

Intermediate code generation + Three-address code

ICG \rightarrow platform Independent

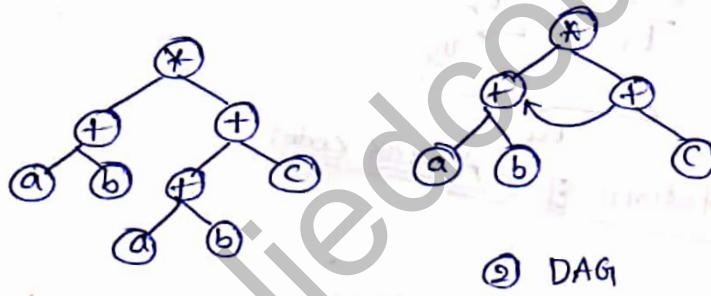
Purpose of ICG is to improve the efficiency of the code generation.

For Evaluating an arithmetic expression, we are having 4-different strategies. one of them is the Syntax tree.

Syntax tree(8) Abstract Syntax Trees are one of the ways to represent the ICG.

Second one is Disjointed Acyclic graphs.

Ex: $(ab+c) * (ab+bc)$



① Syntax tree

② DAG

Another form is postfix notation.

③ $ab+ab+bc+*$

④ Another form of representing the Intermediate Code is the Three-address code.

The IAG (Intermediate code generator) will take the output of Semantic Analysis and produce the output in any of the mentioned ways.

The most popular way of representing the Intermediate Code is
3-address code format.

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$$(a+b) * (a+b+c)$$

$$t_1 = a+b$$

$$t_2 = a+b$$

$$t_3 = t_2 + c$$

$$t_4 = t_1 * t_3$$

In 3-address code format we have atmost three addresses in any expression. We will introduce the temporary variable to store the intermediate results.

$$\frac{(a+b)}{t_1} * \frac{(a+b+c)}{t_2}$$

$$t_3$$

$$t_4$$

Representations of 3-Address code!

$$① x = a + b * c$$

Temporary Variable t_1 $t_1 = a + b$ $t_2 = t_1 * c$ $x = t_2$
Address 1 Address 2
Atmost 3-addresses

We can have 2-addresses also, as in 3-address code format we have atmost 3-addresses in an expression. Assignment operations also represented in 3-address format.

three address code in 3 ways.

We can represent the

① Quadruply

② Triply

③ Indirect Triply

① Quadruply:

t_1	b	c	*
t_2	a	t_1	+
2	-	t_2	=

R A₁ A₂ op

Every operation will be represented with 4 values.

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$$t_1 = b*c$$

$$t_2 = a*t_1$$

$$x = t_2$$

As we have only one address in the operation

A₁ is Empty.

② Triple: No temporary variables in case of Triples.

①	b	c	*
②	a	①	+
③	x	②	=

The result of operation $b*c$ will be stored in the memory location ①.

Instead of the temporary variable we will directly use the memory location (①) address.

③ Indirect Triple:

(101)	b	c	*
(102)	a	(101)	+
(103)	x	(102)	=

pointers

reuse computations.

(104) y (101) +

We are storing the result of computation explicitly in the memory locations. We can reuse the same code when ever required at different location.

Types of 3-Address Code:

① $A_2 \\ x = y \quad op \quad A_2$

$x = op y$

③ $x = y$

④ $x = *y$

⑤ $x = f y$

⑥ $x = a[i]$

⑦ $a[i] = x$

⑧ Goto L

⑨ if (expr) Goto L

⑩ $y = f(x_1, x_2, \dots, x_n)$

$$\textcircled{1} \quad x = y \text{ op } z$$

$A_3 \quad A_1 \downarrow A_2$
operator

we can represent with 3-address format

$$\textcircled{2} \quad x = \text{op } y \rightarrow x = -2 \text{ unary operation also represented}$$

with 3-address code.

$$\textcircled{3} \quad x = y \quad \begin{matrix} \text{Simple} \\ \text{Assignment operation. It is also represented.} \end{matrix}$$

$$\textcircled{4} \quad x = *y \quad \begin{matrix} \text{Unary operation} \end{matrix}$$

$$\textcircled{5} \quad x = &y \quad \begin{matrix} \text{Address of } y. \text{ Unary operation.} \\ A_1 \quad A_2 \end{matrix}$$

$$\textcircled{6} \quad x = a[i] \quad \begin{matrix} \text{Addresses} \\ A_1 \quad A_2 \downarrow A_3 \end{matrix} \quad \begin{matrix} \text{Value at index } i \text{ will be assigned to variable } x. \end{matrix}$$

$$\textcircled{7} \quad a[i] = x$$

$\downarrow \quad \downarrow \quad \downarrow$

$A_1 \quad A_2 \quad A_3$



a represents the base (0) starting address of the array.
We can represent with 3-address code.

We can represent with 3-address code.

$$\textcircled{8} \quad \text{Goto } L \rightarrow \text{unconditional jump}$$

\downarrow
operation Address

$$\textcircled{9} \quad \text{If } (\text{expr}) \text{ Goto } L$$

$\downarrow \quad \downarrow$
Address

Expression needs to be evaluated and stored in the memory location
if
Address

$$\textcircled{10} \quad y = f(x_1, x_2, x_3, \dots, x_n) \rightarrow N^0$$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $A_1 \quad A_2 \quad A_3 \quad A_n$

More than 3-addresses are in the expression. We may not represent with 3-addresses.

Example for the 3-address Code:

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$$\textcircled{1} \quad x = \frac{a-b-c+d}{e}$$

$$t_1 = a-b$$

$$t_2 = t_1 - c$$

$$t_3 = d/e$$

$$t_4 = t_2 + t_3$$

$$x = t_4$$

All are valid 3-address
format instructions (8) operations.

\textcircled{2} \quad \begin{aligned} \text{int } x &= 1; \\ \text{int } y &= 2; \\ \text{int } z &= x+y; \\ \text{print } z; \end{aligned}

\downarrow
 $x=1 \rightarrow$ valid 3-address code.

$y=2$

$z=x+y$

goto L:

L: print(z)

We can represent indifferent ways. One of the possible ways we have written the 3-address code.

\textcircled{3} \quad \begin{aligned} \text{if } (x > y) \\ \text{print("TOC")} \\ \text{else} \\ \text{print("CD")} \end{aligned}

- ① if ($x > y$) goto L5 Conditional jump
- ② L1: print("CD")
- ③ goto ⑤
- ④ L5: print("TOC") unconditional jump.
- ⑤ EXIT / END

(4) `for(int i=1; i<=10; i++)
 {
 int x=2*i;
 print(x);
 }`

We can represent the for loop with the valid 3-address code format.

- Initialization ① $i = 1$
 checking the condition. → ② if ($i > 10$) goto ⑨ : conditional jump if Condition is True then goto ⑨ END/EXIT program.
 perform the operation → ③ $x = 2 * i$ → valid 3-address code.
 ④ Goto L → unconditional jump
 ⑤ L: print(x)
 increment of i value ⑥ $t = i + 1$ } → valid 3-address code.
 ⑦ $i = t$
 ⑧ goto ② → unconditional jump
 ⑨ END/EXIT
- ↳ Loop need to be iterated for the second time followed by 3rd time... .

code optimizer and code generator take the 3-address code and check for the possible optimizations and then generate machine code.

Runtime Environment:

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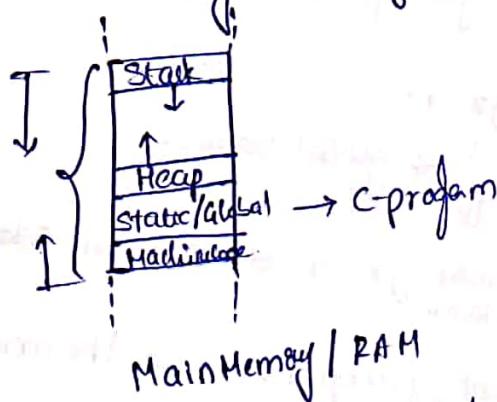
(4)

We can think of Runtime Environment as the support we get from operating system while executing the program.

OS

Code \rightarrow CD \rightarrow HLL

The generated HLL code will be stored in machine code area.



When stack size increases, heap will be allocated in the bottom of the memory.

Operating system needs to allocate the memory in Main memory to our program/code and static/global variable will also be stored in the code area.

External Libraries (DLLs) may not be available through out the program execution.

Operating system will not allow the whole memory to a single process. Whenever we call a function the operating system will help to bring it available in the memory with the help of Linker.

Stack area will help us to store the information related to function calls.

Heap is used for dynamic memory allocation. In C programming we will use the functions like malloc and calloc to dynamically allocate the memory.

Static Memory:

- variable bound to an address @ load time.
- cannot free up in between.

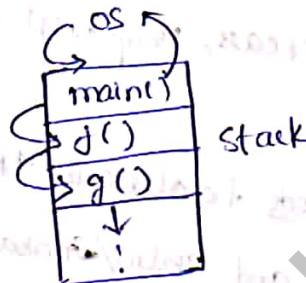
int gx=1;

↳ global variable.

↓

The variable gx is bound to an address @ load time
name

We cannot free up & remove the memory in between

Stack:

- One entry (activation record) per junction call.
- contains local variable in a junction.
- stack is used to store & track junction calls. Each entry in the stack is used to store & track junction calls.
- stack is called by an activation record.
- as itself calls main() to begin the execution of the program.
- All the variables (local variables) are also stored in the stack.

Recursion-stack

Heap: Dynamically allocate memory (calloc, malloc, free)

Operating system provides the memory for the programs which are currently in execution.

Introduction to code-optimization:

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Reducing the number of lines
makes code run-faster

→ Machine Indep & Dependant

The purpose of code-optimizer is to take
the 3-address code as an output of the

ICG (Intermediate Code Generator) and generates
the optimized (i) Reduced code.

The Reduced code can be given input to Code-generator will gener-
ate MLL code (ii) Assembly Language code. If it generates ASL code
will be given to Assembler and it will produce the MLL code.

Two kinds of optimizations

→ Machine dependant optimization. ⇒ [Intel, ARM]
→ Machine Independent optimization.

We can perform (i) optimize irrespective of micro processor,
Hardware configurations.

{ ARM
INTEL .. }

Based on microprocessor architecture, there can be some optimiza-
tions knowing machine dependant optimizations.

Loop-optimization (Machine-Independent-optimization)

In most of the programming languages we spent most of the
time in loops. (80% Approximately)

→ First, detects loops in code [program Flowgraph]

while(0)

```

    {
        x = y
    }

```

It is not a loop.

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In a program flow graph the nodes are nothing but a basic blocks.

Basic-Block!

sequence of 3-addr codes with no jumps.

↳ unconditional
↳ conditional

Eg:

```

    f = t1
    t2 = i + 1
    i = t2
  
```

No jumps in the code. Only one block exists.

Finding Basic Blocks:

Leaders: { 1st statement, target of a goto, stmt after a goto }

→ First statement of a program is always a leader

→ Target of a goto (conditional or unconditional) is also

→ Target of a goto (conditional or unconditional) is also

a leader.

→ Statement after a goto statement is also leader.

Eg:

fact(int x)

{

```

        int j = 1;
        for(i=2; i <= x; i++)
    
```

$j = j * i$

return j;

4

ICG



B1

```

    1. j = 1
    2. i = 2
  
```

→ Leader 1

B2

```

    3. if i > x goto 9 → L2
  
```

→ L2

B3

```

    4. t1 = j * i
    5. j = t1
  
```

→ L3

```

    6. t2 = i + 1
    7. i = t2
  
```

→ L3

```

    8. goto ③
  
```

B4

```

    9. Return j; → L4
  
```

① $l_1 \rightarrow$ First statement is a Leader.

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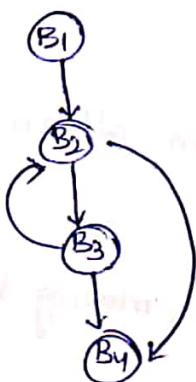
② $l_2 = \text{goto } l_3 \rightarrow$ Target of goto is a Leader

③ $l_3 = l_4 \rightarrow$ Statement after a goto is a Leader.

④ $l_4 = l_1 \rightarrow$ Statement after a goto is a Leader.

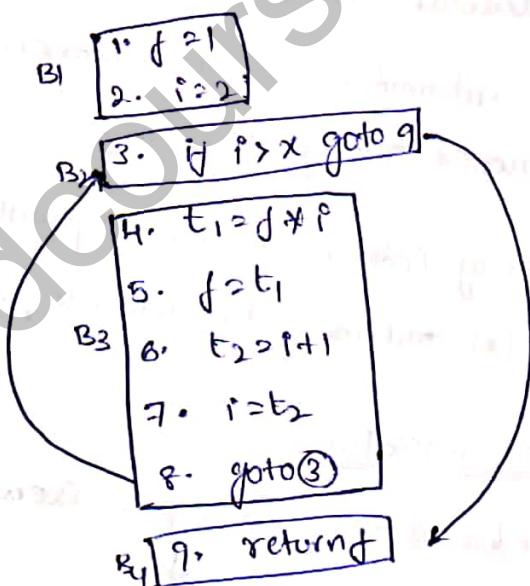
The set of statements between the Leaders are known as a basic block.

program flow graph:



All the possible flow paths in the program.

cycle \rightarrow Loop exists in our code [loop-detection]



Loop-detection Algorithm:

① Find Leaders

② Basic Blocks Construction.

③ Draw program flow graph.

④ If cycle exists in program flow graph, then loop will be there in the code.

Once we identify the loops, then we can proceed with loop-optimizations.

Loop optimization:

→ Reduce # lines of code in a loop.

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Frequency Reduction:
 $i = 0, x = 0, i;$
while($i \leq 5000$)
 $\{$
 $A = \sin(x) * i$
 $i++$

3



We have to call the function
to evaluate $\sin(x)$

The intermediate code corresponding to the function call $\sin(x)$ will
be moved out of while loop.

Lines of code inside the loop will be reduced, after moving the function
 $\sin(x)$ outside of the while loop.

Loop unrolling:

Reduce # times a loop is executed.

↓
looping is leading to more jump statements in the code.

while($i \leq 10$)
 $\{$
 $x[i] = 0$
 $i++$
 $\}$
 10 times

while($i \leq 10$)
 $\{$
 $x[i] = 0;$
 $i++;$
 $x[i] = 0;$
 $i++;$
 $\}$
 Loop 5 times
 will run for

(JCG)
 $x[0]$
 $x[1]$
 In the same loop
 two initializations
 are there

Loop Jamming!# \Rightarrow Reduce Number of LoopsEx: $\text{for } (i=0; i<10; i++)$

{

 $\text{for } (j=0; j<10; j++)$

{

 $x[i,j] = 10$ $x[i,i] = 0$ $\text{for } (i=0; i<10; i++)$

{

 $\text{for } (j=0; j<10; j++)$

{

 $x[i,j] = 10$

{

 $x[i,i] = 0$

{

 $\text{for } (i=0; i<10; i++)$ $x[i,i] = 0$

some how we reduce the number of loops.

Introduction to Code optimization - IIOther Machine Independent optimization:① Folding: $x = 2 + 3 + C + B$ $\xrightarrow[\text{Time}]{\text{Compile}}$ $x = 5 + C + B$ Fold the
Code.

As the Compiler knows it as an Integer Constant, might be able to fold the constants.

② Redundancy Elimination (DAG):

$$a = \begin{array}{c} + \\ b \quad c \end{array}$$

$$q = b + c$$

$$d = 2 + \underline{b} + 3 + \underline{c} \Rightarrow$$

$$a = b + c$$

$$d = 2 + 3 + a$$

Redundancy
EliminationFold the
Constants.

$$\boxed{d = 5 + a}$$

If the Compiler can able to identify the expression which is evaluated earlier then we can reduce the redundancy.

$$B = A * 4 \rightarrow B = A \leftarrow \downarrow \text{cheap}$$

↓
costly operation

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(4)

Algebraic Simplification:

Eliminate the Expressions like

$$a = a + 0; \quad } \text{Not much Significance}$$

$$b = b + 1; \quad } \text{of code in the program.}$$
Machine Dependant optimization:

- ① Register Allocation
- ② peephole optimization

Some of the architectures are having more number of registers and some of them are having less number of registers. As we are aware register memory access faster, we can assign the registers optimally.

Peephole optimizations:

- ⓐ Redundant Load & Store

$$a = b + c$$

$$d = a + e$$

```
mov b, r0
add c, r0
MOV R0, a
MOV a, r0
```

STORE (Redundant)LOAD

add e, r0

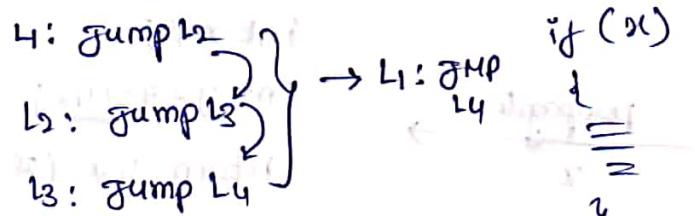
MOV R0, d

Redundant load and store

We can eliminate this kind of

Instructions.

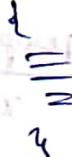
- ① Avoid jump on jump ② Eliminate dead code



We can directly move onto L4 instead of L3

define $x = 0$

if (x)



→ dead code.

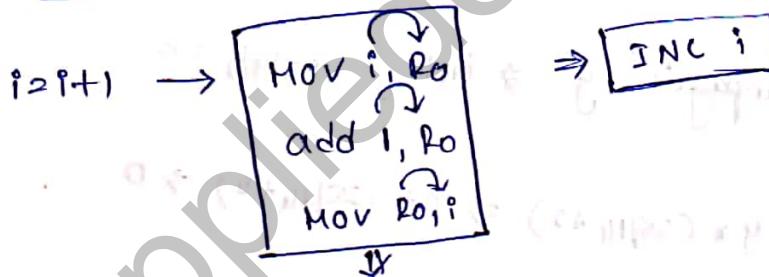
$\Rightarrow x = 0$

$i_d(0)$

$\begin{cases} 1 \\ 0 \end{cases}$ } we will never reach
to code.

We can Eliminate or Ignore the dead code
Instead of converting it into machine code.

- ③ Use machine code more appropriately:



Instead of writing all the instructions, if the microprocessor supports instruction formats like increment (INC) we can write the code with one instruction.

Data flow AnalysisConstant propagation:

```
int x=14;  
int y = 7-x/2;  
return y*(28/x+2)
```

propagate \xrightarrow{x}

```
int x=14;  
int y = 7-14/2;  
return y*(28/14+2)
```

propagate $\downarrow y$

```
int x=14  
int y=0  
return 0;
```

$x=14$
propagate $x \Rightarrow$ substitute x , wherever
 x in the code.

Now propagate $y \Rightarrow \text{int } y = 7-14/2 = 0$

$\Rightarrow y*(28/14+2) \Rightarrow 0*(28/14+2) \Rightarrow 0$

(let f() {
 int x=14;
 int y = 7-x/2;
 return y*(28/x+2);
})

After Constant propagation the function f() return '0'.

Common Subexpression Elimination (CSE):

→ Redundancy elimination is a form of CSE.

Eg: $a = b+c + g; \quad \text{---(1)}$
 $d = b+c+e; \quad \text{---(2)}$

$b+c$ is the common subexpression in both the statements.

$$\Rightarrow \begin{aligned} \text{tmp} &= b+c \\ a &= \text{tmp} + g \\ d &= \text{tmp} + e \end{aligned} \quad \left. \begin{array}{l} \text{Space will also increase due to the} \\ \text{additional temporary variables.} \end{array} \right\}$$

Tradeoff if the computational cost $>$
 if $(b+c) > \text{cost (temp creation \& fetching)}$
 then it is useful.

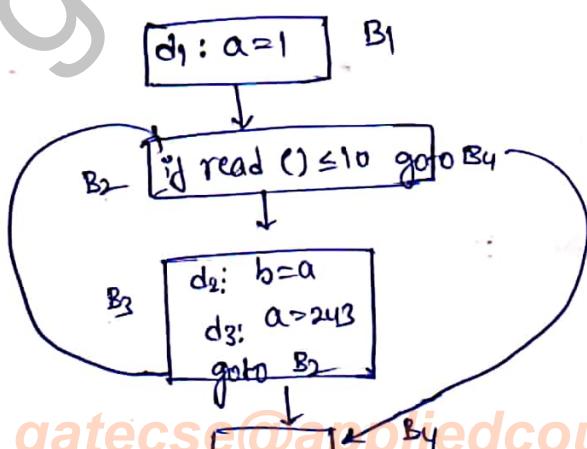
Local Common Subexpression Elimination → Within a single block
Global Common Subexpression Elimination → Entire function/procedure

Data flow Analysis → Structured graph-based analysis of the program.

Flow Graph (B) CFG (Control Flow Graph)

d_i : Definition-i

B_j : Basic Blockj



Block: vertex \square

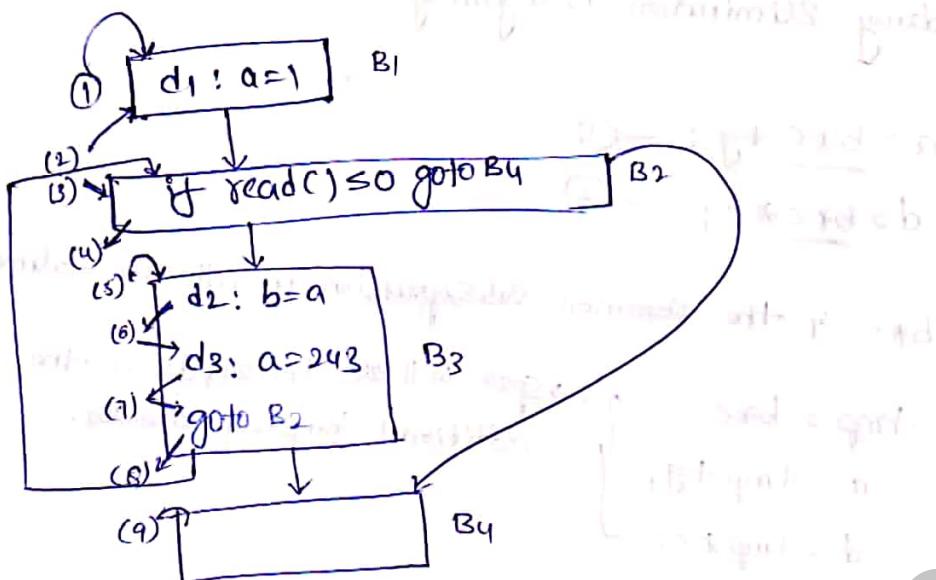
Transit: Edges
- from
(B)

Flow

In the given code, we have a total of 3 definitions

$d_1: a=1$
 $d_2: b=a$
 $d_3: a>243$

4 Basic Blocks.



(Picking B1) d_1 : "reachy point (5)"

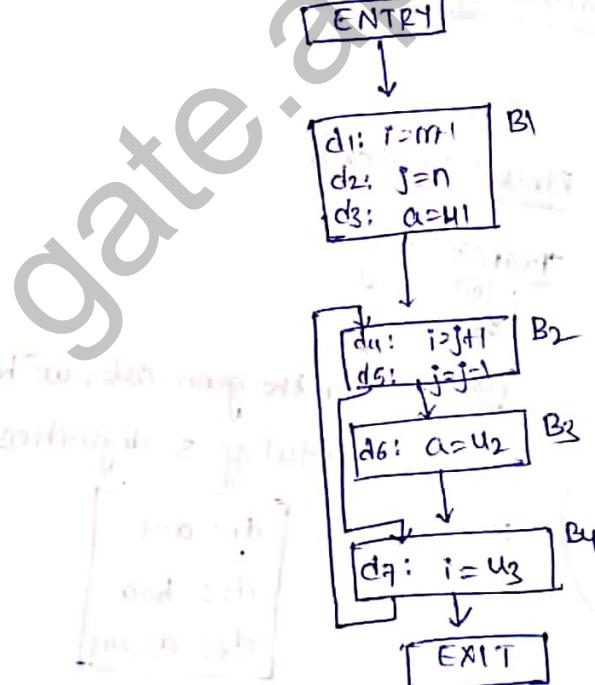
We assigned a value of \perp to a

definition d_1 reachy program point "5"

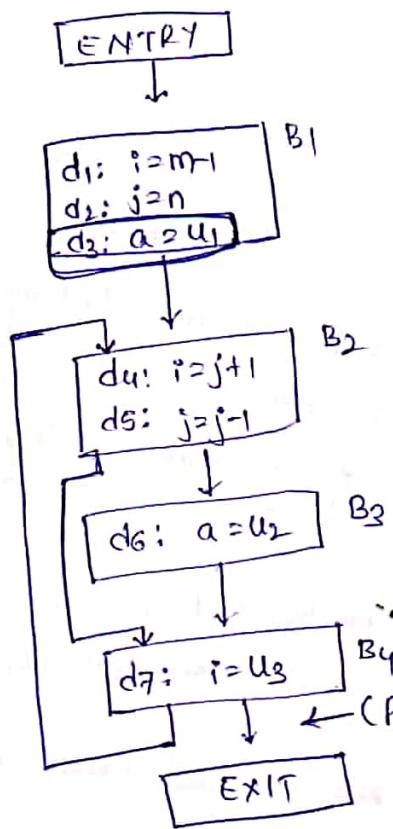
If there exist atleast one path to reach a program point

then we say d_1 reaches point "5"

Flow-Graph: We are going to introduce two more blocks in the flow graph.



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Question: Does d_3 reach end of B_4 ?↓
Conservative Analysis↓
Need to find atleast one path
to reach point P_k .

If we reach B_3 via B_2
in B_3 the definition d_3 is over.
Written by d_6 .

 $B_1 \rightarrow B_2 \rightarrow B_3$

If we follow this path
definition d_3 is not reachable at
point P_k .

 $B_1 \rightarrow B_2 \rightarrow B_4$

If we follow this path $B_1 \rightarrow B_2 \rightarrow B_4$ then the definition d_3
is reachable at point P_k .

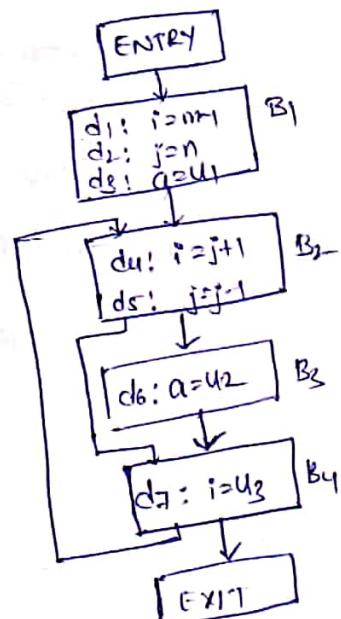
GEN(B), KILL(B):↳ Generators in Block B \rightarrow sets.↳ Kill in Block B \rightarrow bit-vector

$$GEN(B_1) = \{d_1, d_2, d_3\} \rightarrow \begin{smallmatrix} & & \\ 1 & 1 & 1 \end{smallmatrix} 0000$$

$$KILL(B_1) = \{d_4, d_5, d_6, d_7\} \rightarrow \begin{smallmatrix} & & \\ 1 & 1 & 1 \end{smallmatrix} \underbrace{111}_{111}$$

$$GEN(B_2) = \{d_4, d_5\} \quad 0001100$$

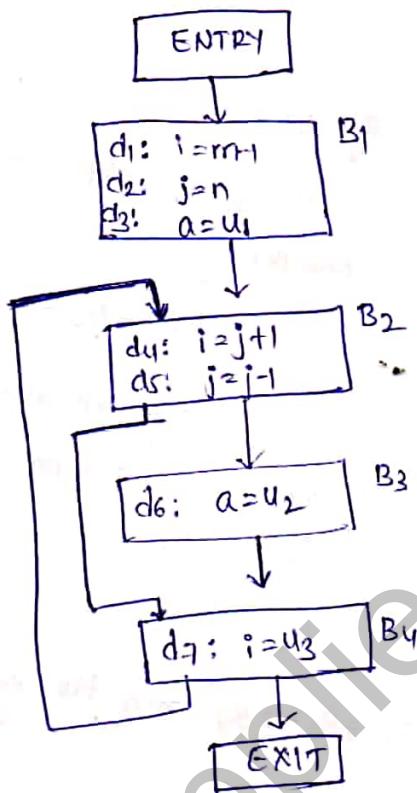
$$KILL(B_2) = \{d_1, d_2, d_3, d_7\} \quad 1100001$$



$\text{gen}(B_3) = \{d_6\} \rightarrow$ only one definition d₆.
 $\text{kil}(B_3) = \{d_3\} \rightarrow$ the value of 'a' killed by d₆.
 $d_3 \uparrow$

$\text{gen}(B_4) = \{d_7\}$
 $\text{kil}(B_4) = \{d_1, d_4\}$

IN & OUT : Sets of definitions



$\text{IN}(B_1) = \emptyset$ point of Entering into the block.
 $\text{OUT}(B_1) = \{d_1, d_2, d_3\}$
 At the time of exiting from block B₁, the definitions that we left with.

$\text{IN}(B_2) = 1110111$
 $d_1, d_2, d_3, d_5, d_6, d_7 \downarrow$

We can also enter into B₂ via B₄.

If we consider the path
 $B_2 - B_4 - B_2$

The definition d₄ is killed by d₇. so on entering into B₂ d₄ is not available.

$\text{IN}[B_2] = 1110111$

$\text{OUT}[B_2] = 001111$
 $d_3 \downarrow d_4 \downarrow d_5$

$d_1 \downarrow$ killed by d₄

$d_2 \downarrow$ killed by d₅

$\text{IN}[B_3] = 0011110$

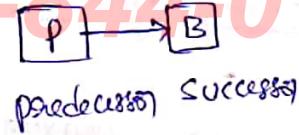
$\text{OUT}[B_3] = 0001110$

$\text{IN}[B_4] = 0011110$

$\text{OUT}[B_4] = 0010111$

Mathematically define IN and OUT

$$IN(B) = \bigcup_{P \text{ predecessor of } B} OUT(P)$$



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Eg: $IN(B_4) = OUT(B_3) \cup OUT(B_2)$

$$= 001110 \cup 001110$$

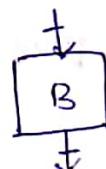
$$= 001110$$

$$OUT(B) = GEN(B) \cup [IN[B] - KILL(B)]$$

We can also write as

$$OUT_B = f_B(IN(B))$$

↓
Some function



Reaching definition Algorithm:

- ① $OUT[ENTRY] = \emptyset$;
- ② for (each basic block B other than ENTRY) $OUT[B] = \emptyset$
- ③ while (changes to any out occur)
 - ④ for (each basic block B other than Entry) {
 - ⑤ $IN[B] = \bigcup_{P \text{ predecessor of } B} OUT[P]$;
 - ⑥ $OUT[B] = gen_B \cup (IN[B] - kill_B)$;
- ⑦ }

* B gen(B) and kill(B)

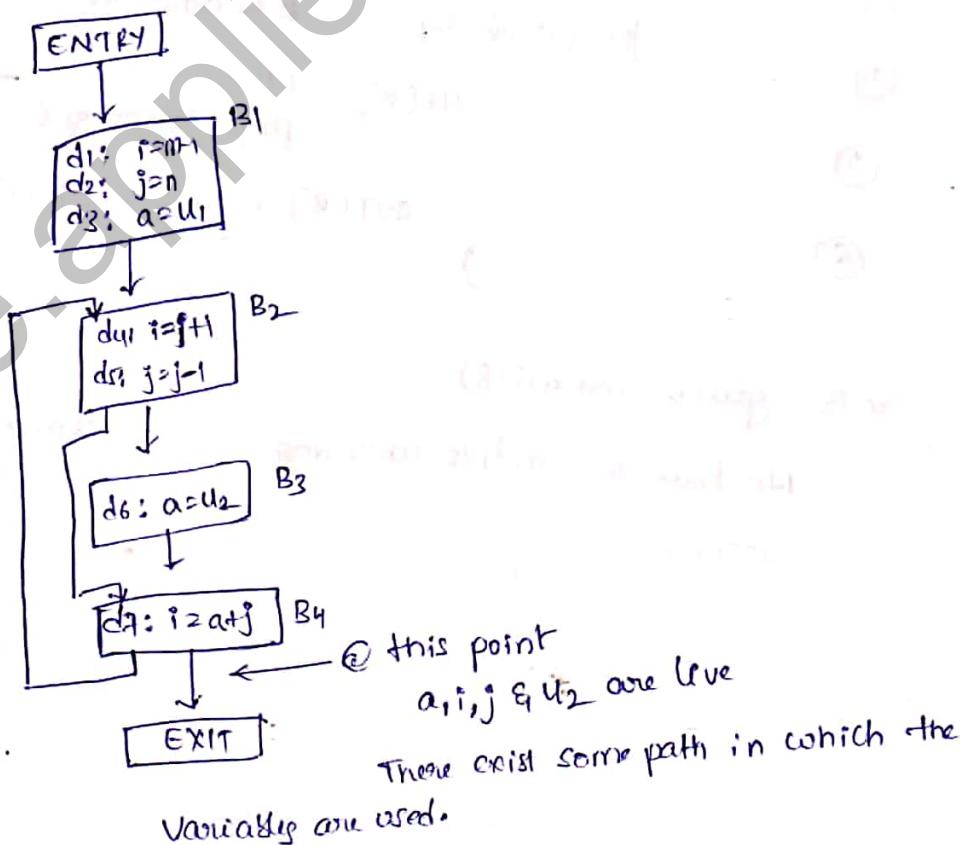
We have to run this while loop until changes to any out occurs.

- ① domain \rightarrow definitions
- ② Transfer fn \rightarrow forward: $OUT(B) = f_B(in(B))$
 $f_B(x) = \text{Gen}_B \cup (x - \text{Kill}_B)$
- ③ Meet operation $\rightarrow in(b) = \bigcup_p OUT(p)$
- ④ Boundary condition $\rightarrow OUT[\text{Entry}] = \emptyset$
- ⑤ Initial interior points $\rightarrow OUT[B] = \emptyset$

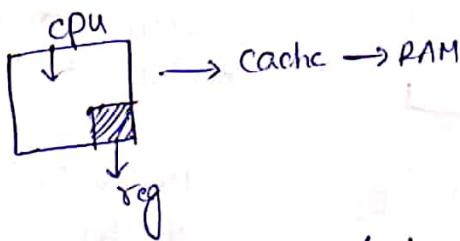
Live Variable Analysis: DFA & CFG

variable V is live @ point P if value of V is used in some path in flowgraph starting at P.
 Else it's dead.

Eg:



Live Variable Analysis



cpu can access the data, very fast in comparison with cache, RAM.
part of code-optimization.

variable that are used very often, that will be stored in Registers.

If the variables a, i, j & u_1 are preferred to store in the Registers.

DEF[B] & USE[B]:

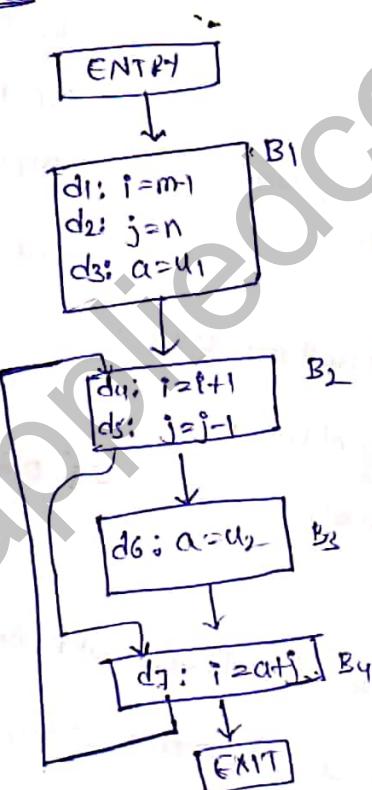
$$\begin{aligned} \text{def}(B_1) &= \{i, j, a\} \\ \text{use}(B_1) &= \{m, n, u_1\} \end{aligned}$$

sets of variable

$$\begin{aligned} \text{def}(B_2) &= \{j\} \\ \text{use}(B_2) &= \{i, j\} \end{aligned}$$

$$\begin{aligned} \text{def}(B_3) &= \{a\} \\ \text{use}(B_3) &= \{u_2\} \end{aligned}$$

$$\begin{aligned} \text{def}(B_4) &= \{i\} \\ \text{use}(B_4) &= \{a, i\} \end{aligned}$$



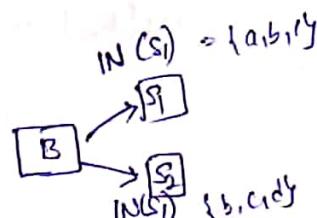
$\text{dy}(B)$ is the set of variables defined in block B , before using them.

$\text{dy}(B_2) = \emptyset$ Null set
Before defining i and j , we are using it.

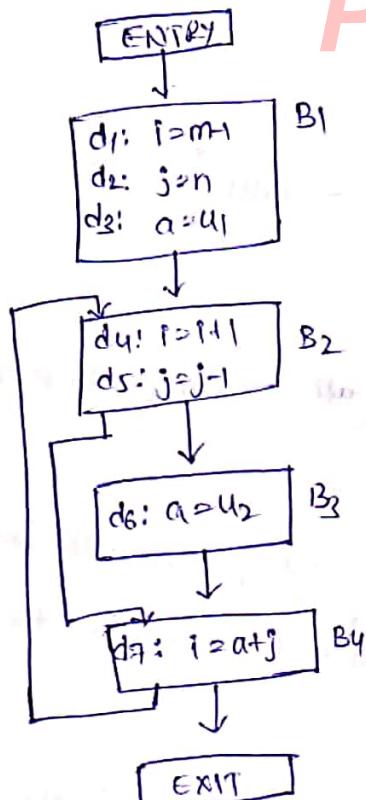
$$\text{① OUT}[B] = \bigcup_{\text{Successor of } B} \text{IN}[S]$$

$$\text{② IN}[B] = \text{USE}[B] \cup (\text{OUT}[B] - \text{DEF}[B])$$

$$\begin{aligned} &= \{c, d\} \cup \{\{a, b, l\} - \{a\}\} \\ &= \{c, d\} \cup \{b, c\} = \{a, b, c, d\} \end{aligned}$$



$$\begin{aligned} \text{path} &\rightarrow [B] \rightarrow \text{out} \\ \text{USE}[B] &= \{c, d\} \\ \text{DEF}[B] &= \{a\} \end{aligned}$$



$$IN(B_1) = \{m, n, u_1, u_2\}$$

The variables m, n, u_1 , and u_2 are used some coherently in the graph.

In $def(B_1)$ a is there, it will not present

$IN(B_1)$ as per the definition

$$IN(B_1) = USE(B_1) \cup (OUT[B_1] - DEF[B_1])$$

$$IN[B_2] = USE[B_2] \cup (OUT[B_2] - DEF[B_2])$$

$$= \{i, j\} \cup ? OUT[B_2] - \{i\}$$

$$\Rightarrow \{i, j\} \cup \{u_2, a\} = \{i, j, a, u_2\}$$

if we follow the path $B_2 - B_4 - B_2$

'a' is used.

'a' will be added to $IN[B_2]$
also

$$\begin{aligned} IN(B_1) &= \{m, n, u_1, u_2\} \\ def(B_1) &= \{i, j, a\} \\ use(B_1) &= \{m, n, u_1\} \\ out(B_1) &= \{i, j, u_2, a\} \end{aligned}$$

$$\begin{aligned} IN(B_2) &= \{i, j, u_2, a\} \\ def(B_2) &= \{j\} \\ use(B_2) &= \{i, j\} \\ out(B_2) &= \{u_2, a, j\} \end{aligned}$$

$$\begin{aligned} IN(B_3) &= \{j, u_2\} \\ def(B_3) &= \{a\} \\ use(B_3) &= \{u_2\} \\ out(B_3) &= \{a, j, u_2\} \end{aligned}$$

$$\begin{aligned} IN(B_4) &= \{a, j, u_2\} \\ def(B_4) &= \{i\} \\ use(B_4) &= \{a, j\} \\ out(B_4) &= \{a, i, j, u_2\} \end{aligned}$$

all variables are live

$$IN[B_3] = \{j, u_2\}$$

$$def[B_3] = \{a\}$$

$$use[B_3] = \{u_1\}$$

$$OUT[B_3] = \{a, j, u_2\}$$

$$IN[B_4] = \{a, j, u_1\}$$

$$def[B_4] = \{i\}$$

$$use[B_4] = \{a, i\}$$

$$OUT[B_4] = \{a, i, j, u_2\}$$

Live-Variable Analysis:

Input: A flowgraph with def and use computed for each block.

Output: $IN[B]$ and $OUT[B]$: the set of variables live on entry and exit of each block B of the flowgraph.

Method:

$$IN[EXIT] = \emptyset$$

for (each basic block B other than EXIT) $IN[B] = \emptyset$

while (changes to any IN occur)

for (each basic block B other than EXIT)

?

$$OUT[B] = \bigcup_{S \text{ a successor}} IN[S];$$

$$IN[B] = USE_B \cup (OUT[B] - def_B)$$

Iterative algorithm to compute live variables.

① domain \rightarrow variable

② Transfer fun \rightarrow Backward : $IN[B] = f_B^{-1}(OUT[B])$

$$f_B(x) = USE_B \cup (x - DEF_B)$$

Meet-operation $\rightarrow OUT[B] = \bigcup_S IN(S)$

Boundary Condition $\rightarrow IN[EXIT] = \emptyset$

Initial Interior points $\rightarrow IN[B] = \emptyset$

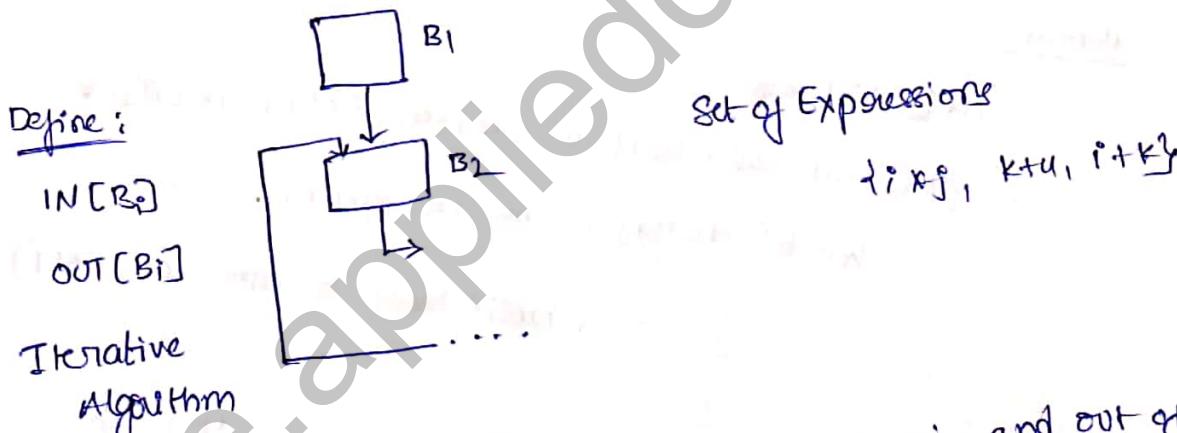
Application of Data flow Analysis:

It is one of the widely used Application in code-optimization.

one of the application is

Available Expression Computation:

↳ useful in Global Common Subexpression Elimination.



Set of expressions which are available at a in and out of particular block.

Similar to live variable analysis, here also we need to define multiple definitions like in and out for each block.

Available expression computation is a type of data flow analysis will be useful to eliminate global common subexpressions.

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$$IN[B_3] = \{ij, u_2\}$$

$$def[B_3] = \{a\}$$

$$use[B_3] = \{u_1\}$$

$$OUT[B_3] = \{a_{ij}, u_2\}$$

$$IN[B_4] = \{a_{ij}, u_2\}$$

$$def[B_4] = \{i\}$$

$$use[B_4] = \{a_{ij}\}$$

$$OUT[B_4] = \{a_{ij}, u_2\}$$

Live-variable Analysis:

Input: A flowgraph with def and use computed for each block.

Output: $IN[B]$ and $OUT[B]$ - the set of variables live on entry

and exit of each block B of the flowgraph.

Method:

$$IN[EXIT] = \emptyset$$

for (each basic block B other than EXIT) $IN[B] = \emptyset$

while (changes to any IN occur)

for (each basic block B other than EXIT)

$$OUT[B] = \bigcup_{S \text{ a successor}} IN[S];$$

$$IN[B] = USE_B \cup (OUT[B] - def_B)$$

Iterative algorithm → to compute live variables.

Constant propagation: can also be done using dataflow analysis
 ↳ More complex but doable.

It is also have in and out and iterative algorithm to perform constant propagation, similar to live variable analysis.

Available Expression.

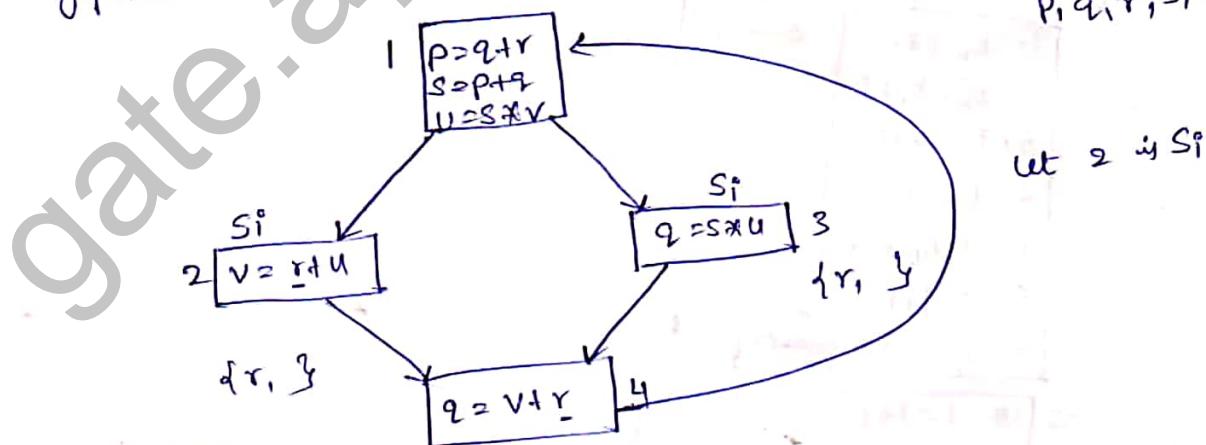
Solved problems: DFA and Code-optimization

GATE-2015 Set-1

- ① A variable x is said to be live at a statement s_i in a program if the following three conditions hold simultaneously.
 - ① There exist a statement s_j that uses x
 - ② There is a path from s_i to s_j in the flow graph corresponding to the program.
 - ③ The path has no intervening assignment to x including at s_i and s_j .

The variables which are live both at the statement in basic blocks and at the statement in basic blocks of the given control flow graph are

The given variables are p, q, r, s, u, v .



A: p, s, u

B: r, s, u

C: r, u

D: q, v

There is a path from s_i to s_j in which 'y' live on B_2 to B_4 .

Similarly there is a path from B_3 to B_4 in which 'r' is live at B_4 .

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so, 'r' will be live on Both $B_3 - B_3$, $B_3 - B_4$

'r' must be there in the Solution.

option 'A' and 'D' does not contain 'r' as a live variable.
we can eliminate them.

Let 'x' = 's', $S_i = B_3$ and $S_j = B_1$

There is a path from B_3 to B_1 via B_4

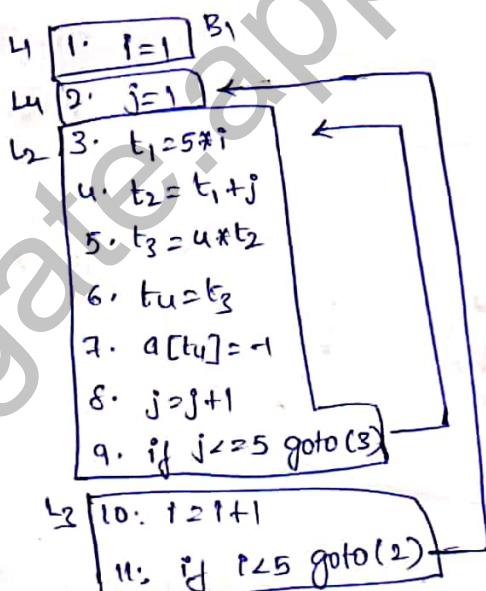
But the variable 's' is redefined at B_1 , before use. So s is not live from S_i to S_j ($B_3 - B_4 - B_1$).

option 'B' is also eliminated.

The most suitable or appropriate answer is 'c' for the given problem.

- ② Consider on the Intermediate code given below.

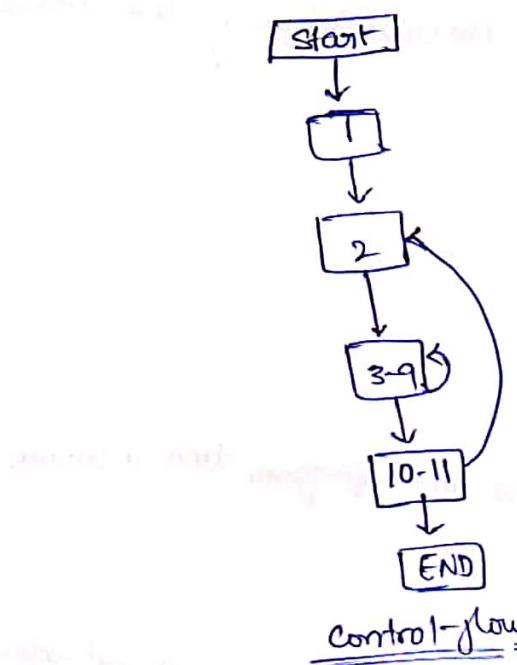
GATE 2015
Set 2



The number of nodes and edges in the control-flow graph constructed for the above code respectively are

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- ① First statement is always a leader.
- ② Target of any conditional (or) unconditional goto is a leader.
- ③ The next statement that immediately follows conditional (or) unconditional goto is a leader.



Total number of nodes are 6 and the edges are 7!

option 'B' is the most suitable answer.

GATE 2014 set-1

- ③ Which of the following is FALSE?
- (A) A basic block is a sequence of instructions where control enters the sequence at the beginning and exits at the end.
 - (B) Available expression analysis can be used for common subexpression elimination.
 - (C) Live variable analysis can be used for dead code elimination.
 - (D) $x = 4 * 5 \Rightarrow x = 20$ is an example of common subexpression elimination.

(A): True

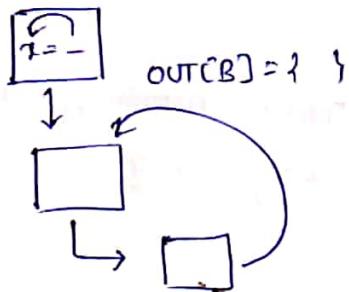
It is the definition of a Basic Block.

(B): True

It is used for Common Subexpression Elimination.

(C): True.

We can identify and eliminate the dead code using live variable analysis.



The variable x is not used in the program, then it results in a dead code.

(D) FALSE

$x = 4 * 5$ it is not the example of common subexpression.
 $\Rightarrow x = 20$ Constant

$$\begin{aligned} z &= 4 * y \\ z &= 4 * y + 5 \end{aligned} \Rightarrow \boxed{z = z + 5}$$

↓
common subexpression.

Consider the following code segment

```
for (i=0; i<n; i++)  
{  
    for (j=0; j<n; j++)  
    {  
        if (i%2)  
        {  
            x += (4*j + 5*i);  
            y += (7 + 4*j);  
        }  
    }  
}
```

Which one of the following is False?

- (A) The code contains loop invariant computation.
- (B) There is scope of common Subexpression Elimination in this code.
- (C) There is scope of strength Reduction in this code.
- (D) There is scope of dead code Elimination in this code.

A. True
 $5*i$ will not impact inner loop. we can move to outside of the loop.

B. True
 $4*j$ is the common Subexpression. we can also eliminate it from the loop.

C. $5*i = j < 22$ True
 \downarrow
Left shifting by '2' will also do the same job.
Costly operation

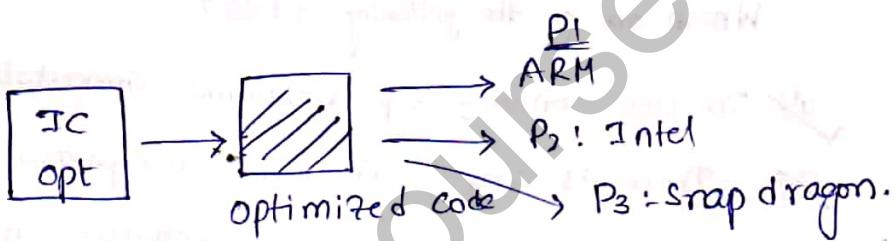
D. False
No scope of dead code elimination for the given code.

Some code optimizations are carried out on the Intermediate code because

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SAT, They enhance the portability of the compiler to other target processes.

- x (B). Program Analysis is more accurate on intermediate code than on machine code.
- x (C). The information from dataflow Analysis cannot otherwise be used for optimization.
- x (D). The information from the front end cannot otherwise be used for optimization.



A seems to be suitable Answer.

- (B): Not necessarily true always.
- (C): The information from dataflow Analysis will be used for optimization.
- (D): The information from the front will also be used for optimization.

A is the right answer for the given problem.