MATH 2132 Problem Workshop 6

1. Compute the Laplace transforms of the following functions. For part (a) use the definition. For the others, you can use the table

(a)
$$f(t) = e^{-2t} \cos 4t$$

(b)
$$f(t) = e^{-2t} \cos 4th(t-3)$$

(c)
$$f(t) = \begin{cases} 2t - 5 & 0 \le t < 4 \\ t^2 & 4 \le t < 8 \\ 1 & t > 8 \end{cases}$$

(d)
$$f(t) = t^2 - 2t + 3$$
, $0 \le t < 2$ $f(t+2) = f(t)$

2. Compute the inverse Laplace Transform for the following functions.

(a)
$$F(s) = \frac{s^2 + 3}{s^3 + 2s^2 + s}$$

(b)
$$F(s) = \frac{e^{-s}(1 + e^{-2s})}{s^2 - s}$$

(c)
$$F(s) = \frac{1}{e^{2s}(s^3 + 2s^2 + 6s)}$$

3. Is it possible for $F(s) = \frac{s(s^2 + 3s - 6)}{4s^3 - 3s + 10}$ to be the Laplace transform for a piecewise continuous function of exponential order.