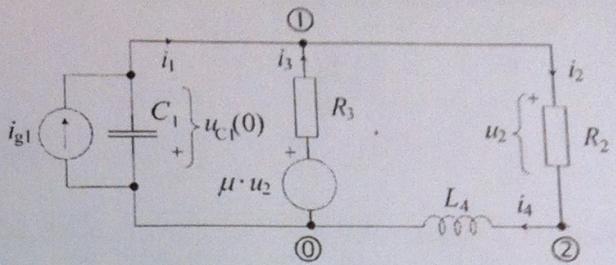
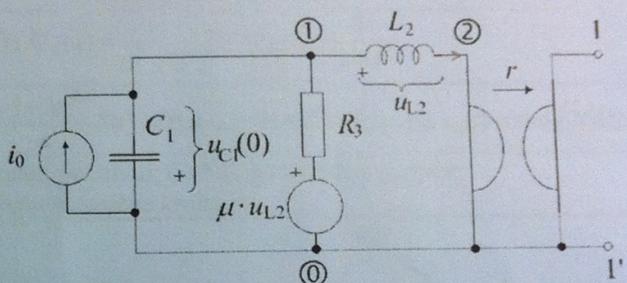


# MEĐUISPIT IZ ELEKTRIČNIH KRUGOVA 2011-2012

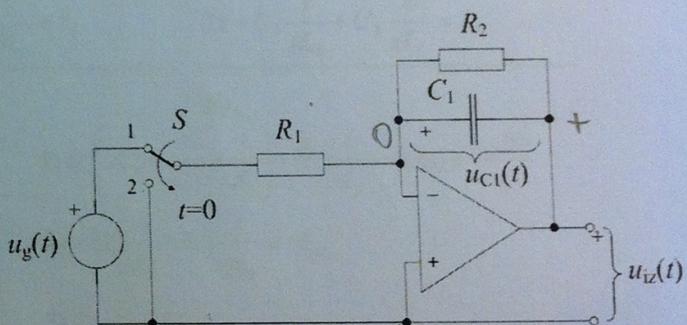
1. Za električni krug na slici i pridruženim orijentacijama grana te čvorovima zadane su normalizirane vrijednosti elemenata  $C_1=1$ ,  $R_2=1$ ,  $R_3=1$ ,  $L_4=1$  te  $\mu=2$ ,  $u_{C1}(0)=1$ ,  $i_{g1}(t)=S(t)$ . Koristeći KZS i KZN te oznake grana i čvorova prema slici, napisati: a) Jednadžbe KZS i KZN; b) Naponsko-strujne jednadžbe za grane; c) Napon na otporu  $R_2$   $U_2(s)$ ; d) Napon na otporu  $R_2$   $u_2(t)$ ; e) Da li je električni krug stabilan? Zašto?



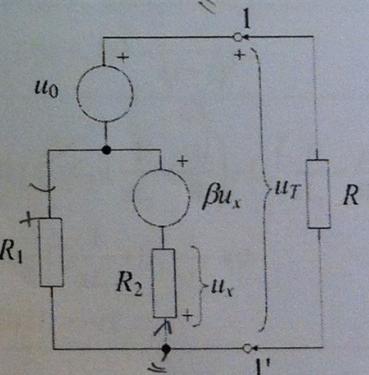
2. Za električni krug na slici zadane su normalizirane vrijednosti elemenata  $C_1=1$ ,  $L_2=1$ ,  $R_3=1$  te  $\mu=2$ ,  $r=1$ ,  $u_{C1}(0)=1$ ,  $i_0(t)=S(t)$ . Odrediti nadomjesne parametre mreže po Northonu s obzirom na polove 1-1'. Koristiti metodu napona čvorišta (čvorište ④ je referentno). U zadatku je potrebno: a) Nacrtati sklop za izračunavanje Nortonove struje, postaviti jednadžbe napona za čvorišta ① i ②; b) Odrediti Nortonovu struju  $I_N(s)$ ; c) Nacrtati sklop za izračunavanje Nortonove admitancije, postaviti jednadžbe napona za čvorišta ① i ②; d) Odrediti Nortonovu admitanciju  $Y_N(s)$ . e) Da li je električni krug recipročan? Zašto?



3. Za električni krug prikazan slikom se u trenutku  $t=0$  prebaci sklopka  $S$  iz položaja 1 u 2 uzrokujući prijelaznu pojavu. Zadane su normalizirane vrijednosti elemenata:  $R_1=1$ ,  $R_2=1/2$ ,  $C_1=1$ ,  $u_g(t)=10 \text{ V}$ ;  $-\infty < t < \infty$  (istosmjerni napon-baterija). Odrediti za  $t < 0$ : a) valni oblik napona na kapacitetu  $u_{C1}(t)$ ; b) početni napon  $u_{C1}(0)$ . Odrediti za  $t \geq 0$ : c) napon na izlazu operacijskog pojačala  $U_{iz}(s)$ ; d) valni oblik napona  $u_{iz}(t)$ . e) Ako je  $R_2=2$  odrediti valni oblik napona  $u_{iz}(t)$  za  $-\infty < t < \infty$ .

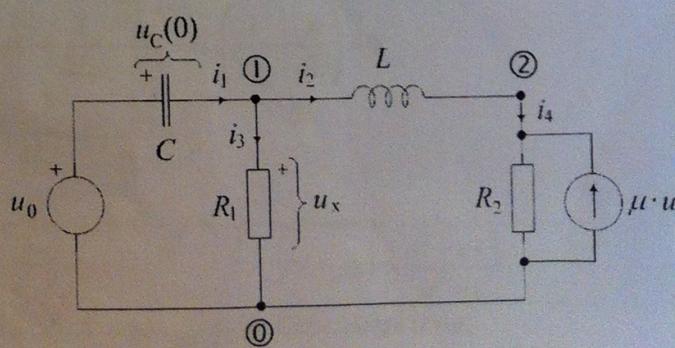


4. Za krug prikazan slikom isključiti otpor  $R$  i obzirom na priključnice 1-1' odrediti:  
 a) Teveninov napon  $u_T$ ;  
 b) Teveninov otpor  $R_T$ ;  
 c) iznos konstante  $\beta$  za koji je  $R_T=R$ ;  
 d) napon  $u_x$  uz uključen otpor  $R$  [ $\beta$  iz zadatka c)].  
 e) Za koji iznos konstante  $\beta$  je  $R_T=\infty$ ?



Zadano je: pobuda  $u_0=2 \text{ V}$  i vrijednosti elemenata  $R_1=R_2=2 \Omega$ ,  $R=4 \Omega$ .

5. Za električni krug prikazan slikom i pridruženim orijentacijama grana te čvorovima (grane stabla: 1, 2) treba odrediti temeljni sustav jednadžbi petlji primjenom grafova. Napisati: a) spojnu matricu  $S$ , b) matricu impedancija grana  $Z_b$ , c) vektor početnih uvjeta i nezavisnih izvora grana  $U_{0b}$ , d) matricu impedancija petlji  $Z_p$  i e) vektor početnih uvjeta i nezavisnih izvora petlji  $U_{0p}$ .



# MEĐUISPIT IZ ELEKTRIČNIH KRUGOVA - Ponuđeni odgovori

(svako pitanje je 1 bod, netočno zaokruženo je -0.25 bodova)

**Pitanja:** (pitanju 1 odgovara potpitanje je u tekstu označeno sa (1.a)) Zaokružiti samo jedan odgovor (A-E)!

- |                               |                           |                           |                          |                           |
|-------------------------------|---------------------------|---------------------------|--------------------------|---------------------------|
| 1) $-I_1 + I_2 = 0$           | 1) $-I_1 + I_2 + I_3 = 0$ | 1) $-I_1 = I_2$           | 1) $-I_1 = I_4 + I_2$    | 1) $-I_1 + I_2 - I_3 = 0$ |
| 2) $-I_2 + I_4 - I_3 = 0$     | 2) $-I_2 + I_4 = 0$       | 2) $-I_2 = I_4 - I_3$     | 2) $-I_2 = I_4 - I_3$    | 2) $-I_2 + I_4 = 0$       |
| 3) $U_1 - U_3 + U_4 = 0$ ; B) | 3) $U_1 + U_3 = 0$        | 3) $U_1 - U_3 = U_4$ ; C) | 3) $U_1 - U_3 + U_4 = 0$ | 3) $U_1 - U_3 = 0$        |
| 4) $U_2 + U_3 = 0$            | 4) $U_2 + U_3 + U_4 = 0$  | 4) $U_2 + U_3 = 0$        | 4) $U_2 + U_3 + U_4 = 0$ | 4) $U_2 + U_3 + U_4 = 0$  |

- |  |  |   |  |   |
|--|--|---|--|---|
| 2 (1.b) A)                                       | B)   | C)  | D)   | E)  |
| 1) $U_1 = \frac{I_1 - I_{g1} + u_{Cl}(0)}{sC_1}$ | 1) $U_1 = \frac{I_1 - I_{g1} - u_{Cl}(0)}{sC_1}$ | 1) $U_1 = sC_1(I_1 - I_{g1}) + C_1 u_{Cl}(0)$ | 1) $U_1 = \frac{I_{g1} - I_1 + u_{Cl}(0)}{sC_1}$ | 1) $U_1 = sC_1(I_1 - I_{g1}) + C_1 u_{Cl}(0)$ |
| 2) $U_2 = R_2 \cdot I_2$                         | 2) $U_2 = R_2 \cdot I_2$                         | 2) $U_2 = R_2 \cdot I_2$                      | 2) $U_2 = R_2 \cdot I_2$                         | 2) $U_2 = 1/R_2 \cdot I_2$                    |
| 3) $U_3 = R_3 \cdot I_3 - \mu R_2 I_2$           | 3) $U_3 = R_3 \cdot I_3 + \mu R_2 I_2$           | 3) $U_3 = R_3 \cdot I_3 + \mu R_2 I_2$        | 3) $U_3 = R_3 \cdot (1-\mu) I_3$                 | 3) $U_3 = -R_3 \cdot I_3 + \mu R_2 I_2$       |
| 4) $U_4 = sL_4 \cdot I_4$                        | 4) $U_4 = sL_4 \cdot I_4$                        | 4) $U_4 = sL_4 \cdot I_4$                     | 4) $U_4 = sL_4 \cdot I_4$                        | 4) $U_4 = -sL_4 \cdot I_4$                    |

3 (1.c) A)  $U_2(s) = \frac{2-s}{s^2-2}$ ; B)  $U_2(s) = \frac{1-s}{s^2(s-2)}$  C)  $U_2(s) = \frac{1-s}{s^2(2+s)}$ ; D)  $U_2(s) = \frac{s}{s^2+2}$ ; E)  $U_2(s) = \frac{5s}{2+s^2}$ .

4 (1.d) A)  $u_2(t) = -\frac{2t-1+e^{2t}}{4} S(t)$  B)  $u_2(t) = \frac{2t-3+3e^{-2t}}{4} S(t)$ ; C)  $u_2(t) = \frac{-1+3e^{-2t}}{4} S(t)$ ; D)  $u_2(t) = \cos(\sqrt{2}t)S(t)$ ; E)  $u_2(t) = \sin(\sqrt{2}t)S(t)$ .

5 (1.e) A) NE, jer ima dvostruki pol u ishodištu; B) DA, jer su mu svi elementi pozitivni; C) NE, jer ima ovisni izvor;  
D) NE, jer ima pol izvan jedinične kružnice; E) DA, jer ima pol unutar jedinične kružnice.

- |   |   |   |
|---|---|---|
| 6 (2.a) A)  | B)  | C)  |
| 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) - U_2 \frac{1}{sL_2} = I_0(s) - C_1 u_{Cl}(0)$ | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \frac{1}{sL_2} = I_0(s) - C_1 u_{Cl}(0)$       | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \frac{1}{sL_2} = I_0(s) - u_{Cl}(0)/s$ ;       |
| 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = 0$   | ;   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = I_N$   |
| 3) $I_N = -\frac{1}{r} U_1$   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = I_N$   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = I_N$   |
| <hr/>   |   |   |
| 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \frac{1}{sL_2} = I_0(s) + C_1 u_{Cl}(0)$ | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \frac{1}{sL_2} = I_0(s) + \frac{u_{Cl}(0)}{s}$ | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \frac{1}{sL_2} = I_0(s) + \frac{u_{Cl}(0)}{s}$ |
| 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = I_{g1}$  | ;   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = -I_{g1}$   |
| 3) $I_N = \frac{1}{r} U_1$  | 3) $I_N = -\frac{1}{r} U_1$   | 3) $I_N = -\frac{1}{r} U_1$   |

7 (2.b) A)  $I_N(s) = \frac{s+1}{s(s+1)}$ ; B)  $I_N(s) = \frac{s-1/s}{s+1}$ ; C)  $I_N(s) = \frac{s^2+1}{s+1}$ ; D)  $I_N(s) = \frac{s-1}{s(s+1)}$ ; E)  $I_N(s) = \frac{s}{(s+1)^2}$ .

- |   |   |   |
|---|---|---|
| 8 (2.c) A)  | B)  | C)  |
| 1) $U_1 \left( sC_1 + \frac{1}{sL_2} \right) + U_2 \left( \frac{1}{sL_2} - \frac{\mu}{R_3} \right) = 0$                     | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1-\mu}{R_3} \right) - U_2 \left( \frac{1}{sL_2} - \frac{\mu}{R_3} \right) = 0$ | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1}{R_3} \right) + U_2 \left( \frac{1}{sL_2} - \frac{\mu}{R_3} \right) = 0$ |
| 2) $-U_1 \frac{1}{sL_2} - U_2 \frac{1}{sL_2} = 0$   | ;   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = 0$   |
| 3) $U_2 = -rI$  | 3) $U_2 = rI$   | 3) $U_2 = -rI$  |
| <hr/>   |   |   |
| D)  | E)  |   |
| 1) $U_1 \left( sC_1 + \frac{1}{sL_2} + \frac{1-\mu}{R_3} \right) - U_2 \left( \frac{1}{sL_2} + \frac{\mu}{R_3} \right) = 0$ | 1) $U_1 \left( sC_1 + \frac{1}{sL_2} - \frac{\mu}{R_3} \right) - U_2 \left( \frac{1}{sL_2} - \frac{\mu}{R_3} \right) = 0$   |   |
| 2) $U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = \frac{U}{r}$  | ;   | 2) $-U_1 \frac{1}{sL_2} + U_2 \frac{1}{sL_2} = \frac{U}{r}$   |
| 3) $U_2 = rI$   | 3) $U_2 = -rI$  |   |

9 (2.d) A)  $Y_N(s) = \frac{s^2+s+1}{s+1}$ ; B)  $Y_N(s) = \frac{s+1/s}{s+1}$ ; C)  $Y_N(s) = \frac{s^2+s+1}{s^2+s}$ ; D)  $Y_N(s) = \frac{s^2-s+1}{s+1}$ ; E)  $Y_N(s) = \frac{s^2-s+1}{s^2+s}$ .

10 (2.e) A) NE, jer sadrži ovisni izvor i girator; B) DA, jer ima početni uvjet; C) NE, jer ima neovisni strujni izvor;  
D) DA, jer ne sadrži idealni transformator; E) DA, jer ima pol u lijevoj poluravnini.

11 (3.a) A)  $u_{C1}(t) = 20 \text{ V}; t < 0$ ; B)  $u_{C1}(t) = -10e^{-t} \text{ V}; t < 0$ ; C)  $u_{C1}(t) = 5 \text{ V}; t < 0$ ; D)  $u_{C1}(t) = 10e^{-2t} \text{ V}; t < 0$ ; E)  $u_{C1}(t) = -5 \text{ V}; t < 0$ .

12 (3.b) A)  $u_{C1}(0) = -5 \text{ V}$ ; B)  $u_{C1}(0) = 5 \text{ V}$ ; C)  $u_{C1}(0) = 0$ ; D)  $u_{C1}(0) = 20 \text{ V}$ ; E)  $u_{C1}(0) = 10 \text{ V}$ .

13 (3.c) A)  $U_{iz}(s) = \frac{-5}{s+2}$ ; B)  $U_{iz}(s) = \frac{1}{s+2}$ ; C)  $U_{iz}(s) = \frac{-1}{s+1/2}$ ; D)  $U_{iz}(s) = \frac{10}{s-1/2}$ ; E)  $U_{iz}(s) = \frac{10}{s-2}$ .

14 (3.d) A)  $u_{iz}(t) = e^{-2t} \cdot S(t)$ ; B)  $u_{iz}(t) = -5e^{-2t} \cdot S(t)$ ; C)  $u_{iz}(t) = -e^{-1/2t} \cdot S(t)$ ; D)  $u_{iz}(t) = 10e^{2t} \cdot S(t)$ ; E)  $u_{iz}(t) = 10e^{1/2t} \cdot S(t)$ .

15 (3.e) A)  $u_{iz}(t) = \begin{cases} 10, & t < 0 \\ 10e^{-\frac{t}{2}}, & t \geq 0 \end{cases}$ ; B)  $u_{iz}(t) = \begin{cases} 10, & t < 0 \\ 10e^{2t}, & t \geq 0 \end{cases}$ ; C)  $u_{iz}(t) = \begin{cases} -20, & t < 0 \\ -20e^{-2t}, & t \geq 0 \end{cases}$ ; D)  $u_{iz}(t) = \begin{cases} -5, & t < 0 \\ -5e^{\frac{t}{2}}, & t \geq 0 \end{cases}$ ; E)  $u_{iz}(t) = \begin{cases} -20, & t < 0 \\ -20e^{\frac{t}{2}}, & t \geq 0 \end{cases}$ .

16 (4.a) A)  $u_T(t) = -2 \text{ V}$ ; B)  $u_T(t) = 2 \text{ V}$ ; C)  $u_T(t) = 0 \text{ V}$ ; D)  $u_T(t) = 1 \text{ V}$ ; E)  $u_T(t) = -1 \text{ V}$ .

17 (4.b) A)  $R_T = \frac{R_1 R_2}{R_1(1-\beta) + R_2}$ ; B)  $R_T = \frac{R_1 R_2 (1+\beta)}{R_1(1+\beta) + R_2}$ ; C)  $R_T = \frac{R_1 R_2 (1-\beta)}{R_2(1-\beta) + R_1}$ ; D)  $R_T = \frac{R_1 R_2 (\beta-1)}{R_2(\beta-1) + R_1}$ ; E)  $R_T = \frac{R_1 R_2 (1+\beta)}{R_2(1+\beta) + R_1}$ .

18 (4.c) A)  $\beta = 3$ ; B)  $\beta = 2$ ; C)  $\beta = 1$ ; D)  $\beta = 4$ ; E)  $\beta = 5$ .

19 (4.d) A)  $u_x = -\frac{1}{2}V$ ; B)  $u_x = \frac{1}{13}V$ ; C)  $u_x = \frac{4}{13}V$ ; D)  $u_x = \frac{4}{9}V$ ; E)  $u_x = -\frac{4}{9}V$ .

20 (4.e) A)  $\beta = 1$ ; B)  $\beta = 2$ ; C)  $\beta = 3$ ; D)  $\beta = 4$ ; E)  $\beta = 5$ .

21 (5.a) A)  $S = \begin{bmatrix} -1 & 1 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{bmatrix}$ ; B)  $S = \begin{bmatrix} -1 & 0 & -1 & 0 \\ -1 & -1 & 0 & -1 \end{bmatrix}$ ; C)  $S = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 1 \end{bmatrix}$ ; D)  $S = \begin{bmatrix} 1 & -1 & -1 & 0 \\ 0 & 1 & 0 & -1 \end{bmatrix}$ ; E)  $S = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & -1 & 1 \end{bmatrix}$ .

22 (5.b) A)  $Z_b = \begin{bmatrix} \frac{1}{sC} & 0 & 0 & 0 \\ 0 & sL & 0 & 0 \\ 0 & 0 & R_1 & 0 \\ 0 & -\mu sLR_2 & 0 & R_2 \end{bmatrix}$ ; B)  $Z_b = \begin{bmatrix} \frac{1}{sC} & 0 & 0 & 0 \\ 0 & sL & 0 & 0 \\ 0 & 0 & R_1 & 0 \\ 0 & 0 & \mu R_1 R_2 & R_2 \end{bmatrix}$ ; C)  $Z_b = \begin{bmatrix} sC & 0 & 0 & 0 \\ 0 & \frac{1}{sL} & 0 & 0 \\ 0 & 0 & \frac{1}{R_1} & 0 \\ 0 & 0 & -\mu R_2 & \frac{1}{R_2} \end{bmatrix}$ ;

D)  $Z_b = \begin{bmatrix} \frac{1}{sC} & 0 & 0 & 0 \\ 0 & sL & 0 & 0 \\ 0 & 0 & R_1 & 0 \\ 0 & 0 & 0 & R_2 \end{bmatrix}$ ; E)  $Z_b = \begin{bmatrix} \frac{1}{sC} & 0 & 0 & 0 \\ 0 & sL & 0 & 0 \\ 0 & 0 & R_1 & 0 \\ 0 & 0 & -\mu R_1 R_2 & R_2 \end{bmatrix}$ .

23 (5.c) A)  $U_{ob} = \begin{bmatrix} \frac{u_c(0)}{s} + U_0(s) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ; B)  $U_{ob} = \begin{bmatrix} -\frac{u_c(0)}{s} + U_0(s) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ; C)  $U_{ob} = \begin{bmatrix} \frac{u_c(0)}{s} - U_0(s) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ; D)  $U_{ob} = \begin{bmatrix} -U_0(s) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ; E)  $U_{ob} = \begin{bmatrix} -\frac{u_c(0)}{s} - U_0(s) \\ 0 \\ 0 \\ 0 \end{bmatrix}$ .

24 (5.d) A)  $Z_p = \begin{bmatrix} \frac{1}{sC} + R_1 & \frac{1}{sC} \\ \frac{1}{sC} + \mu R_1 R_2 & \frac{1}{sC} + sL + R_2 \end{bmatrix}$ ; B)  $Z_p = \begin{bmatrix} \frac{1}{sC} + R_1 & \frac{1}{sC} \\ \frac{1}{sC} + \mu R_1 R_2 & \frac{1}{sC} + sL + \mu sLR_2 + R_2 \end{bmatrix}$ ; C)  $Z_p = \begin{bmatrix} \frac{1}{sC} + sL + R_1 & -sL \\ -sL + \mu R_1 R_2 & sL + R_2 \end{bmatrix}$ ;

D)  $Z_p = \begin{bmatrix} -\frac{1}{sC} + R_1 & \frac{1}{sC} \\ \frac{1}{sC} & \frac{1}{sC} + sL + R_2 \end{bmatrix}$ ; E)  $Z_p = \begin{bmatrix} \frac{1}{sC} + R_1 & \frac{1}{sC} \\ \frac{1}{sC} - \mu R_1 R_2 & \frac{1}{sC} + sL + R_2 \end{bmatrix}$ .

25 (5.e) A)  $U_{0p} = \begin{bmatrix} U_0(s) \\ U_0(s) \end{bmatrix}$ ; B)  $U_{0p} = \begin{bmatrix} -\frac{u_c(0)}{s} - U_0(s) \\ -\frac{u_c(0)}{s} - U_0(s) \end{bmatrix}$ ; C)  $U_{0p} = \begin{bmatrix} \frac{u_c(0)}{s} + U_0(s) \\ \frac{u_c(0)}{s} + U_0(s) \end{bmatrix}$ ; D)  $U_{0p} = \begin{bmatrix} U_0(s) - \frac{u_c(0)}{s} \\ U_0(s) - \frac{u_c(0)}{s} \end{bmatrix}$ ; E)  $U_{0p} = \begin{bmatrix} \frac{u_c(0)}{s} - U_0(s) \\ \frac{u_c(0)}{s} - U_0(s) \end{bmatrix}$ .