

THE UNIVERSITY OF MANITOBA

SN: _____

Faculty of Engineering

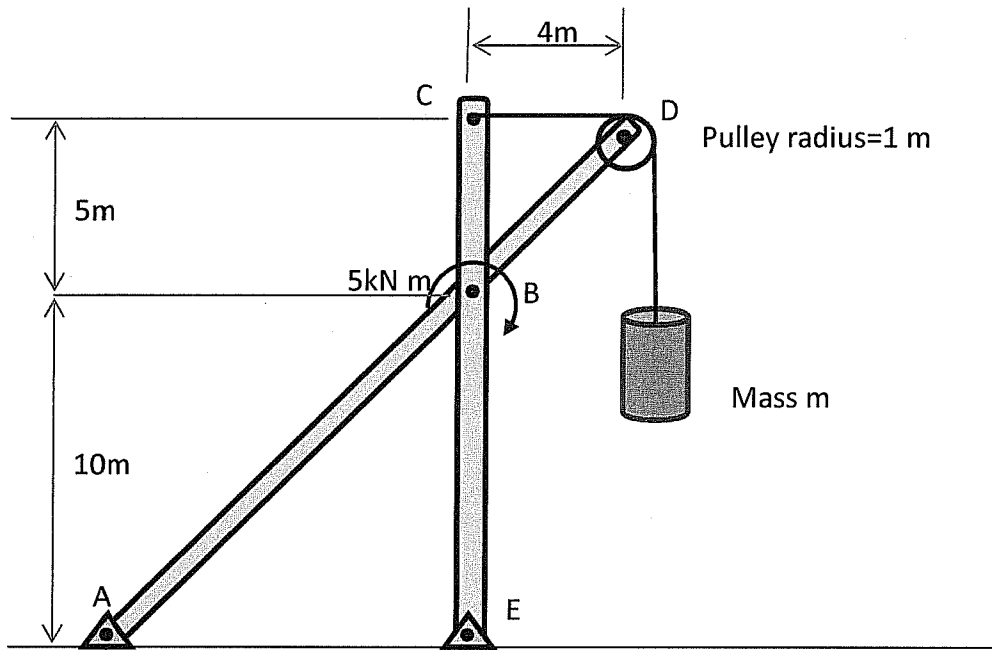
ENG 1440 Introduction to Statics

March 13, 2013

Term Test # 2 Time: 6:00 pm – 7:30 pm

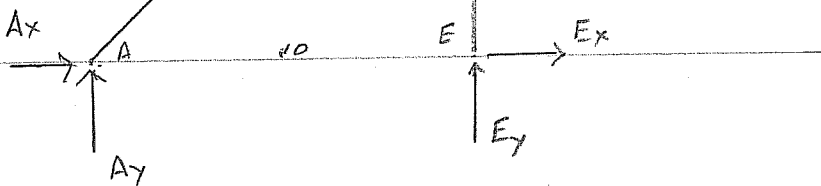
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$W = mg$

Forces in kN



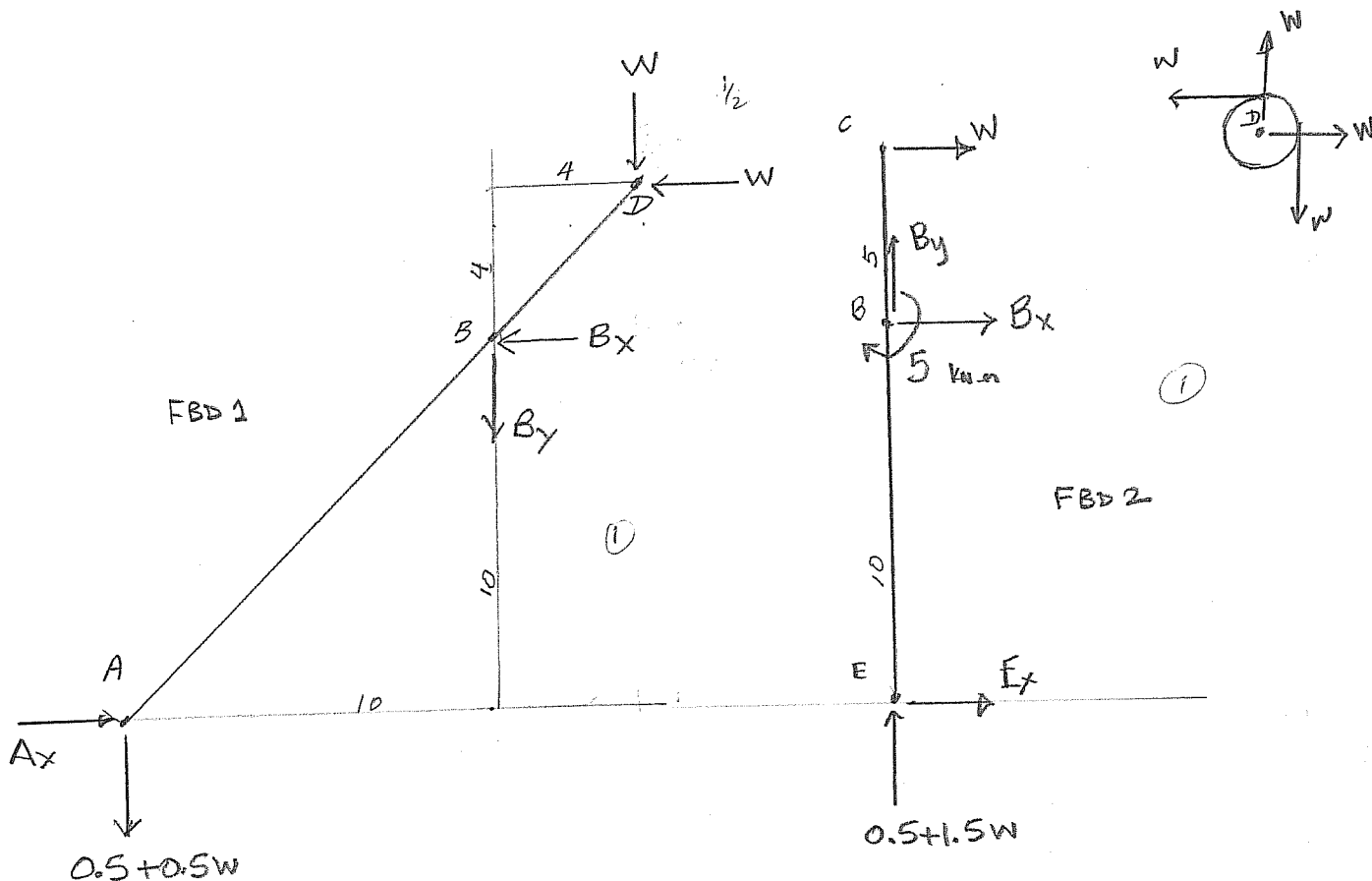
$$\begin{aligned} [\sum F_x = 0] \quad A_x + E_x &= 0 \\ [\sum F_y = 0] \quad A_y + E_y - W &= 0 \end{aligned}$$

$$A_x = -E_x \quad (1)$$

$$A_y + E_y = W \quad (2)$$

$$[\sum M_A = 0] \quad 10E_y - 5 - 15W = 0 \quad E_y = \frac{5 + 15W}{10} = 0.5 + 1.5W \quad (3)$$

$$\therefore A_y = -(0.5 + 0.5W)$$



(Forces in kN)

$$[\sum F_x = 0] \quad A_x - B_x - W = 0 \quad (4)$$

$$A_x - B_x = W$$

$$[\sum F_y = 0] \quad -(0.5 + 0.5W) - B_y - W = 0 \quad (5)$$

$$B_y = -0.5 - 1.5W$$

$$[\sum M_B = 0] \quad 10A_x + 10(0.5 + 0.5W) + 4W - 4W = 0$$

$$A_x = -0.5 - 0.5W \quad (6)$$

From (4) $B_x = A_x - W = -0.5 - 0.5W - W$

$$= -0.5 - 1.5W$$

Force on pin at B.

$$B_x = -0.5 - 1.5W$$

$$B_y = -0.5 - 1.5W$$

$$\begin{aligned} \text{Resultant} &= \sqrt{B_x^2 + B_y^2} \\ &= (0.5 + 1.5W)\sqrt{2} \end{aligned}$$

$$\text{Max. capacity} = 20000 \text{ N} = 20 \text{ kN}$$

$$20 = (0.5 + 1.5W)\sqrt{2}$$

$$W = 9.095 \text{ kN}$$

$$m = \frac{W}{g} = \frac{9095}{9.8} = 928 \text{ kg} \quad \blacktriangleleft$$

Check accuracy of forces at B.

$$\text{From Eq. 1} \quad A_x = -E_x \quad \therefore E_x = -(-0.5 - 0.5W) = 0.5 + 0.5W$$

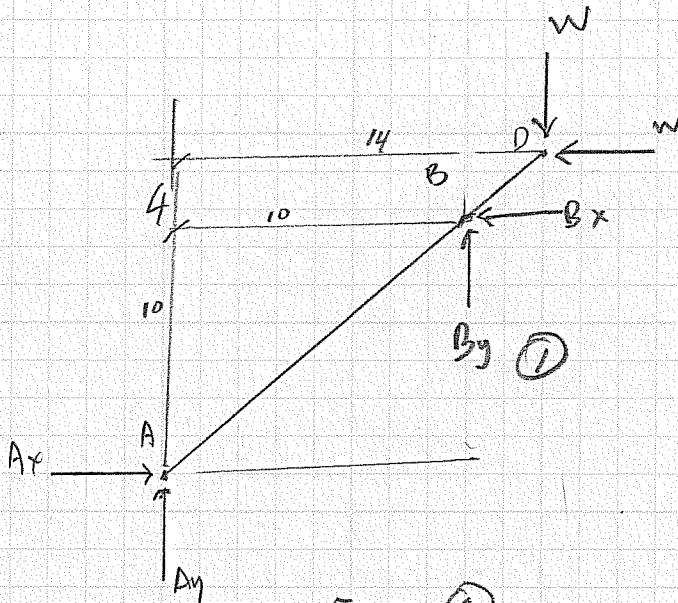
From FBD (2) :

$$\sum F_x = W + B_x + E_x = W - 0.5 - 1.5W + 0.5 + 0.5W = 0 \quad \checkmark$$

$$\sum F_y = B_y + 0.5 + 1.5W = -0.5 - 1.5W + 0.5 + 1.5W = 0 \quad \checkmark$$

$$\sum M_E = -15W - 10B_x - 5 = -15W - 10(-0.5 - 1.5W) - 5 = 0 \quad \checkmark$$

All check

Alternate Solution

From ①

$$(\sum M_B = 0) \quad -10A_y + 10A_x - 4W + 4W = 0$$

$$A_x = A_y$$

(1)

$$(\sum F_x = 0) \quad A_x - B_x - W = 0 \quad A_x - B_x = W \quad (2)$$

$$[\sum F_y = 0] \quad A_y + B_y - W = 0 \quad A_y + B_y = W \quad (3)$$

$$A_x - B_x = A_y + B_y$$

$$\text{Since } A_x = A_y, \quad B_x = -B_y$$

$$\text{from ②} \quad (\sum M_E = 0) \quad -5000 - 10B_x - 15N = 0$$

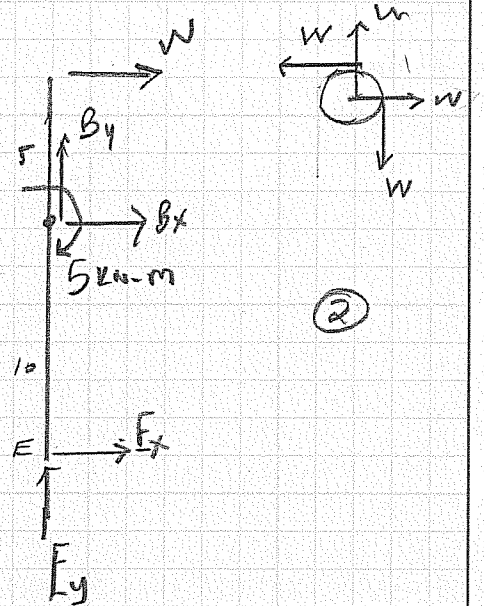
$$B_x = -\frac{5000 - 15W}{10}$$

$$= -500 - 1.5W$$

$$B = \sqrt{B_x^2 + B_y^2} = |B_x| \sqrt{2} = (500 + 1.5W) \sqrt{2} = 20000$$

$$W = 9095 \text{ N}$$

$$m = 928 \text{ kg}$$



(FBD 2)

$$(\sum M_E = 0) \quad -10B_x - 5 - 15W = 0$$

$$10B_x = -5 - 15W$$

$$B_x = -0.5 - 1.5W$$

 $(\sum F_y = 0)$

$$0.5 + 1.5W + B_y = 0$$

$$B_y = -0.5 - 1.5W$$

$$B_x = B_y$$

$$20000 = \sqrt{B_x^2 + B_y^2} = (0.5 + 1.5W) \sqrt{2}$$

$$W = 9.095 \text{ kN}$$

$$m = 928 \text{ kg}$$

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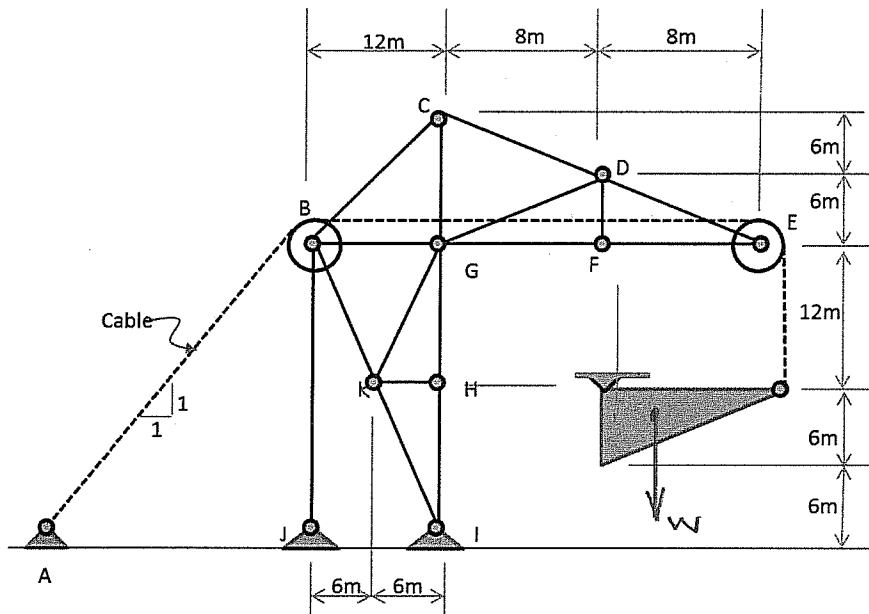
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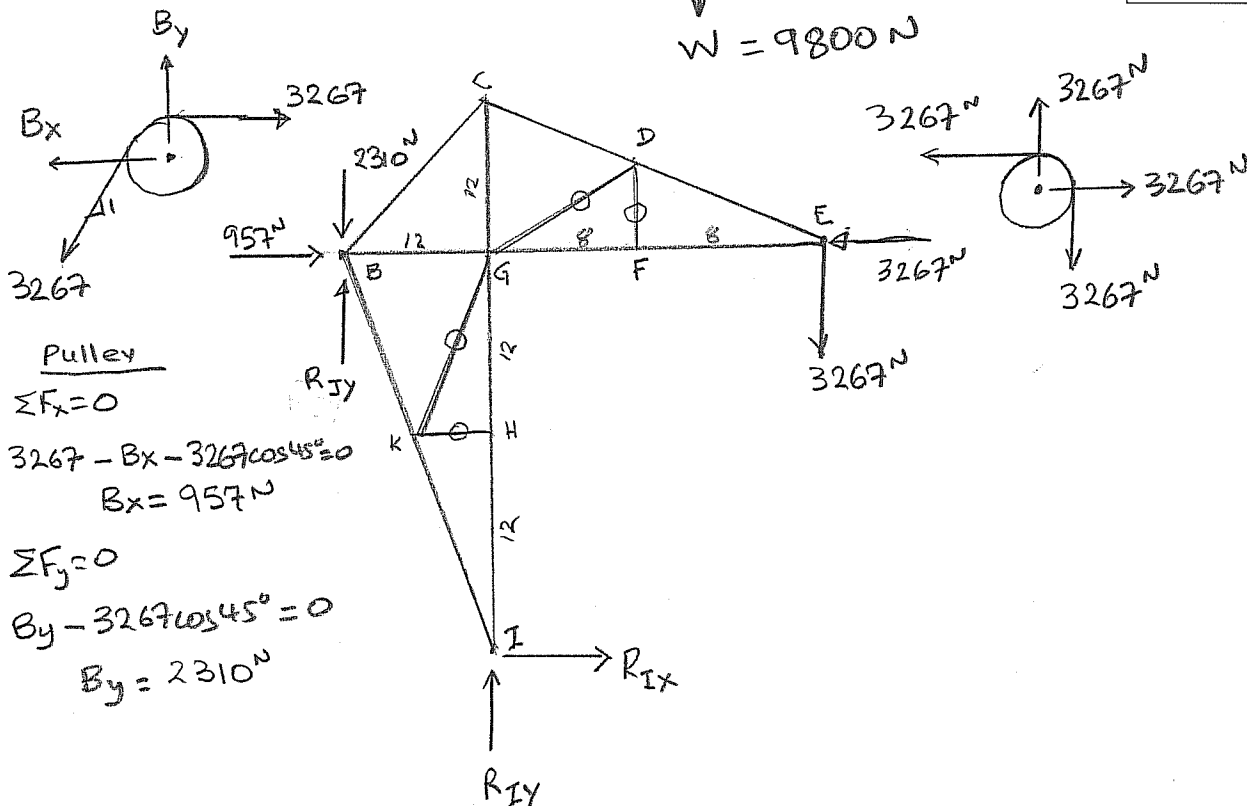


Truss Summary of the results	
Member	Force
JB	2574 C
BC	6160 T
CD	5445 T
DE	5445 T
EF	7623 C
FD	0
FG	7623 C
GC	7623 C
GD	0
GB	7623 C
GH	7623 C
HK	0
HI	7623 C
IK	5165 T
KB	5165 T
KG	0

$$\frac{2}{3}(9800) = 6533 \text{ N}$$

$$\frac{1}{3}(9800) = 3267 \text{ N}$$

$$W = 9800 \text{ N}$$



$$[\Sigma F_x = 0] \quad 957 + R_{Ix} - 3267 = 0 \quad \boxed{R_{Ix} = 2310^N} \quad (1)$$

$$[\Sigma F_y = 0] \quad -2310 + R_{Jy} + R_{Iy} - 3267 = 0$$

$$R_{Jy} + R_{Iy} = 5577 \quad (2)$$

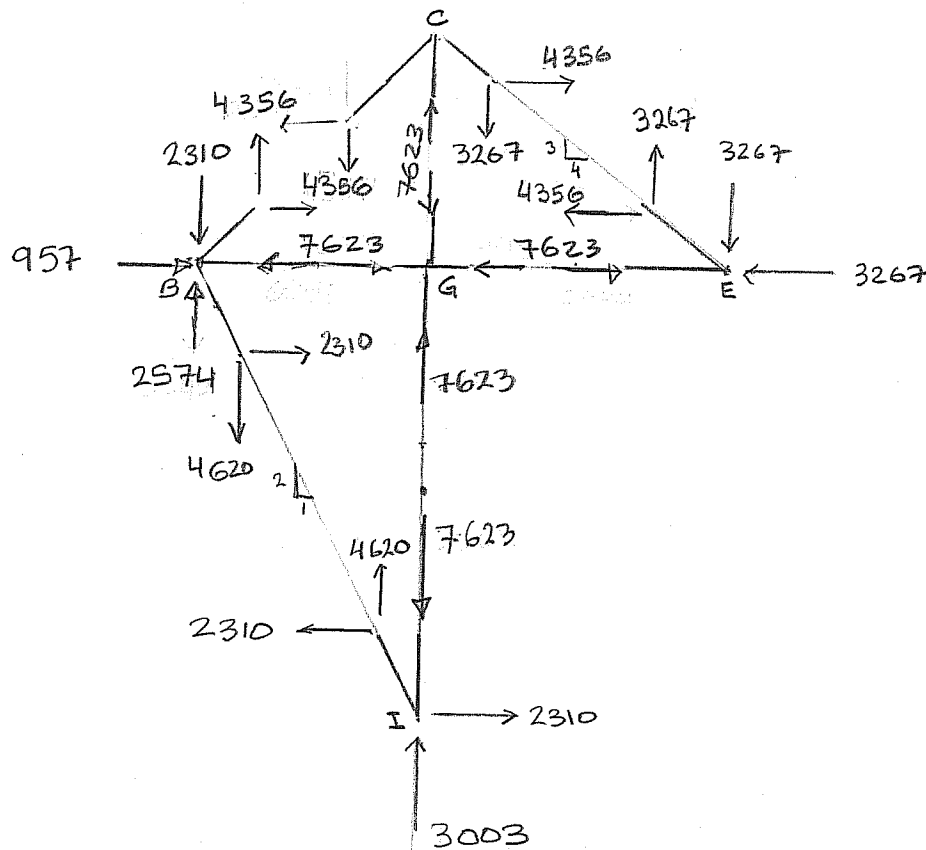
$$[\Sigma M_I = 0] \quad -12 R_{Jy} + 12(2310) - 24(957) - 16(3267) + 24(3267) = 0$$

$$-12 R_{Jy} + 30828 = 0$$

$$\boxed{R_{Jy} = 2574 N} \quad (3)$$

From (2)

$$\boxed{R_{Iy} = 3003 N} \quad (4)$$



(All forces in N)