

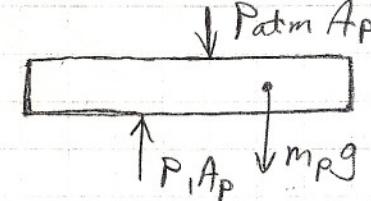
#1.

Water,  $x_1 = 0.25$ ,  $m_p = 80.09 \text{ kg}$ ,  $D_p = 10 \text{ cm}$

$$P_{atm} = 100 \text{ kPa}$$

$$\sum F_y = 0: P_{atm} A_p + m_p g = P_i A_p$$

$$(a) A_p = \frac{\pi}{4} (0.1)^2 = 7.8539 \times 10^{-3} \text{ m}^2$$



$$P_i = P_{atm} + \frac{m_p g}{A_p} = 100 + \frac{80.09 \times 9.80665}{7.8539 \times 10^{-3}} \times \frac{1 \text{ [KN]}}{1000 \text{ [N]}}$$

$$P_i = 200.002 \text{ kPa}$$

[kPa]

For weight  
of piston

Table B.1.2 at  $P = 200 \text{ kPa}$ ,  $T_{sat.} = 120.23^\circ\text{C}$

$$v_f = 0.001061 \text{ m}^3/\text{kg}, v_{fg} = 0.88467 \text{ m}^3/\text{kg}$$

$$\therefore v_1 = v_f + x_1 v_{fg} = 0.001061 + 0.25 \times 0.88467$$

$$v_1 = 0.2222285 \text{ m}^3/\text{kg}$$

$$\text{initial volume: } V_1 = A_p \times h_1 = 7.8539 \times 10^{-3} \times 0.4 = 3.14159 \times 10^{-3} \text{ [m}^3]$$

$$\therefore M = \frac{V_1}{v_1} = \frac{3.14159 \times 10^{-3}}{0.2222285} = 1.41367 \times 10^{-2} \text{ [kg]}$$

(b)

Pressure is constant while piston travels,  $\therefore P = 200 \text{ kPa}$   
 $P < 400 \text{ kPa}$  (Final pressure)  $\therefore$  piston hits stops before the final pressure is reached.

Let state 2 be when the piston just reaches the stops.

$$\therefore P_2 = P_i = 200 \text{ kPa}, \text{ new volume: } V_2 = A_p h_2 = 7.8539 \times 10^{-3} \times 1.81$$

$$V_2 = 0.0142155 \text{ m}^3$$

$$\therefore v_2 = \frac{V_2}{m} = \frac{0.0142155}{1.41367 \times 10^{-2}}$$

$$v_2 = 1.005574 \text{ m}^3/\text{kg}$$

At  $P = 200 \text{ kPa}$ ,  $v_2 > v_g \therefore$  state 2 is superheated vapor.

Table B.1.3

	$T$	$v$
150	0.95964	
$T_2$	1.005574	
200	1.08034	

$\therefore$  by interpolation,

$$T_2 = 169.03^\circ\text{C}$$

#1 (C) Final state:  $P_3 = 400 \text{ kPa}$ ,  $v_3 = v_2 = 1.005574 \text{ m}^3/\text{kg}$ .

At 400 kPa,  $v_3 > v_g$  ∴ state is superheated vapor.

Table B.1.3,  $v_3 \approx 1.00555 \text{ m}^3/\text{kg}$  which is a table entry corresponding to  $T_3 = 600^\circ\text{C}$

(d) Work done only during process 1-2

$$W_2 = P(v_2 - v_1) = mP(v_2 - v_1)$$

$$= 1.41367 \times 10^{-2} \times 200 \times (1.005574 - 0.2222285)$$

$$W_2 = 2.21478 \text{ [kJ]}$$

(e) First law:  $Q_{\text{c.m.}} - W_{\text{c.m.}} = m(u_3 - u_1) + \Delta KE + \Delta PE$

$u_1 = u_f + x, u_{fg}$ , Table B.1.2 at 200 kPa,  $u_f = 504.47 \text{ kJ/kg}$

$$\therefore u_1 = 504.47 + 0.25 \times 2025.02 \quad u_{fg} = 2025.02 \text{ kJ/kg}$$

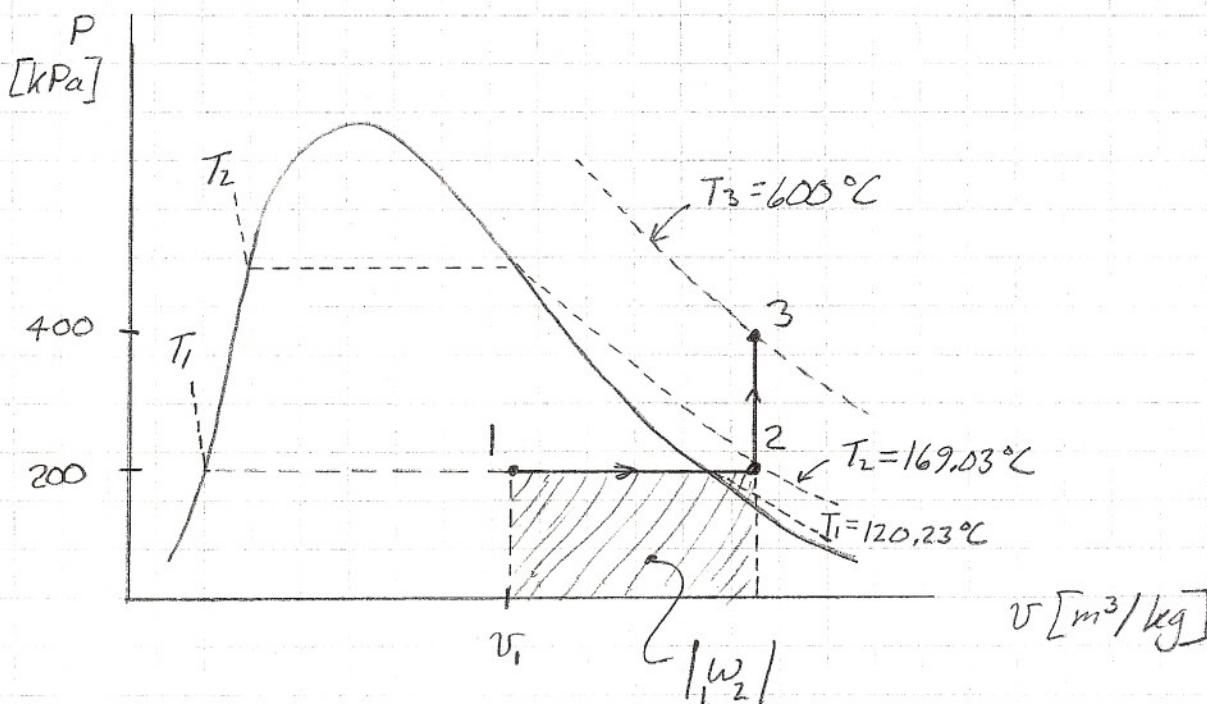
$$u_1 = 1010.725 \text{ kJ/kg}$$

$u_3$ : Table B.1.3, at 400 kPa,  $600^\circ\text{C}$ ,  $u_3 = 3300.22 \text{ kJ/kg}$

$$Q_3 = 2.21478 + 1.41367 \times 10^{-2} \times (3300.22 - 1010.725)$$

$$Q_3 = 34.580 \text{ [kJ]}$$

(f)



2-1  
4#2. (a) First law for the condenser: ( $\Delta p_e = 0, \Delta h_e = 0$ )

$$\dot{Q}_{cv}^o - \dot{W}_{cv}^o = \sum (\dot{m}h)_{out} - \sum (\dot{m}h)_{in}$$

$$0 = \dot{m}_4 h_4 + \dot{m}_2 h_2 - \dot{m}_3 h_3 - \dot{m}_1 h_1$$

$$\dot{m}_4 = \dot{m}_3 = \dot{m}_W \quad \dot{m}_1 = \dot{m}_2 = \dot{m}_{cw}$$

$$0 = \dot{m}_W (h_4 - h_3) + \dot{m}_{cw} (h_2 - h_1)$$

$$\dot{m}_W = \dot{m}_{cw} \frac{(h_2 - h_1)}{(h_3 - h_4)}$$

$$\dot{m}_W = 1750 \frac{(146.66 - 62.98)}{(2345.35 - 191.81)}$$

$$\dot{m}_W = 68.00 \text{ [kg/s]} \quad \leftarrow$$

$$T_1 < T_{sat}(P_1) \Rightarrow \text{compressed liquid}$$

$$h_1 = h_f \Big|_{15^\circ C} = 62.98 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

$$T_2 < T_{sat}(P_2) \Rightarrow \text{compressed liquid}$$

$$h_2 = h_f \Big|_{35^\circ C} = 146.66$$

$$h_3 = (1-x_3) h_f + x_3 h_g$$

$$h_f \Big|_{10 \text{ kPa}} = 191.81 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

$$h_g \Big|_{10 \text{ kPa}} = 2584.63 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

$$h_3 = (1-0.9) 191.81 + (0.9) 2584.63$$

$$h_3 = 2345.35 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

$$h_4 = h_f \Big|_{P_4} = 191.81 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

(b) First law for the steam turbine ( $\Delta p_e = 0, \Delta h_e = 0$ )

$$\dot{Q}_{cv} - \dot{W}_{T1} = \dot{m}_W (h_3 - h_7)$$

$$h_7 = h \Big|_{\substack{10 \text{ MPa} \\ 550^\circ C}} = 3500.92 \left( \frac{\text{kJ}}{\text{kg}} \right)$$

Table B.1.3

$$\dot{W}_{T1} = -\dot{m}_W (h_3 - h_7)$$

$$\dot{W}_{T1} = -68.00 (2345.35 - 3500.92)$$

$$\dot{W}_{T1} = 78579 \text{ [kW]} = 78.579 \text{ [MW]}$$

2(c) Must first compute  $\dot{m}_H$  in order to be able to do the gas turbine analysis.  
First law for the heat exchanger ( $\dot{m}_e = 0$ ,  $\dot{m}_w = 0$ )

$$\dot{Q}_{cv} - \dot{W}_{cv} = \sum (\dot{m} h)_{out} - \sum (\dot{m} h)_{in}$$

$$0 = \dot{m}_g h_g + \dot{m}_6 h_6 - \dot{m}_8 h_8 - \dot{m}_5 h_5$$

$$\dot{m}_g = \dot{m}_8 = \dot{m}_H \quad \dot{m}_6 = \dot{m}_5 = \dot{m}_w$$

$$0 = \dot{m}_H (h_g - h_8) + \dot{m}_w (h_6 - h_5)$$

$$\dot{m}_H = \dot{m}_w \frac{(h_6 - h_5)}{(h_8 - h_g)}$$

$$h_6 = h_g \Big|_{10 \text{ MPa}} = 2724.67 \left[ \frac{\text{kJ}}{\text{kg}} \right]$$

Table B.1.2

Helium is an ideal gas:

$$\Delta h = C_p \Delta T$$

$$(h_8 - h_g) = C_p (T_8 - T_g)$$

$$C_p = 5.193 \left[ \frac{\text{kJ}}{\text{kg K}} \right] \text{ for Helium} \quad (\text{Table A.5})$$

$$\dot{m}_H = \dot{m}_w \frac{(h_6 - h_5)}{C_p (T_8 - T_g)}$$

$$= \frac{68.00 (2724.67 - 207.53)}{5.193 (395 - 80)}$$

$$\dot{m}_H = 104.64 \left[ \frac{\text{kg}}{\text{s}} \right]$$

$T_5 < T_{\text{sat}}(P_5) \Rightarrow \text{compressed liquid}$

$P_5 > 500 \text{ kPa} \rightarrow \text{use Table B.1.4}$

$T [{}^{\circ}\text{C}]$	$h [\text{kJ/kg}]$
40	176.36
47.5	$h_5$
60	259.47

$$h_5 = 176.36 + \frac{(47.5 - 40)}{(60 - 40)} (259.47 - 176.36)$$

$$h_5 = 207.53 \left[ \frac{\text{kJ}}{\text{kg}} \right]$$

To get the net work from the gas turbine, the work input to the compressor is needed.

First Law for the Compressor ( $\dot{m}_e = 0$ ,  $\dot{m}_w = 0$ ,  $\dot{W}_c \text{ in}$ )

$$\dot{Q}_{cv} + \dot{W}_c = \dot{m}_H (h_{10} - h_g) = \dot{m}_H C_p (T_{10} - T_g)$$

$$\dot{W}_c = (104.64) 5.193 (407 - 80) = 177690 \text{ (kW)} = 177.69 \text{ (MW)}$$

2(c) continued

2-3/4

First law for the gas turbine ( $\dot{m}_{\text{pe}} = 0$ ,  $\dot{m}_{\text{ke}} = 0$ )

$$\dot{Q}_{cv}^{\circ} - \dot{W}_{T2,\text{total}} = \dot{m}_H (h_8 - h_{11}) = \dot{m}_H C_p (T_8 - T_{11})$$

$$\dot{W}_{T2,\text{total}} = -\dot{m}_H C_p (T_8 - T_{11}) = -(104.64)(5.193)(395 - 760)$$

$$\dot{W}_{T2,\text{total}} = 198,339 \text{ (kW)} = 198.34 \text{ (MW)}$$

$$\dot{W}_{T2,\text{net}} = \dot{W}_{T2,\text{total}} - \dot{W}_c = 198.34 - 177.69 = 20.65 \text{ [MW]} \leftarrow$$

$$(d) \text{ Thermal efficiency } \eta_{th} = \frac{\text{Net work output}}{\text{Heat input}} = \frac{\dot{W}_{T2,\text{net}} - \dot{W}_p}{\dot{Q}_S + \dot{Q}_R}$$

First law for the pump ( $\dot{m}_{\text{ke}} = 0$ ,  $\dot{m}_{\text{pe}} = 0$ ,  $\dot{W}_p \underline{\text{in}}$ )

$$\dot{Q}_{cv}^{\circ} + \dot{W}_p = \dot{m}_W (h_5 - h_4) = 68.00 (207.53 - 191.81)$$

$$\dot{W}_p = 1069 \text{ (kW)} = 1.069 \text{ (MW)}$$

First law for the superheater ( $\dot{m}_{\text{pe}} = 0$ ,  $\dot{m}_{\text{ke}} = 0$ )

$$\dot{Q}_S - \dot{W}_{cv}^{\circ} = \dot{m}_W (h_7 - h_6) = 68.00 (3500.92 - 2724.67)$$

$$\dot{Q}_S = 52785 \text{ (kW)} = 52.785 \text{ (MW)}$$

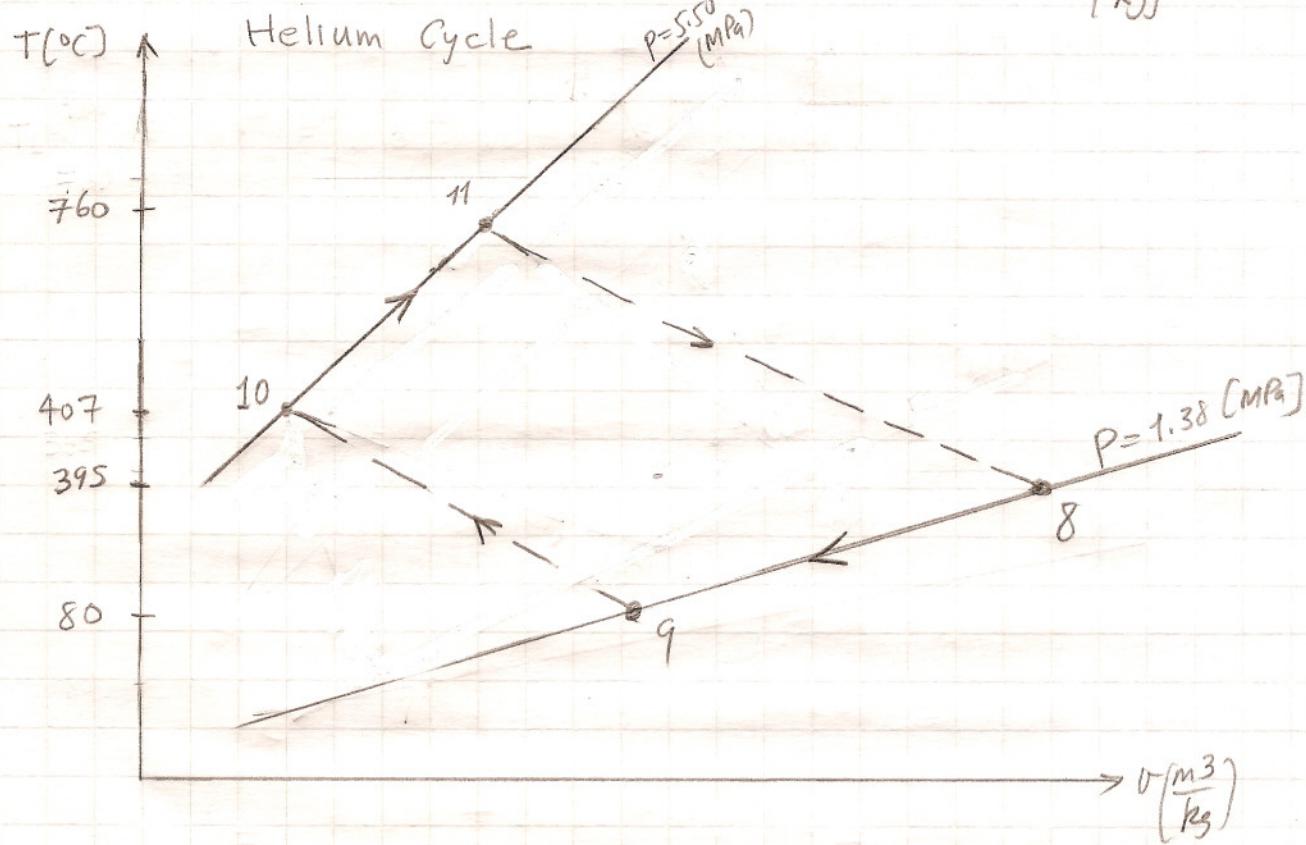
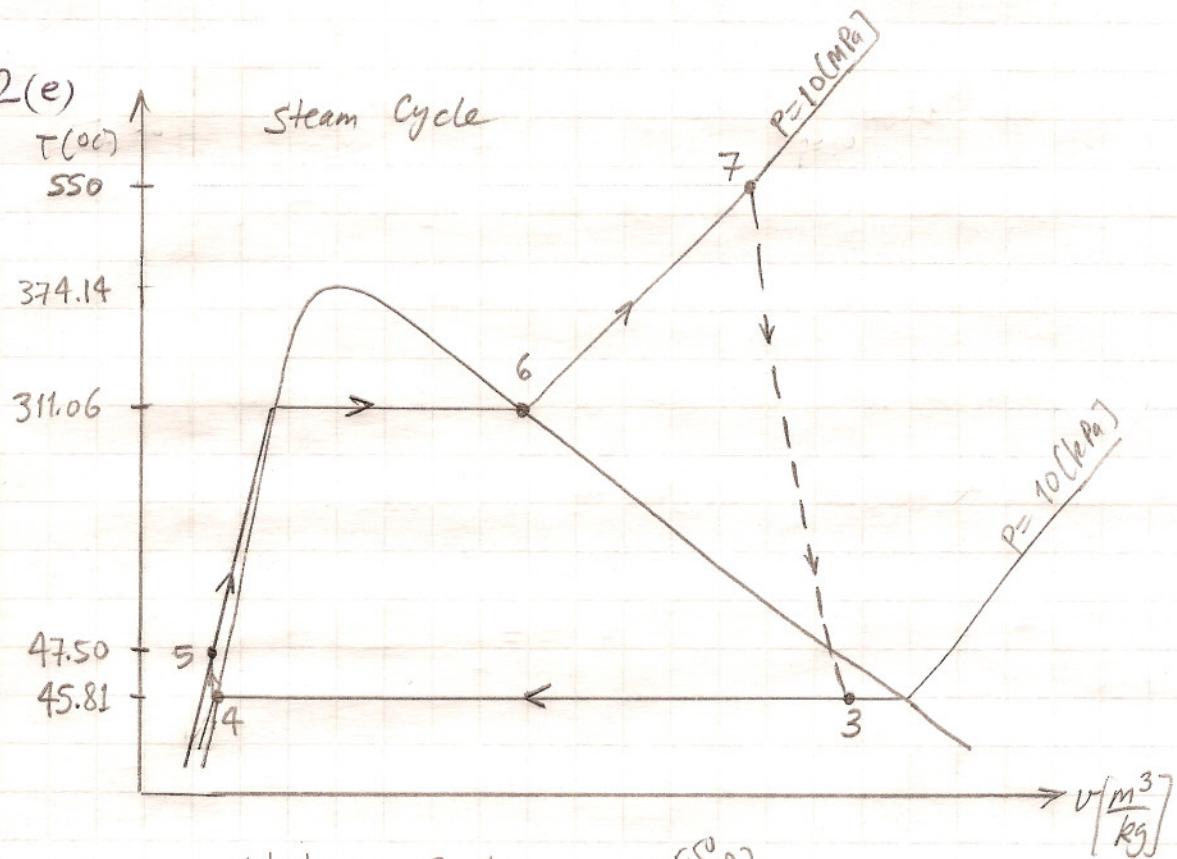
First Law for the heater ( $\dot{m}_{\text{pe}} = 0$ ,  $\dot{m}_{\text{ke}} = 0$ )

$$\dot{Q}_R - \dot{W}_{cv}^{\circ} = \dot{m}_H (h_{11} - h_{10}) = \dot{m}_H C_p (T_4 - T_{10})$$

$$\dot{Q}_R = 104.64 (5.193) (760 - 407) = 191819 \text{ (kW)} = 191.82 \text{ (MW)}$$

$$\eta_{th} = \frac{78.579 + 20.65 - 1.069}{52.785 + 191.82} = \frac{98.16}{244.61} = 0.401 = \underline{40.1\%}$$

2(e)



#3.

ideal gases, air & CO<sub>2</sub> Table A.5 R<sub>air</sub> = 0.287 kJ/kg·K

R<sub>CO<sub>2</sub></sub> = 0.1889 kJ/kg·K

Initial states:

Air m<sub>air</sub> = 1.5 kg PV = mRT

P<sub>air,1</sub> = 500 kPa ∴ V<sub>air,1</sub> =  $\frac{1.5 \times 0.287 \times 350}{500} = 0.30135 \text{ m}^3$

T<sub>air,1</sub> = 350 K

CO<sub>2</sub> m<sub>CO<sub>2</sub></sub> = 4 kg

P<sub>CO<sub>2</sub>,1</sub> = 200 kPa ∴ V<sub>CO<sub>2</sub>,1</sub> =  $\frac{4 \times 0.1889 \times 478}{200} = 1.80588 \text{ m}^3$

T<sub>CO<sub>2</sub>,1</sub> = 478 K

Total volume in chamber = V<sub>air,1</sub> + V<sub>CO<sub>2</sub>,1</sub> = 0.30135 + 1.80588

V<sub>tot</sub> = 2.10723 m<sup>3</sup>

(a)

Final state corresponds to equilibrium, when T<sub>air,2</sub> = T<sub>CO<sub>2</sub>,2</sub>

and P<sub>air,2</sub> = P<sub>CO<sub>2</sub>,2</sub>

Apply First law to the whole chamber:

Q<sub>2 - 1</sub> = U<sub>2</sub> - U<sub>1</sub> + ΔKE + ΔPE

insulated ↳ no boundary work = rigid container.

∴ Q = U<sub>2</sub> - U<sub>1</sub>, i.e., Q = (m<sub>air</sub>U<sub>air,2</sub> + m<sub>CO<sub>2</sub></sub>U<sub>CO<sub>2</sub>,2</sub>) - (m<sub>air</sub>U<sub>air,1</sub> + m<sub>CO<sub>2</sub></sub>U<sub>CO<sub>2</sub>,1</sub>)

∴ Q = m<sub>air</sub>(U<sub>air,2</sub> - U<sub>air,1</sub>) + m<sub>CO<sub>2</sub></sub>(U<sub>CO<sub>2</sub>,2</sub> - U<sub>CO<sub>2</sub>,1</sub>)

(Total mass remains the same: m<sub>air</sub> + m<sub>CO<sub>2</sub></sub> = m<sub>tot</sub>)

Q = m<sub>air</sub>C<sub>v0,air</sub>(T<sub>2</sub> - T<sub>air,1</sub>) + m<sub>CO<sub>2</sub></sub>C<sub>v0,CO<sub>2</sub></sub>(T<sub>2</sub> - T<sub>CO<sub>2</sub>,1</sub>)

Rearrange equation to isolate T<sub>2</sub>:

Table A.5:

T<sub>2</sub> =  $\frac{m_{air}C_{v0,air}T_{air,1} + m_{CO_2}C_{v0,CO_2}T_{CO_2,1}}{m_{air}C_{v0,air} + m_{CO_2}C_{v0,CO_2}}$

C<sub>v0,air</sub> = 0.717  $\frac{\text{kJ}}{\text{kg}\cdot\text{K}}$

C<sub>v0,CO<sub>2</sub></sub> = 0.653  $\frac{\text{kJ}}{\text{kg}\cdot\text{K}}$

T<sub>2</sub> =  $\frac{1.5 \times 0.717 \times 350 + 4 \times 0.653 \times 478}{1.5 \times 0.717 + 4 \times 0.653}$

T<sub>2</sub> = 440.66 [K]

#3 (b) Total volume,  $V_{air} + V_{CO_2}$ , remains conserved  
(constant)  
during process.

$$V_{air,2} = \frac{M_{air} R_{air} T_2}{P_{air,2}}$$

$$V_{CO_2,2} = \frac{M_{CO_2} R_{CO_2} T_2}{P_{CO_2,2}}$$

Add equations:

$$V_{tot.} = \frac{M_{air} R_{air} T_2}{P_{air,2}} + \frac{M_{CO_2} R_{CO_2} T_2}{P_{CO_2,2}}$$

$\nwarrow$        $\nearrow$   
same

$$\therefore P_2 = \frac{(M_{air} R_{air} + M_{CO_2} R_{CO_2}) T_2}{V_{tot.}} = \frac{(1.5 \times 0.287 + 4 \times 0.1889) \times 440.66}{2.10723}$$

$$P_2 = 248.03 \text{ [kPa]}$$

Not required:

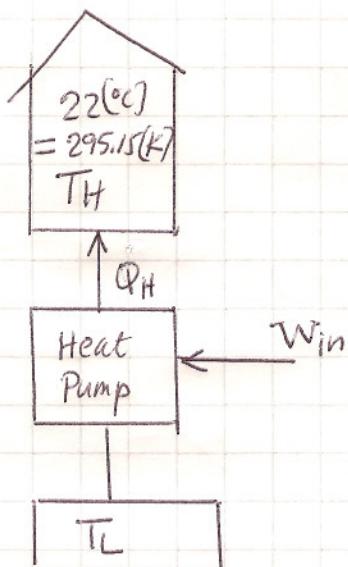
$$V_{2,air} = \frac{1.5 \times 0.287 \times 440.66}{248.03}$$

$$= 0.76483 \text{ [m}^3\text{]}$$

$$V_{2,CO_2} = \frac{4 \times 0.1889 \times 440.66}{248.03}$$

$$= 1.3424 \text{ [m}^3\text{]}$$

## 4. Heat Pump



$$T_H = 295.15 \text{ [K]}$$

Coefficient of performance  
for a heat pump

$$\beta^l = \beta_{HP} = \frac{Q_H}{W_{in}} = \frac{Q_H}{Q_H - Q_L}$$

To find the maximum  $\beta_{HP}$   
use a Carnot heat pump

$$\beta_{HP,rev} = \frac{T_H}{(T_H - T_L)}$$

$$(a) \quad T_L = 0(^\circ\text{C}) = 273.15 \text{ [K]}$$

$$\beta_{HP,rev} = \frac{295.15}{295.15 - 273.15} = 13.42 \leftarrow$$

$$(b) \quad T_L = -20 \text{ [ } ^\circ\text{C} \text{ ]} = 253.15 \text{ [K]}$$

$$\beta_{HP,rev} = \frac{295.15}{295.15 - 253.15} = 7.03 \leftarrow$$

5. Cooling to room temperature first:

$$Q_{\text{cool.}} = m c (T_{\text{room}} - T_{\text{fridge}})$$

Cooling directly from hot temperature:

$$Q_{\text{hot}} = m c (T_{\text{hot}} - T_{\text{fridge}})$$

$$\text{Energy savings } \Delta Q = (Q_{\text{hot}} - Q_{\text{cool}})$$

$$= m c (T_{\text{hot}} - T_{\text{fridge}}) - m c (T_{\text{room}} - T_{\text{fridge}})$$

$$\boxed{\Delta Q = m c (T_{\text{hot}} - T_{\text{room}})}$$

$$\Delta Q = 4.0 \text{ (kg)} \cdot 3.5 \left( \frac{\text{kJ}}{\text{kg K}} \right) (101 - 21) = 1120 \text{ (kJ)} \text{ per time}$$

$$\Delta Q_{\text{year}} = \Delta Q \text{ per time} * \text{Number of times per year}$$

$$= 1120 (156) = 174720 \text{ (kJ)} \text{ per year}$$

This is a savings in  $Q_L$  for the refrigerator.

$$\text{Because } \bar{W}_{\text{in}} = \frac{Q_L}{\beta} \quad \Delta \bar{W}_{\text{in}} = \frac{\Delta Q_L}{\beta} = \frac{174720}{1.2}$$

$$\Delta \bar{W}_{\text{in}} = 145600 \text{ (kJ)} \text{ per year saved in work input} \\ (\text{ie, electrical power input to the refrigerator motor})$$

$$1(\text{kWh}) = 1 \frac{\text{kJ}}{\text{s}} \cdot 3600 \text{ s} = 3600 \text{ (kJ)}$$

$$\frac{\text{Savings}}{\text{year}} = \frac{\Delta \bar{W}_{\text{in}}}{\text{year}} \cdot \frac{\text{Cost}}{\text{unit energy}} = \frac{145600 \text{ (kJ)}}{\text{year}} \cdot \frac{0.10 \text{ $}}{(\text{kWh})} \cdot \frac{1 \text{ (kWh)}}{3600 \text{ (kJ)}}$$

$$\frac{\text{Savings}}{\text{year}} = \$4.04$$