

ENG 1440

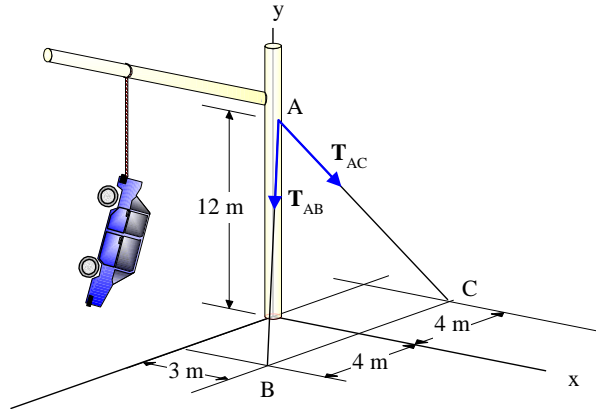
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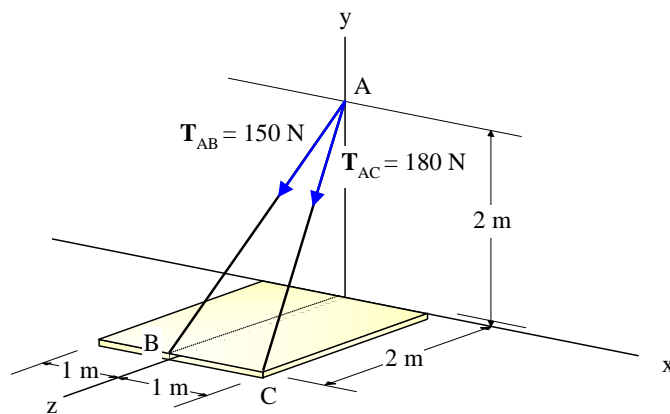
Lab #8. Solution

1. Two cables AB and AC secure the post. The cables are pre-stressed so that the forces exerted by the cables on the post are $T_{AB} = 1200 \text{ N}$ and $T_{AC} = 1800 \text{ N}$. Determine

- The magnitude of the resultant force $\mathbf{R} = \mathbf{T}_{AB} + \mathbf{T}_{AC}$ and,
- The angle \mathbf{R} makes with the coordinate axes.



2. A trap door is held by ropes as shown in the Figure. If the cables exert forces T_{AB} and T_{AC} on the wall at A, determine the magnitude of the resultant force \mathbf{R} acting at A and the angles it makes with the coordinate axes.



1)

$$\vec{T}_{AB} = T_{AB} \vec{\lambda}_{AB} = 1200 \vec{\lambda}_{AB}$$

$$\begin{aligned} A(0, 12, 0) \quad \vec{\lambda}_{AB} &= \frac{\vec{AB}}{AB} \quad \vec{AB} = 3\hat{i} - 12\hat{j} + 4\hat{k} \\ B(3, 0, 4) \\ C(3, 0, -4) \quad AB &= \sqrt{(3)^2 + (-12)^2 + 4^2} = 13 \end{aligned}$$

$$\vec{\lambda}_{AB} = \frac{3}{13}\hat{i} - \frac{12}{13}\hat{j} + \frac{4}{13}\hat{k}$$

$$\vec{T}_{AB} = 1200 \left(\frac{3}{13}\hat{i} - \frac{12}{13}\hat{j} + \frac{4}{13}\hat{k} \right) = 276.92\hat{i} - 1107.69\hat{j} + 369.23\hat{k}$$

$$\vec{T}_{AC} = T_{AC} \vec{\lambda}_{AC} \quad \vec{\lambda}_{AC} = \frac{\vec{AC}}{AC} \quad \vec{AC} = 3\hat{i} - 12\hat{j} - 4\hat{k}$$

$$AC = \sqrt{(3)^2 + (-12)^2 + (-4)^2} = 13$$

$$\vec{\lambda}_{AC} = \frac{3}{13}\hat{i} - \frac{12}{13}\hat{j} - \frac{4}{13}\hat{k}$$

$$\vec{T}_{AC} = 1800 \left(\frac{3}{13}\hat{i} - \frac{12}{13}\hat{j} - \frac{4}{13}\hat{k} \right)$$

$$415.38\hat{i} - 1661.54\hat{j} - 553.85\hat{k}$$

$$\vec{R} = \vec{T}_{AB} + \vec{T}_{AC} = (276.92 + 415.38)\hat{i} + (-1107.69 - 1661.54)\hat{j} + (369.23 - 553.85)\hat{k}$$

$$\vec{R} = 692.3\hat{i} - 2769.23\hat{j} - 184.62\hat{k} \quad N$$

$$R = \sqrt{692.3^2 + (-2769.23)^2 + (-184.62)^2} = 2860.42 \, N$$

$$\cos \theta_x = \frac{R_x}{R} = \frac{692.3}{2860.42} \quad \theta_x = 76^\circ$$

$$\cos \theta_y = \frac{R_y}{R} = \frac{-2769.23}{2860.42} \quad \theta_y = 165.5^\circ$$

$$\cos \theta_z = \frac{R_z}{R} = \frac{-184.62}{2860.42} \quad \theta_z = 93.7^\circ$$

2)

$$\begin{aligned} A(0, 2, 0) \\ B(0, 0, 2) \\ C(1, 0, 2) \end{aligned}$$

$$\vec{T}_{AB} = T_{AB} \vec{\lambda}_{AB} = 150 \vec{\lambda}_{AB}$$

$$\vec{\lambda}_{AB} = \frac{\vec{AB}}{AB} \quad \vec{AB} = 0\hat{i} - 2\hat{j} + 2\hat{k} \\ AB = \sqrt{(-2)^2 + (2)^2} = \sqrt{8}$$

$$\vec{\lambda}_{AB} = \frac{-2\hat{j} + 2\hat{k}}{\sqrt{8}} = \frac{-\hat{j} + \hat{k}}{\sqrt{2}}$$

$$\vec{T}_{AB} = 150 \left(\frac{-\hat{j} + \hat{k}}{\sqrt{2}} \right) = -106.07\hat{j} + 106.07\hat{k} \text{ N}$$

$$\vec{T}_{AC} = T_{AC} \vec{\lambda}_{AC} = 180 \vec{\lambda}_{AC}$$

$$\vec{\lambda}_{AC} = \frac{\vec{AC}}{AC} \quad \vec{AC} = 1\hat{i} - 2\hat{j} + 2\hat{k} \\ AC = \sqrt{(1)^2 + (-2)^2 + (2)^2} = 3$$

$$\vec{\lambda}_{AC} = \frac{1}{3}\hat{i} - \frac{2}{3}\hat{j} + \frac{2}{3}\hat{k}$$

$$\vec{T}_{AC} = 180 \left(\frac{1}{3}\hat{i} - \frac{2}{3}\hat{j} + \frac{2}{3}\hat{k} \right) = 60\hat{i} - 120\hat{j} + 120\hat{k} \text{ N}$$

$$\begin{aligned} \vec{R}_A &= \vec{T}_{AB} + \vec{T}_{AC} = 60\hat{i} + (-106.07 - 120)\hat{j} + (106.07 + 120)\hat{k} \\ &= 60\hat{i} - 226.07\hat{j} + 226.07\hat{k} \text{ N} \end{aligned}$$

$$R_A = \sqrt{(60)^2 + (-226.07)^2 + (226.07)^2} = 325.29 \text{ N}$$

$$\cos \theta_x = \frac{R_x}{R} = \frac{60}{325.29} \quad \theta_x = 79.37^\circ$$

$$\cos \theta_y = \frac{R_y}{R} = \frac{-226.07}{325.29} \quad \theta_y = 134.03^\circ$$

$$\cos \theta_z = \frac{R_z}{R} = \frac{226.07}{325.29} \quad \theta_z = 45.97^\circ$$