

ZADATAK 1

DEF. PERIODIČNOST) VREMENSKI KONTINUIRANOG SIGNALA

Periodičan vremenski kontinuirani signal, periode T_0 , oblikovan je ka-

$$f: \mathbb{R} \rightarrow \mathbb{R}$$

$$\forall t \in \mathbb{R}, T_0 \in \mathbb{R}^+ \quad f(t) = f(t + T_0)$$

ISPITIVANJE PERIODIČNOSTI | ODREĐIVANJE TEHNIČNOG PERIODA

$$1) x_1(t + T_0) = 2 = x_1(t)$$

SIGNAL JE PERIODIČAN, ali nema osnovni period vec' je $T_0 \in \mathbb{R}^+$

$$2) x_2(t + T_0) = \sin\left(\frac{2\pi}{T}(t + T_0)\right) = \sin\frac{2\pi t}{T} \cdot \cos\frac{2\pi T_0}{T} + \cos\frac{2\pi t}{T} \cdot \sin\frac{2\pi T_0}{T}$$

SIGNAL JE PERIODIČAN Ako $\cos\frac{2\pi T_0}{T} = 1$ & $\sin\frac{2\pi T_0}{T} = 0$

tj. $T_0 = T$ i T_0 mu je osnovni period

$$3) x_3(t + T_0) = \sin\left(\frac{2\pi}{T}(t + T_0)^2\right) = \sin\left(\frac{2\pi}{T} \cdot t^2 + \frac{2\pi}{T} 2tT_0 + \frac{2\pi}{T} T_0^2\right)$$

$$\frac{2\pi}{T} T_0 (2t + T_0) = 2k\pi, k \in \mathbb{N}$$

$$\frac{2tT_0 + T_0^2}{T} = k, T_0 = \text{const.} \Rightarrow \text{SIGNAL NIJE PERIODIČAN}$$

ZADATAK 2

DEF. PERIODIČNOST VREMENSKI DISKRETNOG SIGNALA

Periodičan vremenski diskretni signal, periode N , definiran je kao

$$f: \mathbb{Z} \rightarrow \mathbb{R}$$

$$\forall n \in \mathbb{Z}, N \in \mathbb{Z}^+ \quad f(n) = f(n+N)$$

ISPITIVANJE PERIODIČNOSTI | ODREĐIVANJE PREDJELNOG PERIODA

$$1) x_1(n+N_0) = 2 = x_1(n)$$

SIGNAL JE PERIODIČAN, PERIOD BILA KOJI $N_0 \in \mathbb{Z}^+$

$$2) x_2(n+N_0) = \sin\left(\frac{2\pi}{N}(n+N_0)\right) = \sin\left(\frac{2\pi n}{N} + \cos\frac{2\pi N_0}{N} + \sin\frac{2\pi n}{N}\right)$$

SIGNAL JE PERIODIČAN AKO $\cos\frac{2\pi N_0}{N} = 1$ & $\sin\frac{2\pi N_0}{N} = 0$

tj. OSNOVNI PERIOD JE $N_0 = N$

$$3) x_3(n+N_0) = \sin\left(\frac{2\pi}{N}(n+N_0)^2\right) = \sin\left(\frac{2\pi}{N}(n^2 + 2nN_0 + N_0^2)\right) = \sin\left(\frac{2\pi}{N}n^2\right)$$

$$\frac{2\pi}{N}(2nN_0 + N_0^2) = 2k\pi \quad k \in \mathbb{N}$$

$$\frac{N_0}{N}(2n + N_0) = k$$

SIGNAL JE PERIODIČAN

OSNOVNI PERIOD $N_0 = N$

ne smije biti razlomak $\Rightarrow \boxed{N_0 = N}$

Kod za crtanje signala

$$n = [0 : 1 : 30];$$

$$\text{stem}(\sin((2\pi f_1 n)^2 / 5));$$

Temeđem dobivene slike se može ispitati je li signal periodičan ili nije obzirom da graf sadrži konaku mnošta ugodnosti za kog se može govoriti o periodičnosti signalu B
čak i utvrditi periodicitet signala B

$$f_1(n) = \sin\left(\frac{2\pi}{N_1} n\right)$$

$$f_2(n) = \sin\left(\frac{2\pi}{N_2} n\right)$$

$$f_1(n) \cdot f_2(n) = \sin\left(\frac{2\pi}{N_1} n\right) \cdot \sin\left(\frac{2\pi}{N_2} n\right) = \frac{1}{2} \left[\cos\left(2\pi n \left(\frac{1}{N_1} - \frac{1}{N_2}\right)\right) - \cos\left(2\pi n \left(\frac{1}{N_1} + \frac{1}{N_2}\right)\right) \right]$$

$$2\pi N \left(\frac{1}{N_1} - \frac{1}{N_2}\right) = 2\pi k_1, \quad k_1 \in \mathbb{Z}$$

$$2\pi N \left(\frac{1}{N_1} + \frac{1}{N_2}\right) = 2\pi k_2, \quad k_2 \in \mathbb{Z}$$

$$\frac{N}{N_1} - \frac{N}{N_2} = k_1$$

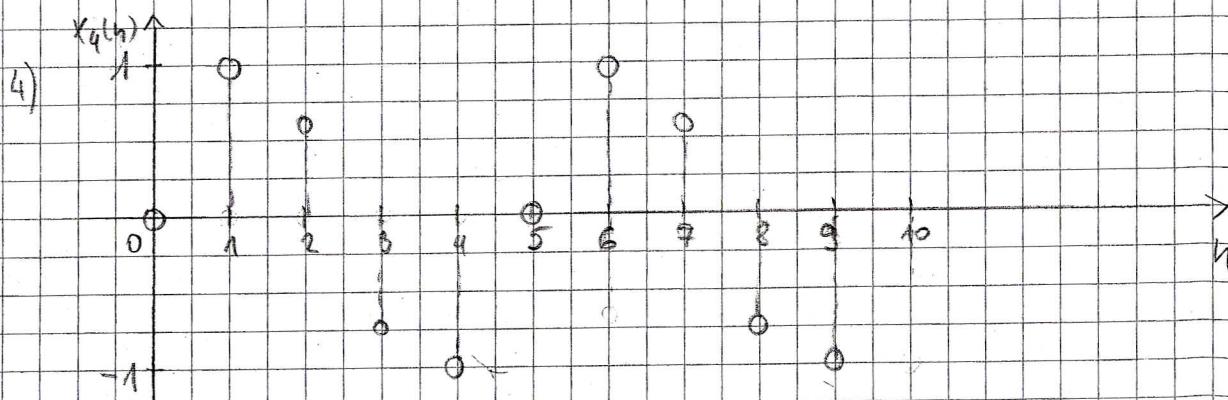
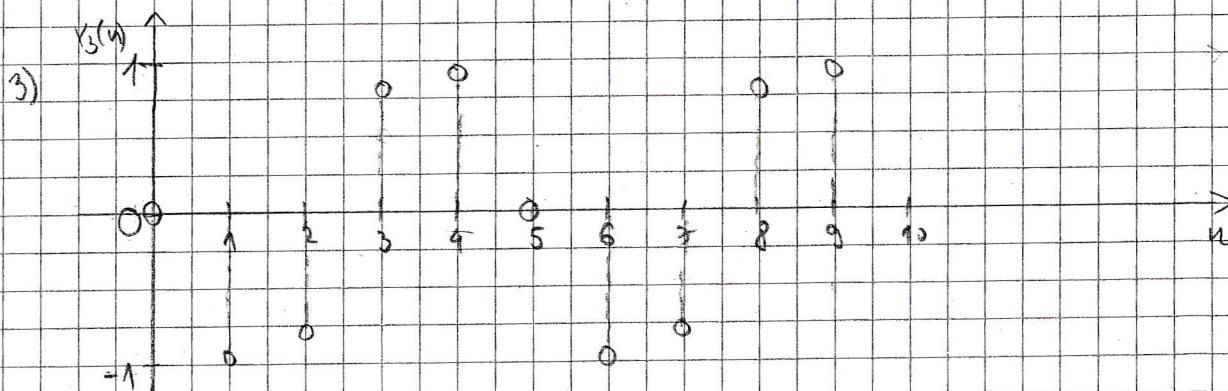
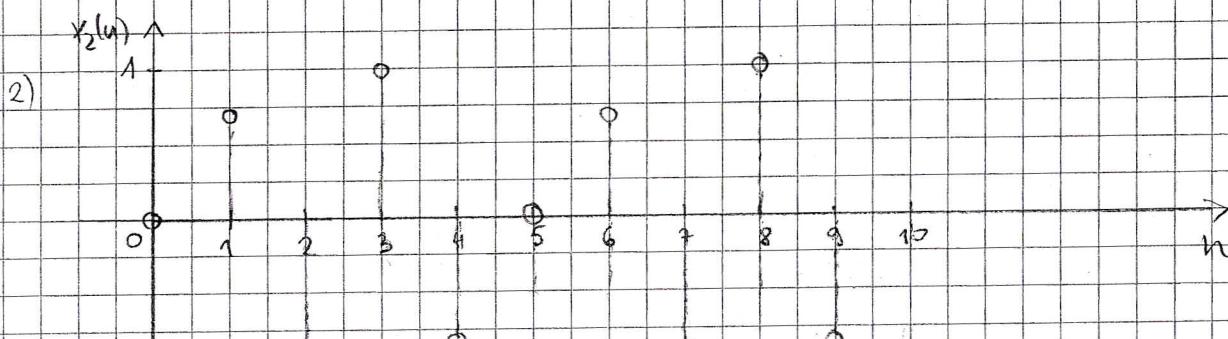
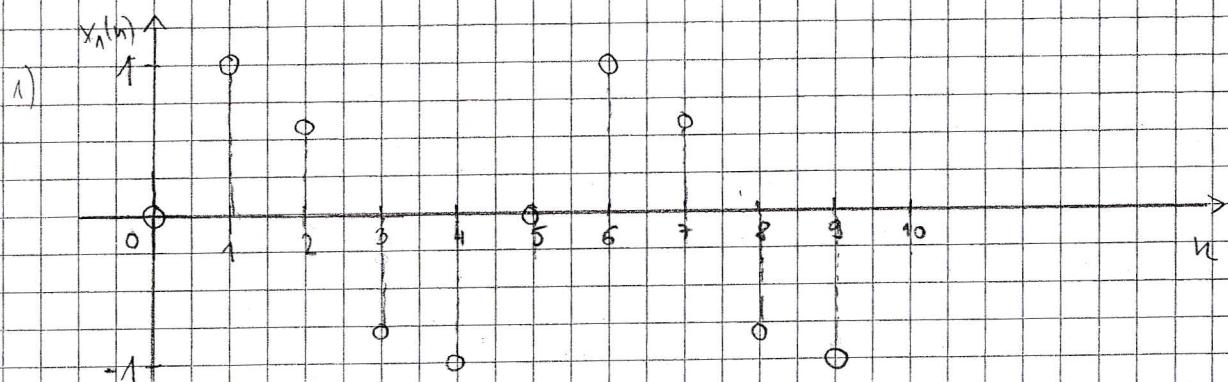
$$\frac{N}{N_1} + \frac{N}{N_2} = k_2$$

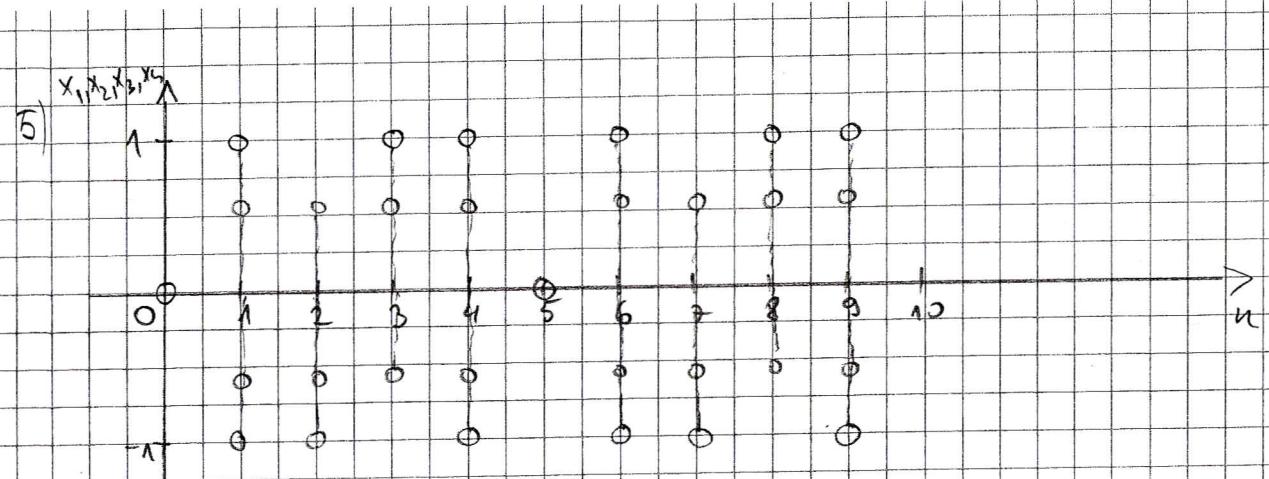
U mora biti celi broj, a to je samo kada je N
najmanji zajednički višekratnik N₁ i N₂

Temeđni period je uprav N tj. najmanji zajednički
višekratnik N₁ i N₂.

ZADATAK 3

$$x_k(n) = \sin(\omega_k n) ; \omega_k = \frac{2\pi k}{5}$$





b) Načrtaj sam 3 različita signala.

c) Signali $x_1(n)$ i $x_2(n)$ su jednaki zbroj aliasinga
(frekvensi skog preklapanja)

$$\omega_{k_1} = \frac{2\pi}{5}$$

$$\omega_{k_2} = \frac{12\pi}{5} = 2\pi + \frac{2\pi}{5}$$

} ALIASING

ZADATAK 4

DEF. ENERGIJE I SNAGE KONTINUIRANOG VREMENSKOG SIGNALA

Energija vremenski kontinuiranog signala, za signal f , definiran na vremenskom intervalu $[t_1, t_2] \subset \mathbb{R}$, definira se kao

$$E_{[t_1, t_2]} = \int_{t_1}^{t_2} |f(t)|^2 dt \quad ; \quad L = t_2 - t_1$$

Srednja snaga vremenski kontinuiranog signala f , definirana je u vremenskom intervalu $[t_1, t_2] \subset \mathbb{R}$, definirana se kao

$$P_{[t_1, t_2]} = \frac{1}{L} \int_{t_1}^{t_2} |f(t)|^2 dt \quad ; \quad L = t_2 - t_1$$

DEF. ENERGIJE I SNAGE DISKRETNOG VREMENSKOG SIGNALA

Energija vremenski odsjekotinog signala (niza) y , definirana je na intervalu $[n_1, n_2] \subset \mathbb{Z}^I$, definirana se kao

$$E_{[n_1, n_2]} = \sum_{n=n_1}^{n_2} |y(n)|^2$$

Srednja snaga vremenski odsjekotinog signala y , definirana je na intervalu $[n_1, n_2] \subset \mathbb{Z}^I$, definirana se kao

$$P_{[n_1, n_2]} = \frac{1}{n_2 - n_1 + 1} \sum_{n=n_1}^{n_2} |y(n)|^2$$

$$x_1(t) = \cos\left(\frac{\pi}{3}t\right) \quad x_2(n) = \sin\left(\frac{\pi}{3}n\right)$$

$$E_{\infty} = \int_{-\infty}^{\infty} |f(t)|^2 dt = \int_{-\infty}^{\infty} \cos^2\left(\frac{\pi}{3}t\right) dt = \int_{-\infty}^{\infty} \left(\frac{1}{2} + \frac{\cos\frac{2\pi}{3}t}{2}\right) dt = \\ = \left. \frac{1}{2}t + \frac{3}{4\pi} \sin\left(\frac{2\pi}{3}t\right) \right|_{-\infty}^{\infty} = \underline{\underline{\infty}}$$

$$P_{\infty} = \lim_{L \rightarrow \infty} \frac{1}{L} \int_{-\frac{L}{2}}^{\frac{L}{2}} |f(t)|^2 dt = \lim_{L \rightarrow \infty} \frac{1}{L} \int_{-\frac{L}{2}}^{\frac{L}{2}} \left(\frac{1}{2} + \frac{\cos\frac{2\pi}{3}t}{2}\right) dt = \\ = \lim_{L \rightarrow \infty} \int_{-\frac{L}{2}}^{\frac{L}{2}} \left(\frac{1}{2} + \frac{1}{4\pi} \sin\left(\frac{2\pi}{3}t\right)\right) dt = \lim_{L \rightarrow \infty} \left(\frac{1}{2} + \frac{1}{2} \frac{\sin\frac{\pi L}{3}}{\frac{\pi L}{3}}\right) = \underline{\underline{\frac{1}{2}}}$$

$$E_{\infty} = \sum_{n=-\infty}^{\infty} |y(n)|^2 = \sum_{n=-\infty}^{\infty} \sin^2\left(\frac{\pi}{3}n\right) = \sum_{n=-\infty}^{\infty} \left(\frac{1}{2} - \frac{\cos\left(\frac{2\pi}{3}n\right)}{2}\right) = \\ = \frac{1}{2} \sum_{n=-\infty}^{\infty} \left(1 - \cos\left(\frac{2\pi}{3}n\right)\right) = \underline{\underline{\infty}}$$

$$P_{\infty} = \lim_{M \rightarrow \infty} \frac{1}{2M+1} \sum_{n=-M}^{M} |y(n)|^2 = \lim_{M \rightarrow \infty} \frac{1}{2M+1} \sum_{n=-M}^{M} \left(\frac{1}{2} - \frac{\cos\left(\frac{2\pi}{3}n\right)}{2}\right) = \underline{\underline{}}$$

ZADATAK 4DIO IId) $\text{syms } t \ a;$

$$E_1 = \text{int}(\cos(\pi * t / 5) * \cos(\pi * t / 5), t, -a, a);$$

$$E_1 = a + (5 * \sin((2 * \pi * a) / 5)) / (2 * \pi);$$

 $\text{syms } x \ h;$

$$x = \sin((\pi / 7) * h);$$

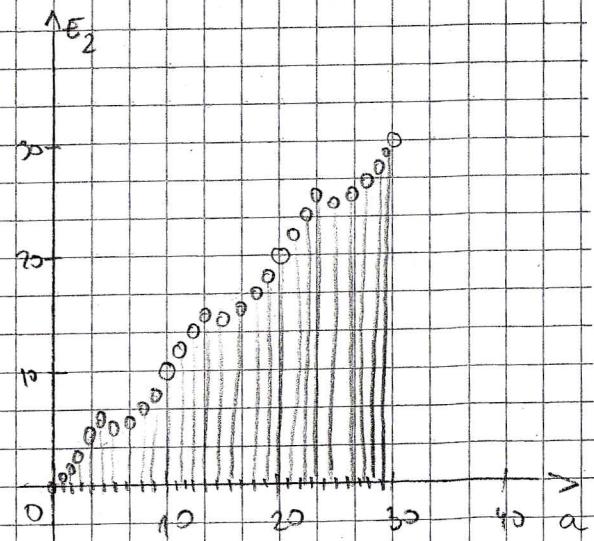
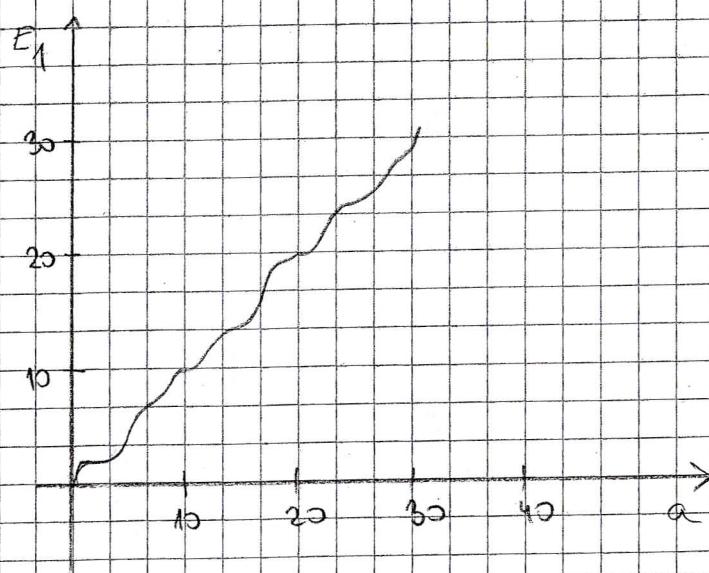
RACUNANJE ENERGIJE NA INTERVALU $[-a, a]$ function $E_2 = \text{energija}(a)$ for $i = -a : a$

$$E(i) = (\sin(\pi * i / 7))^2;$$

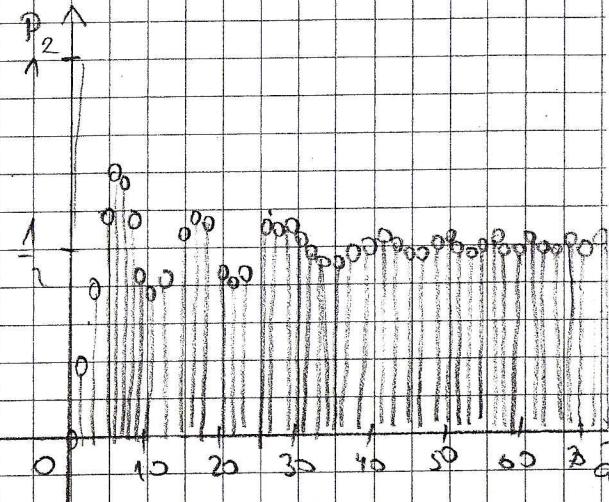
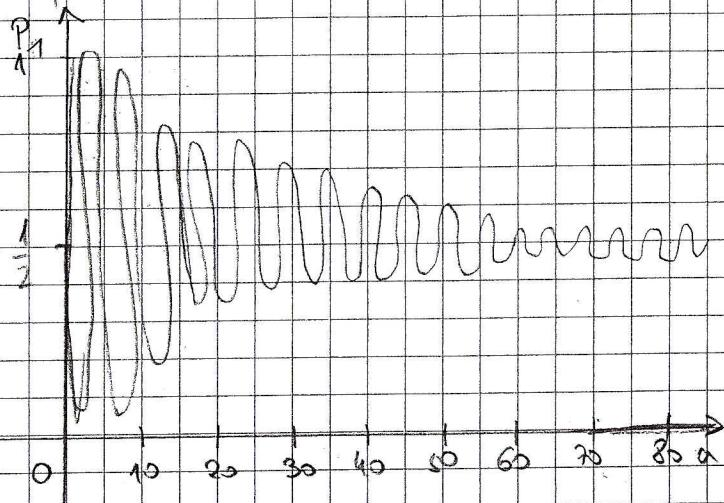
end

$$E = \text{sum}(E);$$

end



Energija signala raste zavisno sa parametrom a jer je signal periodičan stoga ako $a \rightarrow \infty$ onda: $E \rightarrow \infty$



Kako je parametar a povećava tako se signal izdvaja tj.

teži prema $\frac{1}{2}$. Očekujem da kada $a \rightarrow \infty$ da snaga signala iznosi $\frac{1}{2}$.

ZADATAK 5

Vremenski kontinuiran Fourierov red (CTFS)

ANALIZA:

$$X_k = \frac{1}{T_0} \int_{T_0} x(t) \cdot e^{-j\omega_0 k t} dt, \text{ where}$$

$x(t)$ - signal

t - razina vremena signal-a (vreme)

X_k - spektral

k - koeficijen vrednosti spektra (red harmonika)

T_0 - period signal-a

SINTEZA:

$$x(t) = \sum_{-\infty}^{\infty} X_k e^{j\omega_0 k t}$$

$e^{j\omega_0 k t}$ - kompleksna eksponentijska

$$x(t) = 110 \sin(120\pi t) + 50 \cos(360\pi t + \frac{\pi}{3})$$

$$\begin{aligned} T_1 &= \frac{2\pi}{120\pi} = \frac{1}{60} \\ T_2 &= \frac{2\pi}{360\pi} = \frac{1}{180} \end{aligned} \quad T_0 = 2 \cdot \frac{1}{60} = \frac{1}{30} \text{ s} \quad \omega_0 = \frac{2\pi}{T_0} = 60\pi \text{ rad/s}$$

$$\begin{aligned} 110 \sin(120\pi t) &= \frac{110}{2j} (e^{j2\omega_0 t} - e^{-j2\omega_0 t}) = -j55(e^{j2\omega_0 t} - e^{-j2\omega_0 t}) \\ &= 55e^{-j\frac{\pi}{2}} e^{j2\omega_0 t} + 55e^{j\frac{\pi}{2}} e^{-j2\omega_0 t} \end{aligned}$$

$$\begin{aligned} 50 \cos(360\pi t + \frac{\pi}{3}) &= 25 (e^{j6\omega_0 t + j\frac{\pi}{3}} + e^{-j6\omega_0 t - j\frac{\pi}{3}}) = \\ &= 25e^{-j\frac{\pi}{3}} e^{j6\omega_0 t} + 25e^{j\frac{\pi}{3}} e^{-j6\omega_0 t} \end{aligned}$$

$$x(t) = 55 e^{-j\frac{\pi}{2}} e^{j120\pi t} + 55 e^{j\frac{\pi}{2}} e^{-j120\pi t} + 25 e^{j\frac{\pi}{3}} e^{j360\pi t} + 25 e^{-j\frac{\pi}{3}} e^{-j360\pi t}$$

$$x(t) = \sum_{k=-\infty}^{\infty} x_k e^{jk\omega_0 t}$$

$$k=2 \rightarrow x_2 = 55 e^{-j\frac{\pi}{2}}$$

$$k=-2 \rightarrow x_{-2} = 55 e^{j\frac{\pi}{2}}$$

$$k=6 \rightarrow x_6 = 25 e^{j\frac{\pi}{3}}$$

$$k=-6 \rightarrow x_{-6} = 25 e^{-j\frac{\pi}{3}}$$

ostali koeficijenti su 0

b) RACUNANJE CTF-a

syms t T0 k;

$$x = 110 * \sin((4 * \pi * t) / T_0) + 50 * \cos(12 * \pi * t / T_0 + \pi / 3);$$

$$F_k = \text{int}(x * \exp(-2 * \pi * j * k * t / T_0), -T_0 / 2, T_0 / 2) / T_0;$$

$$F_k = \text{subs}(F_k, T_0, 1/30);$$

$$\begin{aligned} F_k = & -(\sin(\pi * k) * ((k * 1) / 2 - 3 * 3^{1/2}) * 50 * i) / (\pi * (k^2 - 36)) \\ & (30 * (\sin(2 * \pi * k) * 11 * i) / 3 - (22 * \sin(\pi * k)^2 / 3 * \\ & \sin(\pi * k) * i + 2 * \sin((\pi * k) / 2)^2 * (-1))) / (\pi * (k^2 - 4)); \end{aligned}$$

c) AMPLITUDNI I FAZNI SPECTR

$$A = \text{zeros}(1, 51);$$

for n = -25 : 25

$$A(n+26) = \text{subs}(\text{Limit}(F_k, k, n));$$

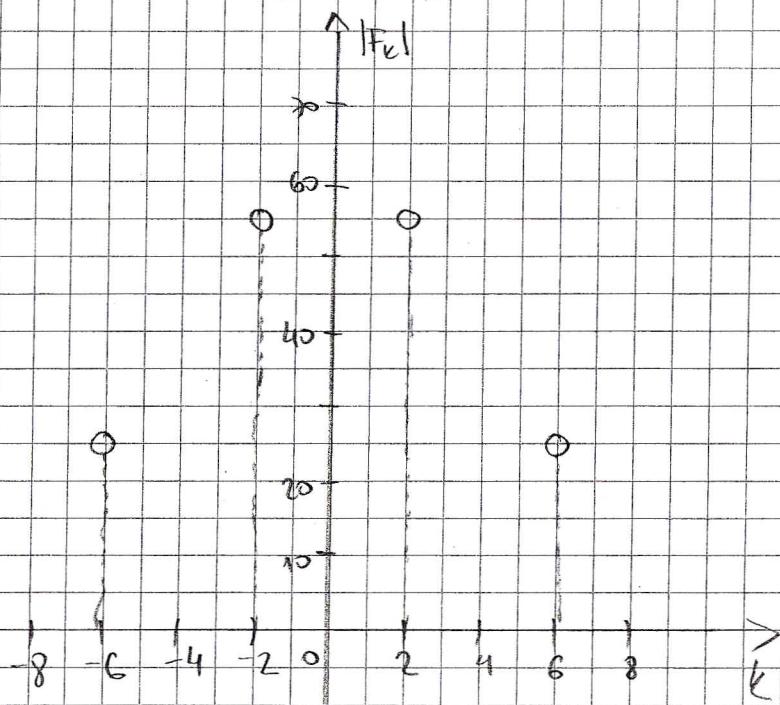
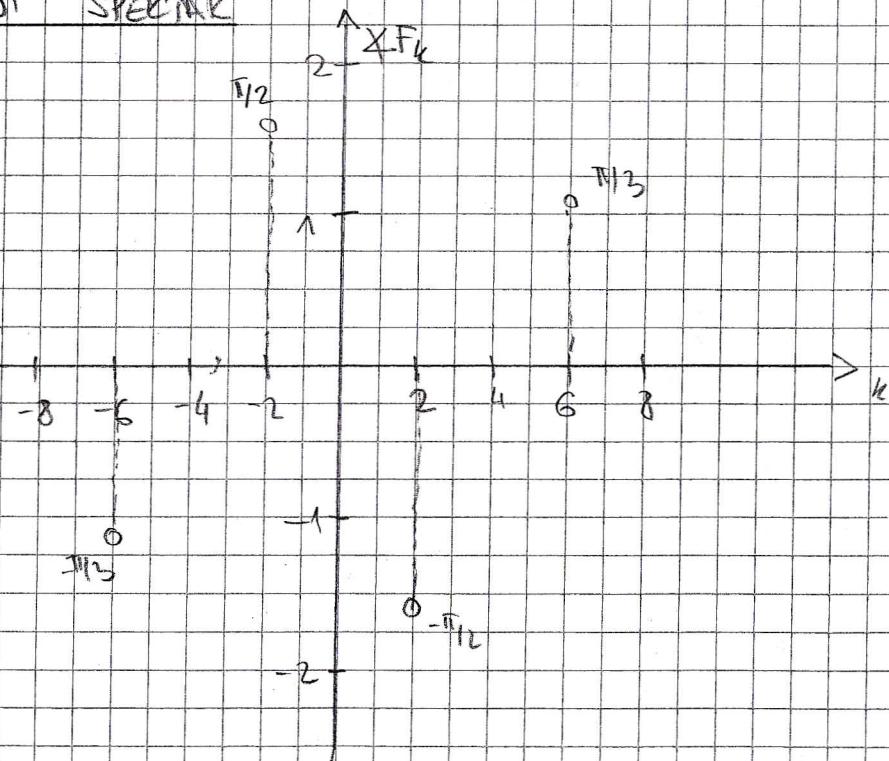
end

$$\text{stem}(F[25:25], \text{abs}(A));$$

$$\text{stem}([-25:25], \text{angle}(A));$$

ZADATAK 5

DIO I

AMPLITUĐNI SPECTARFAZNI SPECTAR

ZADATAK 6

SPEKTRALNA GUSTOĆA SNAGE (CTFS)

$$P = \frac{1}{T_0} \int_{T_0}^{\infty} |x(t)|^2 dt = \sum_{k=-\infty}^{\infty} |X_k|^2$$

$x(t)$ - signal

t - vremenska varijabla signala (vreme)

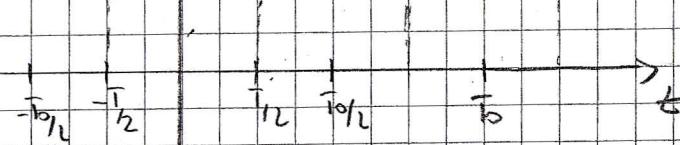
X_k - spektar

k - vremenska varijabla spektra (real harmoni)

T_0 - period signala

$$\uparrow x(t)$$

a)



$$X_k = \frac{1}{T_0} \int_{-\frac{T_0}{2}}^{\frac{T_0}{2}} e^{-j\omega_b k t} dt = \frac{1}{T_0} \left(\frac{1}{-j\omega_b k} e^{-j\omega_b k t} \Big|_{-\frac{T_0}{2}}^{\frac{T_0}{2}} \right) =$$

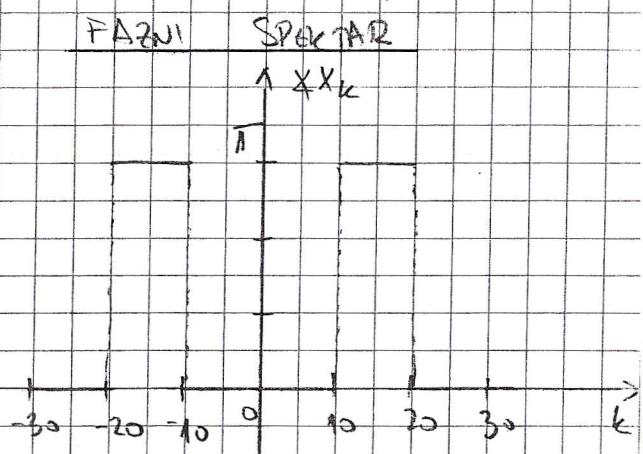
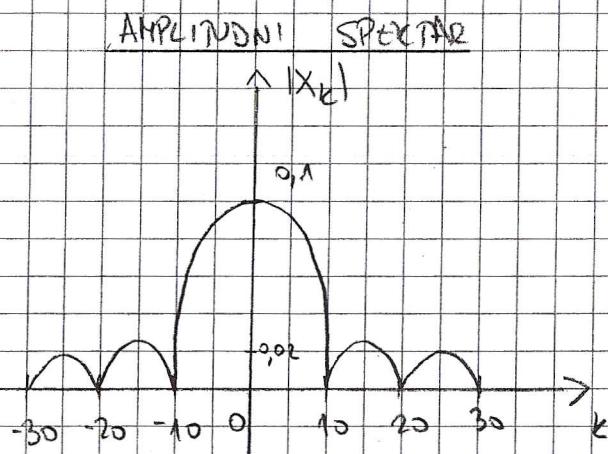
$$= -\frac{1}{j\omega_b k} \left(e^{-j\omega_b k \frac{T_0}{2}} - e^{+j\omega_b k \frac{T_0}{2}} \right) = \frac{\sin(\omega_b k \frac{T_0}{2})}{k \pi}$$

$$= \frac{\sin\left(\frac{2\pi}{T_0} \cdot k \cdot \frac{1}{2}\right)}{k \pi} = \frac{\sin \frac{\pi k T}{T_0}}{k \pi} = \frac{1}{T_0} \cdot \frac{\sin \frac{\pi k T}{T_0}}{\frac{\pi k T}{T_0}}$$

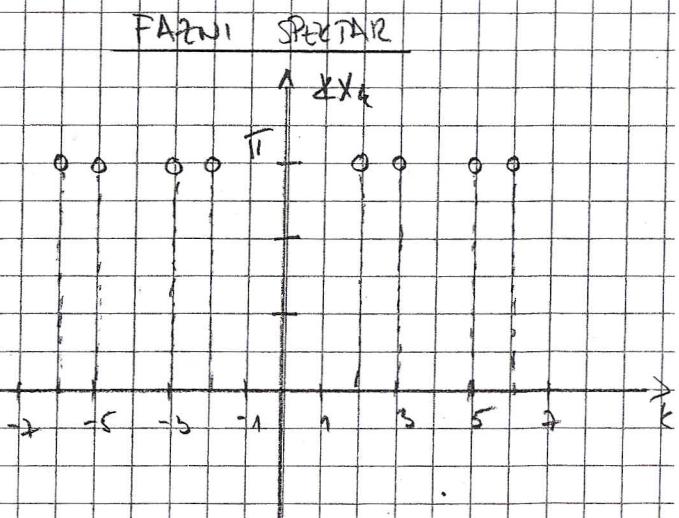
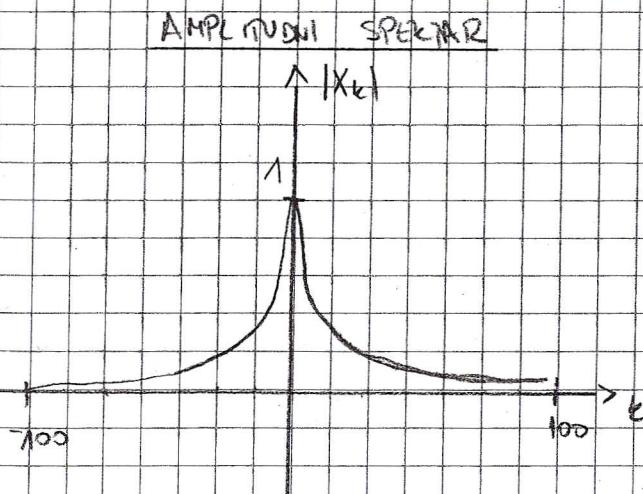
$$b) X_k = \sin((\pi * T * k) / b) / (\pi * k)$$

Matlabovo výsledný soubor s rezultátem je a) požadován.

$$c) X_k = \frac{\sin \frac{k\pi}{10}}{k\pi}$$



$$X_k = \frac{\sin \frac{2k\pi}{3}}{k\pi}$$



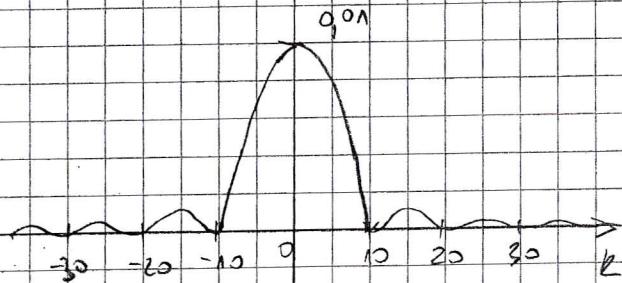
ZADATAK 6II Dio

c)

$$x_k = \frac{\sin \frac{k\pi}{10}}{k\pi}$$

SPEKTRALNA GUSTOĆA

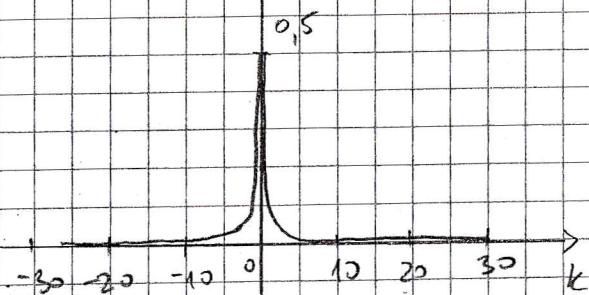
$$\uparrow |x(k)|^2$$

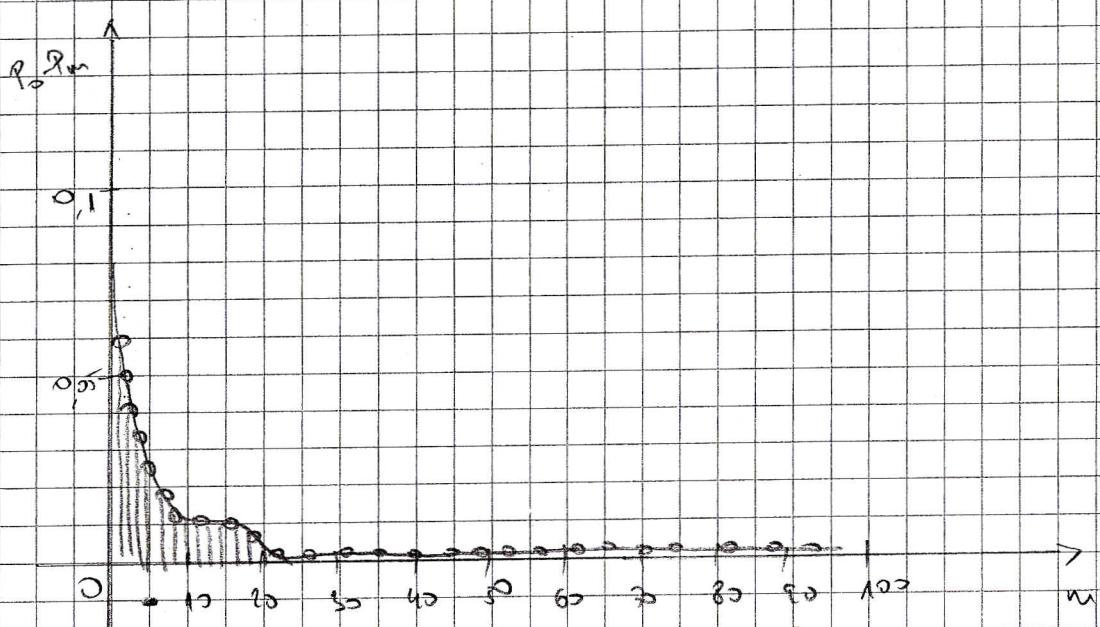
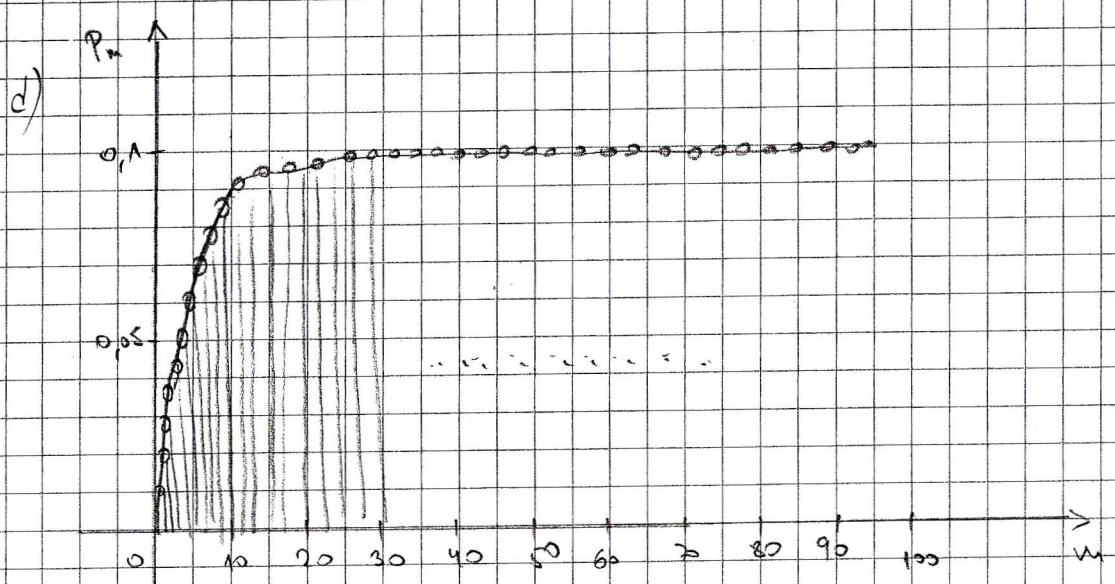


$$x_k = \frac{\sin \frac{2k\pi}{2}}{k\pi}$$

SPEKTRALNA GUSTOĆA

$$\uparrow |x(k)|^2$$





Kada $m \rightarrow \infty$ tada raspodela snaga je vi približno ϕ .

ZADATAK 7

Vremenski kontinuirana fourierova transformacija (CTFT)

ANALIZA:

$$X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt, \quad t, \omega \in \mathbb{R}$$

$x(t)$ - signal

t - vremenska varijabla signala (vrijeme)

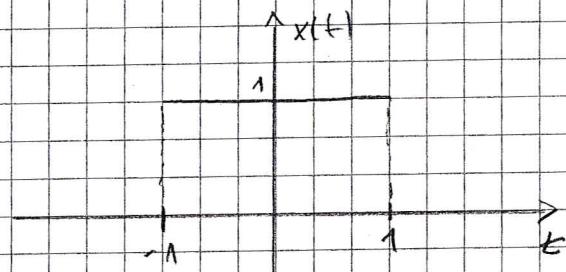
$X(j\omega)$ - spektar

ω - vremenska varijabla spektra (muzna frekv.

SINTEZA:

$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega, \quad t \in \mathbb{R}$$

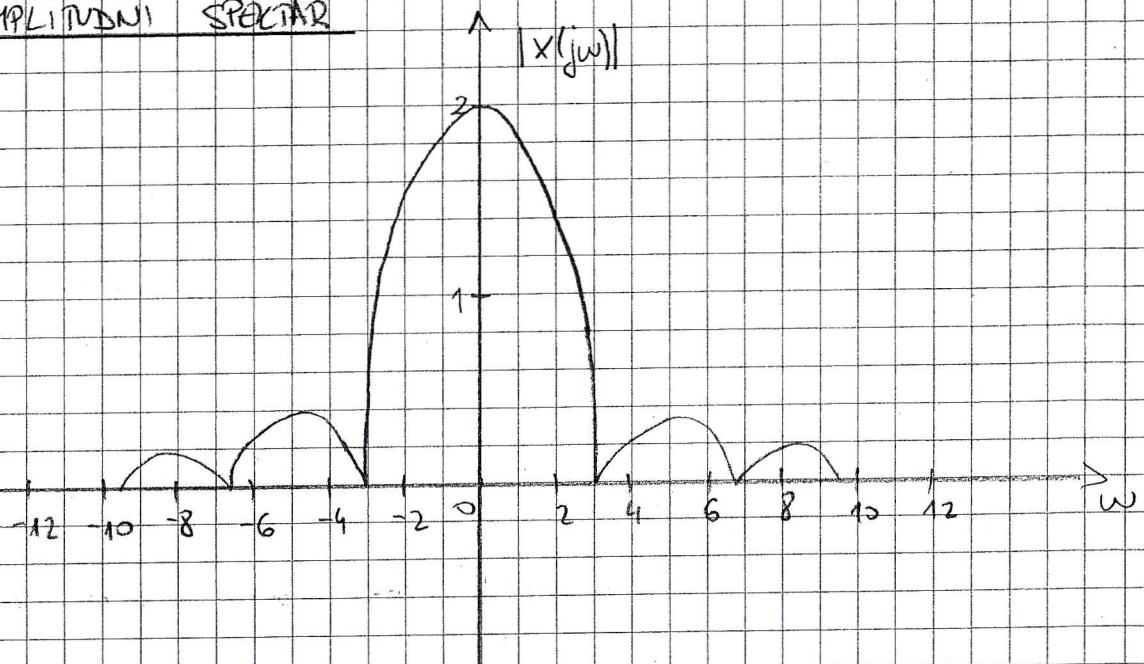
a)



$$\begin{aligned} X(j\omega) &= \int_{-1}^1 e^{-j\omega t} dt = -\frac{1}{j\omega} e^{-j\omega t} \Big|_{t=-1}^1 = -\frac{1}{j\omega} (e^{-j\omega} - e^{j\omega}) \\ &= \frac{2}{\omega} \cdot \frac{e^{j\omega} - e^{-j\omega}}{2j} = 2 \frac{\sin \omega}{\omega} \end{aligned}$$

b) $X = (2 * \sin(\omega)) / \omega$

c) AMPLITUĐNI SPECTAR



FAZNI SPECTAR

$$\angle F(j\omega) = \arctg \frac{\operatorname{Im}(x)}{\operatorname{Re}(x)} = \arctg 0 = 0$$

$\angle F(j\omega)$

ω

Spektar je u 6.c diskretan (ako je način kontinuiran)

a u 7.c je kontinuiran. Oblikom su vrlo slični.

Sivine latice se razlikuju.

ZADATAK 8

DIRICHLETOV VI UVJET

Prirodan signal $\forall f \in L^1$ period T je zadovoljava Dirichletove uvjete

a) ako je apsolutno integrabilan u bilo kojem periodu T :

$$\int_0^T |f(t)| dt < \infty$$

b) ako ima konacan broj maximuma i minimuma na bilo kojoj periodi T

c) ako ima konacan broj diskontinuiteta na bilo kojoj periodi T

d) na mestu diskontinuiteta ($f(t_d^+) \neq f(t_d^-)$), signal konvergira $\frac{f(t_d^+) + f(t_d^-)}{2}$

$$x(t) = 110 \sin(120\pi t) + 50 \cos(360\pi t + \pi/3)$$

b) $\text{syms } x \quad t;$

$$x = 110 * \sin(120 * \pi * t) + 50 * \cos(360 * \pi * t + \pi/3);$$

$x = \text{fourier}(x);$

$x = \text{simplify}(x);$

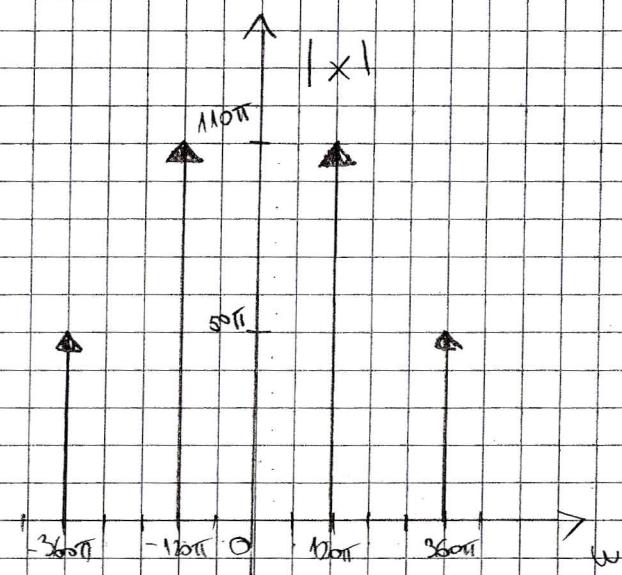
$\text{pretty}(x);$

$$110 \pi (\text{dirac}(-120\pi - w) - \text{dirac}(120\pi - w))i +$$

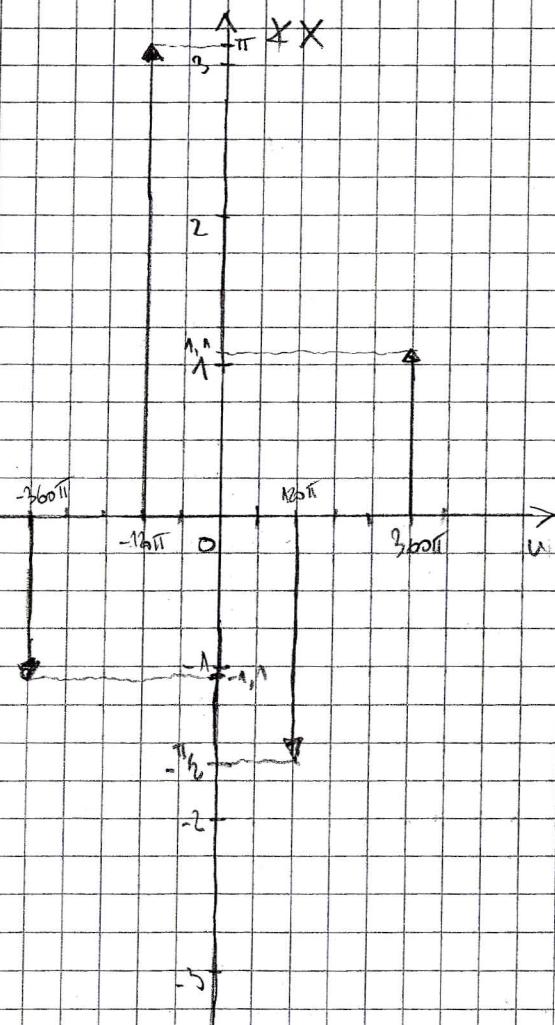
$$-50 \pi (\text{dirac}(-360\pi - w) \left(-\frac{1}{2} + \frac{3\pi^2}{2} \right) - \text{dirac}(360\pi - w) \left(\frac{1}{2} + \frac{3\pi^2}{2} \right))$$

c)

AMPLITUDNI SPECTAR



FAZNI SPECTAR



Razliky u fazii u amplitudi.

ZADATAK 9

SPEKTRALNA GUSTOĆA ENERGIJE (CFFT)

$$E = \int_{-\infty}^{\infty} |x(t)|^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} |X(\omega)|^2 d\omega$$

$x(t)$ - signal

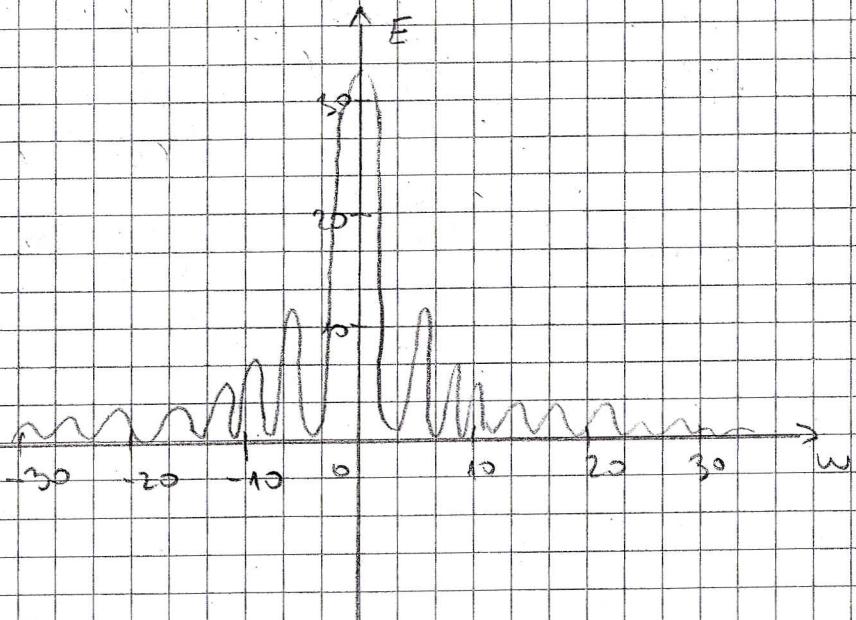
$X(\omega)$ - spekter

t - nezavisna varijabla signala (vremje)

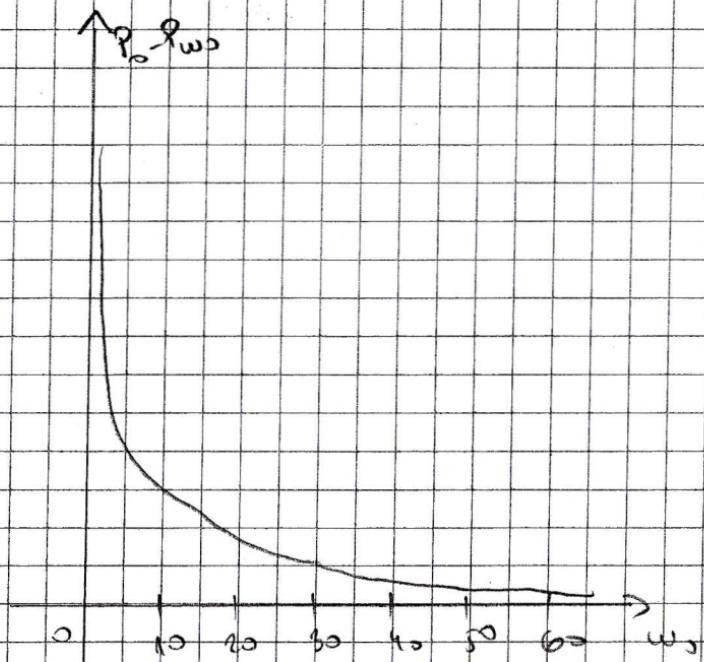
ω - nezavisna varijabla spektra (kruga frekvencija)

a)

$$X = (4 * \text{abs}(\sin(\omega))^2) / \text{abs}(\omega)^2$$



b)



Kada $w_0 \rightarrow \infty$ tada razlike siveg i zelenog

ZADATAK 10

Vremenska diskretna Fourierova transformacija (DTFT)

ANALIZA:

$$F(e^{j\omega}) = \sum_{n=-\infty}^{\infty} f(n) e^{-jn\omega}$$

$f(n)$ - signal

n - kategorija varijable signala (vrijeme)

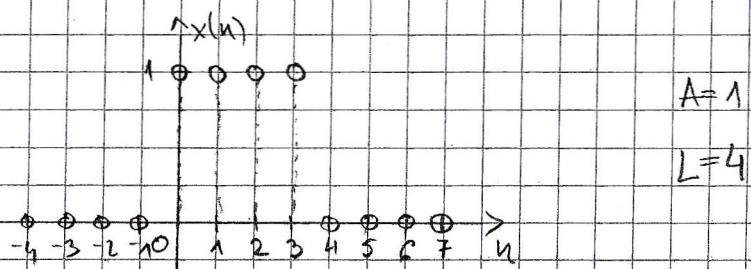
$F(e^{j\omega})$ - spektral

ω - kategorija varijable spektra (kutnica frekvencije)

SINTEZA:

$$f(n) = \frac{1}{2\pi} \int_{-\pi}^{\pi} F(e^{j\omega}) e^{j\omega n} d\omega$$

a)



$$F(e^{j\omega}) = \sum_{n=-\infty}^{\infty} f(n) e^{-jn\omega} = \sum_{n=0}^3 e^{-jn\omega} = \frac{1 - e^{-j4\omega}}{1 - e^{-j\omega}} = \frac{\sin(2\omega)}{\sin(\frac{\omega}{2})} \cdot e^{-j\frac{3}{2}\omega}$$

$$|F(e^{j\omega})| = \begin{cases} 4 & , \omega = 0 \\ \frac{\sin(2\omega)}{\sin(\frac{\omega}{2})} & \text{inace} \end{cases}$$

$$\chi F(e^{j\omega}) = \chi 1 - \frac{3}{2}\omega + \chi \frac{\sin(2\omega)}{\sin(\frac{\omega}{2})} =$$

$$b) \quad n = [1 \ 1 \ 1 \ 1];$$

$$[H, w] = \text{freqz}(n, 1);$$

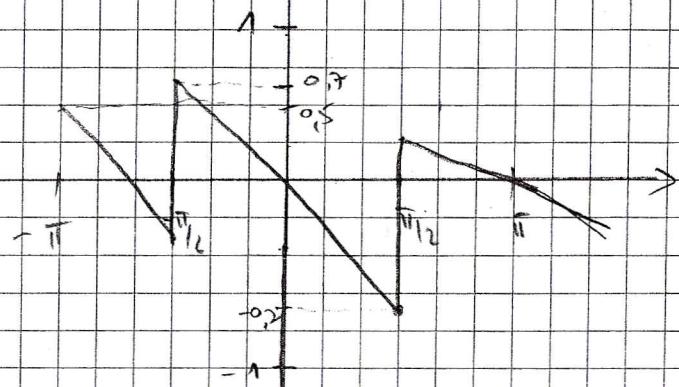
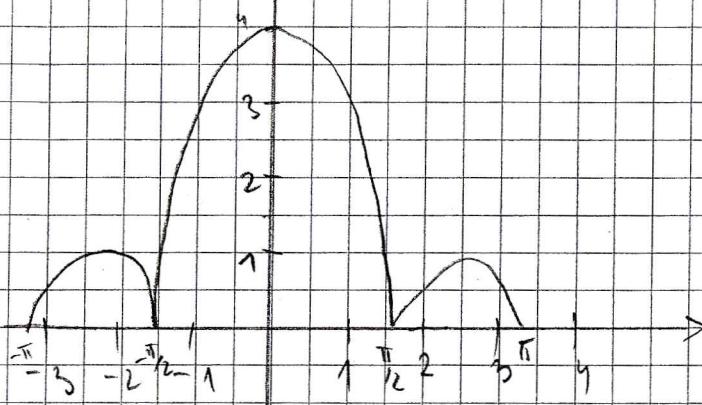
$$H = H * \exp(-j * w * 5);$$

plot (w, abs(H))

plot (w, phase(H))

$$|F(e^{j\omega})|$$

$$|F(e^{j\omega})|$$



d) Ako menjavim vrijas signala, amplitudni faktor spektar postavlja posljednji sa posebnim N-a.

e) Ako menjavim krah u kraj signal postaje tako amplitudni spektar isti isti oblik faktor spektar sive neke pozicije koli u pravac.

ZADATAK 11

SPEKTRA LNA GUSTOĆA ENERGIJE (DTFT)

$$E = \sum_{n=-\infty}^{\infty} |f(n)|^2 = \frac{1}{2\pi} \sum_{n=-\infty}^{\infty} |F(e^{j\omega})|^2$$

$f(n)$ - signal

n - natančna varijabla signala (vremena)

$F(e^{j\omega})$ - spektar

ω - natančna varijabla spektra (kutika frekvencije)

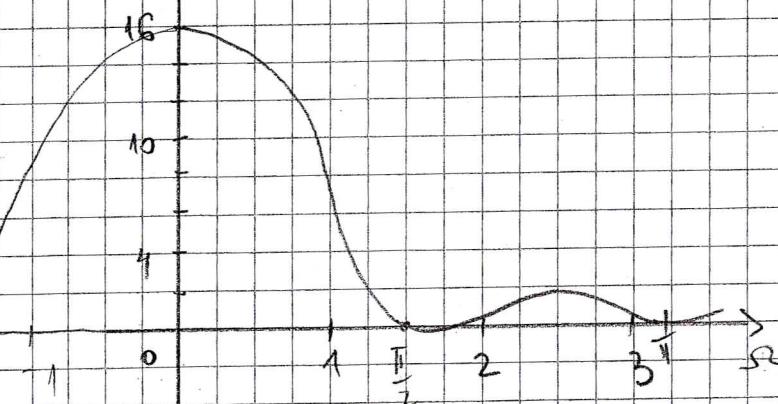
a) $n = [0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0]$,

$$[h, \omega] = f_{\text{freqz}}(n, 1);$$

$$h = H \cdot e^{-j \omega \cdot n};$$

$$\text{plot}(\omega, \text{abs}(H.^2));$$

$|F(e^{j\omega})|$



ZADATAK 12

Vremenski diskretni Fourierov red (DTFS)

ANALIZA:

$$F_k = \frac{1}{N} \sum_{n=0}^{N-1} f(n) e^{-j k \frac{2\pi}{N} n}$$

$f(n)$ - signal

n - nezamena vrednost signal (vreme)

F_k - spektar

k - nezamena vrednost spektar (real harmonika)

SINTESA:

$$f(n) = \sum_{k=0}^{N-1} F_k e^{j k \frac{2\pi}{N} n}$$

$$t = [0 : 1/8000 : 1 - 1/8000]$$

$$x = \sin(2 * \pi * 700 * t),$$

$$X = \text{fft}(x),$$

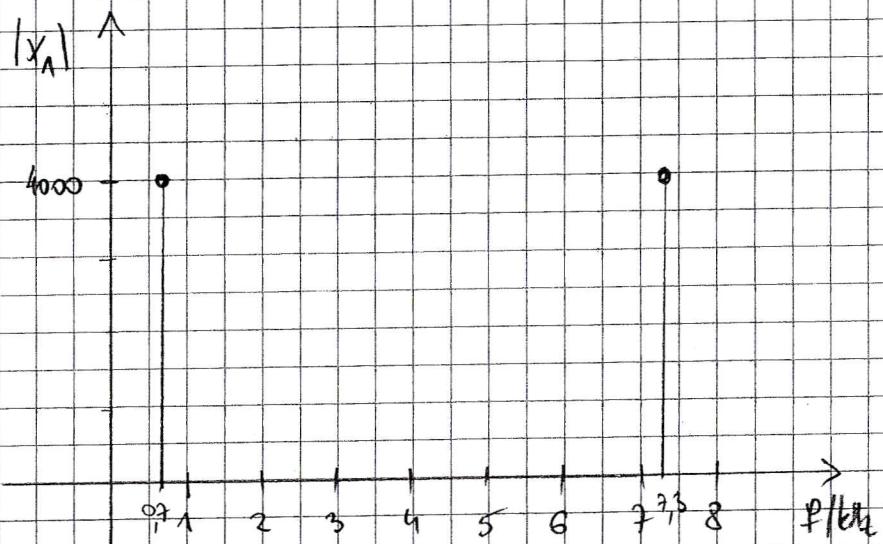
$$N = \text{length}(x),$$

$$\omega = ([1:N]-1) / N * 8000;$$

$$A = \text{abs}(X);$$

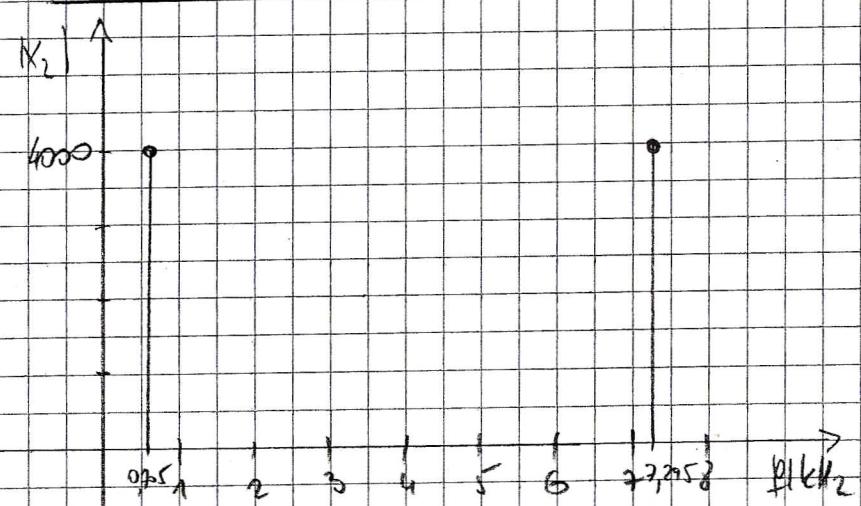
$$\text{plot}(\omega, A);$$

AMPLITUDNI SPECTAR



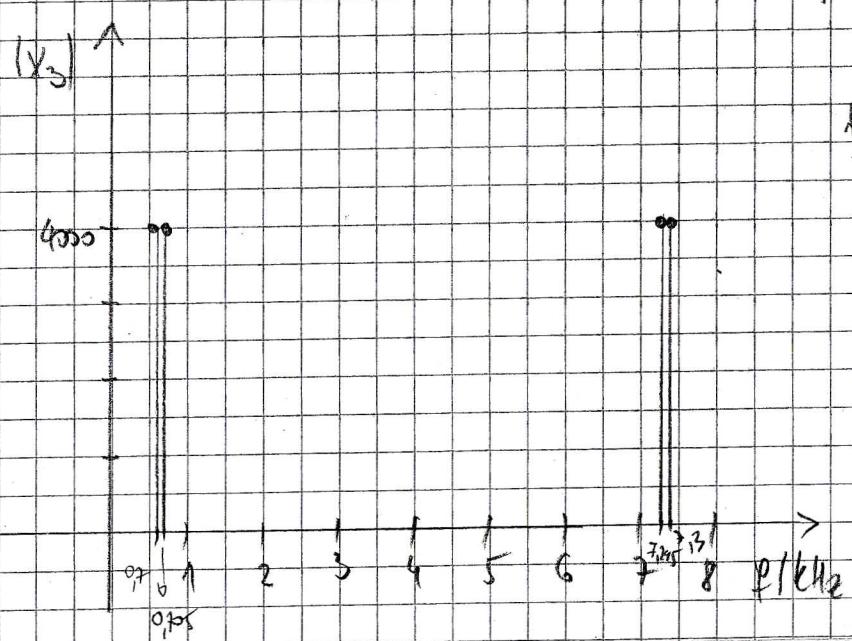
d)

AMPLITUDNI SPECTAR



e)

AMPLITUDNI SPECTAR



q) spectar e) je

dobiven zbrayanju

} superponiranjem b i d