

Volumen valjka $V = \left(\frac{d}{2}\right)^2 \cdot \pi \cdot h$

fiz. veličina \ mjerenje	1.	2.	3.	4.	5.
d [cm]					
h [cm]					

$$\bar{x} = \frac{1}{n} \cdot \sum_{i=1}^n x_i = |n=5| \rightarrow \text{srednja vrijednost}$$

$$\bar{d} = \frac{1}{5} \cdot \sum_{i=1}^5 d_i$$

$$\bar{d} = \text{cm}$$

$$\bar{h} = \frac{1}{5} \cdot \sum_{i=1}^5 h_i$$

$$\bar{h} = \text{cm}$$

$$s(\bar{x}) = \sqrt{\frac{1}{n(n-1)} \cdot \sum_{i=1}^n (x_i - \bar{x})^2} = |n=5| \rightarrow \text{standardna devijacija srednje vrijednosti}$$

$$s(\bar{d}) = \text{cm}$$

$$s(\bar{h}) = \text{cm}$$

$$\delta = \text{cm} \rightarrow \text{rezolucija}$$

$$u_\delta = \frac{\delta}{\sqrt{12}} \rightarrow \text{nesigurnost}$$

$$= \text{cm}$$

Kombinirana nesigurnost

$$u_h = s(\bar{h})$$

$$u_d = s(\bar{d})$$

$$u_{c,d}^2 = u_d^2 + u_\delta^2$$

$$u_{c,h}^2 = u_h^2 + u_\delta^2$$

$$d_{mjer} = \left(\bar{d} \pm u_{c,d} \right) \text{ [m.j.]}$$

$$h_{mjer} = \left(\bar{h} \pm u_{c,h} \right) \text{ [m.j.]}$$

$$d_{mjer} = \left(\pm \right) \text{ cm}$$

$$h_{mjer} = \left(\pm \right) \text{ cm}$$

Nesigurnost volumena

$$u_V^2(h, d) = V^2 \cdot \left[\left(\frac{u_h}{\bar{h}} \right)^2 + \left(\frac{2 u_d}{\bar{d}} \right)^2 \right]$$

$$u_V(h, d) = \text{cm}$$

$$\bar{V} = \left(\frac{\bar{d}}{2} \right)^2 \cdot \pi \cdot \bar{h}$$

$$\bar{V} = \text{cm}^3$$

$$V_{mjer} = \left(\bar{V} \pm u_V \right) \text{ [m.j.]}$$

$$V_{mjer} = \left(\pm \right) \text{ cm}^3$$

• Sila uzgona na tijelo

$$F_u = N_3 - N_1 \quad \swarrow \text{posuda + voda}$$

$$\swarrow$$

$$\text{posuda + voda + tijelo} \quad F_u = g \cdot \rho_v \cdot V_t$$

• Volumen tijela

$$V_t = \frac{N_3 - N_1}{g \cdot \rho_v}$$

$$V_t = \frac{g' (m_3 - m_1)}{g \cdot \rho_v} = |g'| = g$$

$$V_t = \frac{m_3 - m_1}{\rho_v}$$

• Nepreciznost vage

$$\delta_{m_1} = \quad g \quad \delta_{m_3} = \quad g$$

• Nesigurnost mjerenja mase

$$u = \frac{\delta}{\sqrt{12}}$$

$$u_{m_1} = \quad g \quad u_{m_3} = \quad g$$

• Mjerenje mase i računanje volumena

$$m_0 = \quad g \quad m_3 = \quad g$$

$$V_t = \frac{m_3 - m_0}{\rho_v} \quad | t = 22^\circ \text{C} |$$

$$= \frac{\quad}{0.99777} = \quad \text{cm}^3$$

• Nesigurnost volumena

$$u_v^2 = \left(\frac{\partial V}{\partial m_3} \right)^2 \cdot u_{m_3}^2 + \left(\frac{\partial V}{\partial m_0} \right)^2 \cdot u_{m_0}^2$$

$$u_v^2 = \left(\frac{u_{m_3}}{\rho_v} \right)^2 + \left(\frac{u_{m_0}}{\rho_v} \right)^2$$

$$u_v^2 = \frac{u_{m_3}^2 + u_{m_0}^2}{\rho_v^2}$$

$$u_v(m_3, m_0) = \frac{\sqrt{u_{m_3}^2 + u_{m_0}^2}}{\rho_v}$$

$$U_v(m_3, m_0) = \quad \text{cm}^3$$

• Standardni zapis

$$V_t = \bar{V}_t \pm \mu_v$$

$$= \left(\quad \pm \quad \right) \text{cm}^3$$

valjak $V = \left(\frac{d}{2}\right)^2 \cdot \pi \cdot h$

mjerenje	1	2	3	4	5	srednja vrijednost	standardna devijacija
d							
h							

srednja vrijednost: $\bar{d} = \frac{1}{5} \cdot \sum_{i=1}^5 d_i =$

$\bar{h} = \frac{1}{5} \cdot \sum_{i=1}^5 h_i =$

standardna devijacija srednje vrijednosti

$$U_d = S(\bar{d}) = \sqrt{\frac{1}{5 \cdot (5-1)} \cdot \sum_{i=1}^5 (d_i - \bar{d})^2}$$

$$U_h = S(\bar{h}) = \sqrt{\frac{(h_1 - \bar{h})^2 + (h_2 - \bar{h})^2 + (h_3 - \bar{h})^2 + (h_4 - \bar{h})^2 + (h_5 - \bar{h})^2}{5 \cdot (5-1)}}$$

rezolucija $\delta =$ i pripadna nesigurnost $U_\delta = \frac{\delta}{\sqrt{12}} =$

kombinirana nesigurnost mjerenja

$$u_{c,d} = \sqrt{u_d^2 + u_\delta^2} =$$

$$u_{c,h} = \sqrt{u_h^2 + u_\delta^2} =$$

$$\Rightarrow d_{\text{mer.}} = (\bar{d} \pm u_{c,d}) [\text{m.j}]$$

$$h_{\text{mer.}} = (\bar{h} \pm u_{c,h}) [\text{m.j}]$$

$$d_{\text{mer.}} =$$

$$h_{\text{mer.}} =$$

volumen $\bar{V} = \left(\frac{\bar{d}}{2}\right)^2 \cdot \pi \cdot \bar{h}$

$$u_v(d,h) = \bar{V} \cdot \sqrt{\left(\frac{u_h}{\bar{h}}\right)^2 + \left(\frac{2u_d}{\bar{d}}\right)^2}$$

$$\bar{V} =$$

$$u_v(d,h) =$$

$$\Rightarrow V_{\text{mer.}} = (\bar{V} \pm u_v) [\text{m.j}]$$

$$V_{\text{mer.}} =$$

2.2

Koristeći izvod, napišite 2 mjerenja: (1) masa posude i vode, (2) masa posude i vode težištem u vodi

$$\Rightarrow V_t = \frac{m_3 - m_0}{\rho_v} \quad , \text{ gdje je } m_3 \text{ masa očitana na vagi u (2) i } m_0 \text{ masa na vagi u (1)}$$

NEPRECIZNOST VAGE

GUSTOĆA VODE U 30°C (999.97 kg/m³)

$$\delta_{m_0} = \quad \delta_{m_3} = \quad \rho_v =$$

$$\Rightarrow u_{m_0} = \frac{\delta_{m_0}}{\sqrt{12}} = \quad u_{m_3} = \frac{\delta_{m_3}}{\sqrt{12}} =$$

MJERENA MASA:

$$m_0 = \quad m_3 =$$

VOLUMEN

$$\bar{V}_t = \frac{m_3 - m_0}{\rho_v} =$$

$$u_v^2(m_3, m_0) = \left(\frac{\partial V}{\partial m_3} \right)^2 u_{m_3}^2 + \left(\frac{\partial V}{\partial m_0} \right)^2 u_{m_0}^2 = \frac{u_{m_3}^2}{\rho_v^2} + \frac{u_{m_0}^2}{\rho_v^2} = \frac{1}{\rho_v^2} (u_{m_3}^2 + u_{m_0}^2)$$

$$u_v(m_3, m_0) = \frac{1}{\rho_v} \cdot \sqrt{u_{m_3}^2 + u_{m_0}^2} =$$

$$\underline{R_i} \quad V_t = \bar{V}_t \pm u_v =$$