

Name: Key Block _____ Date _____

Essential Question:

WHAT IS SLOPE?

WORDS:

The "steepness" of a line
aka "rate of change"

FORMULA:

$$\frac{\text{rise}}{\text{run}} \text{ or } \frac{y_2 - y_1}{x_2 - x_1} \text{ or } \frac{\Delta y}{\Delta x}$$

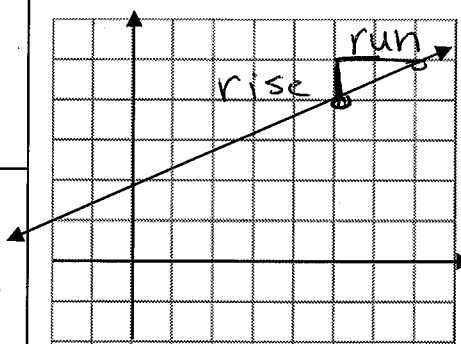
* Do the same order for "x" as you do for "y"!

ex. $(7, 3), (2, 4)$

x_1, y_1, x_2, y_2

$$\frac{4-3}{2-7} = -\frac{1}{5}$$

GRAPH:



Find the slope between the following points.

* Watch signs!

1. $(5, 2)$ and $(4, -1)$

$$\frac{-1-2}{4-5} = \frac{-3}{-1} = \boxed{3}$$

2. $(-2, 3)$ and $(4, 6)$

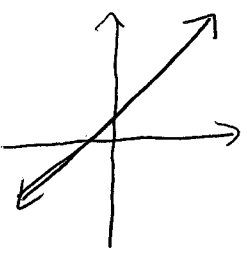
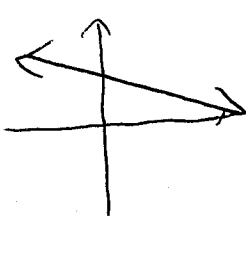
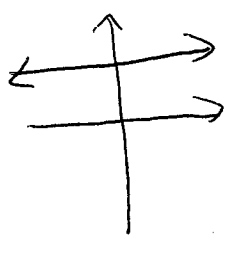
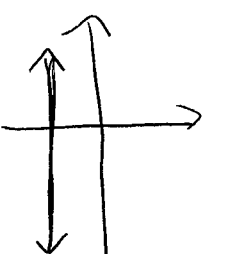
$$\frac{6-3}{4-(-2)} = \frac{3}{6} = \boxed{\frac{1}{2}}$$

3. $(4.5, 5)$ and $(.5, -3)$

$$\frac{-3-5}{.5-4.5} = \frac{-8}{-4} = \boxed{2}$$

4. $(1, 3)$ and $(3, -2)$

$$\frac{-2-3}{3-1} = \boxed{-\frac{5}{2}}$$

Types of Slopes			
			
positive (rises)	negative (falls)	horizontal (0)	vertical (undefined)

* Why ~~are~~ ^{do} vertical lines have undefined slopes?

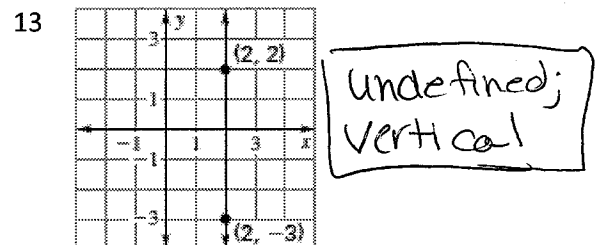
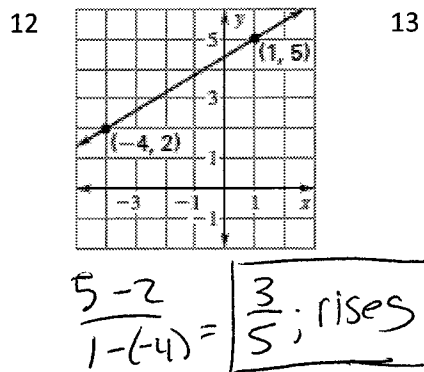
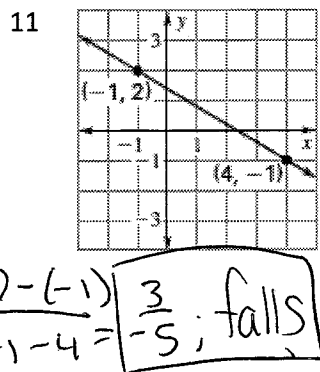
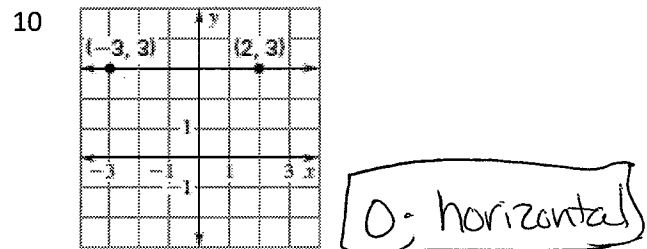
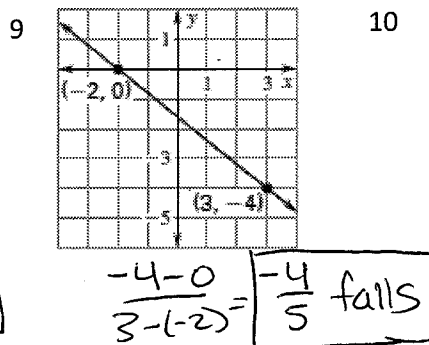
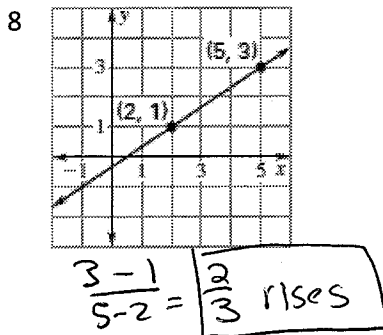
Find the slope of the line that passes through the following points. Tell if it rises, falls, is 0, or undefined.

* Why do horizontal lines have a slope 0?

5) $(5, 2)$ and $(5, -2)$ $\frac{-2-2}{5-5} = \frac{-4}{0}$ undefined Vertical line	6) $(0, 4)$ and $(-3, 4)$ $\frac{4-4}{-3-0} = \frac{0}{-3} = 0$ horizontal line	7) $(0, 6)$ and $(0, -4)$ $\frac{-4-6}{0-0} = \frac{-10}{0} = \text{undefined}$ Vertical line
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Finding slope from a graph:

Find the slope of the line in the following graphs:

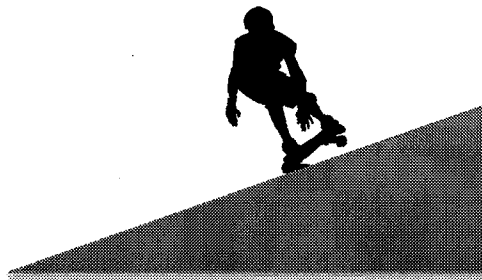


Rate of Change

Slope can be used to represent an average rate of change.

Example 1: A skateboard ramp has a rise of 15 inches and a run of 54 inches. What is its slope?

$$\frac{15}{54} = \frac{5}{18}$$



Example 2: One afternoon your family goes out to pick strawberries. At 1:00 p.m., your family has picked 3 quarts. Your family finishes picking at 3:00 p.m. and has 28 quarts of strawberries. At what rate is your family picking strawberries?

$$\begin{array}{l} (1, 3) \\ (3, 28) \end{array} \quad \begin{array}{l} \text{qts} \\ \text{hr} \end{array} \quad \frac{28-3}{3-1} = \frac{25}{2} \quad 25 \text{ qts} / 2 \text{ hrs} \rightarrow \boxed{12.5 \text{ qts/hr}}$$

Example 3: Kevin's savings account balance changed from \$1,140 in January to \$1,450 in April. Find the average rate of change per month. Round your answers to the nearest dollar. (Let $x = 1$ represent January).

$$\begin{array}{l} (1, 1140) \\ (4, 1450) \end{array} \quad \begin{array}{l} \text{Change} \\ \text{month} \end{array} = \frac{1450-1140}{4-1} = \frac{310}{3} \approx \boxed{\$103/\text{month}}$$

Example 4: John would like to know how much he saved per month last year. In January, his savings account balance was \$300. A year later, in December, his savings account balance was \$1,500. What is the rate of change of John's account per month? (Let $x = 1$ represent January)

$$\begin{array}{l} (1, 300) \\ (12, 1500) \end{array} \quad \begin{array}{l} \text{Change} \\ \text{month} \end{array} = \frac{1500-300}{12-1} = \frac{1200}{11} \approx \boxed{\$109 \text{ per month}}$$

