

QUIZ #1, Math 253

1. Given the vectors $\vec{u} = \vec{i} - 2\vec{j}$ and $\vec{v} = \vec{i} + \vec{j} - 3\vec{k}$, calculate:

$$\vec{u} \cdot \vec{v} =$$

$$\vec{u} \times \vec{v} =$$

2. True or false? Justify your answer: $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$.

3. Consider the three points $O(0, 0, 0)$, $A(1, 0, 0)$ and $B(0, 1, 0)$. Find the point $C(x, y, z)$ whose coordinates are all positive and such that: the angles satisfy

$$\angle AOC = \angle BOC = \pi/3$$

and the area of the triangle $\triangle AOC$ is equal to 1.