MATH 2130 Summer Evening 2013 Problem Workshop 5

- 1. Find the maximum and minimum values of the function $f(x,y) = x^2 y^2$ or the region $x^2 + y^2 \le 1$.
- 2. Find the maximum value of the function f(x,y) = xy(3-x-2y) on the triangle R bounded by the positive axes and the line x + y = 1.
- 3. Find the maximum value of the function $f(x,y) = x^2 y^2 + 2x + \frac{9y}{2}$ on the region R bounded by $x = 1 y^2, x = 0$.
- 4. Evaluate the double iterated integral

$$\int_{-2}^{0} \int_{0}^{-x} \sqrt{y-x} dy dx.$$

- 5. Evaluate the double integral of $f(x,y) = x^3y^3 3xy^2 + y$ over the region bounded by the curves $y = -x^2, y = x^2 1$.
- 6. Evaluate the double iterated integral

$$\int_{-2}^{0} \int_{-3x}^{6} e^{y^2} dy dx.$$

7. Evaluate the double integral

$$\iint_{R} \frac{1}{y-1} dy dx$$

where R is the region bounded by the curves y = 2x, y = x, x = 2, x = 3.

8. Find the volumes of the solids of revolution when the area bounded by the curves

$$y = 2x - x^2, \qquad y = x$$

is rotated about the lines (a)x = 3 (b)y = 1 (c)x + y = -1.

9. A triangular plate has sides with lengths 3,4 and 5 metres. It is submerged vertically in oil with density 950 kilogrms per cubic metre. The side of length 3 metres is vertical, the side of length 4 is horizontal and the uppermost vertex is 1 metre below the surface of the oil. Find the force due to oil pressure on each side of the plate.

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Answers:

- 1. 1, -1
- 2. $2/3(\sqrt{3})$
- 3.65/16
- 4. $16(4-\sqrt{2})/15$
- 5. $-\sqrt{2}/3$
- 6. $(e^{36} 1)/6$
- 7. $(5/2) \ln 5 (3/2) \ln 3 2 \ln 2$
- 8. (a) $5\pi/6$, (b) $2\pi/15$ (c) $7\sqrt{2}\pi/20$
- $9.\ \, 1.68\times 10^5N$