

## Chapter: Area of a Trapezium and a Polygon

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### Exercise: 18A

#### Question 1:

**Solution:**

$$\text{Area of a trapezium} = \frac{1}{2} \times (\text{Sum of parallel sides}) \times (\text{Distance between them})$$

$$= \frac{1}{2} \times (24 + 20) \times 15 \text{ cm}^2$$

$$= \frac{1}{2} \times 44 \times 15 \text{ cm}^2$$

$$= 22 \times 15 \text{ cm}^2$$

$$= 330 \text{ cm}^2$$

Hence the area of trapezium is  $330 \text{ m}^2$

#### Question 2:

**Solution:**

$$\text{Area of a trapezium} = \frac{1}{2} \times (\text{Sum of parallel sides}) \times (\text{Distance between them})$$

$$= \frac{1}{2} \times (38.7 + 22.3) \times 16 \text{ cm}^2$$

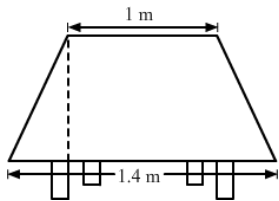
$$= \frac{1}{2} \times 61 \times 16 \text{ cm}^2$$

$$= 61 \times 8 \text{ cm}^2$$

$$= 488 \text{ cm}^2$$

Hence, the area of trapezium is  $488 \text{ cm}^2$

#### Question 3:



**Solution:**

$$\text{Area of a trapezium} = \frac{1}{2} \times (\text{Sum of parallel sides}) \times (\text{Distance between them})$$

$$= \frac{1}{2} \times (1 + 1.4) \times 0.9 \text{ m}^2$$

$$= \frac{1}{2} \times 2.4 \times 0.9 \text{ m}^2$$

$$= 1.2 \times 0.9 \text{ m}^2$$

$$= 1.08 \text{ m}^2$$

Hence the area of the top surface of the table is  $1.08 m^2$

**Question 4:**

**Solution:**

Let the distance between the parallel sides be  $x$ .

$$\text{Now, Area of trapezium} = \frac{1}{2} \times (55 + 35) \times x \text{ cm}^2$$

$$= \frac{1}{2} \times 90 \times x \text{ cm}^2$$

$$= 45x \text{ cm}^2$$

$$\text{Area of the trapezium} = 1080 \text{ cm}^2$$

Given

$$45x = 1080$$

$$x = \frac{1080}{45}$$

$$x = 24 \text{ cm}$$

Hence the distance between the parallel sides is  $24 \text{ cm}$

**Question 5:**

**Solution:**

Let the length of the required side be  $x \text{ cm}$ .

$$\text{Now, Area of trapezium} = \frac{1}{2} \times (84 + x) \times 26 \text{ m}^2$$

$$= 1092 + 13x \text{ m}^2$$

$$\text{Area of trapezium} = 1586 \text{ m}^2 \text{ (given)}$$

$$1092 + 13x = 1586$$

$$13x = 1586 - 1092$$

$$13x = 494$$

$$x = \frac{494}{13}$$

$$x = 38 \text{ m}$$

Hence the length of the other side is  $38 \text{ m}$ .

**Question 6:**

**Solution:**

Let the lengths of the parallel sides of the trapezium be  $4x \text{ cm}$  and  $5x \text{ cm}$ , respectively.

$$\text{Now, Area of trapezium} = \frac{1}{2} \times (4x + 5x) \times 18 \text{ cm}^2$$

$$= \frac{1}{2} \times 9x \times 18 \text{ cm}^2$$

$$= 81x \text{ cm}^2$$

$$\text{Area of trapezium} = 405 \text{ cm}^2$$

Given,

$$81x = 405 \text{ cm}^2$$

$$x = \frac{405}{81} \text{ cm}^2$$

$$x = 5 \text{ cm}^2$$

Length of one side =  $(4 \times 5) = 20 \text{ cm}$

Length of the other side =  $(5 \times 5) = 25 \text{ cm}$

### Question 7:

#### Solution:

Let the lengths of the parallel sides be  $x \text{ cm}$  and  $x + 6 \text{ cm}$ .

$$\begin{aligned} \text{Now, Area of trapezium} &= \frac{1}{2} \times (x + x + 6) \times 9 \text{ cm}^2 \\ &= \frac{1}{2} \times (2x + 6) \times 9 \text{ cm}^2 \\ &= 4.52x + 6 \text{ cm}^2 \\ &= 9x + 27 \text{ cm}^2 \end{aligned}$$

$$\text{Area of trapezium} = 180 \text{ cm}^2$$

$$9x + 27 = 180$$

$$9x = 180 - 27$$

$$9x = 153$$

$$x = \frac{153}{9}$$

$$x = 17$$

Hence the length of the parallel sides are  $17 \text{ cm}$  and  $23 \text{ cm}$ , that is,  $(17 + 6) \text{ cm}$

### Question 8:

#### Solution:

Let the lengths of the parallel sides be  $x \text{ cm}$  and  $2x \text{ cm}$ .

$$\begin{aligned} \text{Area of trapezium} &= \frac{1}{2} \times (x + 2x) \times 84 \text{ m}^2 \\ &= \frac{1}{2} \times 3x \times 84 \text{ m}^2 \\ &= 42 \times 3x \text{ m}^2 \\ &= 126x \text{ m}^2 \end{aligned}$$

$$\text{Area of the trapezium} = 9450 \text{ m}^2$$

Given,

$$126x = 9450 \text{ m}^2$$

$$x = \frac{9450}{126}$$

$$x = 75$$

Thus the lengths of the parallel sides are  $75 \text{ m}$  and  $150 \text{ m}$ , that is  $2 \times 75 \text{ m}$ ,

And the length of the longer side is  $150 \text{ m}$ .

**Question 9:****Solution:**

Length of the side AB =  $[130 - (54 + 19 + 42)]$  m  
 $= 15$  m

$$\begin{aligned}\text{Area of the trapezium-shaped field} &= \frac{1}{2} \times (AD + BC) \times AB \\ &= \frac{1}{2} \times (42 + 54) \times 15 \text{ m}^2 \\ &= \frac{1}{2} \times 96 \times 15 \text{ m}^2 \\ &= 48 \times 15 \text{ m}^2 \\ &= 720 \text{ m}^2\end{aligned}$$

Hence the area of the field is  $720 \text{ m}^2$

**Question 10:****Solution:**

$$\angle ABC = 90^\circ$$

From the right  $\triangle ABC$ , we have:

$$AB^2 = AC^2 - BC^2$$

$$AB^2 = 412 - 402$$

$$AB^2 = 1681 - 1600$$

$$AB^2 = 81$$

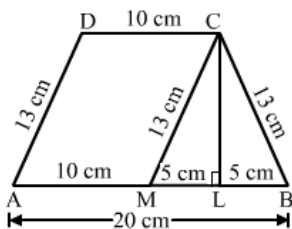
$$AB = \sqrt{81}$$

$$AB = 9 \text{ cm}$$

$$\text{Length } AB = 9 \text{ cm}$$

$$\begin{aligned}\text{Now, Area of the trapezium} &= \frac{1}{2} \times (AD + BC) \times AB \\ &= \frac{1}{2} \times (16 + 40) \times 9 \text{ cm}^2 \\ &= \frac{1}{2} \times 56 \times 9 \text{ cm}^2 \\ &= 28 \times 9 \text{ cm}^2 \\ &= 252 \text{ cm}^2\end{aligned}$$

Hence the area of the trapezium is  $252 \text{ cm}^2$

**Question 11:****Solution:**

Let ABCD be the given trapezium in which  $AB \parallel DC$ ,

AB = 20 cm, DC = 10 cm and AD = BC = 13 cm. Draw  $CL \perp AB$  and  $CM \parallel DA$  meeting AB at L and M, respectively. Clearly, AMCD is a parallelogram.

Now,  $AM = DC = 10$  cm

$$\begin{aligned} MB &= AB - AM \\ &= 20 - 10 \text{ cm} \\ &= 10 \text{ cm} \end{aligned}$$

Also,  $CM = DA = 13$  cm

Therefore,  $\triangle CMB$  is an isosceles triangle and  $CL \perp MB$ .

L is the midpoint of B.

$$\begin{aligned} ML = LB &= \frac{1}{2} \times MB \\ &= \frac{1}{2} \times 10 \text{ cm} \\ &= 5 \text{ cm} \end{aligned}$$

From right  $\triangle CLM$ , we have:

$$CL^2 = CM^2 - ML^2 \text{ cm}^2$$

$$CL^2 = 13^2 - 5^2 \text{ cm}^2$$

$$CL^2 = 169 - 25 \text{ cm}^2$$

$$CL^2 = 144 \text{ cm}^2$$

$$CL = \sqrt{144} \text{ cm}$$

$$CL = 12 \text{ cm}$$

$\therefore$  Length of  $CL = 12$  cm

$$\text{Area of the trapezium} = \frac{1}{2} \times (AB + DC) \times CL$$

$$= \frac{1}{2} \times (20 + 10) \times 12 \text{ cm}^2$$

$$= \frac{1}{2} \times 30 \times 12 \text{ cm}^2$$

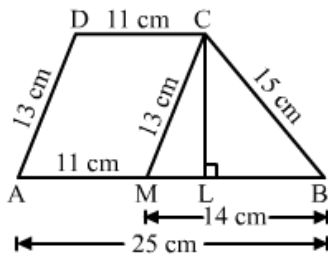
$$= 15 \times 12 \text{ cm}^2$$

$$= 180 \text{ cm}^2$$

Hence, the area of the trapezium is  $180 \text{ cm}^2$

### Question12:

#### Solution:



Let ABCD be the trapezium in which  $AB \parallel DC$ ,  $AB = 25$  cm,  $CD = 11$  cm,  $AD = 13$  cm and  $BC = 15$  cm. Draw  $CL \perp AB$  and  $CM \parallel DA$  meeting AB at L and M, respectively. Clearly, AMCD is a parallelogram.

Now,  $MC = AD = 13$  cm

$AM = DC = 11$  cm

$$\begin{aligned}
 MB &= AB - AM \\
 &= 25 - 11 \text{ cm} \\
 &= 14 \text{ cm}
 \end{aligned}$$

Thus, in  $\Delta CMB$ , we have:

$$CM = 13 \text{ cm}$$

$$MB = 14 \text{ cm}$$

$$BC = 15 \text{ cm}$$

$$\therefore s = \frac{1}{2} (13 + 14 + 15) \text{ cm}$$

$$= \frac{1}{2} \times 42 \text{ cm}$$

$$= 21 \text{ cm}$$

$$s - a = 21 - 13 \text{ cm}$$

$$= 8 \text{ cm}$$

$$s - b = 21 - 14 \text{ cm}$$

$$= 7 \text{ cm}$$

$$s - c = 21 - 15 \text{ cm}$$

$$= 6 \text{ cm}$$

$$\therefore \text{Area of } \Delta CMB = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21 \times 8 \times 7 \times 6} \text{ cm}^2$$

$$= 84 \text{ cm}^2$$

$$= \frac{1}{2} \times MB \times CL = 84 \text{ cm}^2$$

$$= \frac{1}{2} \times 14 \times CL = 84 \text{ cm}^2$$

$$= CL = \frac{84}{7}$$

$$= CL = 12 \text{ cm}$$

$$\text{Area of the trapezium} = \frac{1}{2} \times (AB + DC) \times CL$$

$$= \frac{1}{2} \times (25 + 11) \times 12 \text{ cm}^2$$

$$= \frac{1}{2} \times 36 \times 12 \text{ cm}^2$$

$$= 18 \times 12 \text{ cm}^2$$

$$= 216 \text{ cm}^2$$

Hence, the area of the trapezium is  $216 \text{ cm}^2$

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**Exercise: 18 B**

**Question 1:**

**Solution:**

Area of quadrilateral ABCD = (Area of  $\Delta ADC$ ) + (Area of  $\Delta ACB$ )

$$= \left( \frac{1}{2} \times AC \times DM \right) + \left( \frac{1}{2} \times AC \times BL \right)$$

$$\begin{aligned}
&= \left(\frac{1}{2} \times 24 \times 7\right) + \left(\frac{1}{2} \times 24 \times 8\right) \text{ cm}^2 \\
&= 84 + 96 \text{ cm}^2 \\
&= 180 \text{ cm}^2
\end{aligned}$$

Hence, the area of the quadrilateral is  $180 \text{ cm}^2$

### Question 2:

#### Solution:

Area of quadrilateral ABCD = (Area of  $\triangle ABD$ ) + (Area of  $\triangle BCD$ )

$$\begin{aligned}
&= \left(\frac{1}{2} \times BD \times AL\right) + \left(\frac{1}{2} \times BD \times CM\right) \\
&= \left(\frac{1}{2} \times 36 \times 19\right) + \left(\frac{1}{2} \times 4^2 \sqrt{9} \times 36 \times 11\right) \text{ m}^2 \\
&= 342 + 198 \text{ m}^2 \\
&= 540 \text{ m}^2
\end{aligned}$$

Hence, the area of the field is  $540 \text{ m}^2$

### Question 3:

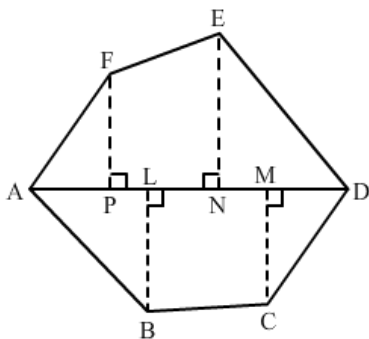
#### Solution:

Area of pentagon ABCDE = (Area of  $\triangle AEN$ ) + (Area of trapezium EDMN) + (Area of  $\triangle DMC$ ) + (Area of  $\triangle ACB$ )

$$\begin{aligned}
&= \frac{1}{2} \times AN \times EN + \frac{1}{2} \times (EN + DM) \times NM + \frac{1}{2} \times MC \times DM + \frac{1}{2} \times AC \times BL \\
&= \frac{1}{2} \times AN \times EN + \frac{1}{2} \times (EN + DM) \times (AM - AN) + \frac{1}{2} \times (AC - AM) \times DM + \frac{1}{2} \times AC \times BL \\
&= \frac{1}{2} \times 6 \times 9 + \frac{1}{2} \times 9 + \frac{1}{2} \times (14 - 6) + \frac{1}{2} \times (18 - 14) \times 12 + \frac{1}{2} \times 18 \times 4 \text{ cm}^2 \\
&= 27 + 84 + 24 + 36 \text{ cm}^2 \\
&= 171 \text{ cm}^2
\end{aligned}$$

Hence, the area of the given pentagon is  $171 \text{ cm}^2$

### Question 4:



#### Solution:

Area of hexagon ABCDEF = (Area of  $\triangle AFP$ ) + (Area of trapezium FENP) + (Area of  $\triangle ALB$ )

$$= \frac{1}{2} \times AP \times FP + \frac{1}{2} \times (FP+EN) \times PN + \frac{1}{2} \times ND \times EN + \frac{1}{2} \times MD \times CM + \frac{1}{2} \times (CM + BL) \times LM + \frac{1}{2} \times AL \times BL$$

$$= \frac{1}{2} \times AP \times FP + \frac{1}{2} \times FP + EN \times PL + LN + \frac{1}{2} \times NM + MD \times CM + \frac{1}{2} \times MD \times CM + \frac{1}{2} \times CM + BL$$

$$\frac{1}{2} \times LN + NM + \frac{1}{2} \times AP + PL \times BL$$

$$= \frac{1}{2} \times 6 \times 8 + \frac{1}{2} \times (8 + 12) \times (2 + 8) + \frac{1}{2} \times (2 + 3) \times 12 + \frac{1}{2} \times 3 \times 6 + \frac{1}{2} \times (6 + 8) \times (8 + 2) + \frac{1}{2} \times (6 + 2) \times 8 \text{ cm}^2$$

$$= 24 + 100 + 30 + 9 + 70 + 32 \text{ cm}^2$$

$$= 265 \text{ cm}^2$$

Hence, the area of the hexagon is  $265 \text{ cm}^2$

#### Question 5:

**Solution:**

$$\text{Area of pentagon ABCDE} = \frac{1}{2} \times (\text{Area of } \triangle ABC) + (\text{Area of } \triangle ACD) + (\text{Area of } \triangle ADE)$$

$$= \frac{1}{2} \times AC \times BL + \frac{1}{2} \times AD \times CM + \frac{1}{2} \times AD \times EM$$

$$= \frac{1}{2} \times 10 \times 3 + \frac{1}{2} \times 12 \times 7 + \frac{1}{2} \times 12 \times 5 \text{ cm}^2$$

$$= 15 + 42 + 30 \text{ cm}^2$$

$$= 87 \text{ cm}^2$$

Hence, the area of the pentagon is  $87 \text{ cm}^2$

#### Question6:

**Solution:**

$$\text{Area enclosed by the given figure} = \frac{1}{2} \times (\text{Area of trapezium FEDC}) + (\text{Area of square ABCF})$$

$$= \frac{1}{2} \times (6 + 20) \times (8 + 20) \times 20 \text{ cm}^2$$

$$= 104 + 400 \text{ cm}^2$$

$$= 504 \text{ cm}^2$$

Hence in the area enclosed by the figure is  $504 \text{ cm}^2$

#### Question7:

**Solution:**

We will find the length of AC. From the right triangles ABC and HGF, we have:

$$AC^2 - HF^2 = 5^2 - 4^2 \text{ cm}$$

$$= 25 - 16 \text{ cm}$$

$$= 9 \text{ cm}$$



$$\begin{aligned} AC-HF &= \sqrt{9} \text{ cm} \\ &= 3 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Area of the given figure ABCDEFGH} &= (\text{Area of rectangle ADEH}) + (\text{Area of } \triangle ABC) + \\ &\quad (\text{Area of } \triangle HGF) \\ &= (\text{Area of rectangle ADEH}) + 2(\text{Area of } \triangle ABC) \\ &= (AD \times DE) + 2(\text{Area of } \triangle ABC) \\ &= (AC+CD) \times DE + 2\left(\frac{1}{2} \times BC \times AC\right) \\ &= 3+4 \times 8 + 2\left(\frac{1}{2} \times 4 \times 3\right) \text{ cm}^2 \\ &= 56 + 12 \text{ cm}^2 \\ &= 68 \text{ cm}^2 \end{aligned}$$

Hence, the area of the given figure is  $68 \text{ cm}^2$ .

### Question8:

#### Solution:

$$\text{Let } AL = DM = x \text{ cm}$$

$$LM = BC = 13 \text{ cm}$$

$$\therefore x + 13 + x = 23$$

$$2x + 13 = 23$$

$$2x = 23 - 13$$

$$2x = 10$$

$$x = 5$$

$$\therefore AL = 5 \text{ cm}$$

From the right  $\triangle AFL$ , we have:

$$FL^2 = AF^2 - AL^2$$

$$FL^2 = 13^2 - 5^2$$

$$FL^2 = 169 - 25$$

$$FL^2 = 144$$

$$FL = \sqrt{144}$$

$$FL = 12 \text{ cm}$$

$$\therefore FL = BL = 12 \text{ cm}$$

$$\begin{aligned} \text{Area of a regular hexagon} &= (\text{Area of the trapezium ADEF}) + (\text{Area of the trapezium ABCD}) \\ &= 2(\text{Area of trapezium ADEF}) \\ &= 2 \left[ \frac{1}{2} \times (AD+EF) \times FL \right] \\ &= 2 \left[ \frac{1}{2} \times (23+13) \times 12 \right] \text{ cm}^2 \\ &= 2 \left[ \frac{1}{2} \times 36 \times 12 \right] \text{ cm}^2 \\ &= 432 \text{ cm}^2 \end{aligned}$$

Hence the area of the given regular hexagon is  $432 \text{ cm}^2$

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**Exercise: 18C**

**Question1:**

**Solution:**

(b)  $144 \text{ cm}^2$

$$\begin{aligned}\text{Area of the trapezium} &= \frac{1}{2} \times (14 + 18) \times 9 \text{ cm}^2 \\ &= \frac{1}{2} \times 32 \times 9 \text{ cm}^2 \\ &= 144 \text{ cm}^2\end{aligned}$$

**Question 2:**

**Solution:**

(c) 8 cm

Let the distance between the parallel sides be  $x$  cm.

$$\begin{aligned}\text{Then, area of the trapezium} &= \frac{1}{2} \times (19 + 13) \times x \text{ cm}^2 \\ &= \frac{1}{2} \times 32 \times x \text{ cm}^2 \\ &= 16x \text{ cm}^2\end{aligned}$$

But it is given that the area of the trapezium is  $128 \text{ cm}^2$

$$16x = 128$$

$$x = \frac{128}{16}$$

$$x = 8 \text{ cm}$$

**Question 3:**

**Solution:**

(a) 45 cm

Let the length of the parallel sides be  $3x$  cm and  $4x$  cm, respectively.

$$\begin{aligned}\text{Then, area of the trapezium} &= \frac{1}{2} \times (3x + 4x) \times 12 \text{ cm}^2 \\ &= \frac{1}{2} \times 7x \times 12 \text{ cm}^2 \\ &= 42x \text{ cm}^2\end{aligned}$$

But it is given that the area of the trapezium is  $630 \text{ cm}^2$ .

$$42x = 630$$

$$x = \frac{620}{42}$$

$$x = 15$$

Length of the parallel sides =  $(3 \times 15)$  cm = 45cm

$$(4 \times 15)\text{cm} = 60\text{cm}$$

Hence, the shorter of the parallel sides is 45cm

#### Question4:

##### Solution:

(a) 23 cm

Let the length of the parallel sides be  $x$  cm and  $x+6$  cm, respectively.

$$\begin{aligned}\text{Then, area of the trapezium} &= \frac{1}{2} \times (x + x + 6) \times 9 \text{ cm}^2 \\ &= \frac{1}{2} \times (2x + 6) \times 9 \text{ cm}^2 \\ &= 4.5x + 6 \text{ cm}^2 \\ &= 9x + 27 \text{ cm}^2\end{aligned}$$

But it is given that the area of the trapezium is  $180 \text{ cm}^2$

$$9x + 27 = 180$$

$$9x = 180 - 27$$

$$9x = 153$$

$$x = \frac{153}{9}$$

$$x = 17$$

Therefore the length of the parallel sides are 17 cm and  $(17 + 6)$  cm which is equal to 23 cm

Hence the length of the longer parallel side is 23 cm.

#### Question 5:

##### Solution:

(a)  $80 \text{ cm}^2$

From the given trapezium, we find:

$$DC = AL = 7 \text{ cm} \quad [\text{since } DA \perp AB \text{ and } CL \perp AB]$$

From the right  $\triangle CBL$ , we have:

$$CL^2 = CB^2 - LB^2$$

$$CL^2 = 10^2 - 6^2$$

$$CL^2 = 100 - 36$$

$$CL^2 = 64$$

$$CL = \sqrt{64}$$

$$CL = 8 \text{ cm}$$

$$\text{Area of the trapezium} = \frac{1}{2} \times (7 + 13) \times 8 \text{ cm}^2$$

$$= \left( \frac{1}{2} \times 20 \times 8 \right) \text{ cm}^2$$

$$= 80 \text{ cm}^2$$

**Test paper 18****Page no. - 212****Question1:****Solution:**

Let the base of the triangular field be  $3x$  cm and its height be  $x$  cm.

$$\begin{aligned}\text{Then, area of the triangle} &= \left(\frac{1}{2} \times 3x \times x\right) m^2 \\ &= \frac{3x^2}{2} m^2\end{aligned}$$

But it is given that the area of the triangular field is  $1350 m^2$

$$\therefore \frac{3x^2}{2} = 1350$$

$$x^2 = \frac{1350 \times 2}{3}$$

$$x^2 = 900$$

$$x = \sqrt{900}$$

$$x = 30 \text{ m}$$

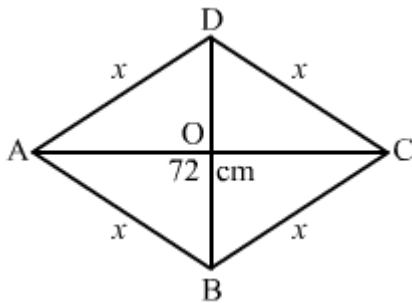
Hence, the height of the field is  $30$  m

Its base =  $(3 \times 30) \text{ m} = 90 \text{ m}$

**Question2:****Solution:**

$$\begin{aligned}\text{Area of an equilateral triangle} &= \frac{\sqrt{3}}{4} \times (\text{side})^2 \text{ square units} \\ &= \frac{\sqrt{3}}{4} \times 6 \times 6 \text{ cm}^2 \\ &= \frac{\sqrt{3}}{4} \times 36 \text{ cm}^2 \\ &= 9\sqrt{3} \text{ cm}^2\end{aligned}$$

Hence, the area of an equilateral triangle is  $9\sqrt{3} \text{ cm}^2$

**Question 3:****Solution:**

Let ABCD be a rhombus whose diagonals AC and BD intersect at a point O. Let the length of the diagonal AC be 72 cm and the side of the rhombus be  $x$  cm.

Perimeter of the rhombus =  $4x$  cm

But it is given that the perimeter of the rhombus is 180 cm.

$$\therefore 4x = 180$$

$$x = \frac{180}{4}$$

$$x = 45$$

Hence, the length of the side of the rhombus is 45 cm.

We know that the diagonals of the rhombus bisect each other at right angles.

$$\therefore AO = \frac{1}{2} AC$$

$$AO = \frac{1}{2} \times 72 \text{ cm}$$

$$AO = 36 \text{ cm}$$

From right  $\triangle AOB$ , we have:

$$BO^2 = AB^2 - AO^2$$

$$BO^2 = 45^2 - 36^2$$

$$BO^2 = 2025 - 1296$$

$$BO^2 = 729$$

$$BO = \sqrt{729}$$

$$BO = 27 \text{ cm}$$

$$\therefore BD = 2 \times BO$$

$$BD = 2 \times 27 \text{ cm}$$

$$BD = 54 \text{ cm}$$

Hence, the length of the other diagonal is 54 cm.

$$\text{Area of the rhombus} = \frac{1}{2} \times 72 \times 54 \text{ cm}^2$$

$$= 1944 \text{ cm}^2$$

#### Question4:

#### Solution:

Let the length of the parallel sides be  $x$  m and  $(x-14)$  m.

$$\text{Then, area of the trapezium} = \frac{1}{2} \times (x + x - 14) \times 12 \text{ m}^2$$

$$= 6(2x - 14) \text{ m}^2$$

$$= 12x - 84 \text{ m}^2$$

But it is given that the area of the trapezium is  $216 \text{ m}^2$

$$12x - 84 = 216$$

$$12x = 216 + 84$$

$$12x = 300$$

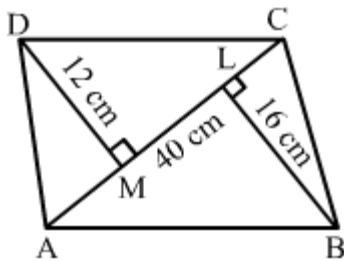
$$x = \frac{300}{12}$$

$$x = 25$$

Hence the length of the parallel sides are 25 m and (25 – 14) m, which is equal to 11m.

**Question 5:**

**Solution:**



Let ABCD be a quadrilateral.

Diagonal, AC=40 cm

BL⊥AC, such that BL=16 cm

DM⊥AC, such that DM=12 cm

Area of the quadrilateral= (Area of ΔDAC) + (Area of ΔACB)

$$\begin{aligned}
 &= \frac{1}{2} \times AC \times DM + \frac{1}{2} \times AC \times BL \text{ cm}^2 \\
 &= \frac{1}{2} \times 40 \times 12 + \frac{1}{2} \times 40 \times 16 \text{ cm}^2 \\
 &= 240 + 320 \text{ cm}^2 \\
 &= 560 \text{ cm}^2
 \end{aligned}$$

Hence, the area of the quadrilateral is  $560 \text{ cm}^2$

**Question6:**

**Solution:**

Let the other side of the triangular field be x m.

$$\begin{aligned}
 \therefore x^2 &= 50^2 - 30^2 \\
 x^2 &= 2500 - 900 \\
 x^2 &= 1600 \\
 x &= \sqrt{1600} \\
 x &= 40
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{Area of the field} &= \frac{1}{2} \times 30 \times 40 \text{ m}^2 \\
 &= 600 \text{ m}^2
 \end{aligned}$$

B. Mark ( ) against the correct answer in each of the following:

**Question 7:**

**Solution:**

(b)  $56 \text{ cm}^2$

$$\begin{aligned}
 \text{Area of the triangle} &= \frac{1}{2} \times 14 \times 8 \text{ cm}^2 \\
 &= 56 \text{ cm}^2
 \end{aligned}$$

**Question 8:****Solution:**

(a) 20 m

Let the height of the triangle be  $x$  m and its base be  $4x$  m respectively.

$$\begin{aligned}\text{Then, area of the triangle} &= \frac{1}{2} \times 4x \times x \, m^2 \\ &= 2x^2 \, m^2\end{aligned}$$

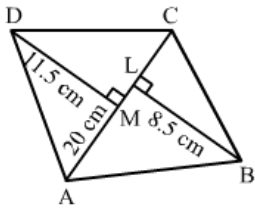
But, the area of the triangle is  $50 \, m^2$ 

$$2x^2 = 50$$

$$x^2 = \frac{50}{2}$$

$$x = \sqrt{25}$$

$$\begin{aligned}\text{Length of its base} &= (4 \times 5) \, m \\ &= 20m\end{aligned}$$

**Question9:****Solution:**(b)  $200 \, cm^2$ 

Let ABCD be a quadrilateral.

Diagonal,  $AC = 20 \, cm$  $BL \perp AC$ , such that  $BL = 8.5 \, cm$  $DM \perp AC$ , such that  $DM = 11.5 \, cm$ Area of the quadrilateral = (Area of  $\triangle DAC$ ) + (Area of  $\triangle ACB$ )

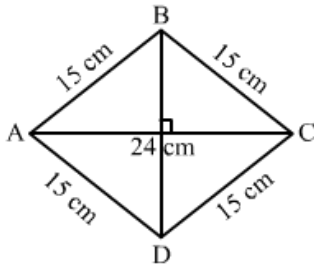
$$= \left( \frac{1}{2} \times AC \times DM \right) + \left( \frac{1}{2} \times AC \times BL \right) \, cm^2$$

$$= \left( \frac{1}{2} \times 20 \times 11.5 \right) + \left( \frac{1}{2} \times 20 \times 8.5 \right) \, cm^2$$

$$= 85 + 115 \, cm^2$$

$$= 200 \, cm^2$$

**Question 10:****Solution:**(b)  $216 \, cm^2$



Let ABCD be a rhombus whose diagonals AC and BD intersect at a point O. Let the length of the diagonal AC be 24 cm and the side of the rhombus be 15 cm.

We know that the diagonals of the rhombus bisect each other at right angles.

$$AO = \frac{1}{2} AC$$

$$AO = \frac{1}{2} \times 24 \text{ cm}$$

$$AO = 12 \text{ cm}$$

From right  $\triangle AOB$ , we have:

$$BO^2 = AB^2 - AO^2$$

$$BO^2 = 15^2 - 12^2$$

$$BO^2 = 225 - 144$$

$$BO^2 = 81$$

$$BO = \sqrt{81}$$

$$BO = 9 \text{ cm}$$

$$\therefore BD = 2 \times BO$$

$$BD = 2 \times 9 \text{ cm}$$

$$BD = 18 \text{ cm}$$

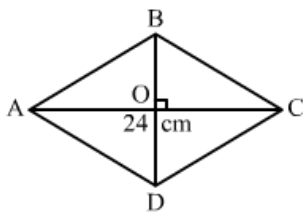
Hence, the length of the other diagonal is 18 cm.

$$\begin{aligned} \text{Area of the rhombus} &= \frac{1}{2} \times 24 \times 18 \text{ cm}^2 \\ &= 216 \text{ cm}^2 \end{aligned}$$

### Question11:

**Solution:**

(b) 13 cm



Let ABCD be a rhombus whose diagonals AC and BD intersect at a point O.

Let the length of the diagonal AC be 24 cm.

$$\text{Area of the rhombus} = \frac{1}{2} \times AC \times BD \text{ cm}^2$$

But the area of the rhombus is  $120 \text{ cm}^2$  (given)



$$\therefore \frac{1}{2} \times AC \times BD = 120$$

$$\text{Or } \frac{1}{2} \times 24 \times BD = 120$$

$$\text{or } 12 \times BD = 120$$

$$\text{or } BD = \frac{120}{12}$$

$$= 10 \text{ cm}$$

$$OB = \frac{BD}{2}$$

$$= \frac{10}{2}$$

$$= 5 \text{ cm}$$

$$\text{And } OA = \frac{AC}{2} = \frac{24}{2} = 12 \text{ cm}$$

Now, in right triangle AOB:

$$AB^2 = OA^2 + OB^2$$

$$AB^2 = 12^2 + 5^2$$

$$AB^2 = 144 + 25$$

$$= 169$$

$$\text{or } AB = \sqrt{169}$$

$$= 13 \text{ cm}$$

Therefore, each side of the rhombus is 13 cm.

### Question 12:

**Solution:**

(a)  $600 \text{ cm}^2$

$$\text{Area of the trapezium} = \frac{1}{2} \times (54 + 26) \times 15 \text{ cm}^2$$

$$= \frac{1}{2} \times 80 \times 15 \text{ cm}^2$$

$$= 600 \text{ cm}^2$$

### Question 13:

**Solution:**

(b) 40 cm

Let the length of the parallel sides be  $5x$  cm and  $3x$  cm, respectively.

$$\text{Area of the trapezium} = \frac{1}{2} \times (5x + 3x) \times 12 \text{ cm}^2$$

$$= \frac{1}{2} \times 8x \times 12 \text{ cm}^2$$

$$= 48x \text{ cm}^2$$

The area of the trapezium is  $384 \text{ cm}^2$

$$48x = 384$$

$$x = \frac{384}{48}$$

$$x = 8$$

Longer side =  $5x$

$$5 \times 8 = 40 \text{ cm}$$

**Question 14:**

(a)

**Solution:** Area of a triangle =  $\frac{1}{2} \times \text{Base} \times \text{Height}$

(b)

**Solution:** Area of a ||gm = Base  $\times$  Height

(c)

**Solution:** Area of a trapezium =  $\frac{1}{2} \times \text{Sum of the parallel sides} \times \text{Distance between them}$

(d)

**Solution:** Area of a trapezium =  $\frac{1}{2} \times (14+18) \times 8 \text{ cm}^2$

$$= \frac{1}{2} \times 32 \times 8 \text{ cm}^2$$

$$= 128 \text{ cm}^2$$