

1. If you wanted to make an image look brighter than what it currently does, which one of the following intensity transformations would you use?

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☐

☐

2. The mean and standard deviation of pixel intensity values in an 8-bit gray-scale image are 120 and 10, respectively. What are the mean and standard deviation of pixel intensity values in the negative of this image?

☒ 255, 10

$256 - 120 = 136$

☐ 120, 10

☐ 110, 20

☐ They can't be determined without knowing the size of the image.

236327 Digital Image and Signal Processing (2025 Spring)

3. Check all statements that are true regarding image histogram equalization:

☒ After histogram equalization, the intensity values are more effectively distributed over the histogram range.

☐ The mean intensity value of the pixels in an image increases after histogram equalization.

☐ After histogram equalization images will always look brighter.

☒ If pixel p is the brightest pixel in image x , it will remain the brightest pixel after histogram equalization.

Q4.

Find point transformation $z = H(r)$

	row	specific	
k	r _k	n _k	m _k
0	0	148	498
1	1/6	300	550
2	2/6	500	600
3	3/6	2200	800
4	4/6	500	600
5	5/6	300	550
6	1	148	498

$$\begin{aligned} \frac{r_k}{6} &= 0 \\ \frac{1}{6} &= 0.167 \\ \frac{2}{6} &= 0.333 \\ \frac{3}{6} &= 0.5 \\ \frac{4}{6} &= 0.666 \\ \frac{5}{6} &= 0.833 \\ \frac{6}{6} &= 1 \end{aligned}$$

$$z = H(r) = G^{-1}(T(r))$$

$$\begin{aligned} T(0) &= \frac{148}{4096} = 0.036 \approx 0 \\ T(\frac{1}{6}) &= \frac{148+300}{4096} = 0.11 \approx \frac{1}{6} \\ T(\frac{2}{6}) &= \frac{148+300+500}{4096} = \frac{948}{4096} \approx 0.23 \approx \frac{1}{3} \\ T(\frac{3}{6}) &= \frac{148+300+500+2200}{4096} = \frac{3148}{4096} = 0.77 \approx \frac{5}{6} \\ T(\frac{4}{6}) &= \frac{148+300+500+2200+500}{4096} = \frac{3648}{4096} \approx 0.9 \approx \frac{5}{6} \\ T(\frac{5}{6}) &= \frac{148+300+500+2200+500+300}{4096} = \frac{3948}{4096} \approx 1 \end{aligned}$$

$$\begin{aligned} G(0) &= \frac{498}{4096} \Rightarrow \frac{1}{6} \\ G(\frac{1}{6}) &= \frac{498+550}{4096} = 0.256 \rightarrow \frac{2}{6} \\ G(\frac{2}{6}) &= \frac{498+550+600}{4096} = 0.402 \rightarrow \frac{2}{6} \\ G(\frac{3}{6}) &= \frac{498+550+600+800}{4096} = 0.597 \rightarrow \frac{3}{6} \\ G(\frac{4}{6}) &= \frac{498+550+600+800+600}{4096} = 0.744 \rightarrow \frac{4}{6} \\ G(\frac{5}{6}) &= \frac{498+550+600+800+600+550}{4096} = 0.878 \rightarrow \frac{5}{6} \\ G(\frac{6}{6}) &= 1 \end{aligned}$$

$$\begin{aligned} T(\frac{6}{6}) &= 1 \\ \text{Summary} \quad \left\{ \begin{array}{l} T(0) = 0 \\ T(\frac{1}{6}) = \frac{1}{6} \\ T(\frac{2}{6}) = \frac{1}{3} \\ T(\frac{3}{6}) = \frac{5}{6} \\ T(\frac{4}{6}) = \frac{5}{6} \\ T(\frac{5}{6}) = 1 \\ T(\frac{6}{6}) = 1 \end{array} \right. & \left\{ \begin{array}{l} G(0) = \frac{1}{6} \\ G(\frac{1}{6}) = \frac{2}{6} \\ G(\frac{2}{6}) = \frac{2}{6} \\ G(\frac{3}{6}) = \frac{3}{6} \\ G(\frac{4}{6}) = \frac{4}{6} \\ G(\frac{5}{6}) = \frac{5}{6} \\ G(\frac{6}{6}) = \frac{6}{6} \end{array} \right. \end{aligned}$$

Finally

Then

$$\begin{aligned} G^{-1}(\frac{1}{6}) &= 0 \quad \checkmark \\ \left\{ \begin{array}{l} G^{-1}(\frac{2}{6}) = \frac{1}{6} \\ G^{-1}(\frac{2}{6}) = \frac{1}{6} \end{array} \right. \\ G^{-1}(\frac{2}{6}) &= \frac{1}{6} \\ G^{-1}(\frac{4}{6}) &= \frac{2}{6} \\ G^{-1}(\frac{4}{6}) &= \frac{4}{6} \\ G^{-1}(\frac{5}{6}) &= \frac{5}{6} \quad \checkmark \\ G^{-1}(\frac{6}{6}) &= \frac{6}{6} \quad \checkmark \end{aligned}$$

$$\begin{aligned} G^{-1}(T(0)) &= 0 \\ G^{-1}(T(\frac{1}{6})) &= G^{-1}(T(\frac{2}{6})) = G^{-1}(\frac{2}{6}) = 0 \\ G^{-1}(T(\frac{2}{6})) &= G^{-1}(T(\frac{2}{6})) = G^{-1}(\frac{2}{6}) = \frac{1}{6} \\ G^{-1}(T(\frac{4}{6})) &= G^{-1}(\frac{4}{6}) = \frac{2}{6} \end{aligned}$$

Q5.

```
clear all
I=[8 1 2 1 7
    9 3 10 4 0
    1 5 10 9 8
    9 10 5 8 9];
M=[0 0 1 0 0
    0 0 1 0 0
    1 1 1 1 1
    0 0 1 0 0
    0 0 1 0 0];
convolvedImage = conv2(I, M, 'same')

convolvedImage = 4x5
    21    20    39    24    18
    40    42    43    35    38
    42    39    50    45    43
    34    40    61    45    30
```