

Koji od navedenih vektora nije normiran? // Which of the following vectors is not normalized?

Odaberite jedan odgovor:

- ☐  $\frac{2}{\sqrt{5}}(|0\rangle + \frac{1}{2}|1\rangle)$
- ☒  $\frac{\sqrt{3}}{2}(i|0\rangle + \frac{1}{2}|1\rangle)$
- ☐  $\frac{3}{5}|0\rangle - \frac{4}{5}|1\rangle$
- ☐  $\frac{1}{3}|0\rangle + \frac{2\sqrt{2}}{3}|1\rangle$
- ☐  $\frac{1}{\sqrt{5}}(2|0\rangle + i|1\rangle)$



Koja dva od navedenih stanja qubita čine ortonormiranu bazu u  $\mathcal{H}^{(2)}$ ? / Which two of the following qubit states comprise a orthonormal basis in  $\mathcal{H}^{(2)}$ ?

- ☐  $\frac{3}{5}|0\rangle + \frac{4i}{5}|1\rangle$
- ☒  $\frac{4}{5}|0\rangle - \frac{3}{5}|1\rangle$
- ☒  $\frac{3}{5}|0\rangle + \frac{4}{5}|1\rangle$
- ☐  $-\frac{3}{5}|0\rangle - \frac{4i}{5}|1\rangle$
- ☐  $\frac{3i}{5}|0\rangle - \frac{4}{5}|1\rangle$

Koji od navedenih vektora predstavljaju isto stanje kvantnog bita? // Which of the following kets represent the same qubit state?

- ☐  $\frac{1}{\sqrt{5}}|0\rangle + \frac{2i}{\sqrt{5}}|1\rangle$
- ☒  $-\frac{2}{\sqrt{5}}|0\rangle - \frac{1}{\sqrt{5}}|1\rangle$
- ☐  $\frac{2}{\sqrt{5}}|0\rangle - \frac{i}{\sqrt{5}}|1\rangle$
- ☒  $\frac{2}{\sqrt{5}}|0\rangle + \frac{1}{\sqrt{5}}|1\rangle$
- ☒  $-\frac{2i}{\sqrt{5}}|0\rangle - \frac{i}{\sqrt{5}}|1\rangle$

Kvantni bit je pripremljen u stanju: // Qubit is prepared in the state:

$$\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$$

Izračunaj vjerojatnost da taj kvantni bit bude izmjeren u stanju: // Compute the probability that this qubit is measured in the state:

$$\frac{3}{5}|0\rangle + \frac{4}{5}|1\rangle$$

Odaberite jedan odgovor:

- ☐  $\frac{7}{5\sqrt{2}}$
- ☒  $\frac{49}{50}$
- ☐ 0
- ☐  $\frac{1}{50}$
- ☐ 1



Operator // Operator

$$\frac{1}{2}(|0\rangle\langle 0| - |0\rangle\langle 1| - |1\rangle\langle 0| + |1\rangle\langle 1|)$$

je projektor na stanje: // is a projector onto the state:

Odaberite jedan odgovor:

- ☐  $|0\rangle$  ili  $|1\rangle$
- ☐  $\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$
- ☐  $\frac{1}{\sqrt{2}}|0\rangle + \frac{i}{\sqrt{2}}|1\rangle$
- ☒  $\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle$
- ☐  $\frac{1}{\sqrt{2}}|0\rangle - \frac{i}{\sqrt{2}}|1\rangle$



Izračunaj očekivanu vrijednost hermitskog operatora // Compute the expectation value of the Hermitean operator

$$|0\rangle\langle 0| - |1\rangle\langle 1|$$

u sustavu koji se nalazi u stanju // in a system that is in the state

$$\frac{2}{\sqrt{13}}|0\rangle + \frac{3}{\sqrt{13}}|1\rangle$$

Odaberite jedan odgovor:

- ☐  $\frac{5}{13}$
- ☐  $-\frac{3}{5}$
- ☒  $-\frac{5}{13}$
- ☐  $0$
- ☐  $\frac{3}{5}$



Matrični prikaz // Matrix representation

$$\begin{pmatrix} \frac{1}{2} & -\frac{i}{2} \\ \frac{i}{2} & \frac{1}{2} \end{pmatrix}$$

odgovara operatoru // corresponds to the operator

Odaberite jedan odgovor:

- ☐  $\frac{1}{2}(|0\rangle\langle 0| + i|0\rangle\langle 1| - i|1\rangle\langle 0| + |1\rangle\langle 1|)$
- ☐  $\frac{1}{2}(|0\rangle\langle 0| + |0\rangle\langle 1| + |1\rangle\langle 0| + |1\rangle\langle 1|)$
- ☐  $\frac{1}{2}(|0\rangle\langle 0| + i|0\rangle\langle 1| + i|1\rangle\langle 0| + |1\rangle\langle 1|)$
- ☐  $\frac{1}{2}(|0\rangle\langle 0| - |0\rangle\langle 1| - |1\rangle\langle 0| + |1\rangle\langle 1|)$
- ☒  $\frac{1}{2}(|0\rangle\langle 0| - i|0\rangle\langle 1| + i|1\rangle\langle 0| + |1\rangle\langle 1|)$



Ako je energija kvantnog bita opisana hamiltonijanom // If qubit energy is described by the Hamiltonian

$$H = \hbar\omega|0\rangle\langle 0|, \quad \omega > 0,$$

i ako je početno stanje kvantnog bita // and if the initial state of the qubit is

$$\frac{1}{\sqrt{2}}|0\rangle + \frac{i}{\sqrt{2}}|1\rangle,$$

nakon  $\Delta t = \frac{\pi}{2\omega}$  sustav će biti u stanju // after  $\Delta t = \frac{\pi}{2\omega}$  the state of the qubit will be

Odaberite jedan odgovor:

- ☐  $\frac{1}{\sqrt{2}}|0\rangle - \frac{i}{\sqrt{2}}|1\rangle$
- ☒  $\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle$
- ☐  $|1\rangle$
- ☐  $\frac{1}{\sqrt{2}}|0\rangle + \frac{i}{\sqrt{2}}|1\rangle$
- ☐  $|0\rangle$
- ☐  $\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle$



Alice i Bob uspostavljaju tajni enkripcijski ključ korištenjem protokola BB84. Alice odabire bazu  $\otimes$  i odašilje foton u stanju **1**. Kolika je vjerojatnost da Bob izmjeri vrijednost **0** ako on odabere bazu  $\oplus$ , a Eve prisluškuje komunikaciju?




*Alice and Bob are establishing a secret encryption key using the BB84 protocol. Alice chooses base  $\otimes$  and sends a foton in the state **1**. What is the probability that Bob measures **0** if he chooses base  $\oplus$ , and if Eve is eavesdropping the communication?*

Odaberite jedan odgovor:

- ☐  $1/4$
- ☐  $3/8$
- ☒  $1/2$
- ☐  $5/8$
- ☐  $3/4$



U kojima od navedenih stanja sustava dvaju kvantnih bitova su stanja samih bitova spregnuta? // In which of the following states of the 2-qubit system are the states of the individual qubits entangled?

- ☐  $\frac{1}{2}(|00\rangle - |01\rangle + |10\rangle - |11\rangle)$
- ☒  $\frac{1}{2}(|00\rangle - |01\rangle + |10\rangle + i|11\rangle)$   

- ☒  $\frac{1}{2}(|00\rangle + i|01\rangle + i|10\rangle - i|11\rangle)$   

- ☒  $\frac{1}{2}(|00\rangle + i|01\rangle + i|10\rangle - i|11\rangle)$   

- ☐  $\frac{1}{2}(|00\rangle - i|01\rangle - i|10\rangle - |11\rangle)$