## Math 1710: Tutorial 6 (inverse trig. functions and their derivatives)

1. Simplify the following expressions provided the expression is well-defined:

(a) 
$$\cos^{-1}\left(\cos\left(\frac{\pi}{11}\right)\right)$$
;

(b) 
$$\cos^{-1}\left(\cos\left(\frac{43\pi}{11}\right)\right)$$
;

(c) 
$$\sin^{-1}\left(\tan\left(\frac{\pi}{3}\right)\right)$$
;

(d) 
$$\cos\left(\cot^{-1}\left(-\frac{12}{5}\right)\right)$$
;

(e) 
$$\tan\left(\sin^{-1}\left(-\frac{15}{17}\right)\right)$$
;

(f) 
$$\cos\left(2\sin^{-1}\left(\frac{3}{5}\right)\right)$$
;

(g) 
$$\sec\left(\csc^{-1}\left(-\frac{25}{7}\right)\right)$$
;

(h) 
$$\cot \left( \sin^{-1} \left( \frac{1}{2} \csc \left( -\frac{11\pi}{4} \right) \right) \right)$$
.

2. Using derivatives of inverse trigonometric functions show that for any x,

$$\tan^{-1}(x) + \cot^{-1}(x) = \frac{\pi}{2}.$$

3. Find  $\frac{dy}{dx}$  (simplify the expressions as much as possible):

(a) 
$$y = \sin^{-1}\left(\frac{x^2}{x^2 + 1}\right);$$

(b) 
$$y = x \tan^{-1}(e^x);$$

(c) 
$$y = 4^{3\cos^{-1}(x)}$$
;

(d) 
$$y = \sin(\cos^{-1}(x^2));$$

(e) 
$$y = x^{\cot^{-1}(x)}$$
;

(f) 
$$y = \frac{[\sin^{-1}(x)]^{10}}{x^3}$$
;

(g) 
$$y = \ln (\sec^{-1}(3x))$$
.

4. Find the equation of the tangent line to the curve given by

$$2y \cot^{-1}(x) = \pi(1+xy)$$

at the point corresponding to x = 1.