

Chapter 3: Squares and Square Roots

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Exercise 3A

Question 1:

Solution:

- (i) 441 – the prime factors are (3, 3, 7, 7). So this is a perfect square.
- (ii) 576 – the prime factors are (2, 2, 2, 2, 2, 2, 3, 3). So this is a perfect square.
- (iii) 11025 – the prime factors are (3, 3, 5, 5, 7, 7). So this is a perfect square.
- (iv) 1176 – the prime factors are (2, 2, 2, 3, 7, 7). So this is not a perfect square.
- (v) 5625 – The prime factors are (3, 3, 5, 5, 5, 5). So this is a perfect square.
- (vi) 9075 – The prime factors are (3, 5, 5, 11, 11). So this is not a perfect square.
- (vii) 4225 – The prime factors are (5, 5, 13, 13). So this is a perfect square.
- (viii) 1089 – The prime factors are (3, 3, 11, 11). So this is a perfect square.

Question 2:

Solution:

- (i) 1225 – This is the product of (5, 5, 7, 7). So the number whose square is the given number is the product of (5, 7) = 35.
- (ii) 2601 – This is the product of (3, 3, 17, 17). So the number whose square is the given number is the product of (3, 17) = 51.
- (iii) 5929 – This is the product of (7, 7, 11, 11). So the number whose square is the given number is the product of (11, 7) = 77.
- (iv) 7056 – This is the product of (2, 2, 2, 2, 3, 3, 7, 7). So the number whose square is the given number is the product of (2, 2, 3, 7) = 84.
- (v) 8281 – This is the product of (7, 7, 13, 13). So the number whose square is the given number is the product of (7, 13) = 91.

Question 3:

Solution:

- (i) 3675 = product of (3, 5, 5, 7, 7). So the number should be multiplied by 3. The number whose square is the new number is the product of (3, 5, 7) = 105.
- (ii) 2156 = product of (2, 2, 7, 7, 11). So the number should be multiplied by 11. The number whose square is the new number is the product of (2, 7, 11) = 154.
- (iii) 3332 = product of (2, 2, 7, 7, 17). So the number should be multiplied by 17. The number whose square is the new number is the product of (2, 7, 17) = 238.
- (iv) 2925 = product of (3, 3, 5, 5, 13). So the number should be multiplied by 13. The number whose square is the new number is the product of (3, 5, 13) = 195.
- (v) 9075 = product of (3, 5, 5, 11, 11). So the number should be multiplied by 3. The number whose square is the new number is the product of (3, 5, 11) = 165.

- (vi) $7623 = \text{product of } (3, 3, 7, 11, 11)$. So the number should be multiplied by 7. The number whose square is the new number is the product of $(3, 7, 11) = 231$.
- (vii) $3380 = \text{product of } (2, 2, 5, 13, 13)$. So the number should be multiplied by 5. The number whose square is the new number is the product of $(2, 5, 13) = 130$.
- (viii) $2475 = \text{product of } (3, 3, 5, 5, 11)$. So the number should be multiplied by 11. The number whose square is the new number is the product of $(3, 5, 11) = 165$.

Question 4:

Solution:

- (i) $1575 = \text{product of } (3, 3, 5, 5, 7)$. So the number should be divided by 7. The number whose square is the new number is the product of $(3, 5) = 15$.
- (ii) $9075 = \text{product of } (3, 5, 5, 11, 11)$. So the number should be divided by 3. The number whose square is the new number is the product of $(5, 11) = 55$.
- (iii) $4851 = \text{product of } (3, 3, 7, 7, 11)$. So the number should be divided by 11. The number whose square is the new number is the product of $(3, 7) = 21$.
- (iv) $3380 = \text{product of } (2, 2, 5, 13, 13)$. So the number should be divided by 5. The number whose square is the new number is the product of $(2, 13) = 26$.
- (v) $4500 = \text{product of } (2, 2, 3, 3, 5, 5, 5)$. So the number should be divided by 5. The number whose square is the new number is the product of $(2, 3, 5) = 30$.
- (vi) $7776 = \text{product of } (2, 2, 2, 2, 2, 3, 3, 3, 3, 3)$. So the number should be divided by 6. The number whose square is the new number is the product of $(2, 2, 3, 3) = 36$.
- (vii) $8820 = \text{product of } (2, 2, 3, 3, 5, 7, 7)$. So the number should be divided by 5. The number whose square is the new number is the product of $(2, 3, 7) = 42$.
- (viii) $4056 = \text{product of } (2, 2, 2, 3, 13, 13)$. So the number should be divided by 6. The number whose square is the new number is the product of $(2, 13) = 26$.

Question 5:

Solution:

The largest 2 digit number is 99.

$$\begin{array}{r}
 9 \\
 9 \overline{) 99} \\
 \underline{81} \\
 18
 \end{array}$$

So 18 is subtracted from 99 to obtain the square of 9 which is equal to 81.

Question 6:

Solution:

The largest 3 digit number is 999.

$$\begin{array}{r}
 31 \\
 \hline
 3 \overline{) 999} \\
 \underline{9} \\
 61 \overline{) 099} \\
 \underline{61} \\
 38
 \end{array}$$

So 38 is subtracted from 999 to obtain the square of 31 which is equal to 961.

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Exercise 3B

Question 1:

Solution:

All the numbers given above either end with a 2, 3, 7, 8 or have an odd number of zeroes in the end. So they are all not perfect squares.

Question 2:

Solution:

- (i) 196 – is an even number so it is the square of an even number.
- (ii) 441 – is an odd number so it is the square of an odd number.
- (iii) 900 – is an even number so it is the square of an even number.
- (iv) 625 – is an odd number so it is the square of an odd number.
- (v) 324 – is an even number so it is the square of an even number.

Question 3:

Solution:

- (i) 484 – is an even number so it is the square of an even number.
- (ii) 961 – is an odd number so it is the square of an odd number.
- (iii) 7396 – is an even number so it is the square of an even number.
- (iv) 8649 – is an odd number so it is the square of an odd number.
- (v) 4225 – is an odd number so it is the square of an odd number.

Question 4:

Solution:

- (i) $(1+3+5+7+9+11+13) = \text{sum of first 7 odd numbers} = \text{square of } 7 = 49.$
- (ii) $(1+3+5+7+9+11+13+15+17+19) = \text{sum of first 10 odd numbers} = \text{square of } 10 = 100.$

- (iii) $(1+3+5+7+9+11+13+15+17+19+21+23) = \text{sum of first 12 odd numbers} = \text{square of } 12 = 144.$

Question 5:

Solution:

We know that n^2 is the sum of the first n odd natural numbers.

- (i) So, $9^2 = 81 = \text{sum of first 9 odd numbers} = (1+3+5+7+9+11+13+15+17)$
(i) So, $10^2 = 100 = \text{sum of first 10 odd numbers} = (1+3+5+7+9+11+13+15+17+19)$

Question 6:

Solution:

- (i) 6

For every natural number $m > 1$, $(2m, m^2-1, m^2+1)$ is a Pythagorean triplet.

Since $2m = 6$, we get $m = 3$

Thus the triplet is $(6, 8, 10)$

- (ii) 14

For every natural number $m > 1$, $(2m, m^2-1, m^2+1)$ is a Pythagorean triplet.

Since $2m = 14$, we get $m = 7$

Thus the triplet is $(14, 48, 50)$

- (iii) 16

For every natural number $m > 1$, $(2m, m^2-1, m^2+1)$ is a Pythagorean triplet.

Since $2m = 16$, we get $m = 8$

Thus the triplet is $(16, 63, 65)$

- (iv) 20

For every natural number $m > 1$, $(2m, m^2-1, m^2+1)$ is a Pythagorean triplet.

Since $2m = 20$, we get $m = 10$

Thus the triplet is $(20, 99, 101)$

Question 7: Evaluate:

Solution:

- (i) $(38)^2 - (37)^2 = (38+37) = 75$
(ii) $(75)^2 - (74)^2 = (75+74) = 149$
(iii) $(92)^2 - (91)^2 = (92+91) = 183$
(iv) $(105)^2 - (104)^2 = (105+104) = 209$
(v) $(141)^2 - (140)^2 = (141+140) = 281$
(vi) $(218)^2 - (217)^2 = (218+217) = 435$

Question 8:**Solution:**

$$(i) (310)^2 = (300+10)^2 = (300)^2 + (2 \times 300 \times 10) + (10)^2 = 90000 + 6000 + 100 = 96100$$

$$(ii) (508)^2 = (500+8)^2 = (500)^2 + (2 \times 500 \times 8) + (8)^2 = 250000 + 8000 + 64 = 258064$$

$$(iii) (630)^2 = (600+30)^2 = (600)^2 + (2 \times 600 \times 30) + (30)^2 = 360000 + 36000 + 900 = 396900$$

Question 9:**Solution:**

$$(i) (196)^2 = (200-4)^2 = (200)^2 - (2 \times 200 \times 4) + (4)^2 = 40000 + 16 - 1600 = 38416$$

$$(ii) (689)^2 = (700-11)^2 = (700)^2 - (2 \times 700 \times 11) + (11)^2 = 490000 + 121 - 15400 = 474721$$

$$(iii) (891)^2 = (900-9)^2 = (900)^2 - (2 \times 900 \times 9) + (9)^2 = 810000 - 16200 + 81 = 793881$$

Question 10:**Solution:**

$$(i) 69 \times 71 = (70-1) \times (70+1) = 70^2 - 1^2 = 4900 - 1 = 4899$$

$$(ii) 94 \times 106 = (100-6) \times (100+6) = 100^2 - 6^2 = 10000 - 36 = 9964$$

Question 11:**Solution:**

$$(i) 88 \times 92 = (90-2) \times (90+2) = 90^2 - 2^2 = 8100 - 4 = 8096$$

$$(ii) 78 \times 82 = (80-2) \times (80+2) = 80^2 - 2^2 = 6400 - 4 = 6396$$

Question 12:**Solution:**

- (i) The square of an even number is **even**.
- (ii) The square of an odd number is **odd**.
- (iii) The square of a proper fraction is **less** than the given fraction.
- (iv) n^2 = the sum of first n **odd** natural numbers.

Question 13:**Solution:**

- (i) (F) as the number of digits in a perfect square is not even always.
- (ii) (F) as the square of a prime number will not be prime.
- (iii) (F) as the sum of two perfect squares will not be a perfect square.
- (iv) (F) as the difference of two perfect squares will not be a perfect square.
- (v) (T) as the product of two perfect squares is another perfect square.

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Exercise 3C

Find the value of each of the following, using the column method:

Question 1:

Solution:

I	II	III
a^2	$2ab$	b^2
$4+1=5$	12	9

Answer is 529.

Question 2:

Solution:

I	II	III
a^2	$2ab$	b^2
$9+3=12$	$30+2=32$	25

Answer is 1225.

Question 3:

Solution:

I	II	III
a^2	$2ab$	b^2
$25+2$	20	4

Answer is 2704.

Question 4:

Solution:

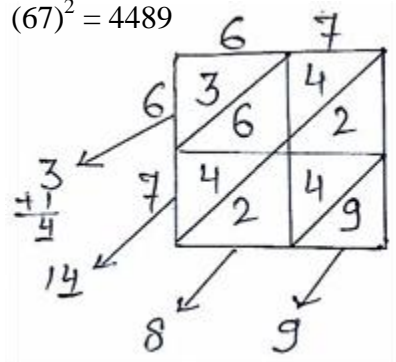
I	II	III
a^2	$2ab$	b^2
$81+11=92$	$108+3=111$	36

Answer is 9216.

Question 5:

Solution:

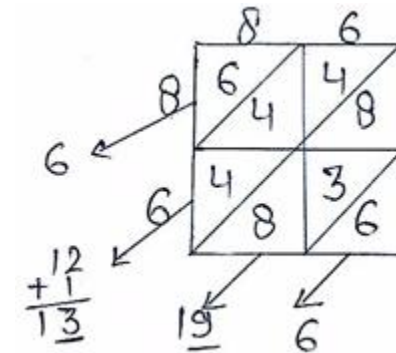
$$(67)^2 = 4489$$



Question 6:

Solution:

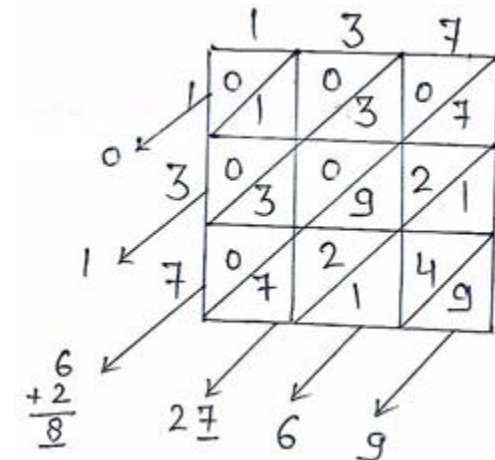
$$(86)^2 = 7396$$



Question 7:

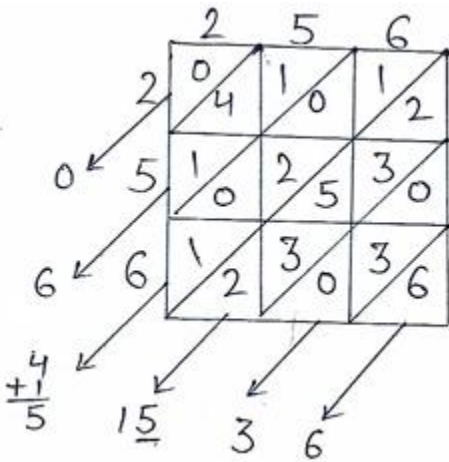
Solution:

$$(137)^2 = 18769$$



Question 8:**Solution:**

$$(256)^2 = 65536$$

**Page No: 50****Exercise 3D****Question 1:****Solution:**

$$5 \overline{)225}$$

$$5 \overline{)45}$$

$$3 \overline{)9}$$

3

Thus 225 is the product of 3, 3, 5, 5

The square root is thus the product of 3, 5 = 15.

Question 2:**Solution:**

$$3 \overline{)441}$$

$$3 \overline{)147}$$

$$7 \overline{)49}$$

7

Thus 441 is the product of 3, 3, 7, 7

The square root is thus the product of 3, 7 = 21.

Question 3:**Solution:**

$$\begin{array}{r}
 3 \overline{)729} \\
 \underline{000000} \\
 3 \overline{)243} \\
 \underline{000000} \\
 3 \overline{)81} \\
 \underline{000000} \\
 3 \overline{)27} \\
 \underline{000000} \\
 3 \overline{)9} \\
 \underline{000000} \\
 3
 \end{array}$$

Thus 729 is the product of 3, 3, 3, 3, 3, 3

The square root is thus the product of 3, 3, $3 = 27$.

Question 4:**Solution:**

$$\begin{array}{r}
 2 \overline{)1296} \\
 \underline{000000} \\
 2 \overline{)648} \\
 \underline{000000} \\
 2 \overline{)324} \\
 \underline{000000} \\
 2 \overline{)162} \\
 \underline{000000} \\
 3 \overline{)81} \\
 \underline{000000} \\
 3 \overline{)27} \\
 \underline{000000} \\
 3 \overline{)9} \\
 \underline{000000} \\
 3
 \end{array}$$

Thus 1296 is the product of 2, 2, 2, 2, 3, 3, 3, 3

The square root is thus the product of 2, 2, 3, 3 $= 36$.

Question 5:**Solution:**

$$\begin{array}{r}
 5 \overline{)2025} \\
 \underline{000000} \\
 5 \overline{)405} \\
 \underline{000000} \\
 3 \overline{)81} \\
 \underline{000000} \\
 3 \overline{)27}
 \end{array}$$

$$\begin{array}{r} \text{-----} \\ 3 \mid 9 \\ \text{-----} \\ 3 \end{array}$$

Thus 2025 is the product of 3, 3, 3, 3, 5, 5.

The square root is thus the product of 3, 3, 5 = 45.

Question 6:

Solution:

$$\begin{array}{r} 2 \mid 4096 \\ \text{-----} \\ 2 \mid 2048 \\ \text{-----} \\ 2 \mid 1024 \\ \text{-----} \\ 2 \mid 512 \\ \text{-----} \\ 2 \mid 256 \\ \text{-----} \\ 2 \mid 128 \\ \text{-----} \\ 2 \mid 64 \\ \text{-----} \\ 2 \mid 32 \\ \text{-----} \\ 2 \mid 16 \\ \text{-----} \\ 2 \mid 8 \\ \text{-----} \\ 2 \mid 4 \\ \text{-----} \\ 2 \end{array}$$

Thus 4096 is the product of 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2

The square root is thus the product of 2, 2, 2, 2, 2, 2 = 64.

Question 7:

Solution:

$$\begin{array}{r} 2 \mid 7056 \\ \text{-----} \\ 2 \mid 3528 \\ \text{-----} \\ 2 \mid 1764 \\ \text{-----} \\ 2 \mid 882 \\ \text{-----} \end{array}$$

$$\begin{array}{r}
 3 \overline{) 441} \\
 \underline{ 132} \\
 3 \overline{) 117} \\
 \underline{ 90} \\
 7 \overline{) 27} \\
 \underline{ 21} \\
 7
 \end{array}$$

Thus 7056 is the product of 2, 2, 2, 2, 3, 3, 7, 7.

The square root is thus the product of 2, 2, 3, 7 = 84.

Question 8:

Solution:

$$\begin{array}{r}
 2 \overline{) 8100} \\
 \underline{ 1620} \\
 2 \overline{) 4050} \\
 \underline{ 2025} \\
 5 \overline{) 2025} \\
 \underline{ 1012} \\
 5 \overline{) 405} \\
 \underline{ 202} \\
 3 \overline{) 81} \\
 \underline{ 40} \\
 3 \overline{) 27} \\
 \underline{ 13} \\
 3 \overline{) 9} \\
 \underline{ 3} \\
 3
 \end{array}$$

Thus 8100 is the product of 2, 2, 5, 5, 3, 3, 3, 3.

The square root is thus the product of 2, 3, 3, 5 = 90.

Question 9:

Solution:

$$\begin{array}{r}
 2 \overline{) 9216} \\
 \underline{ 1843} \\
 2 \overline{) 4608} \\
 \underline{ 2304} \\
 2 \overline{) 2304} \\
 \underline{ 1152} \\
 2 \overline{) 1152} \\
 \underline{ 576} \\
 2 \overline{) 576} \\
 \underline{ 288} \\
 2 \overline{) 288} \\
 \underline{ 144} \\
 2 \overline{) 144} \\
 \underline{ 72} \\
 2 \overline{) 72} \\
 \underline{ 36} \\
 2 \overline{) 36} \\
 \underline{ 18} \\
 2 \overline{) 18} \\
 \underline{ 9} \\
 3
 \end{array}$$

$$\begin{array}{r} \text{-----} \\ 2 \mid 72 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 2 \mid 36 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 2 \mid 18 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 9 \\ \text{-----} \end{array}$$

3

Thus 9216 is the product of 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 3.

The square root is thus the product of 2, 2, 2, 2, 2, 3 = 96.

Question 10:

Solution:

$$5 \mid 11025$$

$$\begin{array}{r} \text{-----} \\ 5 \mid 2205 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 441 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 147 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 7 \mid 49 \\ \text{-----} \end{array}$$

7

Thus 11025 is the product of 5, 5, 3, 3, 7, 7.

The square root is thus the product of 5, 3, 7 = 105.

Question 11:

Solution:

$$2 \mid 15876$$

$$\begin{array}{r} \text{-----} \\ 2 \mid 7938 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 3969 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 1323 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 441 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 147 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 7 \mid 49 \\ \text{-----} \end{array}$$

7

Thus 15876 is the product of 2, 2, 3, 3, 3, 3, 7, 7.

The square root is thus the product of 2, 3, 3, 7 = 126.

Question 12:

Solution:

$$2 \overline{)17424}$$

$$2 \overline{)8712}$$

$$2 \overline{)4356}$$

$$2 \overline{)2178}$$

$$3 \overline{)1089}$$

$$3 \overline{)363}$$

$$11 \overline{)121}$$

11

Thus 17424 is the product of 2, 2, 2, 2, 3, 3, 11, 11.

The square root is thus the product of 2, 2, 3, 11 = 132.

Question 13:

Solution:

252 = product of 2, 2, 3, 3, 7.

So 252 must be multiplied by 7 to obtain a perfect square of 1764.

The square root of 1764 is then determined.

$$4 \overline{)1764} \quad (42$$

16

$$82) 164$$

164

0

Thus the perfect square of 1764 is obtained by multiplying the given number by 7. The square root is 42.

Question 14:

Solution:

The value $2925 = 3 \times 3 \times 5 \times 5 \times 13$

So this number must be divided by 13 $\Rightarrow 2925 \div 13 = 225$

Now the square root of 225 is obtained.

$$\begin{array}{r} 1 \) \ 225 \ (\ 15 \\ \underline{1} \end{array}$$

$$\begin{array}{r} 25 \) \ 125 \\ \underline{125} \end{array}$$

$$\begin{array}{r} \underline{0} \end{array}$$

The square root is thus 15 and the number that must be divided is 13.

Question 15:

Solution:

Given the number of plants = 1225 plants.

So the no. of rows = number of plants in each row = square root of 1225

$$\begin{array}{r} 3 \) \ 1225 \ (\ 35 \\ \underline{9} \end{array}$$

$$\begin{array}{r} 65 \) \ 325 \\ \underline{325} \end{array}$$

$$\begin{array}{r} \underline{0} \end{array}$$

So the no. of rows = number of plants in each row = 35.

Question 16:

Solution:

Given that each student contributed the same amount as the number of children in the class. So,

$$x^2 = 1156 \Rightarrow x = 34$$

$$\begin{array}{r} 3 \) \ 1156 \ (\ 34 \\ \underline{9} \end{array}$$

$$\begin{array}{r} 64 \) \ 256 \\ \underline{256} \end{array}$$

$$\begin{array}{r} \underline{0} \end{array}$$

So the strength of the class is 34.

Question 17:

Solution:

The LCM of numbers 6, 9, 15 and 20 is 180.

$$2 \ | \ 180$$

$$2 \ | \ 90$$

$$3 \ | \ 45$$

$$\begin{array}{r} \text{-----} \\ 3 \mid 15 \\ \text{-----} \end{array}$$

5

So 120 = product of 2, 2, 3, 3, 5. So to make it a perfect square we need to multiply it by 5
So we get product of 180 and 5 to be 900.

Question 18:

Solution:

The LCM of numbers 8, 12, 15 and 20 is 120.

$$\begin{array}{r} 2 \mid 120 \\ \text{-----} \end{array}$$

$$2 \mid 60$$

$$\begin{array}{r} \text{-----} \\ 2 \mid 30 \\ \text{-----} \end{array}$$

$$\begin{array}{r} 3 \mid 15 \\ \text{-----} \end{array}$$

5

So 120 = product of 2, 2, 2, 3, 5. So to make it a perfect square we need to multiply it by 2, 3 and 5 = 30
So we get product of 120 and 30 to be 3600.

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Exercise 3E

Evaluate:

Question 1:

Solution:

$$\begin{array}{r} 2 \mid 576 \quad (24 \\ 4 \end{array}$$

$$\begin{array}{r} \text{-----} \\ 44) 176 \\ 176 \\ \text{-----} \end{array}$$

0

Therefore, square root of 576 = 24

Question 2:

Solution:

$$\begin{array}{r} 3 \mid 1444 \quad (38 \\ 9 \end{array}$$

$$\begin{array}{r} 68) 544 \\ 544 \\ \hline \end{array}$$

0

Therefore, square root of 1444 = 38

Question 3:

Solution:

$$\begin{array}{r} 6) 4489 \\ 36 \\ \hline \end{array}$$

$$\begin{array}{r} 127) 0889 \\ 0889 \\ \hline \end{array}$$

0

Therefore, square root of 4489 = 67

Question 4:

Solution:

$$\begin{array}{r} 7) 6241 \\ 49 \\ \hline \end{array}$$

$$\begin{array}{r} 149) 1341 \\ 1341 \\ \hline \end{array}$$

0

Therefore, square root of 6241 = 79

Question 5:

Solution:

$$\begin{array}{r} 8) 7056 \\ 64 \\ \hline \end{array}$$

$$\begin{array}{r} 164) 656 \\ 656 \\ \hline \end{array}$$

0

Therefore, square root of 7056 = 84

Question 6:

Solution:

$$\begin{array}{r} 9) 9025 \\ 81 \\ \hline \end{array}$$

$$\begin{array}{r}
 185 \overline{)925} \\
 \underline{925} \\
 0
 \end{array}$$

Therefore, square root of 9025 = 95

Question 7:

Solution:

$$\begin{array}{r}
 1 \overline{)11449} \text{ (107} \\
 \underline{1}
 \end{array}$$

$$\begin{array}{r}
 20 \overline{)14} \\
 \underline{00}
 \end{array}$$

$$\begin{array}{r}
 207 \overline{)1449} \\
 \underline{1449}
 \end{array}$$

$$\begin{array}{r}
 0
 \end{array}$$

Therefore, square root of 11449 = 107

Question 8:

Solution:

$$\begin{array}{r}
 1 \overline{)14161} \text{ (119} \\
 \underline{1}
 \end{array}$$

$$\begin{array}{r}
 21 \overline{)041} \\
 \underline{021}
 \end{array}$$

$$\begin{array}{r}
 229 \overline{)02061} \\
 \underline{02061}
 \end{array}$$

$$\begin{array}{r}
 0
 \end{array}$$

Therefore, square root of 14161 = 119

Question 9:

Solution:

$$\begin{array}{r}
 1 \overline{)10404} \text{ (102} \\
 \underline{1}
 \end{array}$$

$$\begin{array}{r}
 20 \overline{)04} \\
 \underline{00}
 \end{array}$$

$$\begin{array}{r}
 102 \overline{)0404} \\
 \underline{0404}
 \end{array}$$

$$\begin{array}{r}
 0
 \end{array}$$

Therefore, square root of 10404 = 102

Question 10:

Solution:

$$\begin{array}{r} 1 \) \ 17956 \ (\ 134 \\ \underline{1} \\ 23 \) \ 79 \\ \underline{69} \\ 264 \) \ 1056 \\ \underline{1056} \\ 0 \end{array}$$

Therefore, square root of 17956 = 134

Question 11:

Solution:

$$\begin{array}{r} 1 \) \ 19600 \ (\ 140 \\ \underline{1} \\ 24 \) \ 96 \\ \underline{96} \\ 0 \end{array}$$

Therefore, square root of 19600 = 140

Question 12:

Solution:

$$\begin{array}{r} 3 \) \ 92416 \ (\ 304 \\ \underline{9} \\ 60 \) \ 24 \\ \underline{00} \\ 604 \) \ 2416 \\ \underline{2416} \\ 0 \end{array}$$

Therefore, square root of 92416 = 304

Question 13:

Solution:

We find the square root of 2509 using the long division method.

$$\begin{array}{r}
 50 \\
 \hline
 5 \overline{) 2509} \\
 \underline{5 25} \\
 100 \overline{) 09}
 \end{array}$$

Here, the remainder is 9.

Hence, $50^2 < 2509$

And we know that, $50^2 = 2500$

Hence, the number to be subtracted is $2509 - 2500 = 9$

Question 14:

Solution:

On finding the square root of 7581

$$\begin{array}{r}
 87 \\
 \hline
 8 \overline{) 7581} \\
 \underline{64} \\
 167 \overline{) 1181} \\
 \underline{1169} \\
 12
 \end{array}$$

Quotient = 87, remainder = 12

Hence we will subtract 12 from 7581 which is 7569 to get the perfect square.

Hence the square root of 7569 is 87

Question 15:

Solution:

$$\begin{array}{r}
 78 \\
 \hline
 7 \overline{) 6203} \\
 \underline{49} \\
 148 \overline{) 1303} \\
 \underline{1184} \\
 119
 \end{array}$$

Since this number is close to the square of 78, the square of 79 is 6241 which is obtained by adding 38 to the given number.

The perfect square of 6241 is obtained by adding 38. Its square root is 79.

Question 16:**Solution:**

$$\begin{array}{r}
 91 \\
 9 \overline{) 8400} \\
 \underline{81} \\
 181 \overline{) 300} \\
 \underline{181} \\
 119
 \end{array}$$

So to obtain the square of 92 which is 8464, we need to add 64 to the given number.

Question 17:**Solution:**

The smallest 4 digit number is 1000.

$$\begin{array}{r}
 31 \\
 3 \overline{) 1000} \\
 \underline{09} \\
 61 \overline{) 0100} \\
 \underline{61} \\
 39
 \end{array}$$

So the least 4 digit number which is a perfect square is 32 and its square is 1024.

Question 18:**Solution:**

The greatest five digit number is 99999.

$$\begin{array}{r}
 316 \\
 3 \overline{) 99,999} \\
 \underline{9} \\
 61 \overline{) 099} \\
 \underline{61} \\
 62 \overline{) 3899} \\
 \underline{3756} \\
 143
 \end{array}$$

So 143 is subtracted from 99,999 to obtain the square of 316 which is equal to 99856.

Question 19:**Solution:**

Area of the field = 60025 = side²

So the side = $\sqrt{60025} = 245$ m

So the perimeter = 4 times the side = 245×4 m

Since the speed = 18 km/h, $18 \text{ km/h} = 18 \times \frac{5}{18} \text{ m/s} = 5 \text{ m/s}$.

Hence the time taken = $\frac{245 \times 4}{5} = 49 \times 4 = 196$ sec

Hence the required time is 196 seconds.

Page No: 56**Exercise 3F****Evaluate:****Question 1:****Solution:**

$$\begin{array}{r}
 1.3 \\
 \hline
 1 \overline{) 1.69} \\
 \underline{1} \\
 23 \overline{) 0.69} \\
 \underline{0.69} \\
 0
 \end{array}$$

So $\sqrt{1.69} = 1.3$

Question 2:**Solution:**

$$\begin{array}{r}
 5.8 \\
 \hline
 5 \overline{) 33.64} \\
 \underline{25} \\
 108 \overline{) 08.64} \\
 \underline{08.64} \\
 0
 \end{array}$$

So $\sqrt{33.64} = 5.8$

Question 3:**Solution:**

12.5

$$\begin{array}{r}
 1 \overline{) 156.25} \\
 \underline{1} \\
 22 \overline{) 056} \\
 \underline{044} \\
 245 \overline{) 12.25} \\
 \underline{12.25} \\
 0
 \end{array}$$

So $\sqrt{156.25} = 12.5$ **Question 4:****Solution:**

8.7

$$\begin{array}{r}
 8 \overline{) 75.69} \\
 \underline{64} \\
 167 \overline{) 11.69} \\
 \underline{11.69} \\
 0
 \end{array}$$

So, $\sqrt{75.69} = 8.7$ **Question 5:****Solution:**

3.14

$$\begin{array}{r}
 3 \overline{) 9.8596} \\
 \underline{9} \\
 61 \overline{) 0.85} \\
 \underline{0.61} \\
 624 \overline{) 0.2496} \\
 \underline{0.2496} \\
 0
 \end{array}$$

So $\sqrt{9.8596} = 3.14$

Question 6:**Solution:**

3.17

$$\begin{array}{r}
 3 \overline{) 10.0489} \\
 \underline{9} \\
 61 \overline{) 1.04} \\
 \underline{0.61} \\
 627 \overline{) 0.4389} \\
 \underline{0.4389} \\
 0
 \end{array}$$

So $\sqrt{10.0489} = 3.17$ **Question 7:****Solution:**

1.04

$$\begin{array}{r}
 1 \overline{) 1.0816} \\
 \underline{1} \\
 204 \overline{) 0.0816} \\
 \underline{0.0816} \\
 0
 \end{array}$$

So, $\sqrt{1.0816} = 1.04$ **Question 8:****Solution:**

0.54

$$\begin{array}{r}
 0 \overline{) 0.2916} \\
 \underline{0} \\
 05 \overline{) 0.29} \\
 \underline{0.25} \\
 104 \overline{) 0.0416} \\
 \underline{0.0416} \\
 0
 \end{array}$$

So, $\sqrt{0.2916} = 0.54$

Question 9:**Solution:**

1.73

$$\begin{array}{r}
 1 \overline{) 3.0000} \\
 \underline{1} \\
 27 \overline{) 2.00} \\
 \underline{1.89} \\
 343 \overline{) 0.1100} \\
 \underline{0.1029} \\
 0.071
 \end{array}$$

 $\sqrt{3}$ up to two places of decimal = 1.73**Question 10:****Solution:**

1.67

$$\begin{array}{r}
 1 \overline{) 2.8000} \\
 \underline{1} \\
 26 \overline{) 1.80} \\
 \underline{1.56} \\
 327 \overline{) 0.2400} \\
 \underline{0.2289} \\
 0.0111
 \end{array}$$

So $\sqrt{2.8}$ correct up to two places of decimal = 1.67**Question 11:****Solution:**

0.948

$$\begin{array}{r}
 0 \overline{) 0.900000} \\
 \underline{0} \\
 09 \overline{) 0.90} \\
 \underline{0.81} \\
 184 \overline{) 0.0900} \\
 \underline{0.0736}
 \end{array}$$

$$\begin{array}{r}
 1888 \mid 0.016400 \\
 0.015104 \\
 \hline
 0.001296
 \end{array}$$

So, $\sqrt{0.9}$ correct up to two places of decimal. = 0.95 obtained by rounding off 0.948.

Question 12:

Solution:

Area of rectangle = product of length and breadth = $13.6 \times 3.4 = 46.24$

Here the area of a square = area of rectangle

So the area of square = 46.24

Therefore, $\text{side}^2 = 46.24$

Side of square = $\sqrt{46.24} = 6.8\text{m}$

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Exercise 3G

Question 1:

Solution:

$$\sqrt{\frac{16}{81}} = \frac{\sqrt{16}}{\sqrt{81}} = \frac{4}{9}$$

Question 2:

Solution:

$$\sqrt{\frac{64}{225}} = \frac{\sqrt{64}}{\sqrt{225}} = \frac{8}{15}$$

Question 3:

Solution:

$$\sqrt{\frac{121}{256}} = \frac{\sqrt{121}}{\sqrt{256}} = \frac{11}{16}$$

Question 4:

Solution:

$$\sqrt{\frac{625}{729}} = \frac{\sqrt{625}}{\sqrt{729}} = \frac{25}{27}$$

Question 5:

Solution:

$$\sqrt{3\frac{13}{36}} = \sqrt{\frac{121}{36}} = \frac{11}{6} = 1\frac{5}{6}$$

Question 6:

Solution:

$$\sqrt{4\frac{73}{324}} = \sqrt{\frac{1396}{324}} = \frac{37}{18} = 2\frac{1}{18}$$

Question 7:

Solution:

$$\sqrt{3\frac{33}{289}} = \sqrt{\frac{900}{289}} = \frac{30}{17} = 1\frac{13}{17}$$

Question 8:

Solution:

$$\frac{\sqrt{80}}{\sqrt{405}} = \sqrt{\frac{80}{405}} = \sqrt{\frac{16}{81}} = \frac{\sqrt{16}}{\sqrt{81}} = \frac{4}{9}$$

Question 9:

Solution:

$$\frac{\sqrt{1183}}{\sqrt{2023}} = \sqrt{\frac{169}{289}} = \frac{\sqrt{169}}{\sqrt{289}} = \frac{13}{17}$$

Question 10:

Solution:

$$\frac{\sqrt{98} \times \sqrt{162}}{126} = \frac{\sqrt{98} \times \sqrt{162}}{126} = \frac{\sqrt{15876}}{126}$$

$$\begin{array}{r} 1 \overline{) 15876} \\ \underline{1} \\ 22 \overline{) 058} \\ \underline{44} \\ 246 \overline{) 1476} \\ \underline{1476} \\ 0 \end{array}$$

So $\sqrt{98} \times \sqrt{162} = 126$.

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Exercise 3H

OBJECTIVE QUESTIONS

Tick (✓) the correct answer in each of the following:

Question 1:

Solution:

(c) Since 5478 ends in 8, it cannot be a perfect square.

Question 2:

Solution:

(d) 2222 ends in 2 and hence cannot be a perfect square.

Question 3:

Solution:

(a) 1843 ends in 3 and hence is not a perfect square.

Question 4:

Solution:

(b) As 4784 ends in 4, it cannot be a perfect square.

Question 5:

Solution:

(c) 81000 as the number of zeros at the end is odd.

Question 6:

Solution:

(d) 8 cannot be the last (unit) digit of a perfect square number.

Question 7:

Solution:

(b) as the square of a proper fraction will usually be smaller than the fraction.

Question 8:

Solution:

(c) n^2 as the sum of the n odd terms is the square of n itself.

Question 9:

Solution:

(d) For every natural number $m > 1$, $(2m, m^2 - 1, m^2 + 1)$ is a Pythagorean triplet.

So, (8, 15, 17) is correct.

Question 10:

Solution: (c)

$$\begin{array}{r} 13 \\ 1 \overline{) 176} \\ \underline{1} \\ 23 \overline{) 076} \\ \underline{69} \\ 7 \end{array}$$

So 7 must be subtracted.

Question 11:

Solution: (a)

$$\begin{array}{r} 22 \\ 2 \overline{) 526} \\ \underline{4} \\ 42 \overline{) 126} \\ \underline{84} \\ 42 \end{array}$$

So the number to be added is 3 as the square root of 529 is 23.

Question 12:

Solution:

(b)

$$\begin{array}{r} 123 \\ 1 \overline{) 15370} \\ \underline{1} \\ 22 \overline{) 053} \\ \underline{44} \\ 243 \overline{) 970} \\ \underline{729} \\ 241 \end{array}$$

So in order to obtain the square of 124, we need to add 6.

Question 13:**Solution:**

(d) 0.94 is the square root of 0.9 found using the usual method.

Question 14:**Solution:**

(c) 0.316 is the square root of 0.1 found using the general method.

Question 15:**Solution:**

$$(b) \sqrt{0.9} \times \sqrt{1.6} = \sqrt{1.44} = 1.2$$

Question 16:**Solution:**

$$(c) \frac{\sqrt{288}}{\sqrt{128}} = \sqrt{\frac{288}{128}} = \sqrt{\frac{9}{4}} = \frac{3}{2}$$

Question 17:**Solution:**

$$(b) \sqrt{2\frac{1}{4}} = \sqrt{\frac{9}{4}} = \frac{3}{2} = 1\frac{1}{2}$$

Question 18:**Solution:**

(a) Since the square of an even number is even, the answer is 196.

Question 19:**Solution:**

(c) Since the square of an odd number is odd, 1369 is the answer.

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TEST PAPER – 3

A.

Question 1:**Solution:**

$$\begin{array}{r} 106 \\ 1 \overline{) 11236} \\ \underline{1} \\ 11236 \\ \underline{1} \\ 11236 \\ \underline{1} \\ 11236 \\ \underline{1} \\ 11236 \end{array}$$

$$\begin{array}{r} \underline{} \\ 20 \overline{) 012} \\ \underline{00} \end{array}$$

$$\begin{array}{r} \underline{} \\ 206 \overline{) 1236} \\ \underline{1236} \end{array}$$

$$\begin{array}{r} \underline{} \\ 0 \end{array}$$

So $\sqrt{11236} = 106$.

Question 2:

Solution:

The largest 5 digit number is 99,999.

316

$$\begin{array}{r} \underline{} \\ 3 \overline{) 99,999} \\ \underline{9} \end{array}$$

$$\begin{array}{r} \underline{} \\ 61 \overline{) 099} \\ \underline{61} \end{array}$$

$$\begin{array}{r} \underline{} \\ 62 \overline{) 3899} \\ \underline{3756} \end{array}$$

$$\begin{array}{r} \underline{} \\ 143 \end{array}$$

So 143 is subtracted from 99,999 to obtain the square of 316 which is equal to 99856.

Question 3:

Solution:

The smallest 4 digit number is 1000.

31

$$\begin{array}{r} \underline{} \\ 3 \overline{) 1000} \\ \underline{09} \end{array}$$

$$\begin{array}{r} \underline{} \\ 61 \overline{) 0100} \\ \underline{61} \end{array}$$

$$\begin{array}{r} \underline{} \\ 39 \end{array}$$

So the least 4 digit number which is a perfect square is 32 and its square is 1024.

Question 4:**Solution:**

0.53

$$\begin{array}{r}
 5 \overline{) 0.2809} \\
 \underline{0.25} \\
 103 \overline{) 0.0309} \\
 \underline{0.0309} \\
 0
 \end{array}$$

So $\sqrt{0.2809} = 0.53$ **Question 5:****Solution:**

1.73

$$\begin{array}{r}
 1 \overline{) 3.0000} \\
 \underline{1} \\
 27 \overline{) 2.00} \\
 \underline{1.89} \\
 343 \overline{) 0.1100} \\
 \underline{0.1029} \\
 0.071
 \end{array}$$

 $\sqrt{3}$ up to two places of decimal = 1.73**Question 6:****Solution:**

$$\frac{\sqrt{48}}{\sqrt{243}} = \sqrt{\frac{48}{243}} = \sqrt{\frac{16}{81}} = \frac{4}{9}$$

B.**Question 7:****Solution:**

(d) As 1222 ends in 2, it is not a perfect square.

Question 8:**Solution:**

$$(c) \sqrt{2\frac{1}{4}} = \sqrt{\frac{9}{4}} = \frac{\sqrt{9}}{\sqrt{4}} = \frac{3}{2} = 1\frac{1}{2}$$

Question 9:**Solution:**

(c) As the square of an even number is even too.

Question 10:**Solution:**

(d)

$$\begin{array}{r}
 22 \\
 \hline
 2 \quad | \quad 521 \\
 \quad 4 \\
 \hline
 42 \quad | \quad 121 \\
 \quad \quad 84 \\
 \hline
 \quad \quad 37
 \end{array}$$

So, 8 must be added to obtain the square of 23.

Question 11:**Solution:**

(c)

$$\begin{array}{r}
 13 \\
 \hline
 1 \quad | \quad 178 \\
 \quad 1 \\
 \hline
 23 \quad | \quad 78 \\
 \quad \quad 69 \\
 \hline
 \quad \quad 9
 \end{array}$$

Question 12:**Solution:**

$$(b) \sqrt{72} \times \sqrt{98} = \sqrt{7056} = 84$$

C.

Question 13:**Solution:**

(i) $1 + 3 + 5 + 7 + 9 + 11 + 13 = (7)^2$ as the sum of n odd terms is n^2

(ii) $\sqrt{1681} = 41$ using the general method of finding square roots.

$$\begin{array}{r}
 41 \\
 \hline
 4 \quad | \quad 1681
 \end{array}$$

$$\begin{array}{r}
 16 \\
 81 \overline{) 0081} \\
 \underline{0081} \\
 0
 \end{array}$$

(iii) The smallest square number exactly divisible by 2, 4, 6 is 36. (The LCM of 2, 4, 6 = 12. By factorization, 12 is the product of (2, 2, 3). So the smallest square number is the product of (2, 2, 3, 3) = 36.)

(iv) A given number is a perfect square having n digits, where n is odd. Then, its square root will have $\frac{1}{2}(n+1)$ digits. (Take the example of 256, there are 3 digits in it. Its square root has 2 digits that satisfies the given result. Similarly for the case of 15376.)