

CLASSICAL AND LINEAR ALGEBRA
MATH 1210 (WINTER 2011) TUTORIAL 4

Q1. Find *all* the solutions to the following equation. Write your answer in exponential form, graphically illustrating these solutions in the complex plane:

$$x^6 + 3\sqrt{2}(1+i) = 0$$

Q2. Solve the following equation and express your answer in polar form.

$$z^4 i = -2 - 2i.$$

Q3. Use DeMoivre's theorem, written in the form

$$(e^{\theta i})^n = e^{n\theta i},$$

to prove the identities:

$$\sin(4\theta) = 4 \cos^3 \theta \sin \theta - 4 \cos \theta \sin^3 \theta, \quad \cos(4\theta) = \cos^4 \theta - 6 \cos^2 \theta \sin^2 \theta + \sin^4 \theta.$$