

Chapter 14: Polygons

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Exercise: 14A

Question 1:

(i)

Solution: for a pentagon: $n=5$

$$\therefore \left(\frac{360}{n}\right)^{\circ} = \left(\frac{360}{5}\right)^{\circ} = 72^{\circ}$$

(ii)

Solution: For a hexagon: $n=6$

$$\therefore \left(\frac{360}{n}\right)^{\circ} = \left(\frac{360}{6}\right)^{\circ} = 60^{\circ}$$

(iii)

Solution: For a heptagon: $n=7$

$$\therefore \left(\frac{360}{n}\right)^{\circ} = \left(\frac{360}{7}\right)^{\circ} = 51.43^{\circ}$$

(iv)

Solution: For a decagon: $n=10$

$$\therefore \left(\frac{360}{n}\right)^{\circ} = \left(\frac{360}{10}\right)^{\circ} = 36^{\circ}$$

(v)

Solution: For a polygon of 15 sides: $n=15$

$$\therefore \left(\frac{360}{n}\right)^{\circ} = \left(\frac{360}{15}\right)^{\circ} = 24^{\circ}$$

Question 2:

Solution:

Each exterior angle of an n -sided polygon = $\left(\frac{360}{n}\right)^{\circ}$

If the exterior angle is 50° , then:

$$\frac{360}{n} = 50^{\circ}$$

$$N = 7.2$$

since n is not an integer, we cannot have a polygon with each exterior angle equal to 50°

Question 3:**Solution:** For a regular polygon with n sides:

$$\text{Each interior angle} = 180 - (\text{Each exterior angle}) = 180 - \frac{360}{n}$$

(i)**Solution:** For a polygon with 10 sides:

$$\text{Each exterior angle} = \frac{360}{10} = 36^\circ$$

$$\text{Each interior angle} = 180 - 36 = 144^\circ$$

(ii)**Solution:** For a polygon with 15 sides:

$$\text{Each exterior angle} = \frac{360}{15} = 24^\circ$$

$$\text{Each interior angle} = 180 - 24 = 156^\circ$$

Question 4:**Solution:**

$$\text{Each interior angle of a regular polygon having } n \text{ sides} = 180 - \frac{360}{n} = \frac{180n - 360}{n}$$

If each interior angle of the polygon is 100° , then:

$$100 = \frac{180n - 360}{n}$$

$$100n = 180n - 360$$

$$180n - 100n = 360$$

$$80n = 360$$

$$n = \frac{360}{80} = 4.5$$

Since n is not an integer, it is not possible to have a regular polygon with each interior angle equal to 100° .

Question 5:**Solution:**

$$\text{Sum of the interior angles of an } n\text{-sided polygon} = (n-2) \times 180^\circ$$

(i)**Solution:** For a pentagon:

$$n = 5$$

$$\therefore (n-2) \times 180^\circ = (5-2) \times 180^\circ = 3 \times 180^\circ = 540^\circ$$

(ii)**Solution:** For a hexagon:

$$n=6$$

$$\therefore (n - 2) \times 180^\circ = (6 - 2) \times 180^\circ = 4 \times 180^\circ = 720^\circ$$

(iii)

Solution: For a nonagon:

$$n=9$$

$$\therefore (n - 2) \times 180^\circ = (9 - 2) \times 180^\circ = 7 \times 180^\circ = 1260^\circ$$

(iv)

Solution: For a polygon of 12 sides:

$$n=12$$

$$\therefore (n - 2) \times 180^\circ = (12 - 2) \times 180^\circ = 10 \times 180^\circ = 1800^\circ$$

Question 6:

Solution:

$$\text{Number of diagonal in an } n\text{-sided polygon} = \frac{n(n-3)}{2}$$

(i)

Solution: For a heptagon:

$$n=7 \Rightarrow \frac{n(n-3)}{2} = \frac{7(7-3)}{2} = \frac{28}{2} = 14$$

(ii)

Solution: For an octagon:

$$n=8 \Rightarrow \frac{n(n-3)}{2} = \frac{8(8-3)}{2} = \frac{40}{2} = 20$$

(iii)

Solution: For a 12-sided polygon:

$$n=12 \Rightarrow \frac{n(n-3)}{2} = \frac{12(12-3)}{2} = \frac{108}{2} = 54$$

Question 7:

Solution: Sum of all the exterior angles of a regular polygon is 360°

(i)

Solution: Each exterior angle = 40°

$$\text{Number of sides of the regular polygon} = \frac{360^\circ}{40} = 9$$

(ii)

Solution: Each exterior angle = 36°

$$\text{Number of sides of the regular polygon} = \frac{360^\circ}{36} = 10$$

(iii)

Solution: Each exterior angle = 72°

$$\text{Number of sides of the regular polygon} = \frac{360^\circ}{72} = 5$$

(iv)

Solution: Each exterior angle = 30°

$$\text{Number of sides of the regular polygon} = \frac{360^\circ}{30} = 12$$

Question 8:

Solution:

Sum of all the interior angles of an n-sided polygon = $(n - 2) \times 180^\circ$

$$m\angle ADC = 180^\circ - 50^\circ = 130^\circ$$

$$m\angle DAB = 180^\circ - 115^\circ = 65^\circ$$

$$m\angle BCD = 180^\circ - 90^\circ = 90^\circ$$

$$m\angle ADC + m\angle DAB + m\angle BCD + m\angle ABC = n - 2 \times 180^\circ = (4 - 2) \times 180^\circ = 2 \times 180^\circ = 360^\circ$$

$$m\angle ADC + m\angle DAB + m\angle BCD + m\angle ABC = 360^\circ$$

$$130^\circ + 65^\circ + 90^\circ + m\angle ABC = 360^\circ$$

$$285^\circ + m\angle ABC = 360^\circ$$

$$m\angle ABC = 75^\circ$$

$$m\angle CBF = 180^\circ - 75^\circ = 105^\circ$$

$$\therefore x = 105^\circ$$

Question 9:

Solution:

For a regular n-sided polygon:

$$\text{Each interior angle} = 180^\circ - \frac{360}{n}$$

In the given figure: $n=5$

$$x^\circ = 180^\circ - \frac{360}{5}$$

$$= 180^\circ - 72^\circ$$

$$= 108^\circ$$

$$\therefore x = 108^\circ$$

Exercise: 14B**Page no.: 182****Question 1:****Solution:**

(a) 5

For a pentagon:

$$n=5$$

$$\text{Number of diagonals} = \frac{n(n-3)}{2} = \frac{5(5-3)}{2} = 5$$

Question 2:**Solution:**

(c) 9

$$\text{Number of diagonals in an } n\text{-sided polygon} = \frac{n(n-3)}{2}$$

For a hexagon:

$$n=6 \therefore \frac{n(n-3)}{2} = \frac{6(6-3)}{2}$$

$$= \frac{18}{2} = 9$$

Question 3:**Solution:**

(d) 20

For a regular n-sided polygon:

$$\text{Number of diagonals} = \frac{n(n-3)}{2}$$

Octagon:

$$n=8, \frac{8(8-3)}{2} = \frac{40}{2} = 20$$

Question 4:**Solution:**

(d) 54

For an n-sided polygon:

$$\text{Number of diagonals} = \frac{n(n-3)}{2}$$

$$\therefore n=12 \Rightarrow \frac{12(12-3)}{2} = 54$$

Question 5:**Solution:**

(c) 9

$$\frac{n(n-3)}{2} = 27$$

$$N(n-3) = 54$$

$$n^2 - 3n - 54 = 0$$

$$n^2 - 9n + 6n - 54 = 0$$

$$N(n-9) + 6(n-9) = 0$$

$$N = -6 \text{ or } n = 9$$

Number of sides cannot be negative.

$$\therefore n = 9$$

Question 6:**Solution:**(b) 68°

Sum of all the interior angles of a polygon with n sides = $(n - 2) \times 180^\circ$

$$(5 - 2) \times 180^\circ = x + x + 20 + x + 40 + x + 60 + x + 80$$

$$540 = 5x + 200$$

$$5x = 340$$

$$x = 68^\circ$$

Question 7:**Solution:**

(b) 9

$$\text{Each exterior angle of a regular n-sided polygon} = \frac{360}{n} = 40$$

$$N = \frac{360}{40} = 9$$

Question 8:**Solution:**

(c) 5

$$\text{Each interior angle for a regular n-sided polygon} = 180 - \frac{360}{n}$$

$$180 - \frac{360}{n} = 108$$

$$\frac{360}{n} = 72$$

$$N = \frac{360}{72} = 5$$

Question 9:**Solution:**

(a) 8

Each interior angle of a regular polygon with n sides = $180 - \frac{360}{n}$

$$180 - \frac{360}{n} = 135$$

$$\frac{360}{n} = 45$$

$$N = 8$$

Question 10:**Solution:**

(b) 8

For a regular polygon with n sides:

$$\text{Each exterior angle} = \frac{360}{n}$$

$$\text{Each interior angle} = 180 - \frac{360}{n}$$

$$180 - \frac{360}{n} = 3 \left(\frac{360}{n} \right)$$

$$180 = 4 \left(\frac{360}{n} \right)$$

$$n = \frac{4 \times 360}{180} = 8$$

Question 11:**Solution:**(c) 144°

$$\text{Each interior angle of a regular decagon} = 180 - \frac{360}{10} = 180 - 36 = 144^\circ$$

Question 12:**Solution:**(b) 8 right \angle s

Sum of all the interior angles of a hexagon is $(2n - 4)$ right angles.

For a hexagon:

$$n = 6$$

$$(2n - 4) \text{ right } \angle\text{s} = (12 - 4) \text{ right } \angle\text{s} = 8 \text{ right } \angle\text{s}$$

Question 13:**Solution:**

(a) 135°

$$(2n - 4) \times 90 = 1080$$

$$(2n - 4) = 12$$

$$2n = 16$$

$$\text{or } n = 8$$

$$\begin{aligned}\text{Each interior angle} &= 180 - \frac{360}{n} \\ &= 180 - \frac{360}{8} \\ &= 180 - 45 \\ &= 135^\circ\end{aligned}$$

Question 14:**Solution:**

(d) 10

$$\text{Each exterior angle of a regular polygon} = \frac{360}{n}$$

$$\text{Each interior angle of a regular polygon} = 180 - \frac{360}{n}$$

$$180 - \frac{360}{n} - 108 = \frac{360}{n}$$

$$\frac{720}{n} = 180 - 108 = 72$$

$$n = \frac{720}{72}$$

$$n = 10$$