kg}$,

$h_2 = 290.42 \text{ kJ/kg}$

Table B.3.2: $h_3 = 335.75 \text{ kJ/kg}$



$$\dot{W}_C = 0.05 \times 278.72 + 0.1 \times 290.42 - 0.15 \times 335.75 = -7.385 \text{ kW}$$

Power input is **7.4 kW**

4.86

Cogeneration is often used where a steam supply is needed for industrial process energy. Assume a supply of 5 kg/s steam at 0.5 MPa is needed. Rather than generating this from a pump and boiler, the setup in Fig. P4.86 is used so the supply is extracted from the high-pressure turbine. Find the power the turbine now cogenerates in this process.

Solution:

C.V. Turbine, steady state, 1 inlet and 2 exit flows, assume adiabatic, $\dot{Q}_{CV} = 0$

Continuity Eq.4.9: $\dot{m}_1 = \dot{m}_2 + \dot{m}_3$

Energy Eq.4.10: $\dot{Q}_{CV} + \dot{m}_1 h_1 = \dot{m}_2 h_2 + \dot{m}_3 h_3 + \dot{W}_T$;

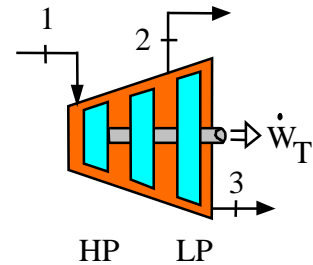
Supply state 1: 20 kg/s at 10 MPa, 500°C

Process steam 2: 5 kg/s, 0.5 MPa, 155°C,

Exit state 3: 20 kPa, $x = 0.9$

Table B.1.3: $h_1 = 3373.7$, $h_2 = 2755.9$ kJ/kg,

Table B.1.2: $h_3 = 251.4 + 0.9 \times 2358.3$
 $= 2373.9$ kJ/kg



$$\begin{aligned}\dot{W}_T &= (20 \times 3373.7 - 5 \times 2755.9 - 15 \times 2373.9) \text{ (kg/s) (kJ/kg)} \\ &= 18\,084 \text{ kW} = \mathbf{18.084 \text{ MW}}\end{aligned}$$

4.87

A steam turbine receives steam from two boilers. One flow is 5 kg/s at 3 MPa, 700°C and the other flow is 10 kg/s at 800 kPa, 500°C. The exit state is 10 kPa, with a quality of 96%. Find the total power out of the adiabatic turbine.

Solution:

C.V. whole turbine steady, 2 inlets, 1 exit, no heat transfer $\dot{Q} = 0$

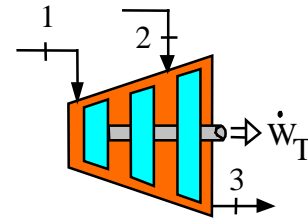
Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3 = 5 + 15 = 20 \text{ kg/s}$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 + \dot{W}_T$

Table B.1.3: $h_1 = 3911.7 \text{ kJ/kg}$,

$h_2 = 3480.6 \text{ kJ/kg}$

Table B.1.2: $h_3 = 191.8 + 0.96 \times 2392.8$
 $= 2488.9 \text{ kJ/kg}$



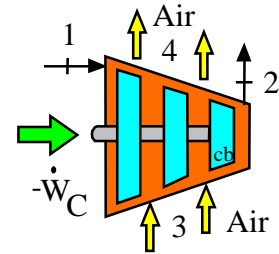
$$\dot{W}_T = 5 \times 3911.7 + 10 \times 3480.6 - 20 \times 2488.9 = 17\,031 \text{ kW} = \mathbf{17 \text{ MW}}$$

4.88

A compressor receives 0.1 kg/s R-134a at 150 kPa, -10°C and delivers it at 1000 kPa, 40°C . The power input is measured to be 3 kW. The compressor has heat transfer to air at 100 kPa coming in at 20°C and leaving at 30°C . How much is the mass flow rate of air?

Solution:

C.V. Compressor, steady state, single inlet and exit flow. For this device we also have an air flow outside the compressor housing no changes in kinetic or potential energy.



Continuity Eq.: $\dot{m}_2 = \dot{m}_1$

Energy Eq. 4.12: $\dot{m}_1 h_1 + \dot{W}_{in} + \dot{m}_{air} h_3 = \dot{m}_2 h_2 + \dot{m}_{air} h_4$

Ideal gas for air and constant specific heat: $h_4 - h_3 \sim C_{p, air} (T_4 - T_3)$

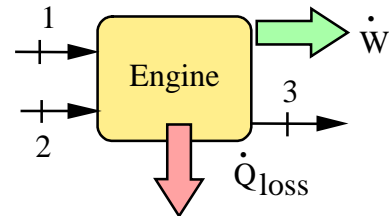
$$\begin{aligned} \dot{m}_{air} &= [\dot{m}_1 (h_1 - h_2) + \dot{W}_{in}] / C_{p, air} (T_4 - T_3) \\ &= \frac{0.1 (393.84 - 420.25) + 3}{1.004 (30 - 20)} = \frac{0.359 \text{ kW}}{10 \text{ kJ/kg}} \\ &= \mathbf{0.0359 \text{ kg/s}} \end{aligned}$$

4.89

Two steady flows of air enters a control volume, shown in Fig. P4.89. One is 0.025 kg/s flow at 350 kPa, 150°C, state 1, and the other enters at 450 kPa, 15°C, state 2. A single flow of air exits at 100 kPa, -40°C, state 3. The control volume rejects 1 kW heat to the surroundings and produces 4 kW of power. Neglect kinetic energies and determine the mass flow rate at state 2.

Solution:

C.V. Steady device with two inlet and one exit flows, we neglect kinetic energies. Notice here the Q is rejected so it goes out.



Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3 = 0.025 + \dot{m}_2$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 + \dot{W}_{CV} + \dot{Q}_{loss}$

Substitute the work and heat transfer into the energy equation and use constant specific heat

$$\begin{aligned} 0.025 \times 1.004 \times 423.2 + \dot{m}_2 \times 1.004 \times 288.2 \\ = (0.025 + \dot{m}_2) 1.004 \times 233.2 + 4.0 + 1.0 \end{aligned}$$

Now solve for \dot{m}_2 .

$$\begin{aligned} \dot{m}_2 &= \frac{4.0 + 1.0 + 0.025 \times 1.004 \times (233.2 - 423.2)}{1.004 (288.2 - 233.2)} \text{ kW/(kJ/kg)} \\ &= \mathbf{0.0042 \text{ kg/s}} \end{aligned}$$

4.90

A large expansion engine has two low velocity flows of water entering. High pressure steam enters at point 1 with 2.0 kg/s at 2 MPa, 500°C and 0.5 kg/s cooling water at 120 kPa, 30°C enters at point 2. A single flow exits at point 3 with 150 kPa, 80% quality, through a 0.15 m diameter exhaust pipe. There is a heat loss of 300 kW. Find the exhaust velocity and the power output of the engine.

Solution:

C.V. : Engine (Steady state)

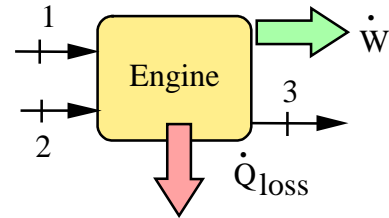
Constant rates of flow, \dot{Q}_{loss} and \dot{W}

State 1: Table B.1.3: $h_1 = 3467.6 \text{ kJ/kg}$

State 2: Table B.1.1: $h_2 = 125.77 \text{ kJ/kg}$

$h_3 = 467.1 + 0.8 \times 2226.5 = 2248.3 \text{ kJ/kg}$

$v_3 = 0.00105 + 0.8 \times 1.15825 = 0.92765 \text{ m}^3/\text{kg}$



Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3 = 2 + 0.5 = 2.5 \text{ kg/s} = (AV/v) = (\pi/4)D^2V/v$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 (h_3 + 0.5 V^2) + \dot{Q}_{\text{loss}} + \dot{W}$

$$V = \dot{m}_3 v_3 / [\frac{\pi}{4} D^2] = 2.5 \times 0.92765 / (0.7854 \times 0.15^2) = \mathbf{131.2 \text{ m/s}}$$

$$0.5 V^2 = (0.5 \times 131.2^2 \text{ m}^2/\text{s}^2) / 1000 \text{ J/kJ} = 8.6 \text{ kJ/kg}$$

$$\dot{W} = 2 \times 3467.6 + 0.5 \times 125.77 - 2.5 (2248.3 + 8.6) - 300 = \mathbf{1056 \text{ kW}}$$

Heat Exchangers

4.91

A condenser (heat exchanger) brings 1 kg/s water flow at 10 kPa quality 95% to saturated liquid at 10 kPa, as shown in Fig. P4.91. The cooling is done by lake water at 20°C that returns to the lake at 30°C. For an insulated condenser, find the flow rate of cooling water.

Solution:

C.V. Heat exchanger

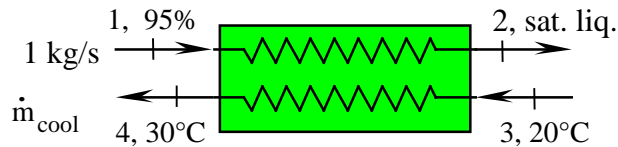


Table B.1.1: $h_{20} = 83.94 \text{ kJ/kg}$, $h_{30} = 125.77 \text{ kJ/kg}$

Table B.1.2: $h_{95\%, 10\text{kPa}} = 191.81 + 0.95 \times 2392.82 = 2465 \text{ kJ/kg}$

$h_{f, 10 \text{ kPa}} = 191.81 \text{ kJ/kg}$

Energy Eq.4.10: $\dot{m}_{\text{cool}} h_{20} + \dot{m}_{\text{H}_2\text{O}} h_{300} = \dot{m}_{\text{cool}} h_{30} + \dot{m}_{\text{H}_2\text{O}} h_{f, 10 \text{ kPa}}$

$$\dot{m}_{\text{cool}} = \dot{m}_{\text{H}_2\text{O}} \frac{h_{95\%} - h_{f, 10\text{kPa}}}{h_{30} - h_{20}} = 1 \text{ kg/s} \times \frac{2465 - 191.81}{125.77 - 83.94} = \mathbf{54.3 \text{ kg/s}}$$

4.92

Air at 600 K flows with 3 kg/s into a heat exchanger and out at 100°C. How much (kg/s) water coming in at 100 kPa, 20°C can the air heat to the boiling point?

C.V. Total heat exchanger. The flows are not mixed so the two flowrates are constant through the device. No external heat transfer and no work.

$$\text{Energy Eq.4.10: } \dot{m}_{\text{air}} h_{\text{air in}} + \dot{m}_{\text{water}} h_{\text{water in}} = \dot{m}_{\text{air}} h_{\text{air out}} + \dot{m}_{\text{water}} h_{\text{water out}}$$

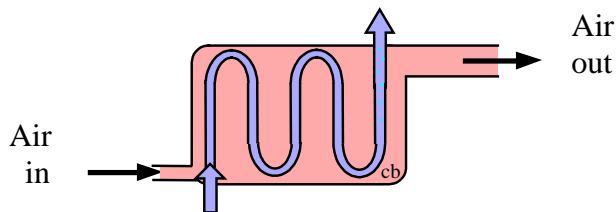
$$\dot{m}_{\text{air}} [h_{\text{air in}} - h_{\text{air out}}] = \dot{m}_{\text{water}} [h_{\text{water out}} - h_{\text{water in}}]$$

$$\text{Table B.1.2: } h_{\text{water out}} - h_{\text{water in}} = 2675.46 - 83.94 = 2591.5 \text{ kJ/kg}$$

$$\text{Table A.7.1: } h_{\text{air in}} - h_{\text{air out}} = 607.32 - 374.14 = 233.18 \text{ kJ/kg}$$

Solve for the flow rate of water from the energy equation

$$\dot{m}_{\text{water}} = \dot{m}_{\text{air}} \frac{h_{\text{air in}} - h_{\text{air out}}}{h_{\text{water out}} - h_{\text{water in}}} = 3 \text{ kg/s} \times \frac{233.18}{2591.5} = \mathbf{0.27 \text{ kg/s}}$$



4.93

Steam at 500 kPa, 300°C is used to heat cold water at 15°C to 75°C for domestic hot water supply. How much steam per kg liquid water is needed if the steam should not condense?

Solution:

C.V. Each line separately. No work but there is heat transfer out of the steam flow and into the liquid water flow.

$$\text{Water line energy Eq.: } \dot{m}_{\text{liq}} h_i + \dot{Q} = \dot{m}_{\text{liq}} h_e \Rightarrow \dot{Q} = \dot{m}_{\text{liq}} (h_e - h_i)$$

For the liquid water look in Table B.1.1

$$\begin{aligned} \Delta h_{\text{liq}} &= h_e - h_i = 313.91 - 62.98 = 250.93 \text{ kJ/kg} \\ &(\cong C_p \Delta T = 4.18 (75 - 15) = 250.8 \text{ kJ/kg}) \end{aligned}$$

Steam line energy has the same heat transfer but it goes out

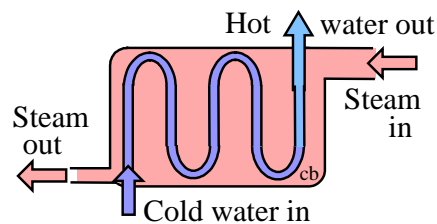
$$\text{Steam Energy Eq.: } \dot{m}_{\text{steam}} h_i = \dot{Q} + \dot{m}_{\text{steam}} h_e \Rightarrow \dot{Q} = \dot{m}_{\text{steam}} (h_i - h_e)$$

For the steam look in Table B.1.3 at 500 kPa

$$\Delta h_{\text{steam}} = h_i - h_e = 3064.2 - 2748.67 = 315.53 \text{ kJ/kg}$$

Now the heat transfer for the steam is substituted into the energy equation for the water to give

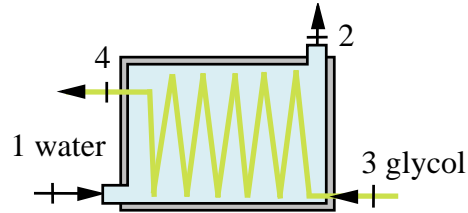
$$\dot{m}_{\text{steam}} / \dot{m}_{\text{liq}} = \Delta h_{\text{liq}} / \Delta h_{\text{steam}} = \frac{250.93}{315.53} = \mathbf{0.795}$$



4.94

A dual-fluid heat exchanger has 5 kg/s water entering at 40°C, 150 kPa and leaving at 10°C, 150 kPa. The other fluid is glycol, entering at −10°C, 160 kPa and leaving at 10°C, 160 kPa. Find the required mass flow rate of glycol and the rate of internal heat transfer.

C.V. Heat exchanger, steady flow 1 inlet and 1 exit for glycol and water each. The two flows exchange energy with no heat transfer to/from the outside.



Continuity Eqs.: Each line has a constant flow rate through it.

Energy Eq.4.10: $\dot{m}_{\text{H}_2\text{O}} h_1 + \dot{m}_{\text{glycol}} h_3 = \dot{m}_{\text{H}_2\text{O}} h_2 + \dot{m}_{\text{glycol}} h_4$

Process: Each line has a constant pressure.

Table B.1: $h_1 = 167.54 \text{ kJ/kg}$, $h_2 = 41.99 \text{ kJ/kg}$

Table A.4: $C_{P \text{ gly}} = 2.42 \text{ kJ/kg}\cdot\text{K}$ so

$$h_4 - h_3 = C_{P \text{ gly}} (T_4 - T_3) = 2.42 [10 - (-10)] = 48.4 \text{ kJ/kg}$$

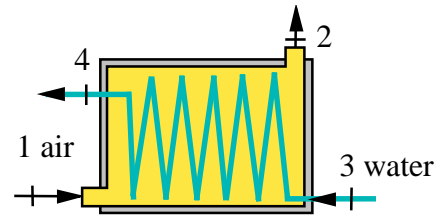
$$\dot{m}_{\text{glycol}} = \dot{m}_{\text{H}_2\text{O}} \frac{h_1 - h_2}{h_4 - h_3} = 5 \frac{167.54 - 41.99}{48.4} = \mathbf{12.97 \text{ kg/s}}$$

4.95

A heat exchanger, shown in Fig. P4.95, is used to cool an air flow from 800 K to 360 K, both states at 1 MPa. The coolant is a water flow at 15°C, 0.1 MPa. If the water leaves as saturated vapor, find the ratio of the flow rates $\dot{m}_{\text{H}_2\text{O}}/\dot{m}_{\text{air}}$

Solution:

C.V. Heat exchanger, steady flow 1 inlet and 1 exit for air and water each. The two flows exchange energy with no heat transfer to/from the outside.



Continuity Eqs.: Each line has a constant flow rate through it.

$$\text{Energy Eq. 4.10: } \dot{m}_{\text{air}}h_1 + \dot{m}_{\text{H}_2\text{O}}h_3 = \dot{m}_{\text{air}}h_2 + \dot{m}_{\text{H}_2\text{O}}h_4$$

Process: Each line has a constant pressure.

Air states, Table A.7.1: $h_1 = 822.20 \text{ kJ/kg}$, $h_2 = 360.86 \text{ kJ/kg}$

Water states, Table B.1.1: $h_3 = 62.98 \text{ kJ/kg}$ (at 15°C),

Table B.1.2: $h_4 = 2675.5 \text{ kJ/kg}$ (at 100 kPa)

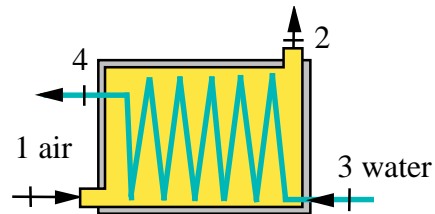
$$\dot{m}_{\text{H}_2\text{O}}/\dot{m}_{\text{air}} = \frac{h_1 - h_2}{h_4 - h_3} = \frac{822.20 - 360.86}{2675.5 - 62.99} = \mathbf{0.1766}$$

4.96

A superheater brings 2.5 kg/s saturated water vapor at 2 MPa to 450°C. The energy is provided by hot air at 1200 K flowing outside the steam tube in the opposite direction as the water, which is a counter flowing heat exchanger. Find the smallest possible mass flow rate of the air so the air exit temperature is 20°C larger than the incoming water temperature (so it can heat it).

Solution:

C.V. Superheater. Steady state with no external \dot{Q} or any \dot{W} the two flows exchanges energy inside the box. Neglect kinetic and potential energies at all states.



$$\text{Energy Eq.4.10: } \dot{m}_{\text{H}_2\text{O}} h_3 + \dot{m}_{\text{air}} h_1 = \dot{m}_{\text{H}_2\text{O}} h_4 + \dot{m}_{\text{air}} h_2$$

Process: Constant pressure in each line.

$$\text{State 1: Table B.1.2} \quad T_3 = 212.42^\circ\text{C}, \quad h_3 = 2799.51 \text{ kJ/kg}$$

$$\text{State 2: Table B.1.3} \quad h_4 = 3357.48 \text{ kJ/kg}$$

$$\text{State 3: Table A.7} \quad h_1 = 1277.81 \text{ kJ/kg}$$

$$\text{State 4:} \quad T_2 = T_3 + 20 = 232.42^\circ\text{C} = 505.57 \text{ K}$$

$$\text{A.7: } h_2 = 503.36 + \frac{5.57}{20} (523.98 - 503.36) = 509.1 \text{ kJ/kg}$$

From the energy equation we get

$$\begin{aligned} \dot{m}_{\text{air}} &= \dot{m}_{\text{H}_2\text{O}} (h_4 - h_3) / (h_1 - h_2) \\ &= 2.5 (3357.48 - 2799.51) / (1277.81 - 509.1) = \mathbf{1.815 \text{ kg/s}} \end{aligned}$$

4.97

A two fluid heat exchanger has 2 kg/s liquid ammonia at 20°C, 1003 kPa entering state 3 and exiting at state 4. It is heated by a flow of 1 kg/s nitrogen at 1500 K, state 1, leaving at 600 K, state 2 similar to Fig. P4.95. Find the total rate of heat transfer inside the heat exchanger. Sketch the temperature versus distance for the ammonia and find state 4 (T, v) of the ammonia.

Solution:

CV: Nitrogen flow line, steady rates of flow, \dot{Q} out and $\dot{W} = 0$

Continuity: $\dot{m}_1 = \dot{m}_2 = 1 \text{ kg/s}$; Energy Eq: $\dot{m}_1 h_1 = \dot{m}_2 h_2 + \dot{Q}_{\text{out}}$

Tbl. A.8: $h_1 = 1680.7 \text{ kJ/kg}$; $h_2 = 627.24 \text{ kJ/kg}$

$$\dot{Q}_{\text{out}} = \dot{m}_1 (h_1 - h_2) = 1 (1680.7 - 627.24) = \mathbf{1053.5 \text{ kW}}$$

If Tbl A.5 is used: $C_p = 1.042 \text{ kJ/kg K}$

$$\dot{Q}_{\text{out}} = \dot{m}_1 C_p (T_1 - T_2) = 1 \times 1.042 (1500 - 600) = \mathbf{937.8 \text{ kW}}$$

CV The whole heat exchanger: No external \dot{Q} , constant pressure in each line.

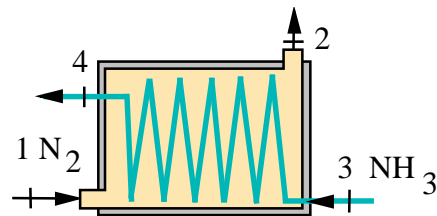
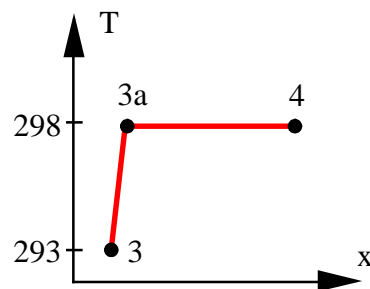
$$\dot{m}_1 h_1 + \dot{m}_3 h_3 = \dot{m}_1 h_2 + \dot{m}_3 h_4 \Rightarrow h_4 = h_3 + \dot{m}_1 (h_1 - h_2) / \dot{m}_3$$

$$h_4 = 274.3 + 1053.5 / 2 = 801 \text{ kJ/kg} < h_g \Rightarrow \text{2-phase}$$

$$x_4 = (h_4 - h_f) / h_{fg} = (801 - 298.25) / 1165.2 = 0.43147$$

$$v_4 = v_f + x_4 v_{fg} = 0.001658 + 0.43147 \times 0.12647 = 0.05623 \text{ m}^3/\text{kg}$$

$$T_4 = T_{3a} = 25^\circ\text{C} \text{ This is the boiling temperature for 1003 kPa.}$$



4.98

In a co-flowing (same direction) heat exchanger 1 kg/s air at 500 K flows into one channel and 2 kg/s air flows into the neighboring channel at 300 K. If it is infinitely long what is the exit temperature? Sketch the variation of T in the two flows.

C.V. Heat Exchanger (no \dot{W})

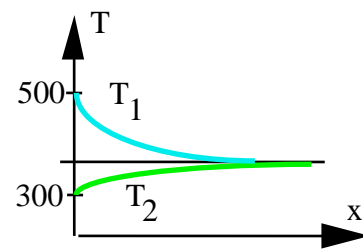
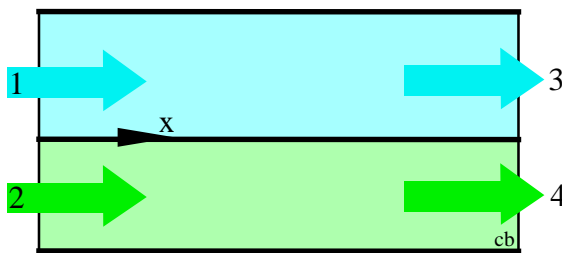
$$\text{Continuity Eq.:} \quad \dot{m}_1 = \dot{m}_3 \quad \text{and} \quad \dot{m}_2 = \dot{m}_4$$

$$\text{Energy Eq.4.10:} \quad \dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_1 h_3 + \dot{m}_2 h_4$$

$$\text{Same exit } T: \quad h_3 = h_4 = [\dot{m}_1 h_1 + \dot{m}_2 h_2] / [\dot{m}_1 + \dot{m}_2]$$

Using constant specific heat

$$T_3 = T_4 = \frac{\dot{m}_1}{\dot{m}_1 + \dot{m}_2} T_1 + \frac{\dot{m}_2}{\dot{m}_1 + \dot{m}_2} T_2 = \frac{1}{3} \times 500 + \frac{2}{3} \times 300 = \mathbf{367 \text{ K}}$$



4.99

An air/water counter flowing heat exchanger has one line with 2 kg/s at 125 kPa, 1000 K entering, and the air is leaving at 100 kPa, 400 K. The other line has 0.5 kg/s water entering at 200 kPa, 20°C and leaving at 200 kPa. What is the exit temperature of the water?

C.V. Heat Exchanger (no \dot{W})

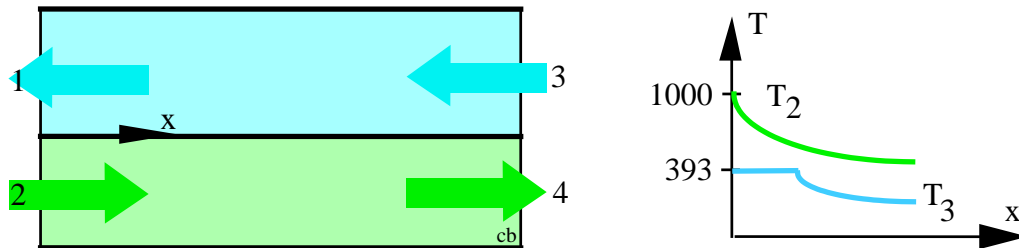
$$\text{Continuity Eq.:} \quad \dot{m}_1 = \dot{m}_3 = \dot{m}_{\text{H}_2\text{O}} \text{ and } \dot{m}_2 = \dot{m}_4 = \dot{m}_{\text{air}}$$

$$\text{Energy Eq.4.10:} \quad \dot{m}_{\text{H}_2\text{O}} h_1 + \dot{m}_{\text{air}} h_4 = \dot{m}_{\text{H}_2\text{O}} h_3 + \dot{m}_{\text{air}} h_2$$

Flowrates and properties known except for T_1

$$\begin{aligned} h_1 &= h_3 + \dot{m}_{\text{air}} (h_2 - h_4) / \dot{m}_{\text{H}_2\text{O}} \\ &= 83.94 + 2 (1046.22 - 401.3) / 0.5 = 2663.6 \text{ kJ/kg} \end{aligned}$$

$h_1 < h_g = 2706.6 \text{ kJ/kg}$ at 200 kPa so two-phase $T = 120.23^\circ\text{C}$



The water is not completely evaporated at the exit.

4.100

An automotive radiator has glycerine at 95°C enter and return at 55°C as shown in Fig. P4.100. Air flows in at 20°C and leaves at 25°C. If the radiator should transfer 25 kW what is the mass flow rate of the glycerine and what is the volume flow rate of air in at 100 kPa?

Solution:

If we take a control volume around the whole radiator then there is no external heat transfer - it is all between the glycerin and the air. So we take a control volume around each flow separately.

Glycerine: $\dot{m}h_i + (-\dot{Q}) = \dot{m}h_e$

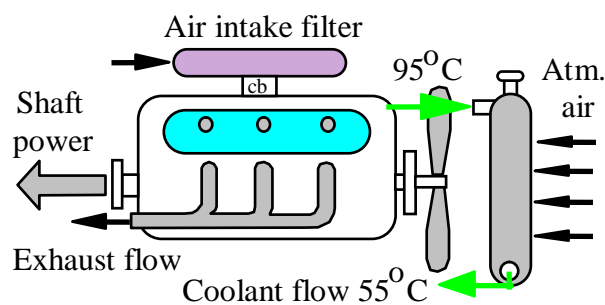
Table A.4: $\dot{m}_{\text{gly}} = \frac{-\dot{Q}}{h_e - h_i} = \frac{-\dot{Q}}{C_{\text{gly}}(T_e - T_i)} = \frac{-25}{2.42(55 - 95)} = \mathbf{0.258 \text{ kg/s}}$

Air $\dot{m}h_i + \dot{Q} = \dot{m}h_e$

Table A.5: $\dot{m}_{\text{air}} = \frac{\dot{Q}}{h_e - h_i} = \frac{\dot{Q}}{C_{\text{air}}(T_e - T_i)} = \frac{25}{1.004(25 - 20)} = 4.98 \text{ kg/s}$

$$\dot{V} = \dot{m}v_i; \quad v_i = \frac{RT_i}{P_i} = \frac{0.287 \times 293 \text{ kJ/kg-K} \times \text{K}}{100 \text{ kPa}} = 0.8409 \text{ m}^3/\text{kg}$$

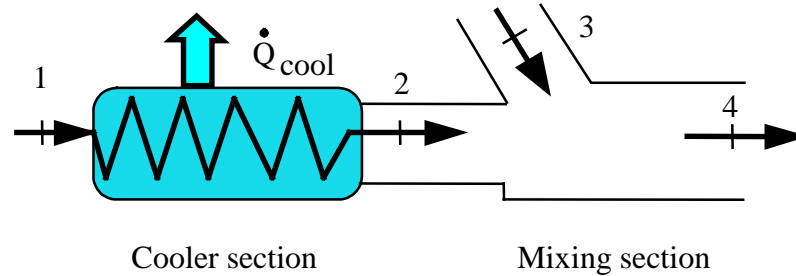
$$\dot{V}_{\text{air}} = \dot{m}v_i = 4.98 \times 0.8409 = \mathbf{4.19 \text{ m}^3/\text{s}}$$



4.101

A cooler in an air conditioner brings 0.5 kg/s air at 35°C to 5°C, both at 101 kPa and it then mix the output with a flow of 0.25 kg/s air at 20°C, 101 kPa sending the combined flow into a duct. Find the total heat transfer in the cooler and the temperature in the duct flow.

Solution:



C.V. Cooler section (no \dot{W})

$$\text{Energy Eq.4.12:} \quad \dot{m}h_1 = \dot{m}h_2 + \dot{Q}_{\text{cool}}$$

$$\dot{Q}_{\text{cool}} = \dot{m}(h_1 - h_2) = \dot{m} C_p (T_1 - T_2) = 0.5 \times 1.004 \times (35 - 5) = 15.06 \text{ kW}$$

C.V. mixing section (no \dot{W} , \dot{Q})

$$\text{Continuity Eq.:} \quad \dot{m}_2 + \dot{m}_3 = \dot{m}_4$$

$$\text{Energy Eq.4.10:} \quad \dot{m}_2 h_2 + \dot{m}_3 h_3 = \dot{m}_4 h_4$$

$$\dot{m}_4 = \dot{m}_2 + \dot{m}_3 = 0.5 + 0.25 = 0.75 \text{ kg/s}$$

$$\dot{m}_4 h_4 = (\dot{m}_2 + \dot{m}_3) h_4 = \dot{m}_2 h_2 + \dot{m}_3 h_3$$

$$\dot{m}_2 (h_4 - h_2) + \dot{m}_3 (h_4 - h_3) = 0$$

$$\dot{m}_2 C_p (T_4 - T_2) + \dot{m}_3 C_p (T_4 - T_3) = 0$$

$$T_4 = (\dot{m}_2 / \dot{m}_4) T_2 + (\dot{m}_3 / \dot{m}_4) T_3 = 5(0.5/0.75) + 20(0.25/0.75) = 10^\circ\text{C}$$

4.102

A copper wire has been heat treated to 1000 K and is now pulled into a cooling chamber that has 1.5 kg/s air coming in at 20°C; the air leaves the other end at 60°C. If the wire moves 0.25 kg/s copper, how hot is the copper as it comes out?

Solution:

C.V. Total chamber, no external heat transfer

$$\text{Energy eq.: } \dot{m}_{\text{cu}} h_{\text{icu}} + \dot{m}_{\text{air}} h_{\text{iair}} = \dot{m}_{\text{cu}} h_{\text{ecu}} + \dot{m}_{\text{air}} h_{\text{eair}}$$

$$\dot{m}_{\text{cu}} (h_e - h_i)_{\text{cu}} = \dot{m}_{\text{air}} (h_i - h_e)_{\text{air}}$$

$$\dot{m}_{\text{cu}} C_{\text{cu}} (T_e - T_i)_{\text{cu}} = \dot{m}_{\text{air}} C_{\text{p air}} (T_e - T_i)_{\text{air}}$$

Heat capacities from A.3 for copper and A.5 for air

$$(T_e - T_i)_{\text{cu}} = \frac{\dot{m}_{\text{air}} C_{\text{p air}}}{\dot{m}_{\text{cu}} C_{\text{cu}}} (T_e - T_i)_{\text{air}} = \frac{1.5 \times 1.004}{0.25 \times 0.42} (20 - 60) \text{ K} = -573.7 \text{ K}$$

$$T_e = T_i - 573.7 = 1000 - 573.7 = \mathbf{426.3 \text{ K}}$$



4.103

A coflowing (same-direction) heat exchanger has one line with 0.25 kg/s oxygen at 17°C, 200 kPa entering and the other line has 0.6 kg/s nitrogen at 150 kPa, 500 K entering. The heat exchanger is very long, so the two flows exit at the same temperature. Use constant heat capacities and find the exit temperature.

C.V. Heat Exchanger (no \dot{W})

$$\text{Continuity Eq.:} \quad \dot{m}_1 = \dot{m}_3 \quad \text{and} \quad \dot{m}_2 = \dot{m}_4$$

$$\text{Energy Eq.4.10:} \quad \dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_1 h_3 + \dot{m}_2 h_4$$

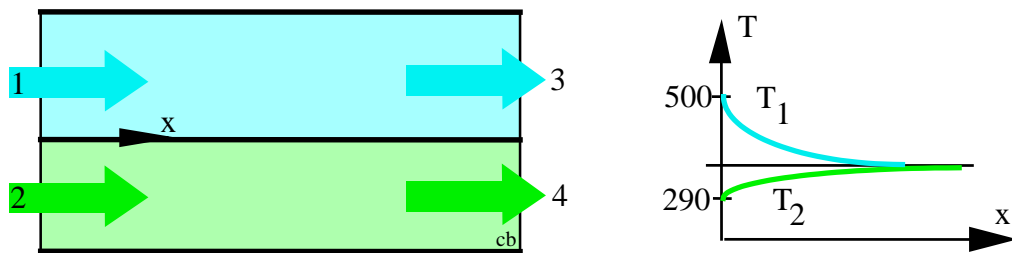
$$\text{Same exit T:} \quad T_3 = T_4 = T_{\text{ex}}$$

Using constant specific heat

$$\dot{m}_1 C_{P \text{ O}_2} T_1 + \dot{m}_2 C_{P \text{ N}_2} T_2 = \dot{m}_1 C_{P \text{ O}_2} T_{\text{ex}} + \dot{m}_2 C_{P \text{ N}_2} T_{\text{ex}}$$

$$T_{\text{ex}} = \frac{\dot{m}_1 C_{P \text{ O}_2}}{\dot{m}_1 C_{P \text{ O}_2} + \dot{m}_2 C_{P \text{ N}_2}} T_1 + \frac{\dot{m}_2 C_{P \text{ N}_2}}{\dot{m}_1 C_{P \text{ O}_2} + \dot{m}_2 C_{P \text{ N}_2}} T_2$$

$$= \frac{0.25 \times 0.922 \times 290 + 0.6 \times 1.042 \times 500}{0.25 \times 0.922 + 0.6 \times 1.042} = \mathbf{443.4 \text{ K}}$$



Mixing processes

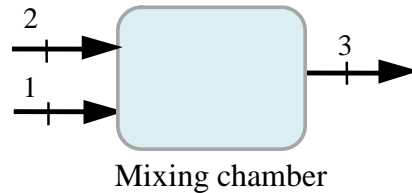
4.104

Two flows of air are both at 200 kPa; one has 1 kg/s at 400 K and the other has 2 kg/s at 290 K. The two flows are mixed together in an insulated box to produce a single exit flow at 200 kPa. Find the exit temperature.

Solution:

$$\text{Cont.:} \quad \dot{m}_1 + \dot{m}_2 = \dot{m}_3$$

$$\begin{aligned} \text{Energy:} \quad \dot{m}_1 h_1 + \dot{m}_2 h_2 &= \dot{m}_3 h_3 \\ &= (\dot{m}_1 + \dot{m}_2) h_3 \end{aligned}$$



Solve for the exit enthalpy

$$h_3 = [\dot{m}_1 h_1 + \dot{m}_2 h_2] / (\dot{m}_1 + \dot{m}_2)$$

since the T's are modest use constant specific heats

$$T_3 = [\dot{m}_1 T_1 + \dot{m}_2 T_2] / (\dot{m}_1 + \dot{m}_2) = \frac{1}{3} \times 400 + \frac{2}{3} \times 290 = \mathbf{326.7 \text{ K}}$$

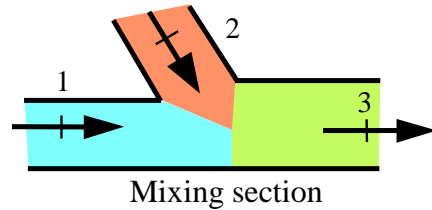
4.105

Two air flows are combined to a single flow. Flow one is $1 \text{ m}^3/\text{s}$ at 20°C and the other is $2 \text{ m}^3/\text{s}$ at 200°C both at 100 kPa . They mix without any heat transfer to produce an exit flow at 100 kPa . Neglect kinetic energies and find the exit temperature and volume flow rate.

Solution:

$$\text{Cont.} \quad \dot{m}_1 + \dot{m}_2 = \dot{m}_3$$

$$\begin{aligned} \text{Energy} \quad \dot{m}_1 h_1 + \dot{m}_2 h_2 &= \dot{m}_3 h_3 \\ &= (\dot{m}_1 + \dot{m}_2) h_3 \end{aligned}$$



$$\dot{m}_1 (h_3 - h_1) + \dot{m}_2 (h_3 - h_2) = 0$$

$$\dot{m}_1 C_p (T_3 - T_1) + \dot{m}_2 C_p (T_3 - T_2) = 0$$

$$T_3 = (\dot{m}_1 / \dot{m}_3) T_1 + (\dot{m}_2 / \dot{m}_3) T_2$$

We need to find the mass flow rates

$$v_1 = RT_1/P_1 = (0.287 \text{ kJ/kg-K} \times 293 \text{ K})/100 \text{ kPa} = 0.8409 \text{ m}^3/\text{kg}$$

$$v_2 = RT_2/P_2 = (0.287 \text{ kJ/kg-K} \times 473 \text{ K})/100 \text{ kPa} = 1.3575 \text{ m}^3/\text{kg}$$

$$\dot{m}_1 = \frac{\dot{V}_1}{v_1} = \frac{1}{0.8409} = 1.1892 \frac{\text{kg}}{\text{s}}, \quad \dot{m}_2 = \frac{\dot{V}_2}{v_2} = \frac{2}{1.3575} = 1.4733 \frac{\text{kg}}{\text{s}}$$

$$\dot{m}_3 = \dot{m}_1 + \dot{m}_2 = 2.6625 \text{ kg/s}$$

$$T_3 = \frac{1.1892}{2.6625} \times 20 + \frac{1.4733}{2.6625} \times 200 = \mathbf{119.6^\circ \text{C}}$$

$$v_3 = \frac{RT_3}{P_3} = \frac{0.287 (119.6 + 273)}{100} = 1.1268 \text{ m}^3/\text{kg}$$

$$\dot{V}_3 = \dot{m}_3 v_3 = 2.6625 \text{ kg/s} \times 1.1268 \text{ m}^3/\text{kg} = \mathbf{3.0 \text{ m}^3/\text{s}}$$

4.106

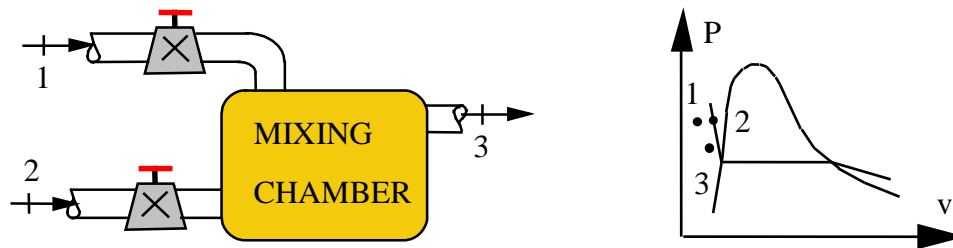
A flow of water at 2000 kPa, 20°C is mixed with a flow of 2 kg/s water at 2000 kPa, 180°C. What should the flowrate of the first flow be to produce an exit state of 200 kPa and 100°C?

Solution:

C.V. Mixing chamber and valves. Steady state no heat transfer or work terms.

Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$



Properties Table B.1.1: $h_1 = 85.8 \text{ kJ/kg}$; $h_3 = 419.0 \text{ kJ/kg}$

Table B.1.4: $h_2 = 763.7 \text{ kJ/kg}$

$$\dot{m}_1 = \dot{m}_2 \times \frac{h_2 - h_3}{h_3 - h_1} = 2 \times \frac{763.7 - 419.0}{419.0 - 85.8} = \mathbf{2.069 \text{ kg/s}}$$

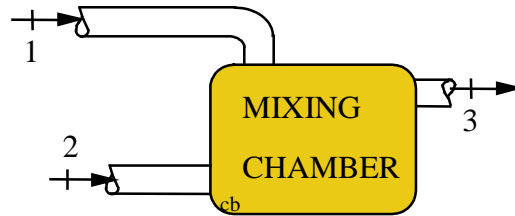
4.107

An open feedwater heater in a powerplant heats 4 kg/s water at 45°C, 100 kPa by mixing it with steam from the turbine at 100 kPa, 250°C. Assume the exit flow is saturated liquid at the given pressure and find the mass flow rate from the turbine.

Solution:

C.V. Feedwater heater.

No external \dot{Q} or \dot{W}



Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$

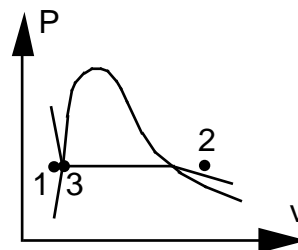
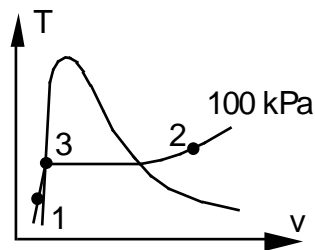
Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$

State 1: Table B.1.1 $h = h_f = 188.42 \text{ kJ/kg}$ at 45°C

State 2: Table B.1.3 $h_2 = 2974.33 \text{ kJ/kg}$

State 3: Table B.1.2 $h_3 = h_f = 417.44 \text{ kJ/kg}$ at 100 kPa

$$\dot{m}_2 = \dot{m}_1 \times \frac{h_1 - h_3}{h_3 - h_2} = 4 \times \frac{188.42 - 417.44}{417.44 - 2974.33} = \mathbf{0.358 \text{ kg/s}}$$



4.108

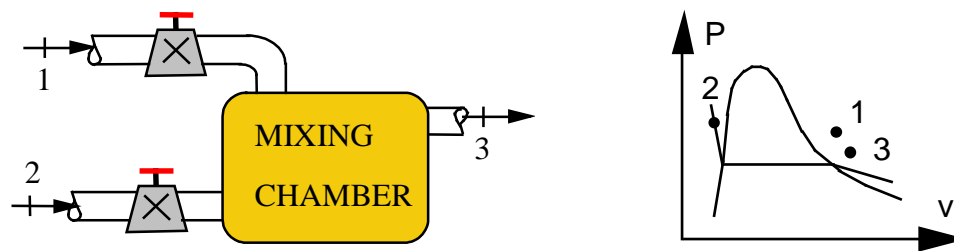
Two flows are mixed to form a single flow. Flow at state 1 is 1.5 kg/s water at 400 kPa, 200°C and flow at state 2 is 500 kPa, 100°C. Which mass flow rate at state 2 will produce an exit $T_3 = 150^\circ\text{C}$ if the exit pressure is kept at 300 kPa?

Solution:

C.V. Mixing chamber and valves. Steady state no heat transfer or work terms.

Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$



Properties Table B.1.3: $h_1 = 2860.51 \text{ kJ/kg}$; $h_3 = 2760.95 \text{ kJ/kg}$

Table B.1.4: $h_2 = 419.32 \text{ kJ/kg}$

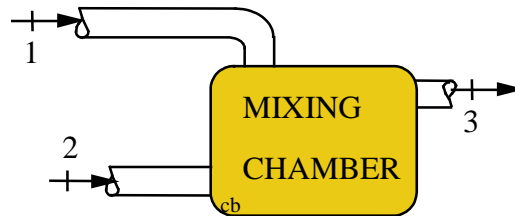
$$\dot{m}_2 = \dot{m}_1 \times \frac{h_1 - h_3}{h_3 - h_2} = 1.5 \times \frac{2860.51 - 2760.95}{2760.95 - 419.32} = \mathbf{0.0638 \text{ kg/s}}$$

4.109

A de-superheater has a flow of ammonia 1.5 kg/s at 1000 kPa, 100°C which is mixed with another flow of ammonia at 25°C and quality 50% in an adiabatic mixing chamber. Find the flow rate of the second flow so the outgoing ammonia is saturated vapor at 1000 kPa.

C.V. Desuperheater.

No external \dot{Q} or \dot{W}



Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$

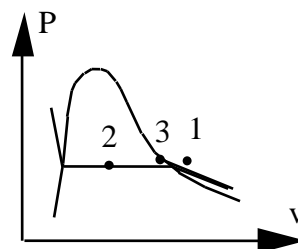
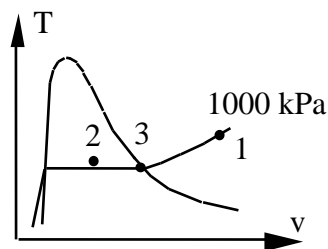
Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$

State 1: Table B.2.2 $h_1 = 1664.3 \text{ kJ/kg}$

State 2: Table B.2.1 $h_2 = 298.25 + 0.5 \times 1165.2 = 880.85 \text{ kJ/kg}$

State 3: Table B.2.2 $h_3 = 1463.4 \text{ kJ/kg}$

$$\dot{m}_2 = \dot{m}_1 \times \frac{h_1 - h_3}{h_3 - h_2} = 1.5 \times \frac{1664.3 - 1463.4}{1463.4 - 880.85} = \mathbf{0.517 \text{ kg/s}}$$

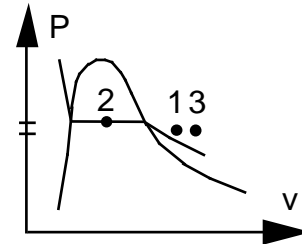
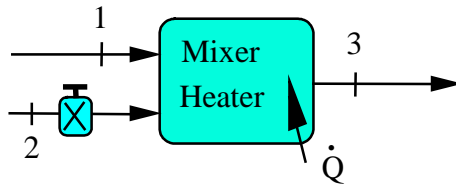


4.110

A mixing chamber with heat transfer receives 2 kg/s of R-410A at 1 MPa, 40°C in one line and 1 kg/s of R-410A at 15°C, quality 50% in a line with a valve. The outgoing flow is at 1 MPa, 60°C. Find the rate of heat transfer to the mixing chamber.

Solution:

C.V. Mixing chamber. Steady with 2 flows in and 1 out, heat transfer in.



$$\text{Continuity Eq. 4.9: } \dot{m}_1 + \dot{m}_2 = \dot{m}_3; \quad \Rightarrow \quad \dot{m}_3 = 2 + 1 = 3 \text{ kg/s}$$

$$\text{Energy Eq. 4.10: } \dot{m}_1 h_1 + \dot{m}_2 h_2 + \dot{Q} = \dot{m}_3 h_3$$

$$\text{Properties: Table B.4.2: } h_1 = 316.05 \text{ kJ/kg}, \quad h_3 = 335.75 \text{ kJ/kg}$$

$$\text{Table B.4.1: } h_2 = 81.15 + 0.5 \times 201.64 = 181.97 \text{ kJ/kg}$$

Energy equation then gives the heat transfer as

$$\dot{Q} = 3 \times 335.75 - 2 \times 316.05 - 1 \times 181.97 = \mathbf{193.18 \text{ kW}}$$

4.111

A geothermal supply of hot water at 500 kPa, 150°C is fed to an insulated flash evaporator at the rate of 1.5 kg/s. A stream of saturated liquid at 200 kPa is drained from the bottom of the chamber, and a stream of saturated vapor at 200 kPa is drawn from the top and fed to a turbine. Find the mass flow rate of the two exit flows.

C.V. Flash chamber. Disregard any kinetic and potential energies

$$\text{Continuity Eq.: } 0 = \dot{m}_1 - \dot{m}_2 - \dot{m}_3$$

$$\text{Energy Eq.: } 0 = \dot{m}_1 h_1 - \dot{m}_2 h_2 - \dot{m}_3 h_3$$

$$\begin{aligned} \text{Process: } \quad \dot{Q} = 0, \dot{W} = 0 \\ h_1 = 632.2 \text{ kJ/kg from Table B.1.4 (B.1.1: 632.18)} \end{aligned}$$

$$\begin{aligned} \text{State 2 and 3: } \quad \text{Saturated vapor } h_2 = 2706.63 \text{ kJ/kg} \\ \text{Saturated liquid } h_3 = 504.68 \text{ kJ/kg} \end{aligned}$$

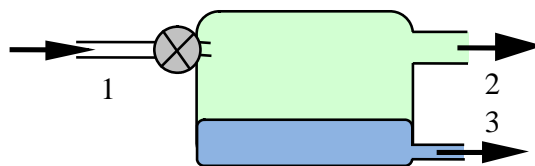
Substitute \dot{m}_3 from continuity eq. into the energy eq. to get

$$0 = \dot{m}_1 h_1 - \dot{m}_2 h_2 - (\dot{m}_1 - \dot{m}_2) h_3$$

$$\begin{aligned} \dot{m}_2 &= \dot{m}_1 (h_1 - h_3) / (h_2 - h_3) = \dot{m}_1 (h_1 - h_f) / (h_g - h_f) \\ &= 1.5 (632.2 - 504.68) / (2706.63 - 504.68) = \mathbf{0.0869 \text{ kg/s}} \end{aligned}$$

$$\dot{m}_3 = \dot{m}_1 - \dot{m}_2 = 1.5 - 0.0869 = \mathbf{1.413 \text{ kg/s}}$$

The fraction of the flow at state 2 equals the quality x in the flow right after the valve and the fraction going out at state 3 is $(1 - x)$



Two-phase out of the valve. The liquid drops to the bottom.

4.112

An insulated mixing chamber receives 2 kg/s R-134a at 1 MPa, 100°C in a line with low velocity. Another line with R-134a as saturated liquid 60°C flows through a valve to the mixing chamber at 1 MPa after the valve, as shown in Fig. P4.110. The exit flow is saturated vapor at 1 MPa flowing at 20 m/s. Find the flow rate for the second line.

Solution:

C.V. Mixing chamber. Steady state, 2 inlets and 1 exit flow.

Insulated $q = 0$, No shaft or boundary motion $w = 0$.

Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$;

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 (h_3 + \frac{1}{2} V_3^2)$

$$\dot{m}_2 (h_2 - h_3 - \frac{1}{2} V_3^2) = \dot{m}_1 (h_3 + \frac{1}{2} V_3^2 - h_1)$$

1: Table B.5.2: 1 MPa, 100°C, $h_1 = 483.36$ kJ/kg

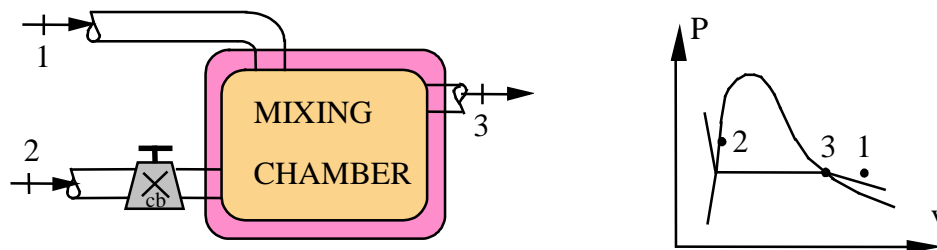
2: Table B.5.1: $x = \emptyset$, 60°C, $h_2 = 287.79$ kJ/kg

3: Table B.5.1: $x = 1$, 1 MPa, 20 m/s, $h_3 = 419.54$ kJ/kg

Now solve the energy equation for \dot{m}_2

$$\begin{aligned} \dot{m}_2 &= 2 \times [419.54 + \frac{1}{2} 20^2 \times \frac{1}{1000} - 483.36] / [287.79 - 419.54 - \frac{1}{2} \frac{20^2}{1000}] \\ &= 2 \times [-63.82 + 0.2] / [-131.75 - 0.2] = \mathbf{0.964 \text{ kg/s}} \end{aligned}$$

Notice how kinetic energy was insignificant.



4.113

To keep a jet engine cool some intake air bypasses the combustion chamber. Assume 2 kg/s hot air at 2000 K, 500 kPa is mixed with 1.5 kg/s air 500 K, 500 kPa without any external heat transfer. Find the exit temperature by using constant specific heat from Table A.5.

Solution:

C.V. Mixing Section

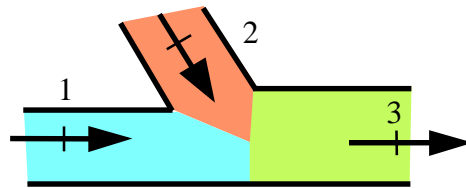
Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3 \Rightarrow \dot{m}_3 = 2 + 1.5 = 3.5 \text{ kg/s}$

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3$

$$h_3 = (\dot{m}_1 h_1 + \dot{m}_2 h_2) / \dot{m}_3 ;$$

For a constant specific heat divide the equation for h_3 with C_p to get

$$T_3 = \frac{\dot{m}_1}{\dot{m}_3} T_1 + \frac{\dot{m}_2}{\dot{m}_3} T_2 = \frac{2}{3.5} 2000 + \frac{1.5}{3.5} 500 = \mathbf{1357 \text{ K}}$$



Mixing section

4.114

Solve the previous problem using values from Table A.7

To keep a jet engine cool some intake air bypasses the combustion chamber.

Assume 2 kg/s hot air at 2000 K, 500 kPa is mixed with 1.5 kg/s air 500 K, 500 kPa without any external heat transfer. Find the exit temperature by using values from Table A.7.

Solution:

C.V. Mixing Section

$$\text{Continuity Eq.4.9:} \quad \dot{m}_1 + \dot{m}_2 = \dot{m}_3 \Rightarrow \dot{m}_3 = 2 + 1.5 = 3.5 \text{ kg/s}$$

$$\text{Energy Eq.4.10:} \quad \dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3$$

$$h_3 = (\dot{m}_1 h_1 + \dot{m}_2 h_2) / \dot{m}_3 ;$$

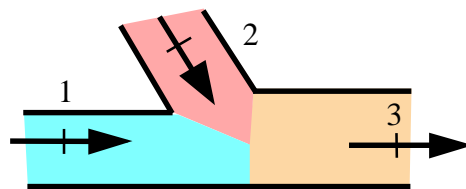
Using A.7 we look up the h at states 1 and 2 to calculate h_3

$$h_3 = \frac{\dot{m}_1}{\dot{m}_3} h_1 + \frac{\dot{m}_2}{\dot{m}_3} h_2 = \frac{2}{3.5} 2251.58 + \frac{1.5}{3.5} 503.36 = 1502 \text{ kJ/kg}$$

Now we can backinterpolate to find at what temperature do we have that h

$$T_3 = 1350 + 50 \frac{1502 - 1455.43}{1515.27 - 1455.43} = \mathbf{1389 \text{ K}}$$

This procedure is the most accurate.



Mixing section

Multiple Devices, Cycle Processes

4.115

A flow of 5 kg/s water at 100 kPa, 20°C should be delivered as steam at 1000 kPa, 350°C to some application. Consider compressing it to 1000 kPa, 20°C and then heat it at constant 1000 kPa to 350°C. Which devices are needed and find the specific energy transfers in those devices.

To raise the pressure of a liquid flow requires a pump which delivers the difference between the flow work going out and in. Constant pressure heating is a simple heater (or heat exchanger).

Inlet state: B.1.1: $h_1 = 83.94 \text{ kJ/kg}$, $v_1 = 0.001002 \text{ m}^3/\text{kg}$

State 3: $h_3 = 3157.65 \text{ kJ/kg}$

The pump delivers the difference between the flow work out and flow work in.

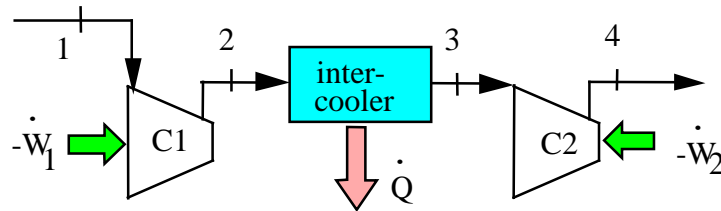
Pump: $-w_p = (P_2 - P_1) v_1 = (1000 - 100) \text{ kPa} \times 0.001002 \text{ m}^3/\text{kg}$
 $= \mathbf{0.9 \text{ kJ/kg}}$.

Heater: $q = h_3 - h_2 = h_3 - (h_1 - w_p)$
 $= 3157.65 - (83.94 + 0.9) = \mathbf{3072.8 \text{ kJ/kg}}$

4.116

A two-stage compressor takes nitrogen in at 20°C, 150 kPa and compresses it to 600 kPa, 450 K. Then it flows through an intercooler, where it cools to 320 K, and the second stage compresses it to 3000 kPa, 530 K. Find the specific work in each of the two compressor stages and the specific heat transfer in the intercooler.

The setup is like this:



C.V.: Stage 1 nitrogen, Steady flow

Process: adiabatic: $q = 0$,

Energy Eq. 4.13: $-w_{C1} = h_2 - h_1$,

Assume constant $C_{p0} = 1.042$ from A.5

$$w_{C1} = h_1 - h_2 = C_{p0}(T_1 - T_2) = 1.042 \text{ kJ/kgK} (293 - 450) \text{ K} = \mathbf{-163.6 \text{ kJ/kg}}$$

C.V. Intercooler, no work and no changes in kinetic or potential energy.

$$q_{23} = h_3 - h_2 = C_{p0}(T_3 - T_2) = 1.042 (320 - 450) = \mathbf{-135.5 \text{ kJ/kg}}$$

C.V. Stage 2. Analysis the same as stage 1.

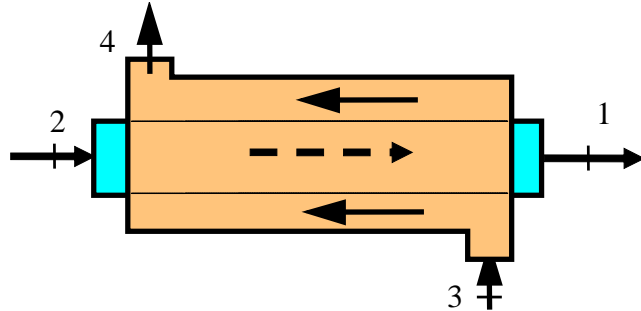
$$w_{C2} = h_3 - h_4 = C_{p0}(T_3 - T_4) = 1.042 (320 - 530) = \mathbf{-218.8 \text{ kJ/kg}}$$

4.117

The intercooler in the previous problem uses cold liquid water to cool the nitrogen. The nitrogen flow is 0.1 kg/s , and the liquid water inlet is 20°C and is set up to flow in the opposite direction from the nitrogen, so the water leaves at 35°C . Find the flow rate of the water.

Solution:

C.V. Heat exchanger, steady
2 flows in and two flows out.



$$\text{Continuity eq.:} \quad \dot{m}_1 = \dot{m}_2 = \dot{m}_{\text{H}_2\text{O}}; \quad \dot{m}_3 = \dot{m}_4 = \dot{m}_{\text{N}_2}$$

$$\text{Energy eq.:} \quad 0 = \dot{m}_{\text{H}_2\text{O}}(h_3 - h_4) + \dot{m}_{\text{N}_2}(h_2 - h_1)$$

Due to the lower range of temperature we will use constant specific heats from A.5 and A.4 so the energy equation is approximated as

$$0 = \dot{m}_{\text{H}_2\text{O}}C_{p\text{H}_2\text{O}}(T_3 - T_4) + \dot{m}_{\text{N}_2}C_p(T_2 - T_1)$$

Now solve for the water flow rate

$$\begin{aligned} \dot{m}_{\text{H}_2\text{O}} &= \dot{m}_{\text{N}_2} C_{p\text{N}_2} (T_2 - T_1) / [C_{p\text{H}_2\text{O}} (T_4 - T_3)] \\ &= 0.1 \text{ kg/s} \times 1.042 \times (450 - 320) / [4.18 \times (35 - 20)] \\ &= \mathbf{0.216 \text{ kg/s}} \end{aligned}$$

4.118

The following data are for a simple steam power plant as shown in Fig. P4.118.

State	1	2	3	4	5	6	7
P MPa	6.2	6.1	5.9	5.7	5.5	0.01	0.009
T °C		45	175	500	490		40
h kJ/kg	-	194	744	3426	3404	-	168

State 6 has $x_6 = 0.92$, and velocity of 200 m/s. The rate of steam flow is 25 kg/s, with 300 kW power input to the pump. Piping diameters are 200 mm from steam generator to the turbine and 75 mm from the condenser to the steam generator. Determine the velocity at state 5 and the power output of the turbine.

Solution:

$$\text{Turbine } A_5 = (\pi/4)(0.2)^2 = 0.03142 \text{ m}^2, v_5 = 0.06163 \text{ m}^3/\text{kg}$$

$$V_5 = \dot{m}v_5/A_5 = 25 \text{ kg/s} \times 0.06163 \text{ m}^3/\text{kg} / 0.03142 \text{ m}^2 = \mathbf{49 \text{ m/s}}$$

$$h_6 = 191.83 + 0.92 \times 2392.8 = 2393.2 \text{ kJ/kg}$$

$$\begin{aligned} w_T &= h_5 - h_6 + \frac{1}{2} (V_5^2 - V_6^2) \\ &= 3404 - 2393.2 + (49^2 - 200^2)/(2 \times 1000) = 992 \text{ kJ/kg} \end{aligned}$$

$$\dot{W}_T = \dot{m}w_T = 25 \text{ kg/s} \times 992 \text{ kJ/kg} = \mathbf{24\,800 \text{ kW}}$$

Remark: Notice the kinetic energy change is small relative to enthalpy change.

4.119

For the same steam power plant as shown in Fig. P4.118, assume the cooling water comes from a lake at 15°C and is returned at 25°C. Determine the rate of heat transfer in the condenser and the mass flow rate of cooling water from the lake.

Solution:

$$\text{Condenser } A_7 = (\pi/4)(0.075)^2 = 0.004\,418 \text{ m}^2, \quad v_7 = 0.001\,008 \text{ m}^3/\text{kg}$$

$$V_7 = \dot{m}v_7/A_7 = 25 \times 0.001\,008 / 0.004\,418 = 5.7 \text{ m/s}$$

$$h_6 = 191.83 + 0.92 \times 2392.8 = 2393.2 \text{ kJ/kg}$$

$$\begin{aligned} q_{\text{COND}} &= h_7 - h_6 + \frac{1}{2} (V_7^2 - V_6^2) \\ &= 168 - 2393.2 + (5.7^2 - 200^2)/(2 \times 1000) = -2245.2 \text{ kJ/kg} \end{aligned}$$

$$\dot{Q}_{\text{COND}} = 25 \text{ kg/s} \times (-2245.2 \text{ kJ/kg}) = \mathbf{-56\,130 \text{ kW}}$$

This rate of heat transfer is carried away by the cooling water so

$$-\dot{Q}_{\text{COND}} = \dot{m}_{\text{H}_2\text{O}}(h_{\text{out}} - h_{\text{in}})_{\text{H}_2\text{O}} = 56\,130 \text{ kW}$$

$$\Rightarrow \dot{m}_{\text{H}_2\text{O}} = \frac{56\,130}{104.9 - 63.0} \frac{\text{kW}}{\text{kJ/kg}} = \mathbf{1339.6 \text{ kg/s}}$$

4.120

For the same steam power plant as shown in Fig. P4.118, determine the rate of heat transfer in the economizer, which is a low temperature heat exchanger. Find also the rate of heat transfer needed in the steam generator.

Solution:

$$\text{Economizer} \quad A_7 = \pi D_7^2/4 = 0.004\,418 \text{ m}^2, \quad v_7 = 0.001\,008 \text{ m}^3/\text{kg}$$

$$V_2 = V_7 = \dot{m}v_7/A_7 = 25 \times 0.001\,008/0.004\,418 = 5.7 \text{ m/s},$$

$$V_3 = (v_3/v_2)V_2 = (0.001\,118 / 0.001\,008) 5.7 = 6.3 \text{ m/s} \approx V_2$$

so kinetic energy change unimportant

$$q_{\text{ECON}} = h_3 - h_2 = 744 - 194 = 550.0 \text{ kJ/kg}$$

$$\dot{Q}_{\text{ECON}} = \dot{m}q_{\text{ECON}} = 25 \text{ kg/s} \times 550.0 \text{ kJ/kg} = \mathbf{13\,750 \text{ kW}}$$

$$\text{Generator} \quad A_4 = \pi D_4^2/4 = 0.031\,42 \text{ m}^2, \quad v_4 = 0.060\,23 \text{ m}^3/\text{kg}$$

$$V_4 = \dot{m}v_4/A_4 = 25 \text{ kg/s} \times 0.060\,23 \text{ m}^3/\text{kg} / 0.031\,42 \text{ m}^2 = 47.9 \text{ m/s}$$

$$q_{\text{GEN}} = 3426 - 744 + (47.9^2 - 6.3^2)/(2 \times 1000) = 2683 \text{ kJ/kg}$$

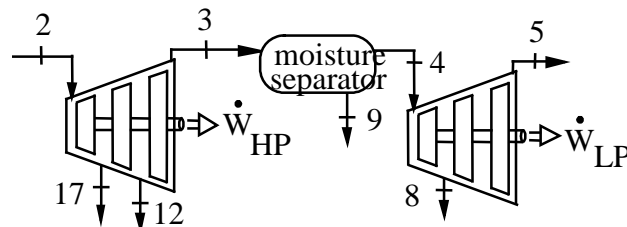
$$\dot{Q}_{\text{GEN}} = \dot{m}q_{\text{GEN}} = 25 \text{ kg/s} \times 2683 \text{ kJ/kg} = \mathbf{67\,075 \text{ kW}}$$

4.121

A somewhat simplified flow diagram for a nuclear power plant is given in Fig. P4.121. Mass flow rates and the various states in the cycle are shown in the accompanying table. The cycle includes a number of heaters in which heat is transferred from steam, taken out of the turbine at some intermediate pressure, to liquid water pumped from the condenser on its way to the steam drum. The heat exchanger in the reactor supplies 157 MW, and it may be assumed that there is no heat transfer in the turbines.

- Assume the moisture separator has no heat transfer between the two turbine sections, determine the enthalpy and quality (h_4, x_4).
- Determine the power output of the low-pressure turbine.
- Determine the power output of the high-pressure turbine.
- Find the ratio of the total power output of the two turbines to the total power delivered by the reactor.

Solution:



- a) Moisture Separator, steady state, no heat transfer, no work

$$\text{Continuity Eq.: } \dot{m}_3 = \dot{m}_4 + \dot{m}_9, \quad \dot{m}_4 = \dot{m}_3 - \dot{m}_9 = 62.874 - 4.662 = 58.212 \text{ kg/s}$$

$$\text{Energy Eq.: } \dot{m}_3 h_3 = \dot{m}_4 h_4 + \dot{m}_9 h_9 ;$$

From the energy equation we get

$$h_4 = (\dot{m}_3 h_3 - \dot{m}_9 h_9) / \dot{m}_4 = \frac{62.874 \times 2517 - 4.662 \times 558}{58.212} = 2673.9 \text{ kJ/kg}$$

$$h_4 = 2673.9 = 566.18 + x_4 \times 2160.6 \Rightarrow x_4 = \mathbf{0.9755}$$

- b) Low Pressure Turbine, steady state no heat transfer

$$\text{Continuity Eq.: } \dot{m}_4 = \dot{m}_5 + \dot{m}_8$$

$$\text{Energy Eq.: } \dot{m}_4 h_4 = \dot{m}_5 h_5 + \dot{m}_8 h_8 + \dot{W}_{CV(LP)}$$

$$\dot{m}_5 = \dot{m}_4 - \dot{m}_8 = 58.212 - 2.772 = 55.44 \text{ kg/s}$$

$$\begin{aligned} \dot{W}_{CV(LP)} &= \dot{m}_4 h_4 - \dot{m}_5 h_5 - \dot{m}_8 h_8 \\ &= 58.212 \times 2673.9 - 55.44 \times 2279 - 2.772 \times 2459 \\ &= 22\,489 \text{ kW} = \mathbf{22.489 \text{ MW}} \end{aligned}$$

c) High Pressure Turbine, steady state no heat transfer

$$\text{Energy Eq.: } \dot{m}_2 h_2 = \dot{m}_3 h_3 + \dot{m}_{12} h_{12} + \dot{m}_{17} h_{17} + \dot{W}_{\text{CV(HP)}}$$

$$\begin{aligned}\dot{W}_{\text{CV(HP)}} &= \dot{m}_2 h_2 - \dot{m}_3 h_3 - \dot{m}_{12} h_{12} - \dot{m}_{17} h_{17} \\ &= 75.6 \times 2765 - 62.874 \times 2517 - 8.064 \times 2517 - 4.662 \times 2593 \\ &= 18\,394 \text{ kW} = \mathbf{18.394 \text{ MW}}\end{aligned}$$

$$\text{d) } \eta = (\dot{W}_{\text{HP}} + \dot{W}_{\text{LP}}) / \dot{Q}_{\text{REACT}} = (22.489 + 18.394) / 157 = \mathbf{0.26}$$

4.122

Consider the power plant as described in the previous problem.

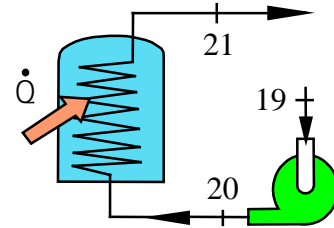
- Determine the quality of the steam leaving the reactor.
- What is the power to the pump that feeds water to the reactor?

Solution:

a) Reactor: Cont.: $\dot{m}_{20} = \dot{m}_{21}$; $\dot{Q}_{CV} = 157 \text{ MW}$

Energy Eq.4.12:

$$\dot{Q}_{CV} + \dot{m}_{20}h_{20} = \dot{m}_{21}h_{21}$$



$$157\,000 \text{ kW} + 1386 \text{ kg/s} \times 1221 \text{ kJ/kg} = 1386 \text{ kg/s} \times h_{21}$$

$$h_{21} = 1334.3 \text{ kJ/kg} = (1282.4 + x_{21} \times 1458.3) \text{ kJ/kg} \quad \Rightarrow \quad x_{21} = \mathbf{0.0349}$$

- b) C.V. Reactor feedwater pump

Cont. $\dot{m}_{19} = \dot{m}_{20}$ Energy Eq.: $\dot{m}_{19}h_{19} = \dot{m}_{19}h_{20} + \dot{W}_{CV,P}$

Table B.1: $h_{19} = h(277^\circ\text{C}, 7240 \text{ kPa}) = 1220 \text{ kJ/kg}$, $h_{20} = 1221 \text{ kJ/kg}$

$$\dot{W}_{CV,P} = \dot{m}_{19}(h_{19} - h_{20}) = 1386 \text{ kg/s} (1220 - 1221) \text{ kJ/kg} = \mathbf{-1386 \text{ kW}}$$

4.123

A R-410A heat pump cycle shown in Fig. P4.123 has a R-410A flow rate of 0.05 kg/s with 5 kW into the compressor. The following data are given

State	1	2	3	4	5	6
P, kPa	3100	3050	3000	420	400	390
T, °C	120	110	45		-10	-5
h, kJ/kg	377	367	134	-	280	284

Calculate the heat transfer from the compressor, the heat transfer from the R-410A in the condenser and the heat transfer to the R-410A in the evaporator.

Solution:

CV: Compressor

$$\dot{Q}_{\text{COMP}} = \dot{m}(h_1 - h_6) + \dot{W}_{\text{COMP}} = 0.05 (377 - 284) - 5.0 = \mathbf{-0.35 \text{ kW}}$$

CV: Condenser

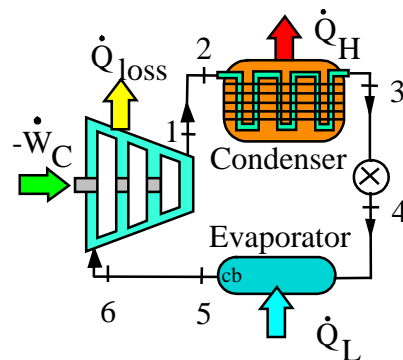
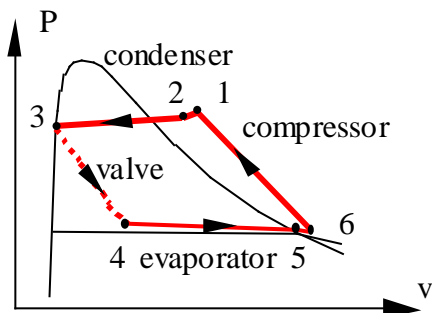
$$\dot{Q}_{\text{COND}} = \dot{m}(h_3 - h_2) = 0.05 \text{ kg/s} (134 - 367) \text{ kJ/kg} = \mathbf{-11.65 \text{ kW}}$$

C.V. Valve:

$$h_4 = h_3 = 134 \text{ kJ/kg}$$

CV: Evaporator

$$\dot{Q}_{\text{EVAP}} = \dot{m} (h_5 - h_4) = 0.05 \text{ kg/s} (280 - 134) \text{ kJ/kg} = \mathbf{7.3 \text{ kW}}$$



4.124

A modern jet engine has a temperature after combustion of about 1500 K at 3200 kPa as it enters the turbine section, see state 3 Fig. P.4.124. The compressor inlet is 80 kPa, 260 K state 1 and outlet state 2 is 3300 kPa, 780 K; the turbine outlet state 4 into the nozzle is 400 kPa, 900 K and nozzle exit state 5 at 80 kPa, 640 K. Neglect any heat transfer and neglect kinetic energy except out of the nozzle. Find the compressor and turbine specific work terms and the nozzle exit velocity.

Solution:

The compressor, turbine and nozzle are all steady state single flow devices and they are adiabatic.

We will use air properties from table A.7.1:

$$h_1 = 260.32, \quad h_2 = 800.28, \quad h_3 = 1635.80, \quad h_4 = 933.15, \quad h_5 = 649.53 \text{ kJ/kg}$$

Energy equation for the compressor gives

$$w_{c \text{ in}} = h_2 - h_1 = 800.28 - 260.32 = \mathbf{539.36 \text{ kJ/kg}}$$

Energy equation for the turbine gives

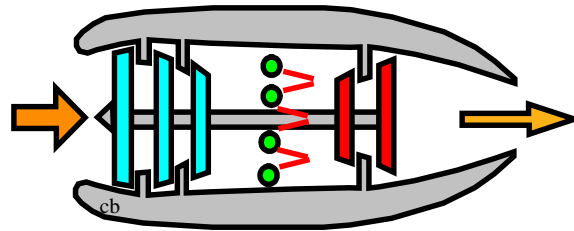
$$w_T = h_3 - h_4 = 1635.80 - 933.15 = \mathbf{702.65 \text{ kJ/kg}}$$

Energy equation for the nozzle gives

$$h_4 = h_5 + \frac{1}{2} V_5^2$$

$$\frac{1}{2} V_5^2 = h_4 - h_5 = 933.15 - 649.53 = 283.62 \text{ kJ/kg}$$

$$V_5 = [2(h_4 - h_5)]^{1/2} = (2 \times 283.62 \times 1000)^{1/2} = \mathbf{753 \text{ m/s}}$$



4.125

A proposal is made to use a geothermal supply of hot water to operate a steam turbine, as shown in Fig. P4.125. The high-pressure water at 1.5 MPa, 180°C, is throttled into a flash evaporator chamber, which forms liquid and vapor at a lower pressure of 400 kPa. The liquid is discarded while the saturated vapor feeds the turbine and exits at 10 kPa, 90% quality. If the turbine should produce 1 MW, find the required mass flow rate of hot geothermal water in kilograms per hour.

Solution:

Separation of phases in flash-evaporator
constant h in the valve flow so

Table B.1.3: $h_1 = 763.5 \text{ kJ/kg}$

$$h_1 = 763.5 = 604.74 + x \times 2133.8$$

$$\Rightarrow x = 0.07439 = \dot{m}_2 / \dot{m}_1$$

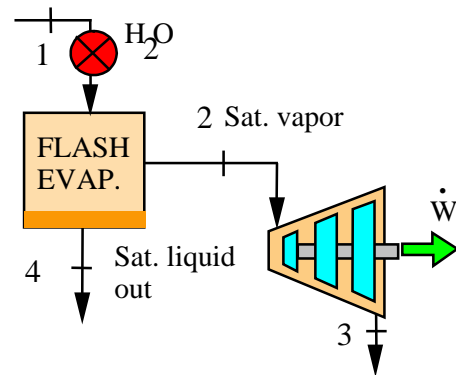
Table B.1.2: $h_2 = 2738.6 \text{ kJ/kg}$;

$$h_3 = 191.83 + 0.9 \times 2392.8 = 2345.4 \text{ kJ/kg}$$

Energy Eq.4.12 for the turbine

$$\dot{W} = \dot{m}_2(h_2 - h_3) \quad \Rightarrow \quad \dot{m}_2 = \frac{1000}{2738.6 - 2345.4} \frac{\text{kW}}{\text{kJ/kg}} = 2.543 \text{ kg/s}$$

$$\Rightarrow \dot{m}_1 = \dot{m}_2 / x = 34.19 \text{ kg/s} = \mathbf{123\,075 \text{ kg/h}}$$



Transient processes

4.126

An initially empty cylinder is filled with air from 20°C, 100 kPa until it is full. Assuming no heat transfer is the final temperature larger, equal to or smaller than 20°C? Does the final T depend on the size of the cylinder?

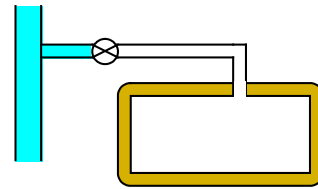
This is a transient problem with no heat transfer and no work. The balance equations for the tank as C.V. become

$$\text{Continuity Eq.:} \quad m_2 - 0 = m_i$$

$$\text{Energy Eq.:} \quad m_2 u_2 - 0 = m_i h_i + Q - W = m_i h_i + 0 - 0$$

$$\text{Final state:} \quad u_2 = h_i \quad \& \quad P_2 = P_i$$

$T_2 > T_i$ and it does not depend on V



4.127

An initially empty canister of volume 0.2 m^3 is filled with carbon dioxide from a line at 800 kPa, 400 K. Assume the process runs until it stops by itself and it is adiabatic. Use constant specific heat to find the final temperature in the canister.

C.V. Canister and valve, transient process with no heat transfer or work.

Continuity Eq.4.15: $m_2 - m_1 = m_{\text{in}} ;$

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = - m_{\text{in}} h_{\text{in}} + {}_1Q_2 - {}_1W_2$

Process: ${}_1Q_2 = 0, V = \text{constant}$ so ${}_1W_2 = 0$

State 1: $m_1 = 0 \Rightarrow m_2 = m_{\text{in}}$

State 2: $P_2 = P_{\text{line}} = 800 \text{ kPa},$ one more property

Energy Eq.: $u_2 = h_{\text{in}} = u_{\text{in}} + RT_{\text{in}} \Rightarrow C_{\text{VO}} T_2 = C_{\text{VO}} T_{\text{in}} + RT_{\text{in}} = C_{\text{Po}} T_{\text{in}}$

$T_2 = (C_{\text{Po}}/C_{\text{VO}}) T_{\text{in}} = k \times T_{\text{in}} = 1.289 \times 400 \text{ K} = \mathbf{515.6 \text{ K}}$

4.128

Repeat the previous problem but use the ideal gas Tables A.8 to solve it.

C.V. Canister and valve, transient process with no heat transfer or work.

Continuity Eq.4.15: $m_2 - m_1 = m_{in}$;

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = - m_{in} h_{in} + {}_1Q_2 - {}_1W_2$

Process: ${}_1Q_2 = 0$, $V = \text{constant}$ so ${}_1W_2 = 0$

State 1: $m_1 = 0 \Rightarrow m_2 = m_{in}$

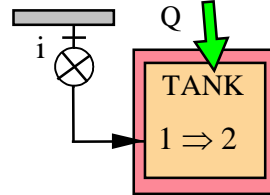
State 2: $P_2 = P_{line} = 800 \text{ kPa}$, one more property

Energy Eq.: $u_2 = h_{in} = 303.76 \text{ kJ/kg}$ from A.8

back interpolate for u_2 : $T_2 = \mathbf{495.9 \text{ K}}$

4.129

A tank contains 1 m^3 air at 100 kPa, 300 K. A pipe flowing air at 1000 kPa, 300 K is connected to the tank and it is filled slowly to 1000 kPa. Find the heat transfer to reach a final temperature of 300 K.



C.V. The tank volume and the compressor.

This is a transient problem (filling of tank).

Continuity Eq.4.15: $m_2 - m_1 = m_{in}$

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = {}_1Q_2 - {}_1W_2 + m_{in} h_{in}$

Process: Constant volume ${}_1W_2 = 0$,

States: $u_1 = u_2 = u_{in} = u_{300}$; $h_{in} = u_{in} + RT_{in}$

$$m_1 = P_1 V_1 / RT_1 = 100 \text{ kPa} \times 1 \text{ m}^3 / (0.287 \text{ kJ/kg-K} \times 300 \text{ K}) \\ = 1.1614 \text{ kg}$$

$$m_2 = P_2 V_2 / RT_2 = 1000 \text{ kPa} \times 1 \text{ m}^3 / (0.287 \text{ kJ/kg-K} \times 300 \text{ K}) \\ = 11.6144 \text{ kg}$$

Heat transfer from the energy equation

$${}_1Q_2 = m_2 u_2 - m_1 u_1 - m_{in} h_{in} = (m_1 + m_{in}) u_1 - m_1 u_1 - m_{in} u_{in} - m_{in} RT_{in} \\ = m_1 u_1 - m_1 u_1 + m_{in} u_1 - m_{in} u_{in} - m_{in} RT_{in} = -m_{in} RT_{in} \\ = (11.6144 - 1.1614) \text{ kg} \times 0.287 \text{ kJ/kg-K} \times 300 \text{ K} = \mathbf{-900 \text{ kJ}}$$

4.130

A 1-m³ tank contains ammonia at 150 kPa, 25°C. The tank is attached to a line flowing ammonia at 1200 kPa, 60°C. The valve is opened, and mass flows in until the tank is half full of liquid, by volume at 25°C. Calculate the heat transferred from the tank during this process.

Solution:

C.V. Tank. Transient process as flow comes in.

State 1 Table B.2.2 interpolate between 20 °C and 30°C:

$$v_1 = 0.9552 \text{ m}^3/\text{kg}; \quad u_1 = 1380.6 \text{ kJ/kg}$$

$$m_1 = V/v_1 = 1/0.9552 = 1.047 \text{ kg}$$

State 2: 0.5 m³ liquid and 0.5 m³ vapor from Table B.2.1 at 25°C

$$v_f = 0.001658 \text{ m}^3/\text{kg}; \quad v_g = 0.12813 \text{ m}^3/\text{kg}$$

$$m_{\text{LIQ}2} = 0.5/0.001658 = 301.57 \text{ kg}, \quad m_{\text{VAP}2} = 0.5/0.12813 = 3.902 \text{ kg}$$

$$m_2 = 305.47 \text{ kg}, \quad x_2 = m_{\text{VAP}2}/m_2 = 0.01277,$$

From continuity equation

$$m_i = m_2 - m_1 = 304.42 \text{ kg}$$

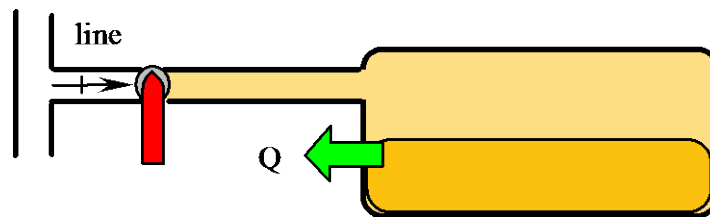
Table B.2.1: $u_2 = 296.6 + 0.01277 \times 1038.4 = 309.9 \text{ kJ/kg}$

State inlet: Table B.2.2 $h_i = 1553.3 \text{ kJ/kg}$

Energy Eq.4.16:

$$Q_{\text{CV}} + m_i h_i = m_2 u_2 - m_1 u_1$$

$$Q_{\text{CV}} = 305.47 \times 309.9 - 1.047 \times 1380.6 - 304.42 \times 1553.3 = \mathbf{-379\,636 \text{ kJ}}$$



4.131

A 2.5-L tank initially is empty and we want 10 g of ammonia in it. The ammonia comes from a line with saturated vapor at 25°C. To end up with the desired amount we cool the can while we fill it in a slow process keeping the can and content at 30°C. Find the final pressure to reach before closing the valve and the heat transfer?

Solution:

C.V. Tank:

Continuity Eq.4.15: $m_i = m_2$

Energy Eq.4.16: $m_2 u_2 - 0 = m_i h_i + {}_1Q_2$

State 2: 30°C, $v_2 = V/m_2 = 0.0025 \text{ m}^3/0.010 \text{ kg} = 0.25 \text{ m}^3/\text{kg}$

From Table B.2.2 we locate the state between 500 and 600 kPa.

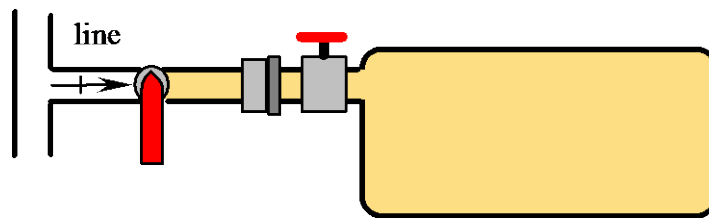
$$P_2 = 500 + (600 - 500) \frac{0.25 - 0.28103}{0.23152 - 0.28103} = \mathbf{562.7 \text{ kPa}}$$

$$u_2 = 1370 \text{ kJ/kg},$$

State i Table B.2.2: $h_i = 1463.5 \text{ kJ/kg}$

Now use the energy equation to solve for the heat transfer

$$\begin{aligned} {}_1Q_2 &= m_2 u_2 - m_i h_i = m_2 (u_2 - h_i) \\ &= 0.01 \text{ kg} \times (1370 - 1463.5) \text{ kJ/kg} = \mathbf{-0.935 \text{ kJ}} \end{aligned}$$



4.132

An evacuated 150-L tank is connected to a line flowing air at room temperature, 25°C, and 8 MPa pressure. The valve is opened allowing air to flow into the tank until the pressure inside is 6 MPa. At this point the valve is closed. This filling process occurs rapidly and is essentially adiabatic. The tank is then placed in storage where it eventually returns to room temperature. What is the final pressure?

Solution:

C.V. Tank:

Continuity Eq.4.15: $m_i = m_2$

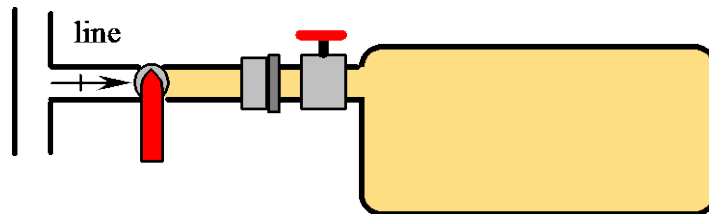
Energy Eq.4.16: $m_i h_i = m_2 u_2 \Rightarrow u_2 = h_i$

Use constant specific heat C_{p0} from table A.5 then energy equation:

$$T_2 = (C_p/C_v) T_i = k T_i = 1.4 \times 298.2 = 417.5 \text{ K}$$

Process: constant volume cooling to T_3 :

$$P_3 = P_2 \times T_3/T_2 = 6.0 \text{ MPa} \times 298.15 \text{ K} / 417.5 \text{ K} = \mathbf{4.29 \text{ MPa}}$$



4.133

An insulated 2-m³ tank is to be charged with R-134a from a line flowing the refrigerant at 3 MPa, 90°C. The tank is initially evacuated, and the valve is closed when the pressure inside the tank reaches 3 MPa. Find the mass in the tank and its final temperature.

C.V. Tank and valve, transient process with no heat transfer or work.

Continuity Eq.4.15: $m_2 - m_1 = m_{in}$;

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = -m_{in} h_{in} + {}_1Q_2 - {}_1W_2$

Process: ${}_1Q_2 = 0$, $V = \text{constant}$ so ${}_1W_2 = 0$

State 1: $m_1 = 0 \Rightarrow m_2 = m_{in}$

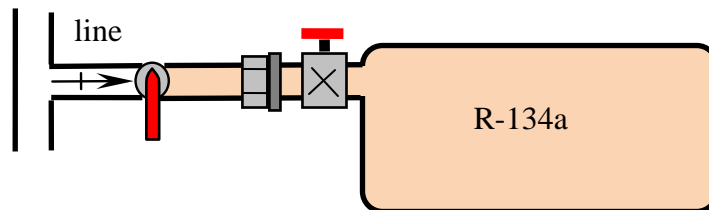
State 2: $P_2 = P_{line} = 3 \text{ MPa}$, one more property

Energy Eq.: $u_2 = h_{in} = 436.19 \text{ kJ/kg}$

State 2: (P, u) interpolate B.5.2: $T_2 = 100 + 10 \frac{436.19 - 433.77}{446.48 - 433.77} = \mathbf{101.9^\circ C}$,

$$v_2 = 0.00665 + 0.1904 (0.00734 - 0.00665) = 0.006781 \text{ m}^3/\text{kg}$$

$$m_2 = V/v_2 = [2 \text{ m}^3 / 0.006781 \text{ m}^3/\text{kg}] = \mathbf{294.9 \text{ kg}}$$



4.134

Find the final state for the previous problem if the valve is closed when the tank reaches 2 MPa.

C.V. Tank and valve, transient process with no heat transfer or work.

Continuity Eq.4.15: $m_2 - m_1 = m_{in}$;

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = - m_{in} h_{in} + {}_1Q_2 - {}_1W_2$

Process: ${}_1Q_2 = 0$, $V = \text{constant}$ so ${}_1W_2 = 0$

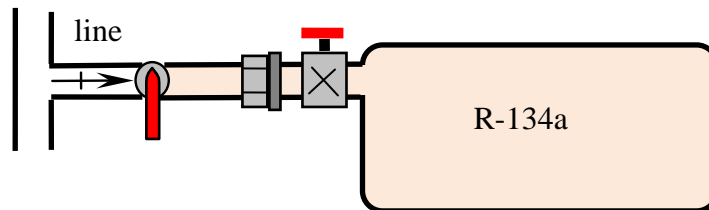
State 1: $m_1 = 0 \Rightarrow m_2 = m_{in}$

State 2: $P_2 = 2 \text{ MPa}$, one more property

Energy Eq.: $u_2 = h_{in} = 436.19 \text{ kJ/kg}$

State 2: (P, u) B.5.2: $T_2 = 90^\circ\text{C}$ very close, $v_2 = 0.01137 \text{ m}^3/\text{kg}$

$$m_2 = V/v_2 = [2 \text{ m}^3 / 0.01137 \text{ m}^3/\text{kg}] = \mathbf{175.9 \text{ kg}}$$



4.135

Helium in a steel tank is at 250 kPa, 300 K with a volume of 0.1 m^3 . It is used to fill a balloon. When the tank pressure drops to 150 kPa the flow of helium stops by itself. If all the helium still is at 300 K how big a balloon did I get? Assume the pressure in the balloon varies linearly with volume from 100 kPa ($V = 0$) to the final 150 kPa. How much heat transfer did take place?

Solution:

Take a C.V. of all the helium.
This is a control mass, the tank mass changes density and pressure.

$$\text{Energy Eq.: } U_2 - U_1 = {}_1Q_2 - {}_1W_2$$

$$\text{Process Eq.: } P = 100 + CV$$

$$\text{State 1: } P_1, T_1, V_1$$

$$\text{State 2: } P_2, T_2, V_2 = ?$$

Ideal gas:

$$P_2 V_2 = mRT_2 = mRT_1 = P_1 V_1$$

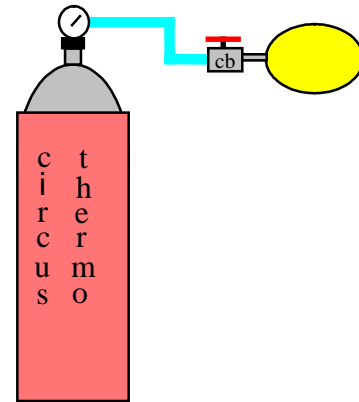
$$V_2 = V_1(P_1/P_2) = 0.1 \times (250/150) = 0.16667 \text{ m}^3$$

$$V_{\text{bal}} = V_2 - V_1 = 0.16667 - 0.1 = 0.06667 \text{ m}^3$$

$$\begin{aligned} {}_1W_2 &= \int P dV = \text{AREA} = \frac{1}{2} (P_1 + P_2) (V_2 - V_1) \\ &= \frac{1}{2} (250 + 150) \text{ kPa} \times 0.06667 \text{ m}^3 = 13.334 \text{ kJ} \end{aligned}$$

$$U_2 - U_1 = {}_1Q_2 - {}_1W_2 = m(u_2 - u_1) = mC_v (T_2 - T_1) = 0$$

$$\text{so } {}_1Q_2 = {}_1W_2 = \mathbf{13.334 \text{ kJ}}$$



Remark: The process is transient, but you only see the flow mass if you select the tank or the balloon as a control volume. That analysis leads to more terms that must be eliminated between the tank control volume and the balloon control volume.

4.136

A 25-L tank, shown in Fig. P4.136, that is initially evacuated is connected by a valve to an air supply line flowing air at 20°C, 800 kPa. The valve is opened, and air flows into the tank until the pressure reaches 600 kPa. Determine the final temperature and mass inside the tank, assuming the process is adiabatic. Develop an expression for the relation between the line temperature and the final temperature using constant specific heats.

Solution:

C.V. Tank:

Continuity Eq.4.15: $m_2 = m_i$

Energy Eq.4.16: $m_2 u_2 = m_i h_i$

Table A.7: $u_2 = h_i = 293.64 \text{ kJ/kg}$

$$\Rightarrow T_2 = \mathbf{410.0 \text{ K}}$$

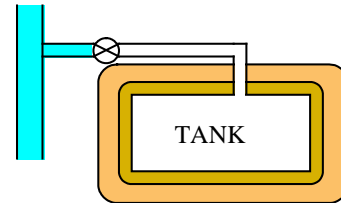
$$m_2 = \frac{P_2 V}{RT_2} = \frac{600 \times 0.025}{0.287 \times 410} = \mathbf{0.1275 \text{ kg}}$$

Assuming constant specific heat,

$$h_i = u_i + RT_i = u_2, \quad RT_i = u_2 - u_i = C_{v0}(T_2 - T_i)$$

$$C_{v0}T_2 = (C_{v0} + R)T_i = C_{p0}T_i, \quad T_2 = \left(\frac{C_{p0}}{C_{v0}}\right)T_i = kT_i$$

$$\text{For } T_i = 293.2\text{K \& constant } C_{p0}, \quad T_2 = 1.40 \times 293.2 = \mathbf{410.5 \text{ K}}$$



4.137

A nitrogen line, 300 K and 0.5 MPa, shown in Fig. P4.137, is connected to a turbine that exhausts to a closed initially empty tank of 50 m³. The turbine operates to a tank pressure of 0.5 MPa, at which point the temperature is 250 K. Assuming the entire process is adiabatic, determine the turbine work.

Solution:

C.V. turbine & tank \Rightarrow Transient process

Conservation of mass Eq.4.15: $m_1 = m_2 \Rightarrow m$

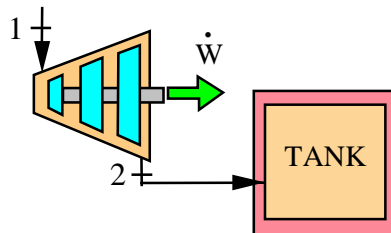
Energy Eq.4.16: $m_1 h_1 = m_2 u_2 + W_{CV}$; $W_{CV} = m(h_1 - u_2)$

Table B.6.2: $P_1 = 0.5$ MPa, $T_1 = 300$ K, Nitrogen; $h_1 = 310.28$ kJ/kg

2: $P_2 = 0.5$ MPa, $T_2 = 250$ K, $u_2 = 183.89$ kJ/kg, $v_2 = 0.154$ m³/kg

$$m_2 = V/v_2 = 50 \text{ m}^3 / (0.154 \text{ m}^3/\text{kg}) = 324.7 \text{ kg}$$

$$W_{CV} = 324.7 \text{ kg} (310.28 - 183.89) \text{ kJ/kg} = 41\,039 \text{ kJ} = \mathbf{41.04 \text{ MJ}}$$



We could with good accuracy have solved using ideal gas and Table A.5

4.138

A 1- m³ rigid tank contains 100 kg R-410A at ambient temperature 15°C. A valve on top of the tank is opened, and saturated vapor is throttled to ambient pressure, 100 kPa, and flows to a collector system. During the process, the temperature inside the tank remains at 15°C. The valve is closed when no more liquid remains inside. Calculate the heat transfer to the tank.

C.V. Tank, no work and neglect kinetic and potential energies.

$$\text{Continuity Eq.4.15: } m_2 - m_1 = -m_e$$

$$\text{Energy Eq.4.16: } m_2 u_2 - m_1 u_1 = {}_1Q_2 - m_e h_e$$

State 1 has $v_1 = V/m_1 = 1/100 = 0.01 \text{ m}^3/\text{kg} < v_g$ so two-phase

$$\text{B.4.1: } x_1 = (0.01 - 0.000904)/0.01955 = 0.46527$$

$$u_1 = u_f + x_1 u_{fg} = 80.02 + x_1 \times 177.1 = 162.42 \text{ kJ/kg}$$

State 2 is saturated vapor $T_2 = 15^\circ\text{C}$

$$v_2 = v_g = 0.02045 \text{ m}^3/\text{kg}, \quad u_2 = u_g = 257.12 \text{ kJ/kg}$$

$$m_2 = V/v_2 = \frac{1 \text{ m}^3}{0.02045 \text{ m}^3/\text{kg}} = 48.9 \text{ kg}$$

The exit state e: $h_e = h_g = 282.79 \text{ kJ/kg}$

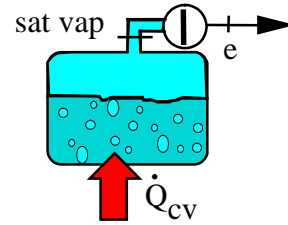
$$\begin{aligned} {}_1Q_2 &= m_2 u_2 - m_1 u_1 + m_e h_e \\ &= 48.9 \times 257.12 - 100 \times 162.42 + (100 - 48.9) \times 282.79 \\ &= \mathbf{10\,782 \text{ kJ}} \end{aligned}$$

4.139

A 200 liter tank initially contains water at 100 kPa and a quality of 1%. Heat is transferred to the water thereby raising its pressure and temperature. At a pressure of 2 MPa a safety valve opens and saturated vapor at 2 MPa flows out. The process continues, maintaining 2 MPa inside until the quality in the tank is 90%, then stops. Determine the total mass of water that flowed out and the total heat transfer.

Solution:

C.V. Tank, no work but heat transfer in and flow out. Denoting State 1: initial state, State 2: valve opens, State 3: final state.



$$\text{Continuity Eq.: } m_3 - m_1 = -m_e$$

$$\text{Energy Eq.: } m_3 u_3 - m_1 u_1 = -m_e h_e + {}_1Q_3$$

$$\begin{aligned} \text{State 1 Table B.1.2: } v_1 &= v_f + x_1 v_{fg} = 0.001043 + 0.01 \times 1.69296 \\ &= 0.01797 \text{ m}^3/\text{kg} \end{aligned}$$

$$u_1 = u_f + x_1 u_{fg} = 417.33 + 0.01 \times 2088.72 = 438.22 \text{ kJ/kg}$$

$$m_1 = V/v_1 = 0.2 \text{ m}^3 / (0.01797 \text{ m}^3/\text{kg}) = 11.13 \text{ kg}$$

$$\begin{aligned} \text{State 3 (2MPa): } v_3 &= v_f + x_3 v_{fg} = 0.001177 + 0.9 \times 0.09845 = 0.08978 \text{ m}^3/\text{kg} \end{aligned}$$

$$u_3 = u_f + x_3 u_{fg} = 906.42 + 0.9 \times 1693.84 = 2430.88 \text{ kJ/kg}$$

$$m_3 = V/v_3 = 0.2 \text{ m}^3 / (0.08978 \text{ m}^3/\text{kg}) = 2.23 \text{ kg}$$

$$\text{Exit state (2MPa): } h_e = h_g = 2799.51 \text{ kJ/kg}$$

$$\text{Hence: } m_e = m_1 - m_3 = 11.13 \text{ kg} - 2.23 \text{ kg} = \mathbf{8.90 \text{ kg}}$$

Applying the 1st law between state 1 and state 3

$$\begin{aligned} {}_1Q_3 &= m_3 u_3 - m_1 u_1 + m_e h_e \\ &= 2.23 \times 2430.88 - 11.13 \times 438.22 + 8.90 \times 2799.51 \\ &= 25\,459 \text{ kJ} = \mathbf{25.46 \text{ MJ}} \end{aligned}$$

4.140

A 1-L can of R-134a is at room temperature 20°C with a quality 50%. A leak in the top valve allows vapor to escape and heat transfer from the room takes place so we reach a final state of 5°C with a quality of 100%. Find the mass that escaped and the heat transfer.

Solution:

CV The can of R-134a not including the nozzle/valve out to ambient 20°C

Continuity Eq.: $m_2 - m_1 = -m_e$

Energy Eq.: $m_2 u_2 - m_1 u_1 = -m_e h_e + {}_1Q_2 - {}_1W_2$

Process Eq.: $V = \text{constant} \Rightarrow {}_1W_2 = \int P dV = 0$

State 1: (T,x) $v_1 = v_f + x_1 v_{fg} = 0.000817 + 0.5 \times 0.03524 = 0.018437 \text{ m}^3/\text{kg}$

$$u_1 = u_f + x_1 u_{fg} = 227.03 + 0.5 \times 162.16 = 308.11 \text{ kJ/kg}$$

$$m_1 = V / v_1 = 0.001 \text{ m}^3 / 0.018437 \text{ m}^3/\text{kg} = 0.05424 \text{ kg}$$

State 2: (T,x)

$$v_2 = v_g = 0.05833 \text{ m}^3/\text{kg}, \quad u_2 = u_g = 380.85 \text{ kJ/kg}$$

$$m_2 = V / v_2 = 0.001 \text{ m}^3 / 0.05833 \text{ m}^3/\text{kg} = 0.017144 \text{ kg}$$

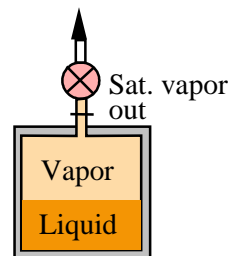
Exit state e: Saturated vapor starting at 20°C ending at 5°C so we take an **average**

$$h_e = 0.5(h_{e1} + h_{e2}) = 0.5 (409.84 + 401.32) = 405.58 \text{ kJ/kg}$$

$$m_e = m_1 - m_2 = \mathbf{0.0371 \text{ kg}}$$

The heat transfer from the energy equation becomes

$${}_1Q_2 = m_2 u_2 - m_1 u_1 + m_e h_e = 6.5293 - 16.7119 + 15.047 = \mathbf{4.864 \text{ kJ}}$$



4.141

A 2 m tall cylinder has a small hole in the bottom. It is filled with liquid water 1 m high, on top of which is 1 m high air column at atmospheric pressure of 100 kPa. As the liquid water near the hole has a higher P than 100 kPa it runs out. Assume a slow process with constant T . Will the flow ever stop? When?

Solution:

$$P_{\text{bot}} = P_{\text{air}} + \rho_f g L_f$$

For the air $PV = mRT$ and the total height is $H = 2$ m

$$P_{\text{air}} = mRT/V_{\text{air}} \quad ; \quad V_{\text{air}} = A L_{\text{air}} = A (H - L_f)$$

$$P_{\text{bot}} = \frac{m_a R_a T_a}{A(H-L_f)} + \rho_f g L_f = \frac{P_{a1} V_{a1}}{A(H-L_f)} + \rho_f g L_f = \frac{P_{a1} L_{a1}}{H-L_f} + \rho_f g L_f \geq P_o$$

Solve for L_f ; $\rho_f = 1/(v_f) = 1/0.0021002 = 998 \text{ kg/m}^3$

$$P_{a1} L_{a1} + \rho_f g L_f (H - L_f) \geq P_o (H - L_f)$$

$$(\rho_f g H + P_o) L_f - \rho_f g L_f^2 = P_o H - P_{a1} L_{a1} \geq 0$$

Put in numbers and solve quadratic eq.

$$L_f^2 - [H + (P_o/\rho_f g)] L_f + \frac{P_o H - P_{a1} L_{a1}}{\rho_f g} = 0$$

$$(P_o/\rho_f g) = \frac{100 \text{ kPa m}^3 \text{ s}^3}{998 \times 9.807 \text{ kg m}} = 10.217 \text{ m}$$

$$\frac{P_o H - P_{a1} L_{a1}}{\rho_f g} = \frac{100 (2-1)}{998 \times 9.807} = 10.217 \text{ m}$$

$$L_f^2 - 12.217 L_f + 10.217 = 0$$

$$L_f = \frac{12.217}{2} \pm \sqrt{\frac{12.217^2}{4} - \frac{12.217}{4}} = 6.1085 \pm 5.2055$$

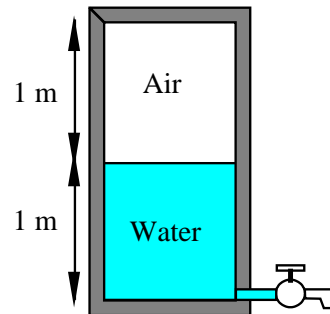
$\Rightarrow 11.314 \quad \text{or} \quad \mathbf{0.903 \text{ m}} \quad \text{so the second root is the solution}$

Verify

$$P_{a2} = P_{a1} \cdot \frac{L_{a1}}{H-L_f} = 100 \frac{1}{2 - 0.903} = 91.158 \text{ kPa}$$

$$\rho_f g L_f = 998 \times 9.807 \times 0.903 = 8838 \text{ Pa} = 8.838 \text{ kPa}$$

$$P_{\text{bot}} = P_{a2} + \rho_f g L_f = 91.158 + 8.838 = 99.996 \text{ kPa} \quad \text{OK}$$



Review Problems

4.142

A pipe of radius R has a fully developed laminar flow of air at P_o , T_o with a velocity profile as: $V = V_c [1 - (r/R)^2]$, where V_c is the velocity on the center-line and r is the radius as shown in Fig. P4.142. Find the total mass flow rate and the average velocity both as functions of V_c and R .

$$\dot{m} = A V / v = \dot{V} / v$$

Since the velocity is distributed we need to integrate over the area. From Eq.4.2

$$\dot{V} = \int V_{\text{local}} dA = \int V(r) 2\pi r dr$$

where W is the depth. Substituting the velocity we get

$$\begin{aligned} \dot{V} &= \int V_c 2\pi r [1 - (r/R)^2] dr \\ &= 2\pi V_c R^2 \int_0^1 z (1 - z^2) dz \\ &= 2\pi V_c R^2 \left(\frac{1}{2} z^2 - \frac{1}{4} z^4 \right) \Big|_0^1 = \frac{\pi}{2} V_c R^2 = \frac{1}{2} V_c A \end{aligned}$$

$$V = \dot{V} / A = \frac{1}{2} V_c$$

$$\dot{m} = \dot{V} / v = \frac{\pi}{2} V_c R^2 / v$$

4.143

Steam at 3 MPa, 400°C enters a turbine with a volume flow rate of 5 m³/s. An extraction of 15% of the inlet mass flow rate exits at 600 kPa, 200°C. The rest exits the turbine at 20 kPa with a quality of 90%, and a velocity of 20 m/s. Determine the volume flow rate of the extraction flow and the total turbine work.

Solution:

Inlet flow (Table B.1.3): $v_1 = 0.09936 \text{ m}^3/\text{kg}$, $h_1 = 3230.82 \text{ kJ/kg}$

$$\dot{m}_1 = \dot{V}/v_1 = 5/0.09936 = 50.32 \text{ kg/s}$$

Extraction flow : $v_2 = 0.35202 \text{ m}^3/\text{kg}$; $h_2 = 2850.12 \text{ kJ/kg}$

$$\dot{m}_2 = 0.15 \dot{m}_1 = 7.55 \text{ kg/s};$$

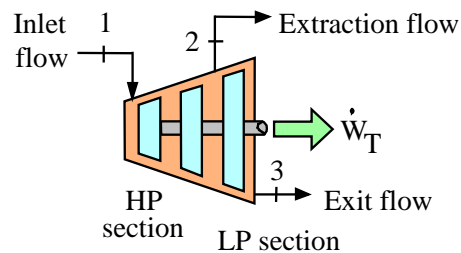
$$\dot{V}_2 = \dot{m}_2 v = 7.55 \text{ kg/s} \times 0.35202 \text{ m}^3/\text{kg} = \mathbf{2.658 \text{ m}^3/\text{s}}$$

Exit flow : $\dot{m}_3 = 0.85 \dot{m}_1 = 42.77 \text{ kg/s}$

Table B.1.2 $h_3 = 251.38 + 0.9 \times 2358.33 = 2373.88 \text{ kJ/kg}$

$$\text{Energy Eq.: } 0 = \dot{m}_1 h_1 - \dot{m}_2 h_2 - \dot{m}_3 h_3 - \dot{W}_T$$

$$\begin{aligned} \dot{W}_T &= \dot{m}_1 h_1 - \dot{m}_2 h_2 - \dot{m}_3 h_3 \\ &= 50.32 \times 3230.82 - 7.55 \times 2850.12 - 42.77 \times 2373.88 \\ &= \mathbf{39\,525 \text{ kW}} = 39.5 \text{ MW} \end{aligned}$$



4.144

In a glass factory a 2 m wide sheet of glass at 1500 K comes out of the final rollers that fix the thickness at 5 mm with a speed of 0.5 m/s. Cooling air in the amount of 20 kg/s comes in at 17°C from a slot 2 m wide and flows parallel with the glass. Suppose this setup is very long so the glass and air comes to nearly the same temperature (a co-flowing heat exchanger) what is the exit temperature?

Solution:

$$\text{Energy Eq.: } \dot{m}_{\text{glass}} h_{\text{glass } 1} + \dot{m}_{\text{air}} h_{\text{air } 2} = \dot{m}_{\text{glass}} h_{\text{glass } 3} + \dot{m}_{\text{air}} h_{\text{air } 4}$$

$$\dot{m}_{\text{glass}} = \rho \dot{V} = \rho A V = 2500 \text{ kg/m}^3 \times 2 \text{ m} \times 0.005 \text{ m} \times 0.5 \text{ m/s} = 12.5 \text{ kg/s}$$

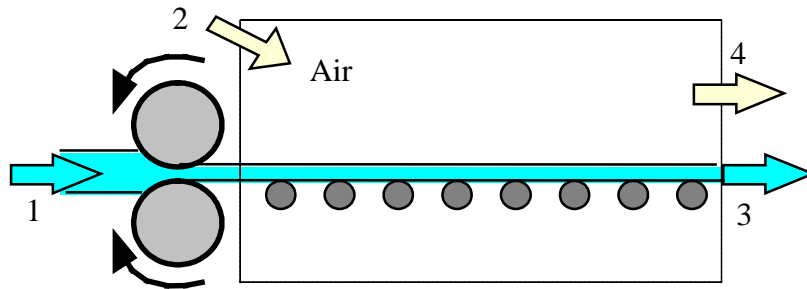
$$\dot{m}_{\text{glass}} C_{\text{glass}} (T_3 - T_1) + \dot{m}_{\text{air}} C_{\text{Pa}} (T_4 - T_2) = 0$$

$$T_4 = T_3, C_{\text{glass}} = 0.80 \text{ kJ/kg K}, C_{\text{Pa}} = 1.004 \text{ kJ/kg K}$$

$$T_3 = \frac{\dot{m}_{\text{glass}} C_{\text{glass}} T_1 + \dot{m}_{\text{air}} C_{\text{Pa}} T_2}{\dot{m}_{\text{glass}} C_{\text{glass}} + \dot{m}_{\text{air}} C_{\text{Pa}}} = \frac{12.5 \times 0.80 \times 1500 + 20 \times 1.004 \times 290}{12.5 \times 0.80 + 20 \times 1.004} \text{ K}$$

$$= \mathbf{692.3 \text{ K}}$$

We could use table A.7.1 for air, but then it will be trial and error



4.145

Assume a setup similar to the previous problem but the air flows in the opposite direction of the glass, it comes in where the glass goes out. How much air flow at 17°C is required to cool the glass to 450 K assuming the air must be at least 120 K cooler than the glass at any location?

Solution:

$$\text{Energy Eq.: } \dot{m}_1 h_1 + \dot{m}_4 h_4 = \dot{m}_3 h_3 + \dot{m}_2 h_2$$

$$T_4 = 290 \text{ K} \quad \text{and} \quad T_3 = 450 \text{ K}$$

$$\dot{m}_{\text{glass}} = \rho \dot{V} = \rho A V = 2500 \text{ kg/m}^3 \times 2 \text{ m} \times 0.005 \text{ m} \times 0.5 \text{ m/s} = 12.5 \text{ kg/s}$$

$$T_2 \leq T_1 - 120 \text{ K} = 1380 \text{ K}$$

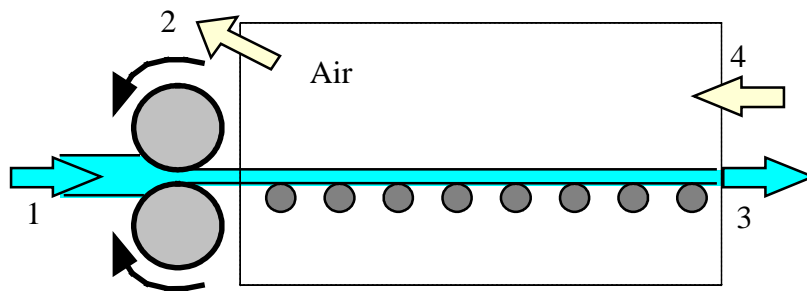
$$\dot{m} = \dot{m}_4 = \dot{m}_2 = \dot{m}_1 \frac{h_1 - h_3}{h_2 - h_4}$$

Let us check the limit and since T is high use table A.7.1 for air.

$$h_4 = 290.43 \text{ kJ/kg}, \quad h_2 = 1491.33 \text{ kJ/kg}$$

$$\dot{m} = \dot{m}_4 = \dot{m}_2 = \dot{m}_1 \frac{h_1 - h_3}{h_2 - h_4} = \dot{m}_1 \frac{C_{\text{glass}}(T_1 - T_3)}{h_2 - h_4}$$

$$\dot{m} = 12.5 \text{ kg/s} \frac{0.8 (1500 - 450)}{1491.33 - 290.43} = \mathbf{8.743 \text{ kg/s}}$$



4.146

Two kg of water at 500 kPa, 20°C is heated in a constant pressure process to 1700°C. Find the best estimate for the heat transfer.

Solution:

C.V. Heater; steady state 1 inlet and exit, no work term, no ΔKE , ΔPE .

Continuity Eq.: $\dot{m}_{in} = \dot{m}_{ex} = \dot{m}$,

Energy Eq.4.13: $q + h_{in} = h_{ex} \Rightarrow q = h_{ex} - h_{in}$

steam tables only go up to 1300°C so use an intermediate state at lowest pressure (closest to ideal gas) $h_X(1300^\circ\text{C}, 10 \text{ kPa})$ from Table B.1.3 and table

A.8 for the high T change Δh from 1300°C to 1700°C.

$$\begin{aligned} h_{ex} - h_{in} &= (h_{ex} - h_X) + (h_X - h_{in}) \\ &= (4515.55 - 3416.77) + (5409.7 - 83.96) = 6424.5 \text{ kJ/kg} \\ Q &= m(h_{ex} - h_{in}) = 2 \times 6424.5 = \mathbf{12\,849\,kJ} \end{aligned}$$

Why is it done this way? The two tables have different offset values for h . Once differences in h between two states are taken from the same table the offset goes out.

4.147

A 500-L insulated tank contains air at 40°C, 2 MPa. A valve on the tank is opened, and air escapes until half the original mass is gone, at which point the valve is closed. What is the pressure inside then?

Solution:

$$\text{State 1: ideal gas} \quad m_1 = P_1 V / RT_1 = \frac{2000 \times 0.5}{0.287 \times 313.2} = 11.125 \text{ kg}$$

$$\text{Continuity eq. 4.15: } m_e = m_1 - m_2, \quad m_2 = m_1/2 \Rightarrow m_e = m_2 = 5.5625 \text{ kg}$$

$$\text{Energy Eq. 4.16: } m_2 u_2 - m_1 u_1 = -m_e h_{e \text{ avg}}$$

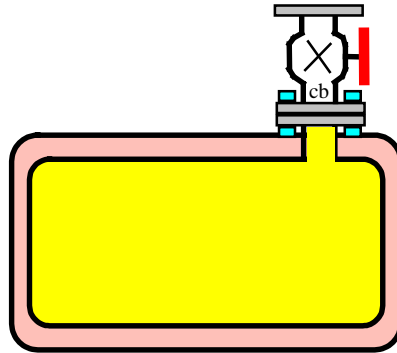
Substitute constant specific heat from table A.5 and evaluate the exit enthalpy as the average between the beginning and the end values

$$h_{e \text{ avg}} \approx C_p (T_1 + T_2)/2$$

$$5.5625 \times 0.717 T_2 - 11.125 \times 0.717 \times 313.2 = -5.5625 \times 1.004 (313.2 + T_2)/2$$

Solving, $T_2 = 239.4 \text{ K}$

$$P_2 = \frac{m_2 R T_2}{V} = \frac{5.5625 \times 0.287 \times 239.4}{0.5} = \mathbf{764 \text{ kPa}}$$



4.148

Three air flows all at 200 kPa are connected to the same exit duct and mix without external heat transfer. Flow one has 1 kg/s at 400 K, flow two has 3 kg/s at 290 K and flow three has 2 kg/s at 700 K. Neglect kinetic energies and find the volume flow rate in the exit flow.

Solution:

$$\text{Continuity Eq. } \dot{m}_1 + \dot{m}_2 + \dot{m}_3 = \dot{m}_4$$

$$\text{Energy Eq.: } \dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 + \dot{m}_4 h_4$$

$$\dot{V}_4 = \dot{m}_4 v_4$$

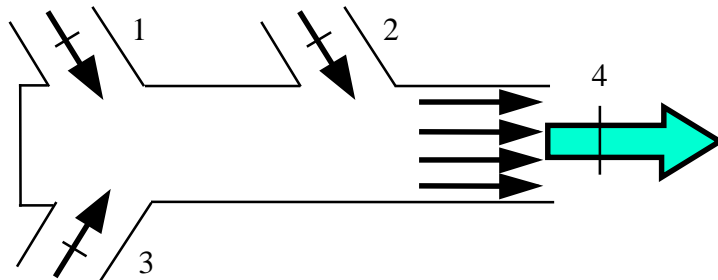
$$h_4 = \frac{\dot{m}_1}{\dot{m}_4} h_1 + \frac{\dot{m}_2}{\dot{m}_4} h_2 + \frac{\dot{m}_3}{\dot{m}_4} h_3 = \frac{1}{6} \times 401.3 + \frac{3}{6} \times 290.43 + \frac{2}{6} \times 713.56$$

$$= 449.95 \text{ kJ/kg}$$

$$T_4 = 440 + 20 \frac{449.95 - 441.93}{462.34 - 441.93} = 447.86 \text{ K}$$

$$v_4 = RT_4 / P_4 = 0.287 \text{ kJ/kg-K} \times 447.86 \text{ K} / 200 \text{ kPa} = \mathbf{0.643 \text{ m}^3/\text{kg}}$$

$$\dot{V}_4 = \dot{m}_4 v_4 = 6 \times 0.643 = \mathbf{3.858 \text{ m}^3/\text{s}}$$



4.149

Consider the power plant as described in Problem 4.121.

- Determine the temperature of the water leaving the intermediate pressure heater, T_{13} , assuming no heat transfer to the surroundings.
- Determine the pump work, between states 13 and 16.

Solution:

a) Intermediate Pressure Heater

Continuity Eq.: $\dot{m}_{11} = \dot{m}_{13}$; $\dot{m}_{12} + \dot{m}_{15} = \dot{m}_{14}$ feedwater line closed

Energy Eq.4.10: $\dot{m}_{11}h_{11} + \dot{m}_{12}h_{12} + \dot{m}_{15}h_{15} = \dot{m}_{13}h_{13} + \dot{m}_{14}h_{14}$

$$\dot{m}_{14} = \dot{m}_{12} + \dot{m}_{15} = 8.064 + 4.662 = 12.726 \text{ kg/s}$$

$$75.6 \times 284.6 + 8.064 \times 2517 + 4.662 \times 584 = 75.6 \times h_{13} + 12.726 \times 349$$

$$h_{13} = 530.35 \text{ kJ/kg} \rightarrow T_{13} = \mathbf{126.3^\circ\text{C}}$$

b) The high pressure pump

Energy Eq.4.12: $\dot{m}_{13}h_{13} = \dot{m}_{16}h_{16} + \dot{W}_{\text{CV,P}}$

$$\dot{W}_{\text{CV,P}} = \dot{m}_{13}(h_{13} - h_{16}) = 75.6 \text{ kg/s} (530.35 - 565) \text{ kJ/kg} = \mathbf{-2620 \text{ kW}}$$

4.150

Consider the powerplant as described in Problem 4.121.

- Find the power removed in the condenser by the cooling water (not shown).
- Find the power to the condensate pump.
- Do the energy terms balance for the low pressure heater or is there a heat transfer not shown?

Solution:

a) Condenser:

$$\text{Continuity Eq.: } \dot{m}_5 + \dot{m}_{10} = \dot{m}_6; \quad \text{also} \quad \dot{m}_5 = \dot{m}_3 - \dot{m}_9 - \dot{m}_8$$

$$\text{Energy Eq.4.10: } \dot{Q}_{CV} + \dot{m}_5 h_5 + \dot{m}_{10} h_{10} = \dot{m}_6 h_6$$

$$\begin{aligned} \dot{m}_{10} &= \dot{m}_6 - \dot{m}_5 = \dot{m}_6 - (\dot{m}_3 - \dot{m}_9 - \dot{m}_8) \\ &= 75.6 - (62.874 - 4.662 - 2.772) = 75.6 - 55.44 = 20.16 \text{ kg/s} \end{aligned}$$

$$\dot{Q}_{CV} + 55.44 \times 2279 + 20.16 \times 142.51 = 75.6 \times 138.3$$

$$\dot{Q}_{CV} = -118\,765 \text{ kW} = \mathbf{-118.77 \text{ MW}}$$

b) The condensate pump

$$\dot{W}_{CV,P} = \dot{m}_6 (h_6 - h_7) = 75.6 \text{ kg/s} (138.31 - 140) \text{ kJ/kg} = \mathbf{-127.8 \text{ kW}}$$

c) Low pressure heater Assume no heat transfer

$$\dot{m}_{14} h_{14} + \dot{m}_8 h_8 + \dot{m}_7 h_7 + \dot{m}_9 h_9 = \dot{m}_{10} h_{10} + \dot{m}_{11} h_{11}$$

$$\text{LHS} = 12.726 \times 349 + 2.772 \times 2459 + 75.6 \times 140 + 4.662 \times 558 = 24\,443 \text{ kW}$$

$$\text{RHS} = (12.726 + 2.772 + 4.662) \times 142.51 + 75.6 \times 284.87 = 24\,409 \text{ kW}$$

A slight imbalance, but OK.

4.151

A 1-m³, 40-kg rigid steel tank contains air at 500 kPa, and both tank and air are at 20°C. The tank is connected to a line flowing air at 2 MPa, 20°C. The valve is opened, allowing air to flow into the tank until the pressure reaches 1.5 MPa and is then closed. Assume the air and tank are always at the same temperature and the final temperature is 35°C. Find the final air mass and the heat transfer.

Solution:

Control volume: Air and the steel tank.

Continuity Eq.4.15: $m_2 - m_1 = m_i$

Energy Eq.4.16: $(m_2 u_2 - m_1 u_1)_{\text{AIR}} + m_{\text{ST}}(u_2 - u_1)_{\text{ST}} = m_i h_i + {}_1Q_2$

$$m_1 \text{ AIR} = \frac{P_1 V}{RT_1} = \frac{500 \times 1}{0.287 \times 293.2} = 5.94 \text{ kg}$$

$$m_2 \text{ AIR} = \frac{P_2 V}{RT_2} = \frac{1500 \times 1}{0.287 \times 308.2} = \mathbf{16.96 \text{ kg}}$$

$$m_i = (m_2 - m_1)_{\text{air}} = 16.96 - 5.94 = 11.02 \text{ kg}$$

The energy equation now gives

$$\begin{aligned} {}_1Q_2 &= (m_2 u_2 - m_1 u_1)_{\text{air}} + m_{\text{st}}(u_2 - u_1)_{\text{st}} - m_i h_i \\ &= m_1(u_2 - u_1) + m_i(u_2 - u_i - RT_i) + m_{\text{st}}C_{\text{st}}(T_2 - T_1) \\ &\cong m_1 C_v(T_2 - T_1) + m_i[C_v(T_2 - T_i) - RT_i] + m_{\text{st}}C_{\text{st}}(T_2 - T_1) \\ &= 5.94 \times 0.717(35 - 20) + 11.02[0.717(35 - 20) - 0.287 \times 293.2] \\ &\quad + 40 \times 0.46(35 - 20) \\ &= 63.885 - 808.795 + 276 \\ &= \mathbf{-468.9 \text{ kJ}} \end{aligned}$$

4.152

A steam engine based on a turbine is shown in Fig. P4.152. The boiler tank has a volume of 100 L and initially contains saturated liquid with a very small amount of vapor at 100 kPa. Heat is now added by the burner, and the pressure regulator does not open before the boiler pressure reaches 700 kPa, which it keeps constant. The saturated vapor enters the turbine at 700 kPa and is discharged to the atmosphere as saturated vapor at 100 kPa. The burner is turned off when no more liquid is present in the boiler. Find the total turbine work and the total heat transfer to the boiler for this process.

Solution:

C.V. Boiler tank. Heat transfer, no work and flow out.

$$\text{Continuity Eq. 4.15: } m_2 - m_1 = -m_e$$

$$\text{Energy Eq. 4.16: } m_2 u_2 - m_1 u_1 = Q_{CV} - m_e h_e$$

$$\text{State 1: Table B.1.1, 100 kPa} \Rightarrow v_1 = 0.001\,043, u_1 = 417.36 \text{ kJ/kg}$$

$$\Rightarrow m_1 = V/v_1 = 0.1/0.001\,043 = 95.877 \text{ kg}$$

$$\text{State 2: Table B.1.1, 700 kPa} \Rightarrow v_2 = v_g = 0.2729, u_2 = 2572.5 \text{ kJ/kg}$$

$$\Rightarrow m_2 = V/v_g = 0.1/0.2729 = 0.366 \text{ kg,}$$

$$\text{Exit state: Table B.1.1, 100 kPa} \Rightarrow h_e = 2673.5 \text{ kJ/kg}$$

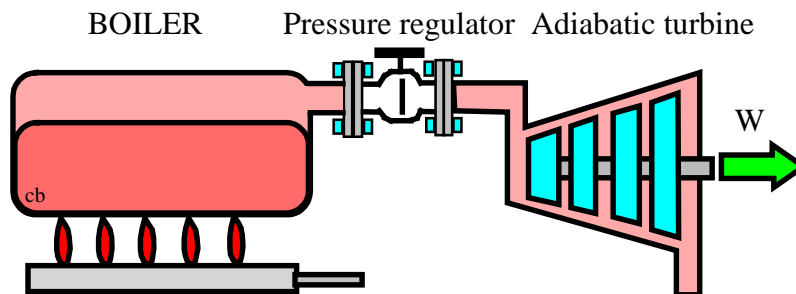
$$\text{From continuity eq.: } m_e = m_1 - m_2 = 95.511 \text{ kg}$$

$$\begin{aligned} Q_{CV} &= m_2 u_2 - m_1 u_1 + m_e h_e \\ &= 0.366 \times 2572.5 - 95.877 \times 417.36 + 95.511 \times 2763.5 \\ &= 224\,871 \text{ kJ} = \mathbf{224.9 \text{ MJ}} \end{aligned}$$

C.V. Turbine, steady state, inlet state is boiler tank exit state.

$$\text{Turbine exit state: Table B.1.1, 100 kPa} \Rightarrow h_e = 2675.5 \text{ kJ/kg}$$

$$W_{\text{turb}} = m_e (h_{\text{in}} - h_{\text{ex}}) = 95.511 \times (2763.5 - 2675.5) = \mathbf{8405 \text{ kJ}}$$



4.153

An insulated spring-loaded piston/cylinder, shown in Fig. P4.153, is connected to an air line flowing air at 600 kPa, 700 K by a valve. Initially the cylinder is empty and the spring force is zero. The valve is then opened until the cylinder pressure reaches 300 kPa. By noting that $u_2 = u_{\text{line}} + C_v(T_2 - T_{\text{line}})$ and $h_{\text{line}} - u_{\text{line}} = RT_{\text{line}}$ find an expression for T_2 as a function of P_2 , P_0 , T_{line} . With $P = 100$ kPa, find T_2 .

Solution:

C.V. Air in cylinder, insulated so ${}_1Q_2 = 0$

Continuity Eq.4.15: $m_2 - m_1 = m_{\text{in}}$

Energy Eq.4.16: $m_2 u_2 - m_1 u_1 = m_{\text{in}} h_{\text{line}} - {}_1W_2$

$$m_1 = 0 \Rightarrow m_{\text{in}} = m_2 ; m_2 u_2 = m_2 h_{\text{line}} - \frac{1}{2}(P_0 + P_2)m_2 v_2$$

$$\Rightarrow u_2 + \frac{1}{2}(P_0 + P_2)v_2 = h_{\text{line}}$$

Use constant specific heat in the energy equation

$$C_v(T_2 - T_{\text{line}}) + u_{\text{line}} + \frac{1}{2}(P_0 + P_2)RT_2/P_2 = h_{\text{line}}$$

$$\left[C_v + \frac{1}{2} \frac{P_0 + P_2}{P_2} R \right] T_2 = (R + C_v) T_{\text{line}}$$

$$\text{with \#s: } T_2 = \frac{R + C_v}{\frac{2}{3}R + C_v} T_{\text{line}} ; \quad C_v/R = 1/(k-1), \quad k = 1.4$$

$$T_2 = \frac{k - 1 + 1}{\frac{2}{3}k - \frac{2}{3} + 1} T_{\text{line}} = \frac{3k}{2k + 1} T_{\text{line}} = 1.105 T_{\text{line}} = \mathbf{773.7 \text{ K}}$$

4.154

A mass-loaded piston/cylinder, shown in Fig. P4.154, containing air is at 300 kPa, 17°C with a volume of 0.25 m³, while at the stops $V = 1$ m³. An air line, 500 kPa, 600 K, is connected by a valve that is then opened until a final inside pressure of 400 kPa is reached, at which point $T = 350$ K. Find the air mass that enters, the work, and heat transfer.

Solution:

C.V. Cylinder volume.

$$\text{Continuity Eq. 4.15: } m_2 - m_1 = m_{\text{in}}$$

$$\text{Energy Eq. 4.16: } m_2 u_2 - m_1 u_1 = m_{\text{in}} h_{\text{line}} + Q_{\text{CV}} - {}_1W_2$$

Process: P_1 is constant to stops, then constant V to state 2 at P_2

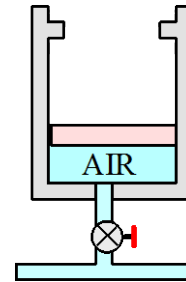
$$\text{State 1: } P_1, T_1 \quad m_1 = \frac{P_1 V}{RT_1} = \frac{300 \times 0.25}{0.287 \times 290.2} = 0.90 \text{ kg}$$

State 2:

Open to $P_2 = 400$ kPa, $T_2 = 350$ K

$$m_2 = \frac{400 \times 1}{0.287 \times 350} = 3.982 \text{ kg}$$

$$m_i = 3.982 - 0.90 = \mathbf{3.082 \text{ kg}}$$



Only work while constant P

$${}_1W_2 = P_1(V_2 - V_1) = 300(1 - 0.25) = \mathbf{225 \text{ kJ}}$$

$$\text{Energy Eq.: } Q_{\text{CV}} + m_i h_i = m_2 u_2 - m_1 u_1 + {}_1W_2$$

$$Q_{\text{CV}} = 3.982 \times 0.717 \times 350 - 0.90 \times 0.717 \times 290.2 + 225 \\ - 3.082 \times 1.004 \times 600 = \mathbf{-819.2 \text{ kJ}}$$

We could also have used the air tables A.7.1 for the u 's and h_i .

4.155

A 2-m³ storage tank contains 95% liquid and 5% vapor by volume of liquified natural gas (LNG) at 160 K, as shown in Fig. P4.155. It may be assumed that LNG has the same properties as pure methane. Heat is transferred to the tank and saturated vapor at 160 K flows into a steady flow heater which it leaves at 300 K. The process continues until all the liquid in the storage tank is gone. Calculate the total amount of heat transfer to the tank and the total amount of heat transferred to the heater.

Solution:

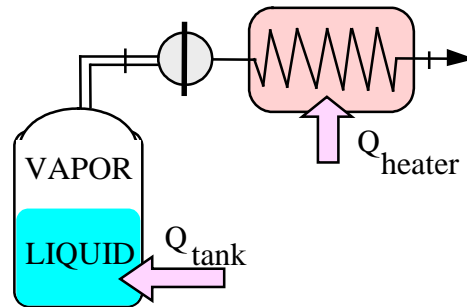
CV: Tank, flow out, transient.

Continuity Eq.: $m_2 - m_1 = -m_e$

Energy Eq.:

$$Q_{\text{Tank}} = m_2 u_2 - m_1 u_1 + m_e h_e$$

At 160 K, from Table B.7:



$$m_f = V_f / v_f = \frac{0.95 \times 2}{0.00297} = 639.73 \text{ kg}, \quad m_g = V_g / v_g = \frac{0.05 \times 2}{0.03935} = 2.541 \text{ kg}$$

$$m_1 = 642.271 \text{ kg}, \quad m_2 = V / v_{g2} = 2 / 0.03935 = 50.826 \text{ kg}$$

$$m_1 u_1 = 639.73(-106.35) + 2.541(207.7) = -67507 \text{ kJ}$$

$$m_e = m_1 - m_2 = 591.445 \text{ kg}$$

$$Q_{\text{Tank}} = 50.826 \times 207.7 - (-67507) + 591.445 \times 270.3 \\ = +237\,931 \text{ kJ}$$

CV: Heater, steady flow, $P = P_G$ 160 K = 1593 kPa

$$Q_{\text{Heater}} = m_e \text{ Tank}(h_e - h_i)_{\text{Heater}} \\ = 591.445(612.9 - 270.3) = 202\,629 \text{ kJ}$$

ENGLISH UNIT PROBLEMS

Borgnakke Sonntag

Fundamentals of
Thermodynamics

SOLUTION MANUAL
CHAPTER 4
English units

8e

CHAPTER 4

SUBSECTION	PROB NO.
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Continuity and Flow Rates

4.156E

Refrigerant R-410A at 100 psia, 60 F flows at 0.1 lbm/s in a 2.5 ft² cross sectional area pipe. Find the velocity and the volume flow rate.

$$\dot{m} = A\mathbf{V}/v = \dot{V}/v$$

Table F.9.2: $v = 0.6848 \text{ ft}^3/\text{lbm}$

$$\dot{V} = v \dot{m} = 0.6848 \text{ ft}^3/\text{lbm} \times 0.1 \text{ lbm/s} = \mathbf{0.06848 \text{ ft}^3/\text{s}}$$

$$\mathbf{V} = \dot{V} / A = 0.06848 (\text{ft}^3/\text{s}) / 2.5 \text{ ft}^2 = \mathbf{0.0274 \text{ ft/s}}$$

4.157E

Air at 95 F, 16 lbf/in.², flows in a 4 in. × 6 in. rectangular duct in a heating system. The volumetric flow rate is 30 cfm (ft³/min). What is the velocity of the air flowing in the duct?

Solution:

Assume a constant velocity across the duct area with

$$A = 4 \times 6 \times \frac{1}{144} = 0.167 \text{ ft}^2$$

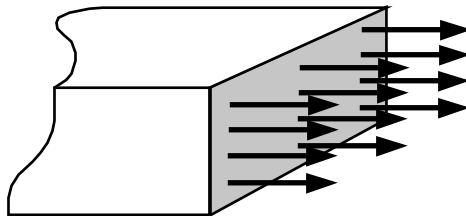
and the volumetric flow rate from Eq.4.3,

$$\dot{V} = \dot{m}v = A\mathbf{V}$$

$$\mathbf{V} = \frac{\dot{V}}{A} = \frac{30}{60 \times 0.167} = \mathbf{3.0 \text{ ft/s}}$$

Ideal gas so note:

$$\left(\begin{array}{l} \text{note ideal gas: } v = \frac{RT}{P} = \frac{53.34 \times 554.7}{16 \times 144} = 12.842 \text{ ft}^3/\text{lbm} \\ \dot{m} = \frac{\dot{V}}{v} = \frac{30}{60 \times 12.842} = 0.0389 \text{ lbm/s} \end{array} \right)$$



4.158E

A pool is to be filled with 2500 ft³ water from a garden hose of 1 in. diameter flowing water at 6 ft/s. Find the mass flow rate of water and the time it takes to fill the pool.

Solution:

With constant velocity we have

$$\dot{V} = \dot{m}v = A\mathbf{V} = \pi \times (1/12)^2 \text{ ft}^2 \times 6 \text{ ft/s} = 0.1309 \text{ ft}^3/\text{s}$$

$$\Delta t = V / \dot{V} = 2500 \text{ ft}^3 / (0.1309 \text{ ft}^3/\text{s}) = 19\,098 \text{ s} = \mathbf{5 \text{ h } 18 \text{ min } 18 \text{ s}}$$

From table F.3 we get the water density

$$\dot{m} = \dot{V} / v = \rho \dot{V} = 62.2 \text{ lbm/ft}^3 \times 0.1309 \text{ ft}^3/\text{s} = \mathbf{8.14 \text{ lbm/s}}$$

4.159E

A hot air home heating system takes 500 ft³/min (cfm) air at 14.7 psia, 65 F into a furnace and heats it to 130 F and delivers the flow to a square duct 0.5 ft by 0.5 ft at 15 psia. What is the velocity in the duct?

Solution:

The inflow flow is given by a \dot{m}_i

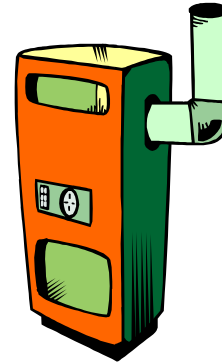
Continuity Eq.: $\dot{m}_i = \dot{V}_i / v_i = \dot{m}_e = A_e \mathbf{V}_e / v_e$

$$\text{Ideal gas: } v_i = \frac{RT_i}{P_i} = \frac{53.34 \times 525}{14.7 \times 144} = 13.23 \frac{\text{ft}^3}{\text{lbm}}$$

$$v_e = \frac{RT_e}{P_e} = \frac{53.34 \text{ lbf-ft/lbm-R} \times (130 + 460) \text{ R}}{15 \text{ psi} \times 144 \text{ in}^2/\text{ft}^2} \\ = 14.57 \text{ ft}^3/\text{lbm}$$

$$\dot{m}_i = \dot{V}_i / v_i = 500 \text{ (ft}^3/\text{min)} / [60 \text{ (s/min)} \times 13.23 \frac{\text{ft}^3}{\text{lbm}}] = 0.63 \text{ lbm/s}$$

$$\mathbf{V}_e = \dot{m}_i v_e / A_e = \frac{0.63 \times 14.57}{0.5 \times 0.5} \frac{\text{ft}^3/\text{s}}{\text{ft}^2} = \mathbf{36.7 \text{ ft/s}}$$



4.160E

Liquid water at 60 F flows out of a nozzle straight up 40 ft. What is nozzle \mathbf{V}_{exit} ?

Energy Eq.4.13:
$$h_{\text{exit}} + \frac{1}{2} \mathbf{V}_{\text{exit}}^2 + gH_{\text{exit}} = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gH_2$$

If the water can flow 40 ft up it has specific potential energy of gH_2 which must equal the specific kinetic energy out of the nozzle $\mathbf{V}_{\text{exit}}^2/2$. The water does not change P or T so h is the same.

$$\begin{aligned} \mathbf{V}_{\text{exit}}^2/2 &= g(H_2 - H_{\text{exit}}) = gH \quad \Rightarrow \\ \mathbf{V}_{\text{exit}} &= \sqrt{2gH} = \sqrt{2 \times 32.174 \times 40 \text{ ft}^2/\text{s}^2} = \mathbf{50.7 \text{ ft/s}} \end{aligned}$$



4.161E

A diffuser receives 0.2 lbm/s steam at 80 psia, 600 F. The exit is at 150 psia, 700 F with negligible kinetic energy and the flow is adiabatic. Find the diffuser inlet velocity and the inlet area.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process: } Z_1 = Z_2$$

$$\text{State 1: Table F.7.2 } h_1 = 1330.66 \text{ Btu/lbm, } v_1 = 7.794 \text{ ft}^3/\text{lbm}$$

$$\text{State 2: } V_2 = 0, \text{ Table F.7.2 } h_2 = 1376.55 \text{ Btu/lbm}$$

Then from the energy equation

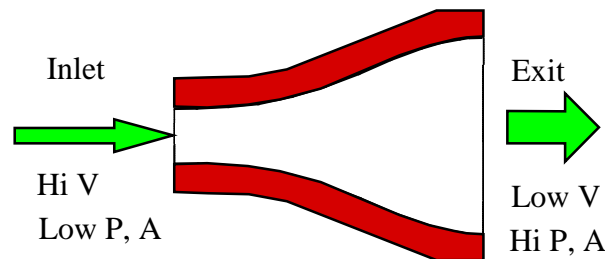
$$\frac{1}{2} \mathbf{V}_1^2 = h_2 - h_1 = 1376.55 - 1330.66 = 45.89 \text{ Btu/lbm}$$

$$\mathbf{V}_1 = \sqrt{2(h_2 - h_1)} = \sqrt{2 \times 32.174 \times 778 \times 45.89} = \mathbf{1515.7 \text{ ft/s}}$$

The mass flow rate from Eq.4.3

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V} / v$$

$$A = \dot{m} v / \mathbf{V} = 0.2 \text{ lbm/s} \times (7.794 \text{ ft}^3/\text{lbm}) / 1515.7 \text{ ft/s} \\ = 0.000103 \text{ ft}^2 = \mathbf{0.148 \text{ in.}^2}$$



4.162E

Saturated vapor R-134a leaves the evaporator in a heat pump at 50 F, with a steady mass flow rate of 0.2 lbm/s. What is the smallest diameter tubing that can be used at this location if the velocity of the refrigerant is not to exceed 20 ft/s?

Solution:

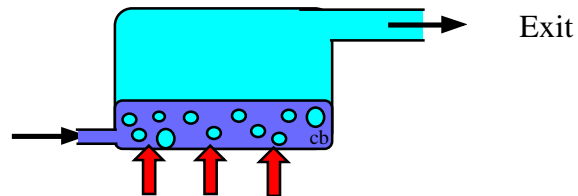
Mass flow rate Eq.4.3: $\dot{m} = \dot{V}/v = A\mathbf{V}/v$

Exit state Table F.10.1: (T = 50 F, x = 1) $\Rightarrow v = v_g = 0.792 \text{ ft}^3/\text{lbm}$

The minimum area is associated with the maximum velocity for given \dot{m}

$$A_{\text{MIN}} = \frac{\dot{m}v_g}{V_{\text{MAX}}} = \frac{0.2 \text{ lbm/s} \times 0.792 \text{ ft}^3/\text{lbm}}{20 \text{ ft/s}} = 0.00792 \text{ ft}^2 = \frac{\pi}{4} D_{\text{MIN}}^2$$

$$D_{\text{MIN}} = 0.1004 \text{ ft} = 1.205 \text{ in}$$



Single Flow Devices

4.163E

In a jet engine a flow of air at 1800 R, 30 psia and 90 ft/s enters a nozzle where the air exits at 1500 R, 13 psia, as shown in Fig. P.4.23. What is the exit velocity assuming no heat loss?

Solution:

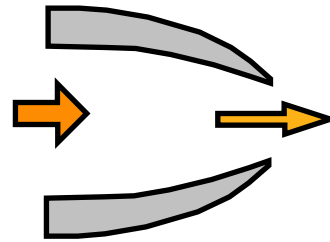
C.V. nozzle. No work, no heat transfer

Continuity $\dot{m}_i = \dot{m}_e = \dot{m}$

Energy : $\dot{m} (h_i + \frac{1}{2}V_i^2) = \dot{m}(h_e + \frac{1}{2}V_e^2)$

Due to high T take h from table F.5

$$\begin{aligned}\frac{1}{2}V_e^2 &= \frac{1}{2}V_i^2 + h_i - h_e \\ &= \frac{90^2}{2 \times 32.174 \times 778} + 449.79 - 369.28 \\ &= 0.16 + 80.51 = 80.67 \text{ Btu/lbm}\end{aligned}$$



$$\begin{aligned}V_e &= (2 \times 32.174 \text{ lbm-ft/s}^2\text{-lbf} \times 778 \text{ lbf-ft/Btu} \times 80.67 \text{ Btu/lbm})^{1/2} \\ &= \mathbf{2010 \text{ ft/s}}\end{aligned}$$

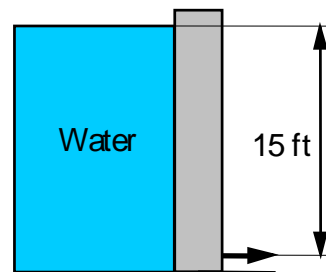
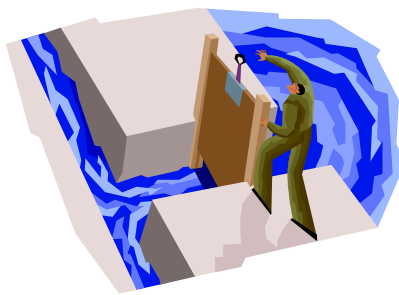
4.164E

A sluice gate dams water up 15 ft. A 0.5 in. diameter hole at the bottom of the gate allows liquid water at 70 F to come out. Neglect any changes in internal energy and find the exit velocity and mass flow rate.

Solution:

$$\text{Energy Eq.4.13: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\begin{array}{lll} \text{Process:} & h_1 = h_2 & \text{both at } P = 1 \text{ atm} \\ & V_1 = 0 & Z_1 = Z_2 + 15 \text{ ft} \end{array}$$



$$\frac{1}{2} \mathbf{V}_2^2 = g (Z_1 - Z_2)$$

$$\mathbf{V}_2 = \sqrt{2g(Z_1 - Z_2)} = \sqrt{2 \times 32.174 \times 15} = \mathbf{31.07 \text{ ft/s}}$$

$$\dot{m} = \rho A \mathbf{V} = A \mathbf{V} / v = \frac{\pi}{4} D^2 \times (\mathbf{V}_2 / v)$$

$$\begin{aligned} &= \frac{\pi}{4} \times (0.5/12)^2 \text{ ft}^2 \times (31.07 \text{ ft/s}) / (0.01605 \text{ ft}^3/\text{lbm}) \\ &= \mathbf{2.639 \text{ lbm/s}} \end{aligned}$$

4.165E

A diffuser shown in Fig. P4.28 has air entering at 14.7 lbf/in.², 540 R, with a velocity of 600 ft/s. The inlet cross-sectional area of the diffuser is 0.2 in.². At the exit, the area is 1.75 in.², and the exit velocity is 60 ft/s. Determine the exit pressure and temperature of the air.

Solution:

Continuity Eq.4.3: $\dot{m}_i = A_i \mathbf{V}_i / v_i = \dot{m}_e = A_e \mathbf{V}_e / v_e,$

Energy Eq.(per unit mass flow) 4.13: $h_i + \frac{1}{2} \mathbf{V}_i^2 = h_e + \frac{1}{2} \mathbf{V}_e^2$

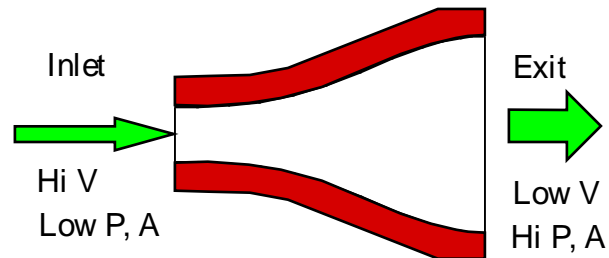
$$h_e - h_i = (1/2) \times (600^2 - 60^2) / (32.174 \times 778) = 7.119 \text{ Btu/lbm}$$

$$T_e = T_i + (h_e - h_i) / C_p = 540 \text{ R} + \frac{7.119 \text{ Btu/lbm}}{0.24 \text{ Btu/lbm-R}} = \mathbf{569.7 \text{ R}}$$

Now use the continuity equation and the ideal gas law

$$v_e = v_i \left(\frac{A_e \mathbf{V}_e}{A_i \mathbf{V}_i} \right) = (RT_i / P_i) \left(\frac{A_e \mathbf{V}_e}{A_i \mathbf{V}_i} \right) = RT_e / P_e$$

$$P_e = P_i \left(\frac{T_e}{T_i} \right) \left(\frac{A_i \mathbf{V}_i}{A_e \mathbf{V}_e} \right) = 14.7 \left(\frac{569.7}{540} \right) \left(\frac{0.2 \times 600}{1.75 \times 60} \right) = \mathbf{17.72 \text{ lbf/in.}^2}$$

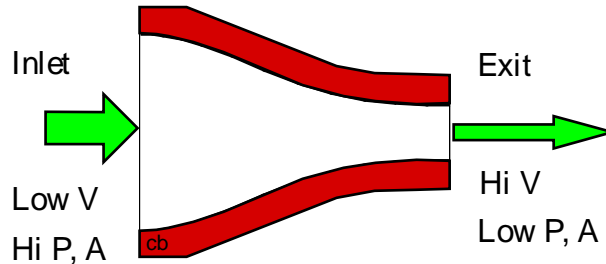


4.166E

Nitrogen gas flows into a convergent nozzle at 30 lbf/in.², 600 R and very low velocity. It flows out of the nozzle at 15 lbf/in.², 500 R. If the nozzle is insulated find the exit velocity.

Solution:

C.V. Nozzle steady state one inlet and exit flow, insulated so it is adiabatic.



Energy Eq.4.13: $h_1 + 0 = h_2 + \frac{1}{2} V_2^2$

$$\begin{aligned} V_2^2 &= 2 (h_1 - h_2) \cong 2 C_{PN_2} (T_1 - T_2) \\ &= 2 \times 0.249 \text{ Btu/lbm-R} \times (600 - 500) \text{ R} \\ &= 24.9 \text{ Btu/lbm} \end{aligned}$$

$$\begin{aligned} V_2^2 &= 2 \times 24.9 \text{ Btu/lbm} \times 778 \text{ lbf-ft/Btu} \times 32.174 \text{ lbm-ft/s}^2\text{-lbf} \\ &= 1\,246\,562 \text{ ft}^2 / \text{s}^2 \\ \mathbf{V_2} &= \mathbf{1116 \text{ ft/s}} \end{aligned}$$

4.167E

A meteorite hits the upper atmosphere at 10 000 ft/s, where the pressure is 0.1 atm and the temperature is -40°F . How hot does the air become right in front of the meteorite assuming no heat transfer in this adiabatic stagnation process?

Solution:

$$\text{Energy Eq.: } h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2$$

$$\text{Process: } Z_1 = Z_2 \quad \text{and} \quad \mathbf{V}_2 = 0$$

$$h_2 = h_1 + \frac{1}{2} \mathbf{V}_1^2$$

$$T_2 = T_1 + \frac{1}{2}(\mathbf{V}_1^2/C_p) = 419.67 + \frac{1}{2} \times \frac{10\,000^2}{0.24 \times 778 \times 32.174} = \mathbf{8742\text{ R}}$$

At this high temperature we cannot assume constant specific heats, so use F.5

$$h_2 = h_1 + \frac{1}{2} \mathbf{V}_1^2 = 100.4 + \frac{1}{2} \times \frac{10\,000^2}{778 \times 32.174} = 2097.9 \text{ Btu/lbm}$$

Table F.5 is listed to 5400 R so we have to extrapolate to get

$$T_2 = 5400 + 100 \frac{2097.9 - 1515.632}{1515.632 - 1484.762} = \mathbf{7286\text{ R}}$$

The value of C_p over 5400 R is 0.309 Btu/lbmR from the last two table entries. At this temperature there will be some chemical reactions that should be considered to have a more realistic temperature.

4.168E

Refrigerant R-410A flows out of a cooler at 70 F, 220 psia after which it is throttled to 77 psia. Find the state (T, x) for the exit flow.

C.V. Throttle. Steady state,

Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

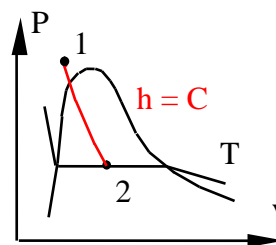
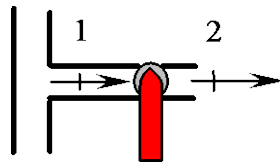
Energy Eq.4.13: $h_i = h_e$,

Inlet state: Table F.9.1 $h_i = 39.17$ Btu/lbm

Exit state: Table F.9.1 since $h < h_g = 118.21$ Btu/lbm

Interpolate: $T = 10$ F, $h_f = 17.0$ Btu/lbm, $h_{fg} = 101.22$ Btu/lbm

$$x = (39.17 - 17.0) / 101.22 = \mathbf{0.219}$$



4.169E

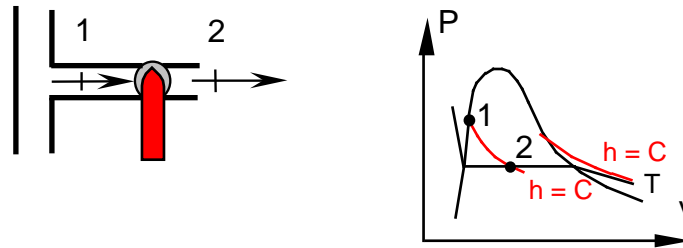
R-410A at 90 F, 300 psia is throttled so it becomes cold at 10 F. What is exit P?

State 1 is slightly compressed liquid so

Table F.9.1: $h = h_f = 47.30 \text{ Btu/lbm}$

At the lower temperature it becomes two-phase since the throttle flow has constant h and at 10 F: $h_g = 118.21 \text{ Btu/lbm}$

$$P = P_{\text{sat}} = \mathbf{76.93 \text{ psia}}$$



4.170E

Saturated liquid R-410A at 30 F is throttled to 40 psia in a refrigerator. What is the exit temperature? Find the percent increase in the volume flow rate.

Solution:

Steady throttle flow. Assume no heat transfer and no change in kinetic or potential energy.

$$h_e = h_i = h_{f\ 30\text{ F}} = 24.11\text{ Btu/lbm} = h_{f\ e} + x_e h_{fg\ e} \quad \text{at 40 psia}$$

From table F.9.1 we get $T_e = T_{\text{sat}}(40\text{ psia}) = -21\text{ F}$

$$x_e = \frac{h_e - h_{f\ e}}{h_{fg\ e}} = \frac{24.11 - 6.354}{108.776} = 0.1632$$

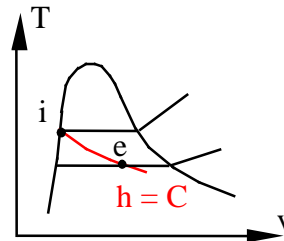
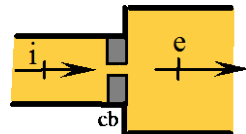
$$v_e = v_f + x_e v_{fg} = 0.01253 + x_e 1.47584 = 0.25338\text{ ft}^3/\text{lbm}$$

$$v_i = v_{f\ 30\text{ F}} = 0.01364\text{ ft}^3/\text{lbm}$$

$\dot{V} = \dot{m}v$ so the ratio becomes

$$\frac{\dot{V}_e}{\dot{V}_i} = \frac{\dot{m}v_e}{\dot{m}v_i} = \frac{v_e}{v_i} = \frac{0.25338}{0.01364} = \mathbf{18.58}$$

So the increase is 17.58 times or **1758 %**



4.171E

Saturated vapor R-410A at 75 psia is throttled to 15 psia. What is the exit temperature. Repeat the question if you assumed it behaves like an ideal gas.

C.V. Throttle. Steady state,

Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

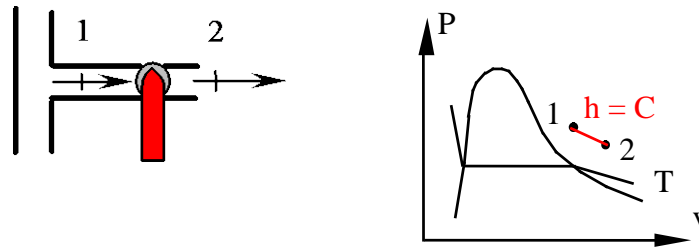
Energy Eq.4.13: $h_i = h_e$,

Inlet state: Table F.9.2 $h_i = 118.09$ Btu/lbm

Exit state: Table F.9.2 since $h > h_g$

Exit state very close to $T = -20$ F,

For an ideal gas h is only a function of T , so $T_e = T_i = 8.71$ F



4.172E

Helium is throttled from 175 lbf/in.², 70 F, to a pressure of 15 lbf/in.². The diameter of the exit pipe is so much larger than the inlet pipe that the inlet and exit velocities are equal. Find the exit temperature of the helium and the ratio of the pipe diameters.

C.V. Throttle. Steady state,

Process with: $q = w = 0$; and $V_i = V_e$, $Z_i = Z_e$

Energy Eq.4.13: $h_i = h_e$, Ideal gas $\Rightarrow T_i = T_e = 70 \text{ F}$

$$\dot{m} = \frac{AV}{RT/P} \quad \text{But } \dot{m}, V, T \text{ are constant} \Rightarrow P_i A_i = P_e A_e$$

$$\Rightarrow \frac{D_e}{D_i} = \left(\frac{P_i}{P_e} \right)^{1/2} = \left(\frac{175}{15} \right)^{1/2} = 3.416$$



4.173E

A liquid water turbine receives 4 lbm/s water at 300 psia, 77 F with a velocity of 50 ft/s. The exit is at 15 psia, 77 F with very low velocity. Find the specific work and the power produced.

Solution:

Energy Eq.4.13: $h_1 + \frac{1}{2} \mathbf{V}_1^2 + gZ_1 = h_2 + \frac{1}{2} \mathbf{V}_2^2 + gZ_2 + w_T$

Process: $Z_1 = Z_2$ and $\mathbf{V}_2 = 0$

State 1: Table F.7.1 $h_1 = 45.09$ Btu/lbm

Add $\Delta P_v = (300 - 0.464) \times 0.01606 \times 32.174/144 = 1.075$ Btu/lbm

State 2: Table F.7.1 $h_2 = 45.09$

Add $\Delta P_v = (15 - 0.464) \times 0.01606 \times 32.174/144 = 0.052$ Btu/lbm

$$\begin{aligned} w_T &= h_1 + \frac{1}{2} \mathbf{V}_1^2 - h_2 \\ &= (45.09 + 1.075) + \frac{1}{2} \times \frac{50^2}{778 \times 32.174} - (45.09 + 0.052) \\ &= \mathbf{1.073 \text{ Btu/lbm}} \end{aligned}$$

$$\dot{W}_T = \dot{m} \times w_T = 4 \times 1.073 = \mathbf{4.29 \text{ Btu/s}}$$

Notice how insignificant the specific kinetic energy is (0.05 Btu/lbm).

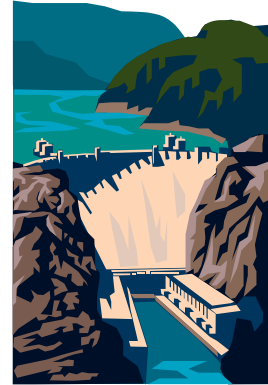
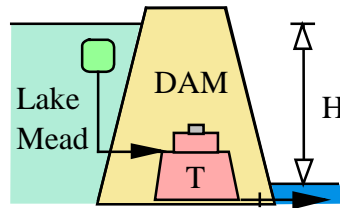
The added ΔP_v terms are due to P being higher than saturated P, see p.134.

4.174E

Hoover Dam across the Colorado River dams up Lake Mead 600 ft higher than the river downstream, as shown in Fig. P4.47. The electric generators driven by water-powered turbines deliver 1.2×10^6 Btu/s. If the water is 65 F, find the minimum amount of water running through the turbines.

Solution:

C.V.: H₂O pipe + turbines,



Continuity: $\dot{m}_{\text{in}} = \dot{m}_{\text{ex}}$

Energy Eq.4.13: $(h + \mathbf{V}^2/2 + gz)_{\text{in}} = (h + \mathbf{V}^2/2 + gz)_{\text{ex}} + w_T$

Water states: $h_{\text{in}} \cong h_{\text{ex}} ; \quad v_{\text{in}} \cong v_{\text{ex}}$

Now the specific turbine work becomes

$$\begin{aligned} w_T &= gz_{\text{in}} - gz_{\text{ex}} \\ &= 32.174 \text{ ft/s}^2 \times 600 \text{ ft} / (778 \text{ lbf-ft/Btu} \times 32.174 \text{ lbf-ft/s}^2\text{-lbf}) \\ &= 0.771 \text{ Btu/lbm} \end{aligned}$$

$$\dot{m} = \dot{W}_T / w_T = 1.2 \times 10^6 (\text{Btu/s}) / 0.771 (\text{Btu/lbm}) = 1.556 \times 10^6 \text{ lbm/s}$$

$$\dot{V} = \dot{m}v = 1.556 \times 10^6 \times 0.016043 = \mathbf{24\,963 \text{ ft}^3/\text{s}}$$

4.175E

A small expander (a turbine with heat transfer) has 0.1 lbm/s helium entering at 160 psia, 1000 R and it leaves at 40 psia, 540 R. The power output on the shaft is measured to 55 Btu/s. Find the rate of heat transfer neglecting kinetic energies.

Solution:

C.V. Expander. Steady operation

$$\text{Continuity Eq.:} \quad \dot{m}_i = \dot{m}_e = \dot{m}$$

$$\text{Energy Eq.:} \quad \dot{m}h_i + \dot{Q} = \dot{m}h_e + \dot{W}$$

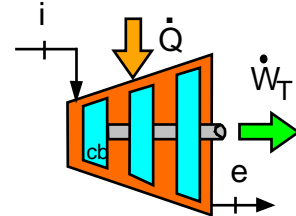
$$\dot{Q} = \dot{m} (h_e - h_i) + \dot{W}$$

Use heat capacity from Table F.4: $C_{p, \text{He}} = 1.24 \text{ Btu/lbm R}$

$$\dot{Q} = \dot{m}C_p (T_e - T_i) + \dot{W}$$

$$= 0.1 \text{ lbm/s} \times 1.24 \text{ Btu/lbm-R} \times (540 - 1000) \text{ R} + 55 \text{ Btu/s}$$

$$= -57.04 + 55 = \mathbf{-2.0 \text{ Btu/s}}$$



4.176E

A small, high-speed turbine operating on compressed air produces a power output of 0.1 hp. The inlet state is 60 lbf/in.², 120 F, and the exit state is 14.7 lbf/in.², –20 F. Assuming the velocities to be low and the process to be adiabatic, find the required mass flow rate of air through the turbine.

Solution:

C.V. Turbine, no heat transfer, no ΔKE , no ΔPE

Energy Eq.4.13: $h_{in} = h_{ex} + w_T$

Ideal gas so use constant specific heat from Table A.5

$$\begin{aligned} w_T &= h_{in} - h_{ex} \cong C_p(T_{in} - T_{ex}) \\ &= 0.24(120 - (-20)) = 33.6 \text{ Btu/lbm} \end{aligned}$$

$$\dot{W} = \dot{m}w_T \Rightarrow$$

$$\dot{m} = \dot{W}/w_T = \frac{0.1 \text{ hp} \times 550 \text{ lbf-ft/s-hp}}{778 \text{ lbf-ft/Btu} \times 33.6 \text{ Btu/lbm}} = \mathbf{0.0021 \text{ lbm/s} = 7.57 \text{ lbm/h}}$$

The dentist's drill has a small air flow and is not really adiabatic.

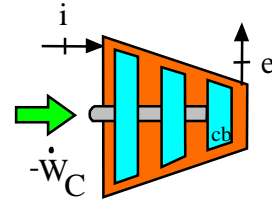


4.177E

A compressor in a commercial refrigerator receives R-410A at -10 F and $x = 1$. The exit is at 200 psia, 120 F. Neglect kinetic energies and find the specific work.

Solution:

C.V. Compressor, steady state, single inlet and exit flow. For this device we also assume no heat transfer and $Z_i = Z_e$



From Table F.9.1 : $h_i = 116.29 \text{ Btu/lbm}$

From Table F.9.2 : $h_e = 137.02 \text{ Btu/lbm}$

Energy Eq.4.13 reduces to

$$w_c = h_i - h_e = (116.29 - 137.02) = \mathbf{-20.73 \text{ Btu/lbm}}$$

4.178E

A compressor in an industrial air-conditioner compresses ammonia from a state of saturated vapor at 20 psia to a pressure of 125 psia. At the exit the temperature is measured to be 200 F and the mass flow rate is 1 lbm/s. What is the required power input to this compressor?

Solution:

C.V. Compressor. Assume adiabatic and neglect kinetic energies.

Energy Eq.4.13: $w_C = h_1 - h_2$

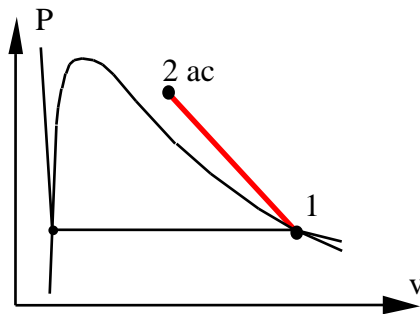
States: 1: F.8.2: $h_1 = 605.47$ Btu/lbm

2: F.8.2 $h_{2,AC} = 710.44$ Btu/lbm

Energy equation:

$$-w_C = h_2 - h_1 = 710.44 - 605.47 = 104.97 \text{ Btu/lbm}$$

$$\dot{W} = 1 \text{ lbm/s} \times 104.97 \text{ Btu/lbm} = \mathbf{105 \text{ Btu/s}}$$



4.179E

An exhaust fan in a building should be able to move 6 lbm/s air at 14.4 psia, 68 F through a 1.4 ft diameter vent hole. How high a velocity must it generate and how much power is required to do that?

Solution:

C.V. Fan and vent hole. Steady state with uniform velocity out.

Continuity Eq.: $\dot{m} = \text{constant} = \rho A \mathbf{V} = A \mathbf{V} / v = A \mathbf{V} P / RT$

Ideal gas : $Pv = RT$, and area is $A = \frac{\pi}{4} D^2$

Now the velocity is found

$$\mathbf{V} = \frac{\dot{m} RT}{(\frac{\pi}{4} D^2 P)} = \frac{6 \text{ lbm/s} \times 53.34 \text{ lbf-ft/lbm-R} \times (459.7 + 68) \text{ R}}{\frac{\pi}{4} \times 1.4^2 \times 14.4 \text{ psi} \times 144 \text{ in}^2/\text{ft}^2}$$

$$= \mathbf{52.908 \text{ ft/s}}$$

The kinetic energy out is

$$\frac{1}{2} \mathbf{V}_2^2 = \frac{1}{2} \times 52.908^2 / 32.174 = 43.502 \text{ lbf-ft/lbm}$$

which is provided by the work (only two terms in energy equation that does not cancel, we assume $\mathbf{V}_1 = 0$)

$$\dot{W}_{\text{in}} = \dot{m} \frac{1}{2} \mathbf{V}_2^2 = 6 \times 43.502 = \mathbf{261 \text{ lbf-ft/s} = 0.335 \text{ Btu/s}}$$

4.180E

An air flow is brought from 77 F, 14.7 psia to 150 psia, 620 F by an adiabatic compressor driven by a 50-kW motor. What are the mass flow rate and the exit volume flow rate of air?

C.V. Compressor. Assume adiabatic and neglect kinetic, potential energies.

Energy Eq.4.13: $w = h_1 - h_2$

$$\begin{aligned} -w_C = h_2 - h_1 &\approx C_P (T_2 - T_1) = 0.24 \text{ Btu/lbm-R} \times (620 - 77) \text{ R} \\ &= 130.32 \text{ Btu/lbm} \end{aligned}$$

The mass flow rate scale the work term so

$$\dot{m} = \dot{W} / -w_C = \frac{(50/1.055) \text{ Btu/s}}{130.32 \text{ Btu/lbm}} = \mathbf{0.3637 \text{ lbm/s}}$$

$$\begin{aligned} \dot{V} = \dot{m} v = \dot{m} \frac{RT}{P} &= 0.3637 \text{ lbm/s} \frac{53.34 \times (620 + 459.67) \text{ ft-lbf/lbm}}{150 \text{ lbf/in}^2 \times 144 (\text{in/ft})^2} \\ &= \mathbf{2.666 \text{ ft}^3/\text{s}} \end{aligned}$$

4.181E

Carbon dioxide gas enters a steady-state, steady-flow heater at 45 lbf/in.², 60 F, and exits at 40 lbf/in.², 1800 F. It is shown in Fig. P4.65 here changes in kinetic and potential energies are negligible. Calculate the required heat transfer per lbm of carbon dioxide flowing through the heater.

Solution:

C.V. Heater Steady state single inlet and exit flow.

Energy Eq.4.13: $q + h_i = h_e$

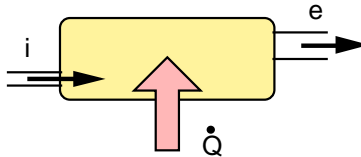


Table F.6 $q = h_e - h_i = \frac{20470.8 - (-143.4)}{44.01} = \mathbf{468.4 \text{ Btu/lbm}}$

[If we use C_{p0} then $q \cong 0.203 \text{ Btu/lbm-R} (1800 - 60) \text{ R} = 353.2 \text{ Btu/lbm}$]

Too large ΔT , T_{ave} to use C_{p0} at room temperature.

4.182E

A condenser (cooler) receives 0.1 lbm/s of R-410A at 300 psia, 140 F and cools it to 70 F. Assume the exit properties are as for saturated liquid same T. What cooling capacity (Btu/h) must the condenser have?

Solution:

C.V. R-410A condenser. Steady state single flow, heat transfer out and no work.

$$\text{Energy Eq.4.12:} \quad \dot{m} h_1 = \dot{m} h_2 + \dot{Q}_{\text{out}}$$

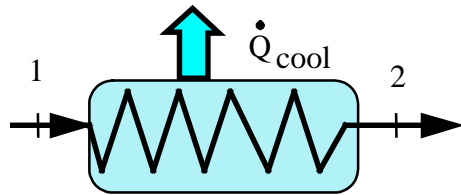
$$\text{Inlet state: Table F.9.2} \quad h_1 = 137.34 \text{ Btu/lbm,}$$

$$\text{Exit state: Table F.9.1} \quad h_2 = 39.17 \text{ Btu/lbm (compressed liquid)}$$

Process: Neglect kinetic and potential energy changes.

Cooling capacity is taken as the heat transfer out i.e. positive out so

$$\begin{aligned} \dot{Q}_{\text{out}} &= \dot{m} (h_1 - h_2) = 0.1 \text{ lbm/s} (137.34 - 39.17) \text{ Btu/lbm} \\ &= \mathbf{9.82 \text{ Btu/s}} \end{aligned}$$



4.183E

In a steam generator, compressed liquid water at 1500 lbf/in.², 100 F, enters a 1-in. diameter tube at the rate of 5 ft³/min. Steam at 1250 lbf/in.², 750 F exits the tube. Find the rate of heat transfer to the water.

Solution:

C.V. Steam generator. Steady state single inlet and exit flow.

Constant diameter tube: $A_i = A_e = \frac{\pi}{4} \left(\frac{1}{12} \right)^2 = 0.00545 \text{ ft}^2$

Table B.1.4 $\dot{m} = \dot{V}_i / v_i = 5 \times 60 / 0.016058 = 18\,682 \text{ lbm/h}$

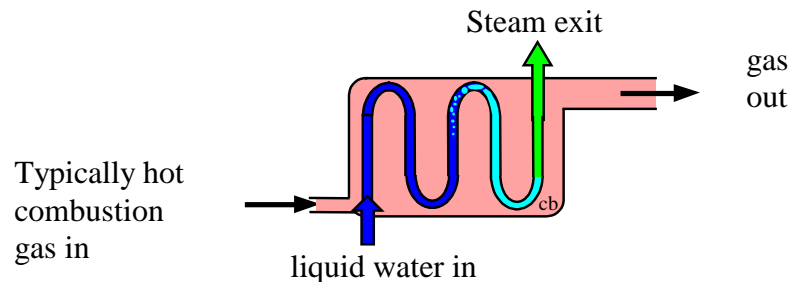
$$\mathbf{V}_i = \dot{V}_i / A_i = 5 / (0.00545 \times 60) = 15.3 \text{ ft/s}$$

Exit state properties from Table F.7.2 and inlet from F.7.3

$$\mathbf{V}_e = \mathbf{V}_i \times v_e / v_i = 15.3 \text{ ft/s} \times (0.526 / 0.01605) = 501.4 \text{ ft/s}$$

The energy equation Eq.4.12 is solved for the heat transfer as

$$\begin{aligned} \dot{Q} &= \dot{m} \left[(h_e - h_i) + (\mathbf{V}_e^2 - \mathbf{V}_i^2) / 2 \right] \\ &= 18\,682 \left[1341.5 - 71.99 + \frac{501.4^2 - 15.3^2}{2 \times 32.174 \times 778} \right] = 2.381 \times 10^7 \text{ Btu/h} \end{aligned}$$



4.184E

An oven has five radiant heaters; each one is rated at 15 Btu/s. It should heat some 4-lbm steel plates from 77 F to 1400 R. How many of these plates per minute can it heat?

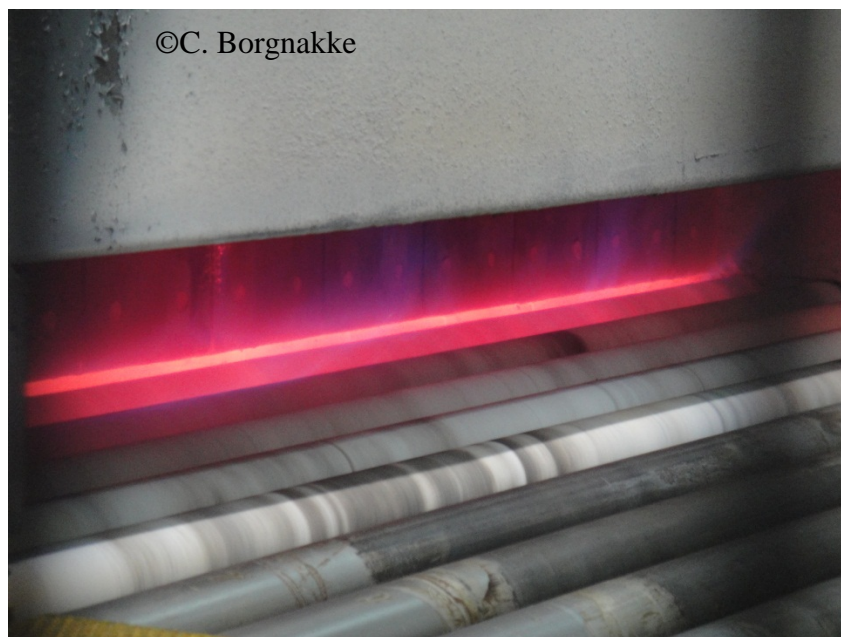
C.V. Oven, steady state operation. A flow of plates in (represents an \dot{m})

Energy Eq.: $0 = \dot{m} (h_i - h_e) + \dot{Q}$

$$\dot{Q} = \dot{m} (h_e - h_i) = \dot{m} C (T_e - T_i)$$

$$\dot{m} = \dot{Q} / C (T_e - T_i) = \frac{5 \times 15 \text{ Btu/s}}{0.11 (1400 - 536.7) \text{ Btu/lbm}} = 0.79 \text{ lbm/s}$$

$$N = \dot{m}/m = (0.79 / 4) \text{ 1/s} = 0.197 \text{ per s} = \mathbf{11.85 \text{ per min}}$$



Front end of oven with steel rollers to bring the plates in, a skirt hangs down to limit heat losses.

4.185E

An evaporator has R-410A at 0 F and quality 20% flowing in, with the exit flow being saturated vapor at 0 F. Knowing that there is no work, find the specific heat transfer.

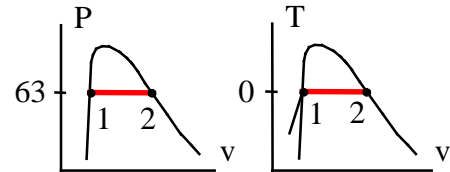
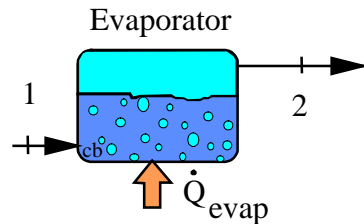
C.V. Heater Steady state single inlet and exit flow.

Energy Eq.4.13: $0 = q + h_1 - h_2$

Table F.9.1: $h_1 = 13.52 + 0.2 \times 103.76 = 34.27 \text{ Btu/lbm}$

$h_2 = 117.28 \text{ Btu/lbm}$

$q = h_2 - h_1 = 117.28 - 34.27 = \mathbf{83.01 \text{ Btu/lbm}}$



4.186E

A flow of liquid glycerine flows around an engine, cooling it as it absorbs energy. The glycerine enters the engine at 140 F and receives 13 hp of heat transfer. What is the required mass flow rate if the glycerine should come out at a maximum 200 F?

Solution:

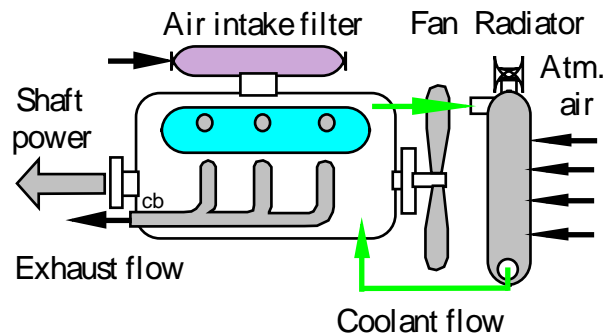
C.V. Liquid flow (glycerine is the coolant), steady flow. no work.

Energy Eq.: $\dot{m}h_i + \dot{Q} = \dot{m}h_e$

$$\dot{m} = \dot{Q} / (h_e - h_i) = \frac{\dot{Q}}{C_{\text{gly}} (T_e - T_i)}$$

From table F.3: $C_{\text{gly}} = 0.58 \text{ Btu/lbm R}$

$$\dot{m} = \frac{13 \text{ hp} \times (2544.4/3600) \text{ btu/s-hp}}{0.58 \text{ btu/lbm-R} (200 - 140) \text{ R}} = \mathbf{0.264 \text{ lbm/s}}$$



4.187E

A small water pump is used in an irrigation system. The pump takes water in from a river at 50 F, 1 atm at a rate of 10 lbm/s. The exit line enters a pipe that goes up to an elevation 100 ft above the pump and river, where the water runs into an open channel. Assume the process is adiabatic and that the water stays at 50 F. Find the required pump work.

Solution:

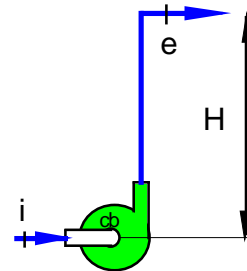
C.V. pump + pipe. Steady state, 1 inlet, 1 exit flow. Assume same velocity in and out, no heat transfer.

Continuity Eq.: $\dot{m}_{in} = \dot{m}_{ex} = \dot{m}$

Energy Eq.4.12:

$$\dot{m}(h_{in} + (1/2)V_{in}^2 + gz_{in}) = \dot{m}(h_{ex} + (1/2)V_{ex}^2 + gz_{ex}) + \dot{W}$$

States: $h_{in} = h_{ex}$ same (T, P)



$$\begin{aligned} \dot{W} &= \dot{m}g(z_{in} - z_{ex}) = 10 \text{ lbm/s} \times \frac{32.174 \text{ ft/s}^2}{32.174 \text{ lbm ft/s}^2 / \text{lbf}} \times (-100) \text{ ft} \\ &= \mathbf{-1000 \text{ lbf-ft/s} = -1.285 \text{ Btu/s}} \end{aligned}$$

I.E. 1.285 Btu/s required input

Multiple Flow Devices

4.188E

A steam turbine receives water at 2000 lbf/in.², 1200 F at a rate of 200 lbm/s as shown in Fig. P4.84. In the middle section 50 lbm/s is withdrawn at 300 lbf/in.², 650 F and the rest exits the turbine at 10 lbf/in.², 95% quality. Assuming no heat transfer and no changes in kinetic energy, find the total turbine work.

C.V. Turbine Steady state, 1 inlet and 2 exit flows.

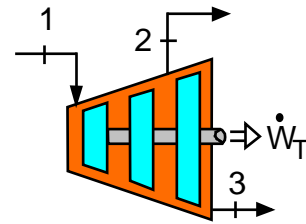
Continuity Eq.4.9: $\dot{m}_1 = \dot{m}_2 + \dot{m}_3$; $\Rightarrow \dot{m}_3 = \dot{m}_1 - \dot{m}_2 = 150 \text{ lbm/s}$

Energy Eq.4.10: $\dot{m}_1 h_1 = \dot{W}_T + \dot{m}_2 h_2 + \dot{m}_3 h_3$

Table F.7.2 $h_1 = 1598.6 \text{ Btu/lbm}$,

$h_2 = 1341.6 \text{ Btu/lbm}$

Table F.7.1 : $h_3 = h_f + x_3 h_{fg} = 161.2 + 0.95 \times 982.1$
 $= 1094.2 \text{ Btu/lbm}$



From the energy equation, Eq.4.10

$$\begin{aligned}\dot{W}_T &= \dot{m}_1 h_1 - \dot{m}_2 h_2 - \dot{m}_3 h_3 = 200 \times 1598.6 - 50 \times 1341.6 - 150 \times 1094.2 \\ &= \mathbf{8.85 \times 10^4 \text{ Btu/s}}\end{aligned}$$

4.189E

A condenser, as the heat exchanger shown in Fig. P4.91, brings 1 lbm/s water flow at 1 lbf/in.² from 500 F to saturated liquid at 1 lbf/in.². The cooling is done by lake water at 70 F that returns to the lake at 90 F. For an insulated condenser, find the flow rate of cooling water.

Solution:

C.V. Heat exchanger

Energy Eq.4.10: $\dot{m}_{\text{cool}}h_{70} + \dot{m}_{\text{H}_2\text{O}}h_{500} = \dot{m}_{\text{cool}}h_{90} + \dot{m}_{\text{H}_2\text{O}}h_{f,1}$

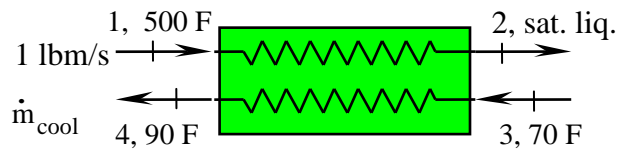


Table F.7.1: $h_{70} = 38.09$ Btu/lbm, $h_{90} = 58.07$ Btu/lbm, $h_{f,1} = 69.74$ Btu/lbm

Table F.7.2: $h_{500,1} = 1288.5$ btu/lbm

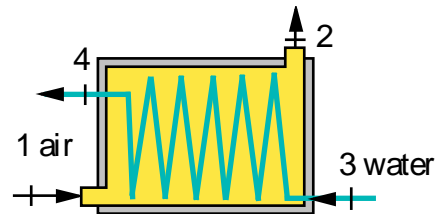
$$\dot{m}_{\text{cool}} = \dot{m}_{\text{H}_2\text{O}} \frac{h_{500} - h_{f,1}}{h_{90} - h_{70}} = 1 \text{ lbm/s} \times \frac{1288.5 - 69.74}{58.07 - 38.09} = \mathbf{61 \text{ lbm/s}}$$

4.190E

A heat exchanger is used to cool an air flow from 1400 to 680 R, both states at 150 lbf/in.². The coolant is a water flow at 60 F, 15 lbf/in.² and it is shown in Fig. P4.95. If the water leaves as saturated vapor, find the ratio of the flow rates $\dot{m}_{\text{H}_2\text{O}}/\dot{m}_{\text{air}}$.

Solution:

C.V. Heat exchanger, steady flow 1 inlet and 1 exit for air and water each. The two flows exchange energy with no heat transfer to/from the outside.



Continuity Eqs.: Each line has a constant flow rate through it.

$$\text{Energy Eq. 4.10: } \dot{m}_{\text{air}}h_1 + \dot{m}_{\text{H}_2\text{O}}h_3 = \dot{m}_{\text{air}}h_2 + \dot{m}_{\text{H}_2\text{O}}h_4$$

Process: Each line has a constant pressure.

Table F.5: $h_1 = 343.016$ Btu/lbm, $h_2 = 162.86$ Btu/lbm

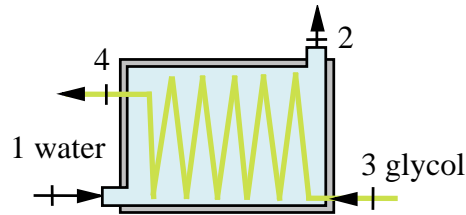
Table F.7: $h_3 = 28.08$ Btu/lbm, $h_4 = 1150.9$ Btu/lbm (at 15 psia)

$$\dot{m}_{\text{H}_2\text{O}}/\dot{m}_{\text{air}} = \frac{h_1 - h_2}{h_4 - h_3} = \frac{343.016 - 162.86}{1150.9 - 28.08} = \mathbf{0.1604}$$

4.191E

A dual-fluid heat exchanger has 10 lbm/s water entering at 100 F, 20 psia and leaving at 50 F, 20 psia. The other fluid is glycol, entering at 10 F, 22 psia and leaving at 50 F, 22 psia. Find the required mass flow rate of glycol and the rate of internal heat transfer.

C.V. Heat exchanger, steady flow 1 inlet and 1 exit for glycol and water each. The two flows exchange energy with no heat transfer to/from the outside.



Continuity Eqs.: Each line has a constant flow rate through it.

$$\text{Energy Eq. 4.10: } \dot{m}_{\text{H}_2\text{O}} h_1 + \dot{m}_{\text{glycol}} h_3 = \dot{m}_{\text{H}_2\text{O}} h_2 + \dot{m}_{\text{glycol}} h_4$$

Process: Each line has a constant pressure.

Table F.7: $h_1 = 68.04$ Btu/lbm, $h_2 = 18.05$ Btu/lbm

Table F.3: $C_{P \text{ gly}} = 0.58$ Btu/lbm-R so

$$h_4 - h_3 = C_{P \text{ gly}} (T_4 - T_3) = 0.58 [50 - 10] = 23.2 \text{ Btu/lbm}$$

$$\dot{m}_{\text{glycol}} = \dot{m}_{\text{H}_2\text{O}} \frac{h_1 - h_2}{h_4 - h_3} = 10 \text{ lbm/s} \frac{68.04 - 18.05}{23.2} = \mathbf{21.55 \text{ lbm/s}}$$

4.192E

An automotive radiator has glycerine at 200 F enter and return at 130 F as shown in Fig. P4.100. Air flows in at 68 F and leaves at 77 F. If the radiator should transfer 33 hp what is the mass flow rate of the glycerine and what is the volume flow rate of air in at 15 psia?

Solution:

If we take a control volume around the whole radiator then there is no external heat transfer - it is all between the glycerin and the air. So we take a control volume around each flow separately.

Heat transfer: $\dot{Q} = 33 \text{ hp} = 33 \times 2544.4 / 3600 = 23.324 \text{ Btu/s}$

Glycerine energy: $\dot{m}h_i + (-\dot{Q}) = \dot{m}h_e$

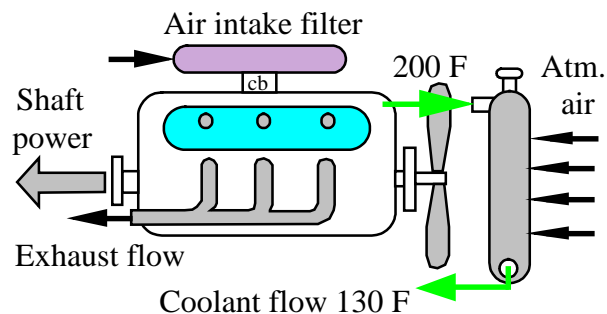
$$\text{Table F.3: } \dot{m}_{\text{gly}} = \frac{-\dot{Q}}{h_e - h_i} = \frac{-\dot{Q}}{C_{\text{gly}}(T_e - T_i)} = \frac{-23.324}{0.58(130 - 200)} = \mathbf{0.574 \text{ lbm/s}}$$

Air $\dot{m}h_i + \dot{Q} = \dot{m}h_e$

$$\text{Table F.4: } \dot{m}_{\text{air}} = \frac{\dot{Q}}{h_e - h_i} = \frac{\dot{Q}}{C_{\text{air}}(T_e - T_i)} = \frac{23.324}{0.24(77 - 68)} = 8.835 \text{ lbm/s}$$

$$\dot{V} = \dot{m}v_i; \quad v_i = \frac{RT_i}{P_i} = \frac{53.34 \times 527.7}{15 \times 144} = 13.03 \text{ ft}^3/\text{lbm}$$

$$\dot{V}_{\text{air}} = \dot{m}v_i = 8.835 \times 13.03 = \mathbf{115 \text{ ft}^3/\text{s}}$$



4.193E

Steam at 80 psia, 600 F is used to heat cold water at 60 F to 170 F for domestic hot water supply. How much steam per lbm liquid water is needed if the steam should not condense?

Solution:

C.V. Each line separately. No work but there is heat transfer out of the steam flow and into the liquid water flow.

$$\text{Water line energy Eq.: } \dot{m}_{\text{liq}} h_i + \dot{Q} = \dot{m}_{\text{liq}} h_e \Rightarrow \dot{Q} = \dot{m}_{\text{liq}} (h_e - h_i)$$

For the liquid water look in Table F.7.1

$$\begin{aligned} \Delta h_{\text{liq}} &= h_e - h_i = 137.96 - 28.08 = 109.88 \text{ btu/lbm} \\ &(\cong C_p \Delta T = 1.0 (170 - 60) = 110 \text{ btu/lbm}) \end{aligned}$$

Steam line energy has the same heat transfer but it goes out

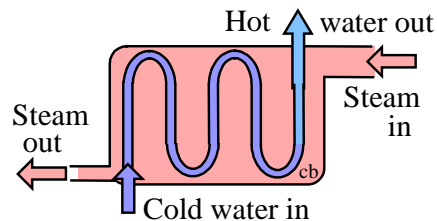
$$\text{Steam Energy Eq.: } \dot{m}_{\text{steam}} h_i = \dot{Q} + \dot{m}_{\text{steam}} h_e \Rightarrow \dot{Q} = \dot{m}_{\text{steam}} (h_i - h_e)$$

For the steam look in Table F.7.2 at 80 psia

$$\Delta h_{\text{steam}} = h_i - h_e = 1330.66 - 1183.61 = 147.05 \text{ btu/lbm}$$

Now the heat transfer for the steam is substituted into the energy equation for the water to give

$$\dot{m}_{\text{steam}} / \dot{m}_{\text{liq}} = \Delta h_{\text{liq}} / \Delta h_{\text{steam}} = \frac{109.88}{147.05} = \mathbf{0.747}$$



4.194E

A copper wire has been heat treated to 1800 R and is now pulled into a cooling chamber that has 3 lbm/s air coming in at 70 F; the air leaves the other end at 120 F. If the wire moves 0.5 lbm/s copper, how hot is the copper as it comes out?

Solution:

C.V. Total chamber, no external heat transfer

$$\begin{aligned}\text{Energy eq.: } \dot{m}_{\text{cu}} h_{i\text{cu}} + \dot{m}_{\text{air}} h_{i\text{air}} &= \dot{m}_{\text{cu}} h_{e\text{cu}} + \dot{m}_{\text{air}} h_{e\text{air}} \\ \dot{m}_{\text{cu}} (h_e - h_i)_{\text{cu}} &= \dot{m}_{\text{air}} (h_i - h_e)_{\text{air}} \\ \dot{m}_{\text{cu}} C_{\text{cu}} (T_e - T_i)_{\text{cu}} &= \dot{m}_{\text{air}} C_{\text{p air}} (T_e - T_i)_{\text{air}}\end{aligned}$$

Heat capacities from F.2 for copper and F.4 for air

$$\begin{aligned}(T_e - T_i)_{\text{cu}} &= \frac{\dot{m}_{\text{air}} C_{\text{p air}}}{\dot{m}_{\text{cu}} C_{\text{cu}}} (T_e - T_i)_{\text{air}} \\ &= \frac{3 \times 0.24}{0.5 \times 0.1} (70 - 120) \text{ R} = -720 \text{ R}\end{aligned}$$

$$T_e = T_i - 720 = 1800 - 720 = \mathbf{1080 \text{ R}}$$

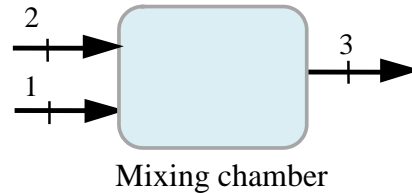


4.195E

Two flows of air are both at 30 psia; one has 1 lbm/s at 720 R and the other has 2 lbm/s at 520 R. The two flows are mixed together in an insulated box to produce a single exit flow at 30 psia. Find the exit temperature.

Solution:

$$\begin{aligned}\text{Cont.:} \quad & \dot{m}_1 + \dot{m}_2 = \dot{m}_3 \\ \text{Energy:} \quad & \dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 \\ & = (\dot{m}_1 + \dot{m}_2) h_3\end{aligned}$$



Solve for the exit enthalpy

$$h_3 = [\dot{m}_1 h_1 + \dot{m}_2 h_2] / (\dot{m}_1 + \dot{m}_2)$$

since the T's are modest use constant specific heats

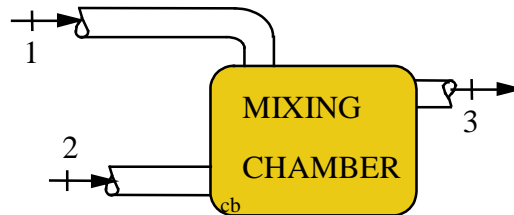
$$T_3 = [\dot{m}_1 T_1 + \dot{m}_2 T_2] / (\dot{m}_1 + \dot{m}_2) = \frac{1}{3} \times 720 + \frac{2}{3} \times 520 = \mathbf{586.7 \text{ R}}$$

4.196E

A de-superheater has a flow of ammonia 3 lbm/s at 150 psia, 200 F which is mixed with another flow of ammonia at 80 F and quality 25% in an adiabatic mixing chamber. Find the flow rate of the second flow so the outgoing ammonia is saturated vapor at 150 psia.

C.V. Desuperheater.

No external \dot{Q} or \dot{W}



Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$

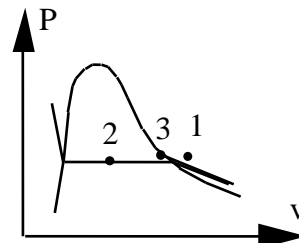
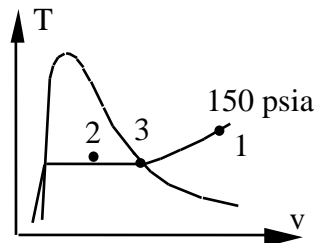
Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 = (\dot{m}_1 + \dot{m}_2) h_3$

State 1: Table F.8.2 $h_1 = 707.96$ Btu/lbm

State 2: Table F.8.1 $h_2 = 131.68 + 0.25 \times 497.94 = 256.17$ Btu/lbm

State 3: Table F.8.2 $h_3 = 629.45$ Btu/lbm

$$\dot{m}_2 = \dot{m}_1 \times \frac{h_1 - h_3}{h_3 - h_2} = 3 \times \frac{707.96 - 629.45}{629.45 - 256.17} = \mathbf{0.631 \text{ lbm/s}}$$



4.197E

An insulated mixing chamber receives 4 lbm/s R-134a at 150 lbf/in.², 220 F in a line with low velocity. Another line with R-134a as saturated liquid 130 F flows through a valve to the mixing chamber at 150 lbf/in.² after the valve. The exit flow is saturated vapor at 150 lbf/in.² flowing at 60 ft/s. Find the mass flow rate for the second line.

Solution:

C.V. Mixing chamber. Steady state, 2 inlets and 1 exit flow.

Insulated $q = 0$, No shaft or boundary motion $w = 0$.

Continuity Eq.4.9: $\dot{m}_1 + \dot{m}_2 = \dot{m}_3$;

Energy Eq.4.10: $\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 (h_3 + \frac{1}{2} V_3^2)$

$$\dot{m}_2 (h_2 - h_3 - \frac{1}{2} V_3^2) = \dot{m}_1 (h_3 + \frac{1}{2} V_3^2 - h_1)$$

State 1: Table F.10.1: 150 psia, 220 F, $h_1 = 209.63$ Btu/lbm

State 2: Table F.10.1: $x = 0$, 130 F, $h_2 = 119.88$ Btu/lbm

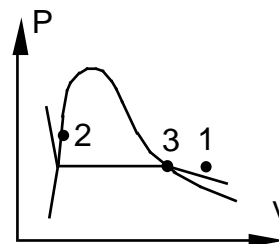
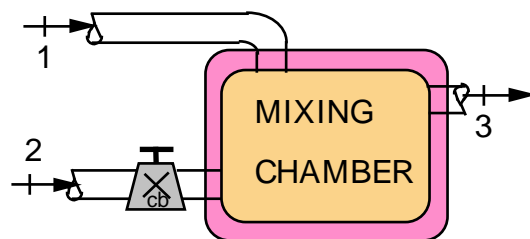
State 3: Table F.10.2: $x = 1$, 150 psia, $h_3 = 180.61$ Btu/lbm

$$\frac{1}{2} V_3^2 = \frac{1}{2} \times 60^2 / (32.174 \times 778) = 0.072 \text{ Btu/lbm}$$

$$\dot{m}_2 = \dot{m}_1 (h_3 + \frac{1}{2} V_3^2 - h_1) / (h_2 - h_3 - \frac{1}{2} V_3^2)$$

$$= 4 (180.61 + 0.072 - 209.63) / (119.88 - 180.61 - 0.072) = \mathbf{1.904 \text{ lbm/s}}$$

Notice how kinetic energy was insignificant.



Multiple Devices, Cycle Processes

4.198E

The following data are for a simple steam power plant as shown in Fig. P4.118.

State	1	2	3	4	5	6	7
P psia	900	890	860	830	800	1.5	1.4
T F		115	350	920	900		110
h Btu/lbm	-	85.3	323	1468	1456	1029	78

State 6 has $x_6 = 0.92$, and velocity of 600 ft/s. The rate of steam flow is 200 000 lbm/h, with 400 hp input to the pump. Piping diameters are 8 in. from steam generator to the turbine and 3 in. from the condenser to the steam generator. Determine the power output of the turbine and the heat transfer rate in the condenser.

$$\text{Turbine: } A_5 = \pi D_5^2/4 = 0.349 \text{ ft}^2, \quad v_5 = 0.964 \text{ ft}^3/\text{lbm}$$

$$V_5 = \dot{m}v_5/A_5 = \frac{200\,000 \times 0.964}{3600 \times 0.349} = 153 \text{ ft/s}$$

$$w = (h_5 + 0.5V_5^2) - (h_6 + 0.5V_6^2) = 1456 - 1029 - \frac{600^2 - 153^2}{2 \times 25\,037} \\ = 420.2 \text{ Btu/lbm}$$

Recall the conversion $1 \text{ Btu/lbm} = 25\,037 \text{ ft}^2/\text{s}^2$, $1 \text{ hp} = 2544 \text{ Btu/h}$

$$\dot{W}_{\text{TURB}} = \frac{420.2 \times 200\,000}{2544} = \mathbf{33\,000 \text{ hp}}$$

$$\text{Condenser: } A_7 = \pi D_7^2/4 = 0.0491 \text{ ft}^2, \quad v_7 = 0.01617 \text{ ft}^3/\text{lbm}$$

$$V_7 = \dot{m}v_7/A_7 = \frac{200\,000 \times 0.01617}{3600 \times 0.0491} = 18 \text{ ft/s}$$

$$q = 78.02 - 1028.7 + \frac{18^2 - 600^2}{2 \times 25\,037} = -957.9 \text{ Btu/lbm}$$

$$\dot{Q}_{\text{COND}} = 200\,000 (-957.9) = \mathbf{-1.916 \times 10^8 \text{ Btu/h}}$$

4.199E

For the same steam power plant as shown in Fig. P4.118 and Problem 4.198E determine the rate of heat transfer in the economizer which is a low temperature heat exchanger and the steam generator. Determine also the flow rate of cooling water through the condenser, if the cooling water increases from 55 to 75 F in the condenser.

$$\text{Condenser: } A_7 = \pi D_7^2/4 = 0.0491 \text{ ft}^2, \quad v_7 = 0.01617 \text{ ft}^3/\text{lbm}$$

$$V_7 = \dot{m}v_7/A_7 = \frac{200000 \times 0.01617}{3600 \times 0.0491} = 18 \text{ ft/s}$$

$$q = 78.02 - 1028.7 + \frac{18^2 - 600^2}{2 \times 25\,037} = -957.9 \text{ Btu/lbm}$$

$$\dot{Q}_{\text{COND}} = 200\,000 (-957.9) = \mathbf{-1.916 \times 10^8 \text{ Btu/h}}$$

Economizer $V_3 \approx V_2$ since liquid v is constant: $v_3 \approx v_2$ and $A_3 = A_2$,

$$q = h_3 - h_2 = 323.0 - 85.3 = 237.7 \text{ Btu/lbm}$$

$$\dot{Q}_{\text{ECON}} = 200\,000 (237.7) = \mathbf{4.75 \times 10^7 \text{ Btu/h}}$$

$$\text{Generator: } A_4 = \pi D_4^2/4 = 0.349 \text{ ft}^2, \quad v_4 = 0.9595 \text{ ft}^3/\text{lbm}$$

$$V_4 = \dot{m}v_4/A_4 = \frac{200\,000 \times 0.9505}{3600 \times 0.349} = 151 \text{ ft/s}$$

$$A_3 = \pi D_3^2/4 = 0.349 \text{ ft}^2, \quad v_3 = 0.0491 \text{ ft}^3/\text{lbm}$$

$$V_3 = \dot{m}v_3/A_3 = \frac{200\,000 \times 0.0179}{3600 \times 0.0491} = 20 \text{ ft/s},$$

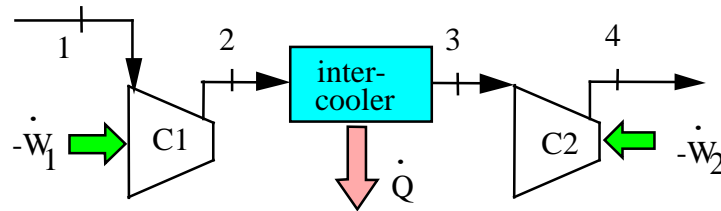
$$q = 1467.8 - 323.0 + \frac{151^2 - 20^2}{2 \times 25\,037} = \mathbf{1145.2 \text{ Btu/lbm}}$$

$$\dot{Q}_{\text{GEN}} = 200\,000 \times (1145.2) = \mathbf{2.291 \times 10^8 \text{ Btu/h}}$$

4.200E

A two-stage compressor takes nitrogen in at 80 F, 20 psia and compresses it to 80 psia, 800 R. Then it flows through an intercooler, where it cools to 580 R, and the second stage compresses it to 400 psia, 1000 R. Find the specific work in each of the two compressor stages and the specific heat transfer in the intercooler.

The setup is like this:



C.V.: Stage 1 nitrogen, Steady flow

Process: adiabatic: $q = 0$, reversible: $s_{\text{gen}} = 0$

Energy Eq. 4.13: $-w_{C1} = h_2 - h_1$,

Assume constant $C_{p0} = 0.249$ from F.4

$$w_{C1} = h_1 - h_2 = C_{p0}(T_1 - T_2) = 0.249 \text{ Btu/lbmR} (540 - 800) \text{ K} \\ = \mathbf{-64.74 \text{ Btu/lbm}}$$

C.V. Intercooler, no work and no changes in kinetic or potential energy.

$$q_{23} = h_3 - h_2 = C_{p0}(T_3 - T_2) = 0.249 (800 - 580) = \mathbf{-135.5 \text{ Btu/lbm}}$$

C.V. Stage 2. Analysis the same as stage 1.

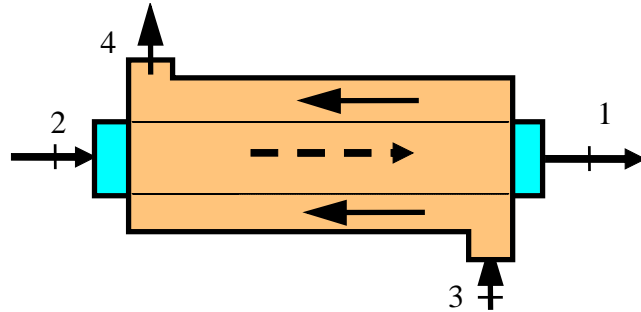
$$w_{C2} = h_3 - h_4 = C_{p0}(T_3 - T_4) = 0.249 (580 - 1000) = \mathbf{-104.6 \text{ Btu/lbm}}$$

4.201E

The intercooler in the previous problem uses cold liquid water to cool the nitrogen. The nitrogen flow is 0.1 lbm/s, and the liquid water inlet is 77 F and is set up to flow in the opposite direction from the nitrogen, so the water leaves at 105 F. Find the flow rate of the water.

Solution:

C.V. Heat exchanger, steady
2 flows in and two flows out.



Continuity eq.: $\dot{m}_1 = \dot{m}_2 = \dot{m}_{\text{H}_2\text{O}}$; $\dot{m}_3 = \dot{m}_4 = \dot{m}_{\text{N}_2}$

Energy eq.: $0 = \dot{m}_{\text{H}_2\text{O}}(h_3 - h_4) + \dot{m}_{\text{N}_2}(h_2 - h_1)$

Due to the lower range of temperature we will use constant specific heats from F.4 and F.3 so the energy equation is approximated as

$$0 = \dot{m}_{\text{H}_2\text{O}} C_{p\text{H}_2\text{O}} (T_3 - T_4) + \dot{m}_{\text{N}_2} C_p (T_2 - T_1)$$

Now solve for the water flow rate

$$\begin{aligned} \dot{m}_{\text{H}_2\text{O}} &= \dot{m}_{\text{N}_2} C_{p\text{N}_2} (T_2 - T_1) / [C_{p\text{H}_2\text{O}} (T_4 - T_3)] \\ &= 0.1 \text{ lbm/s} \times \frac{0.249 \text{ Btu/lbm-R} \times (800 - 580) \text{ R}}{1.0 \text{ Btu/lbm-R} \times (105 - 77) \text{ R}} \\ &= \mathbf{0.196 \text{ lbm/s}} \end{aligned}$$

4.202E

A R-410A heat pump cycle shown in Fig. P4.123 has a R-410A flow rate of 0.1 lbm/s with 4 Btu/s into the compressor. The following data are given

State	1	2	3	4	5	6
P, psia	410	405	400	62	60	58
T, F	220	200	110		10	14
h, Btu/lbm	154	150	56	-	120	122

Calculate the heat transfer from the compressor, the heat transfer from the R-410A in the condenser and the heat transfer to the R-410A in the evaporator.

Solution:

CV: Compressor

$$\dot{Q}_{\text{COMP}} = \dot{m}(h_1 - h_6) + \dot{W}_{\text{COMP}} = 0.1 (154 - 122) - 4.0 = \mathbf{-0.8 \text{ Btu/s}}$$

CV: Condenser

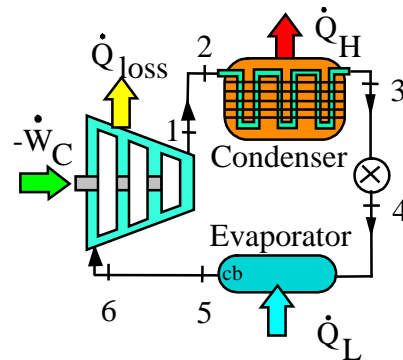
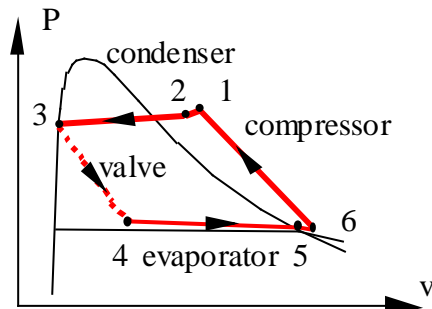
$$\dot{Q}_{\text{COND}} = \dot{m}(h_3 - h_2) = 0.1 \text{ lbm/s} (56 - 150) \text{ Btu/lbm} = \mathbf{-9.4 \text{ Btu/s}}$$

C.V. Valve:

$$h_4 = h_3 = 56 \text{ Btu/lbm}$$

CV: Evaporator

$$\dot{Q}_{\text{EVAP}} = \dot{m} (h_5 - h_4) = 0.1 \text{ lbm/s} (120 - 56) \text{ Btu/lbm} = \mathbf{6.4 \text{ Btu/s}}$$



4.203E

A proposal is made to use a geothermal supply of hot water to operate a steam turbine, as shown in Fig. P4.125. The high pressure water at 200 lbf/in.², 350 F, is throttled into a flash evaporator chamber, which forms liquid and vapor at a lower pressure of 60 lbf/in.². The liquid is discarded while the saturated vapor feeds the turbine and exits at 1 lbf/in.², 90% quality. If the turbine should produce 1000 hp, find the required mass flow rate of hot geothermal water in pound-mass per hour.

Solution:

Separation of phases in flash-evaporator
constant h in the valve flow so

Table F.7.3: $h_1 = 321.8$ Btu/lbm

$$h_1 = 321.8 = 262.25 + x \times 915.8$$

$$\Rightarrow x = 0.06503 = \dot{m}_2/\dot{m}_1$$

Table F.7.2: $h_2 = 1178.0$ Btu/lbm;

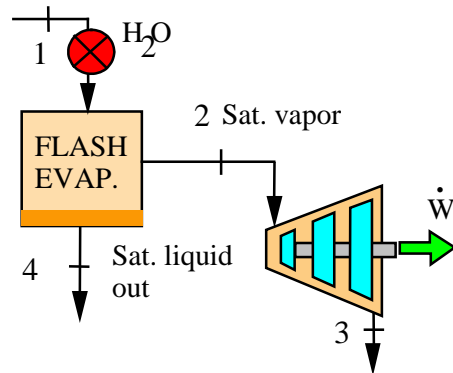


Table F.7.1: $h_3 = 69.74 + 0.9 \times 1036 = 1002.1$ Btu/lbm

$$\dot{W} = \dot{m}_2(h_2 - h_3) \Rightarrow \dot{m}_2 = \frac{1000 \times 2545}{1178.0 - 1002.1} = 14\,472 \text{ lbm/h}$$

$$\Rightarrow \dot{m}_1 = \mathbf{222\,539 \text{ lbm/h}}$$

Notice conversion 1 hp = 2545 Btu/h from Table A.1

Transient Processes

4.204E

A 1 Gallon tank initially is empty and we want to have 0.03 lbm of R-410A in it. The R-410A comes from a line with saturated vapor at 20 F. To end up with the desired amount we cool the can while we fill it in a slow process keeping the can and content at 20 F. Find the final pressure to reach before closing the valve and the heat transfer.

Solution:

C.V. Tank:

Continuity Eq.4.20: $m_2 - 0 = m_i$

Energy Eq.4.21: $m_2 u_2 - 0 = m_i h_i + {}_1Q_2$

State 2: 20 F, $v_2 = V/m_2 = 1 (231/12^3)/0.030 = 4.456 \text{ ft}^3/\text{lbm}$

From Table F.9.2 we locate the state between 15 and 20 psia.

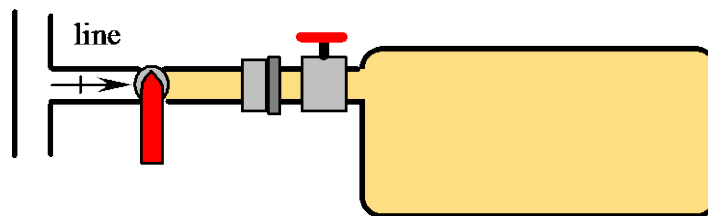
$$P_2 = 15 + (20 - 15) \frac{4.456 - 4.6305}{3.4479 - 4.6305} = \mathbf{15.74 \text{ psia}}$$

$$u_2 = 112.68 \text{ Btu/lbm},$$

$$\text{State i Table F.9.1: } h_i = 119.07 \text{ Btu/lbm}$$

Now use the energy equation to solve for the heat transfer

$$\begin{aligned} {}_1Q_2 &= m_2 u_2 - m_i h_i = m_2 (u_2 - h_i) \\ &= 0.03 \times (112.68 - 119.07) = \mathbf{-0.192 \text{ Btu}} \end{aligned}$$



4.205E

An initially empty cylinder is filled with air from 70 F, 15 psia until it is full. Assuming no heat transfer is the final temperature larger, equal to or smaller than 70 F? Does the final T depends on the size of the cylinder?

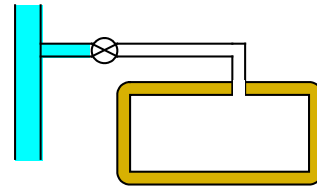
This is a transient problem with no heat transfer and no work. The balance equations for the tank as C.V. become

$$\text{Continuity Eq.:} \quad m_2 - 0 = m_i$$

$$\text{Energy Eq.:} \quad m_2 u_2 - 0 = m_i h_i + Q - W = m_i h_i + 0 - 0$$

$$\text{Final state:} \quad u_2 = h_i \quad \& \quad P_2 = P_i$$

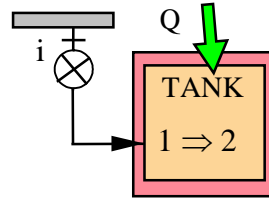
$$T_2 > T_i \quad \text{and it does not depend on } V$$



4.206E

A tank contains 10 ft^3 air at 15 psia, 540 R. A pipe flowing air at 150 psia, 540 R is connected to the tank and it is filled slowly to 150 psia. Find the heat transfer to reach a final temperature of 540 R.

C.V. The tank volume and the compressor.
This is a transient problem (filling of tank).



Continuity Eq.4.20: $m_2 - m_1 = m_{in}$

Energy Eq.4.21: $m_2 u_2 - m_1 u_1 = {}_1Q_2 - {}_1W_2 + m_{in} h_{in}$

Process: Constant volume ${}_1W_2 = 0$,

States: $u_1 = u_2 = u_{in} = u_{540}$; $h_{in} = u_{in} + RT_{in}$

$$m_1 = P_1 V_1 / RT_1 = 15 \times 144 \times 10 / (53.34 \times 540) = 0.75 \text{ lbm}$$

$$m_2 = P_2 V_2 / RT_2 = 150 \times 144 \times 10 / (53.34 \times 540) = 7.499 \text{ lbm}$$

Heat transfer from the energy equation

$$\begin{aligned} {}_1Q_2 &= m_2 u_2 - m_1 u_1 - m_{in} h_{in} = (m_1 + m_{in}) u_1 - m_1 u_1 - m_{in} u_{in} - m_{in} RT_{in} \\ &= m_1 u_1 - m_1 u_1 + m_{in} u_1 - m_{in} u_{in} - m_{in} RT_{in} = -m_{in} RT_{in} \\ &= -(7.499 - 0.75) \text{ lbm} \times 53.34 \text{ ft-lbf/lbm-R} \times 540 \text{ R} \\ &= \mathbf{-194\,395 \text{ ft-lbf} = -250 \text{ Btu}} \end{aligned}$$

4.207E

A 1-ft³ tank, shown in Fig. P4.136, that is initially evacuated is connected by a valve to an air supply line flowing air at 70 F, 120 lbf/in.². The valve is opened, and air flows into the tank until the pressure reaches 90 lbf/in.². Determine the final temperature and mass inside the tank, assuming the process is adiabatic. Develop an expression for the relation between the line temperature and the final temperature using constant specific heats.

Solution:

C.V. Tank:

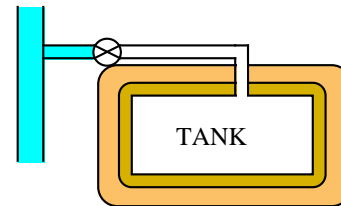
Continuity Eq.4.20: $m_2 = m_i$

Energy Eq.4.21: $m_2 u_2 = m_i h_i$

Table F.5: $u_2 = h_i = 126.78 \text{ Btu/lbm}$

$$\Rightarrow T_2 = \mathbf{740 \text{ R}}$$

$$m_2 = \frac{P_2 V}{RT_2} = \frac{90 \times 144 \times 1}{53.34 \times 740} = \mathbf{0.3283 \text{ lbm}}$$



Assuming constant specific heat,

$$h_i = u_i + RT_i = u_2, \quad RT_i = u_2 - u_i = C_{V0}(T_2 - T_i)$$

$$C_{V0}T_2 = (C_{V0} + R)T_i = C_{P0}T_i,$$

$$T_2 = \left(\frac{C_{P0}}{C_{V0}} \right) T_i = kT_i$$

For $T_i = 529.7 \text{ R}$ & constant C_{P0} ,

$$T_2 = 1.40 \times 529.7 = \mathbf{741.6 \text{ R}}$$

4.208E

Helium in a steel tank is at 40 psia, 540 R with a volume of 4 ft³. It is used to fill a balloon. When the tank pressure drops to 24 psia the flow of helium stops by itself. If all the helium still is at 540 R how big a balloon did I get? Assume the pressure in the balloon varies linearly with volume from 14.7 psia ($V = 0$) to the final 24 psia. How much heat transfer did take place?

Solution:

Take a C.V. of all the helium.

This is a control mass, the tank mass changes density and pressure.

$$\text{Energy Eq.: } U_2 - U_1 = {}_1Q_2 - {}_1W_2$$

$$\text{Process Eq.: } P = 14.7 + CV$$

$$\text{State 1: } P_1, T_1, V_1$$

$$\text{State 2: } P_2, T_2, V_2 = ?$$

Ideal gas:

$$P_2 V_2 = mRT_2 = mRT_1 = P_1 V_1$$

$$V_2 = V_1(P_1/P_2) = 4 \times (40/24) = 6.6667 \text{ ft}^3$$

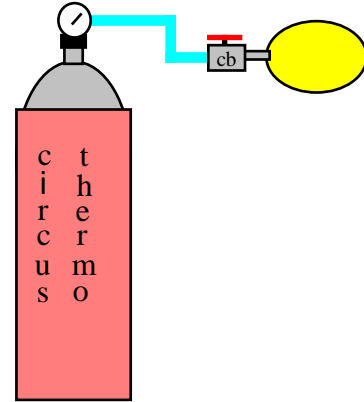
$$V_{\text{bal}} = V_2 - V_1 = 6.6667 - 4 = 2.6667 \text{ ft}^3$$

$${}_1W_2 = \int P dV = \text{AREA} = \frac{1}{2} (P_1 + P_2) (V_2 - V_1)$$

$$= \frac{1}{2} (40 + 24) \times 2.6667 \times 144 = 12\,288 \text{ lbf-ft} = 15.791 \text{ Btu}$$

$$U_2 - U_1 = {}_1Q_2 - {}_1W_2 = m(u_2 - u_1) = mC_v (T_2 - T_1) = 0$$

$$\text{so } {}_1Q_2 = {}_1W_2 = \mathbf{15.79 \text{ Btu}}$$



Remark: The process is transient, but you only see the flow mass if you select the tank or the balloon as a control volume. That analysis leads to more terms that must be eliminated between the tank control volume and the balloon control volume.

4.209E

A 20-ft³ tank contains ammonia at 20 lbf/in.², 80 F. The tank is attached to a line flowing ammonia at 180 lbf/in.², 140 F. The valve is opened, and mass flows in until the tank is half full of liquid, by volume at 80 F. Calculate the heat transferred from the tank during this process.

Solution:

C.V. Tank. Transient process as flow comes in.

$$m_1 = V/v_1 = 20/16.765 = 1.193 \text{ lbm}$$

$$m_{f2} = V_{f2}/v_{f2} = 10/0.026677 = 374.855 \text{ lbm},$$

$$m_{g2} = V_{g2}/v_{g2} = 10/1.9531 = 5.120 \text{ lbm}$$

$$m_2 = m_{f2} + m_{g2} = 379.975 \text{ lbm} \Rightarrow x_2 = m_{g2}/m_2 = 0.013475$$

$$\text{Table F.8.1, } u_2 = 130.9 + 0.013475 \times 443.4 = 136.9 \text{ Btu/lbm}$$

$$u_1 = 595.0 \text{ Btu/lbm, } h_i = 667.0 \text{ Btu/lbm}$$

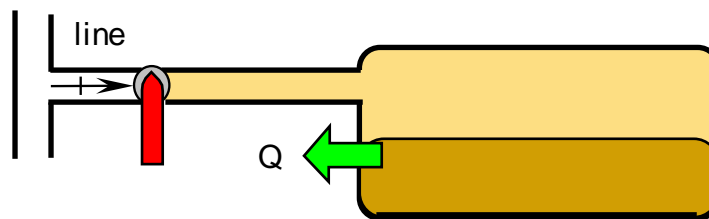
$$\text{Continuity Eq.: } m_i = m_2 - m_1 = 378.782 \text{ lbm,}$$

From continuity equation

$$m_i = m_2 - m_1 = 379.975 - 1.193 = 378.782 \text{ lbm}$$

$$\text{Energy eq.: } Q_{CV} + m_i h_i = m_2 u_2 - m_1 u_1$$

$$\begin{aligned} Q_{CV} &= 379.975 \times 136.9 - 1.193 \times 595.0 - 378.782 \times 667.0 \\ &= \mathbf{-201\,339 \text{ Btu}} \end{aligned}$$



4.210E

A nitrogen line, 540 R, and 75 lbf/in.², is connected to a turbine that exhausts to a closed initially empty tank of 2000 ft³, as shown in Fig. P4.137. The turbine operates to a tank pressure of 75 lbf/in.², at which point the temperature is 450 R. Assuming the entire process is adiabatic, determine the turbine work.

C.V. turbine & tank \Rightarrow Transient problem

Conservation of mass: $m_i = m_2 = m$

Energy Eq.: $m_i h_i = m_2 u_2 + W_{CV}$; $W_{CV} = m(h_i - u_2)$

Inlet state: $P_i = 75 \text{ lbf/in.}^2$, $T_i = 540 \text{ R}$

Final state 2: $P_2 = 75 \text{ lbf/in.}^2$, $T_2 = 450 \text{ R}$

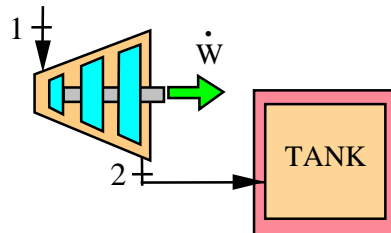
$$v_2 = RT_2/P_2 = 55.15 \times 450 / (75 \times 144) = 2.298 \text{ ft}^3/\text{lbm}$$

$$m_2 = V/v_2 = 2000/2.298 = 870.32 \text{ lbm}$$

$$h_i - u_2 = u_i + RT_i - u_2 = RT_i + C_v (T_i - T_2)$$

$$= \frac{55.15}{778.17} 540 + 0.178 (540 - 450) = 38.27 + 16.02 = 54.29 \frac{\text{Btu}}{\text{lbm}}$$

$$W_{CV} = 870.32 \times 54.29 = \mathbf{47\,250 \text{ Btu}}$$



4.211E

A mass-loaded piston/cylinder containing air is at 45 lbf/in.², 60 F with a volume of 9 ft³, while at the stops $V = 36$ ft³. An air line, 75 lbf/in.², 1100 R, is connected by a valve, as shown in Fig. P4.154. The valve is then opened until a final inside pressure of 60 lbf/in.² is reached, at which point $T = 630$ R. Find the air mass that enters, the work, and heat transfer.

Solution:

C.V. Cylinder volume.

Continuity Eq.4.20: $m_2 - m_1 = m_{in}$

Energy Eq.4.21: $m_2 u_2 - m_1 u_1 = m_{in} h_{line} + {}_1Q_2 - {}_1W_2$

Process: P_1 is constant to stops, then constant V to state 2 at P_2

$$\text{State 1: } P_1, T_1 \quad m_1 = \frac{P_1 V}{RT_1} = \frac{45 \times 9 \times 144}{53.34 \times 519.7} = 2.104 \text{ lbm}$$

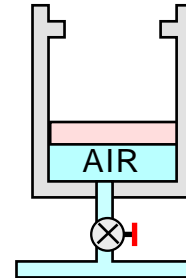
State 2: Open to: $P_2 = 60$ lbf/in.², $T_2 = 630$ R

Table F.5:

$$h_i = 266.13 \text{ Btu/lbm}$$

$$u_1 = 88.68 \text{ Btu/lbm}$$

$$u_2 = 107.62 \text{ Btu/lbm}$$



$${}_1W_2 = \int P dV = P_1(V_{\text{stop}} - V_1) = 45 \times (36 - 9) \frac{144}{778} = \mathbf{224.9 \text{ Btu}}$$

$$m_2 = P_2 V_2 / RT_2 = 60 \times 36 \times 144 / (53.34 \times 630) = 9.256 \text{ lbm}$$

$$m_i = m_2 - m_1 = 9.256 - 2.104 = 7.152 \text{ lbm}$$

$$\begin{aligned} {}_1Q_2 &= m_2 u_2 - m_1 u_1 - m_i h_i + {}_1W_2 \\ &= 9.256 \times 107.62 - 2.104 \times 88.68 - 7.152 \times 266.13 + 224.9 \\ &= \mathbf{-868.9 \text{ Btu}} \end{aligned}$$