

NAME: \_\_\_\_\_ Student # \_\_\_\_\_ GROUP: \_\_\_\_\_  
ENG 1440 Lab # 10 BONUS

A UFO (Unidentified Flying Object) landed in South Winnipeg (near the U of M campus) and was seen taking off carrying three (3) unidentified packages (rumor has it they were Engineering students). The masses of the students are  $M_1 = 100 \text{ kg}$ ,  $M_2 = 65 \text{ kg}$  and  $M_3 = 140 \text{ kg}$ . Their location in the  $5 \text{ m}$  radius space craft is shown in Figure 1(b) below.

The message back from the space craft is that the students will be returned if you can replace these forces by a single force and correctly locate its point of application with respect to the origin,  $O$  in the figure. (Use  $g = 9.8 \text{ m/sec}^2$ )

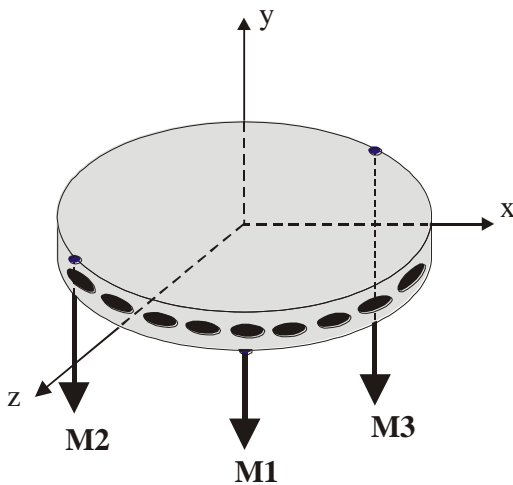


Figure 1(a)

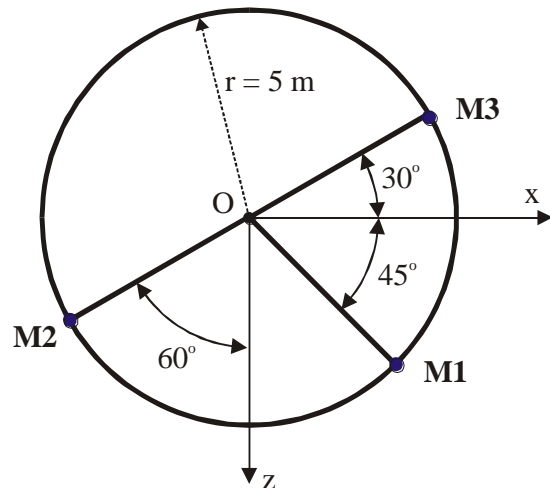


Figure 1(b) - Location of Masses

ANSWER (Provide detailed solution):

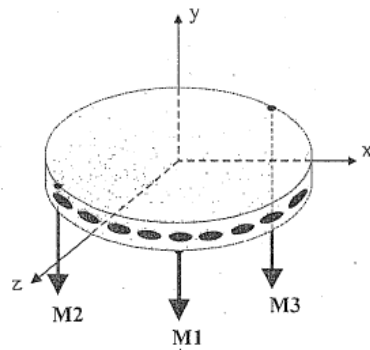


Figure 1(a)

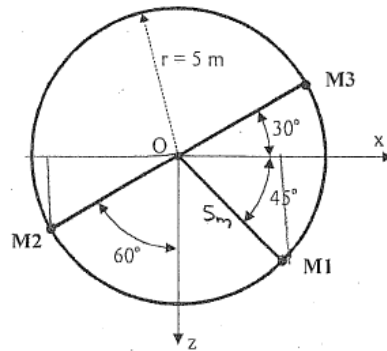


Figure 1(b) - Location of Masses

FORCE	MAGN(N)	$\vec{F}$	$\vec{r}$ (m)	$\vec{M}_o = \vec{r} \times \vec{F}$
M1	980	$-980\hat{j}$	$5 \cos 45^\circ \hat{i} + 5 \sin 45^\circ \hat{k}$ $= 3.535\hat{i} + 3.535\hat{k}$	$3.535 \times (-980)\hat{k} + 3.535 \times (-980)(-\hat{i})$ $= -3464.3\hat{k} + 3464.3\hat{i}$
M2	637	$-637\hat{j}$	$-5 \sin 60^\circ \hat{i} + 5 \cos 60^\circ \hat{k}$ $= -4.330\hat{i} + 2.5\hat{k}$	$-4.330(-637)\hat{k} + 2.5(-637)(-\hat{i})$ $= 2758.21\hat{k} + 1592.5\hat{i}$
M3	1372	$-1372\hat{j}$	$5 \cos 30^\circ \hat{i} - 5 \sin 30^\circ \hat{k}$ $= 4.330\hat{i} - 2.5\hat{k}$	$4.330(-1372)\hat{k} + (-2.5)(-1372)(-\hat{i})$ $= -5940.76\hat{k} - 3430\hat{i}$

$$\vec{R} = \sum \vec{F} = -2989\hat{j} \text{ (N)} \quad \sum \vec{M}_o = -6646.85\hat{k} + 1626.8\hat{i}$$

$$\therefore \sum \vec{M}_o = (x\hat{i} + z\hat{k}) \times \vec{R} = (x\hat{i} + z\hat{k}) \times (-2989\hat{j})$$

$$1626.8\hat{i} - 6646.85\hat{k} = -2989x\hat{k} - 2989z(-\hat{i})$$

$$= -2989x\hat{k} + 2989z\hat{i}$$

$$\therefore 1626.8 = 2989z \quad z = 0.544 \text{ m} \quad \blacktriangleleft$$

$$-6646.85 = -2989x \quad x = 2.22 \text{ m} \quad \blacktriangleleft$$