

Chapter 7: Factorisation

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Exercise 7A

Question 1. (i)

Solution:

$$12x + 15 = 3(4x + 5)$$

(ii)

Solution:

$$14m - 21 = 7(2m - 3)$$

(iii)

Solution:

$$9n - 12n^2 = 3n(3 - 4n)$$

Question 2. (i)

Solution:

$$16a^2 - 24ab = 8a(2a - 3b)$$

(ii)

Solution:

$$15ab^2 - 20a^2b = 5ab(3b - 4a)$$

(iii)

Solution:

$$12x^2y^3 - 21x^3y^2 = 3x^2y^2(4y - 7x)$$

Question 3. (i)

Solution:

$$24x^3 - 36x^2y = 6x^2(4x - 6y)$$

(ii)

Solution:

$$10x^3 - 15x^2 = 5x^2(2x - 3)$$

(iii)

Solution:

$$36x^3y - 60x^2y^3z = 12x^2y(3x - 5y^2z)$$

Question 4. (i)

Solution:

$$9x^3 - 6x^2 + 12x = 3x(3x^2 - 2x + 4)$$

(ii)

Solution:

$$8x^2 - 72xy + 12x = 4x(2x^2 - 18y + 3)$$

(iii)

Solution:

$$18a^3b^3 - 27a^2b^3 + 36a^3b^2 = 9a^2b^2(2ab - 3b + 4a)$$

Question 5. (i)

Solution:

$$14x^3 + 21x^4y - 28x^2y^2 = 7x^2(2x + 3x^2y - 4y^2)$$

(ii)

Solution:

$$-5 - 10t + 20t^2 = 5(-1 - 2t + 4t^2)$$

Question 6. (i)

Solution:

$$x(x + 3) + 5(x + 3) = (x + 3)(x + 5)$$

(ii)

Solution:

$$5x(x - 4) - 7(x - 4) = (x - 4)(5x - 7)$$

(iii)

Solution:

$$2m(1 - n) + 3(1 - n) = (1 - n)(2m + 3)$$

Question 7.

Solution:

$$6a(a - 2b) + 5b(a - 2b) = (a - 2b)(6a + 5b)$$

Question 8.

Solution:

$$x^3(2a - b) + x^2(2a - b)$$

$$= (2a - b)(x^3 + x^2)$$

$$= x^2(x + 1)(2a - b)$$

Question 9.

Solution:

$$9a(3a - 5b) - 12a^2(3a - 5b)$$

$$= (3a - 5b)(9a - 12a^2)$$

$$= 3a(3 - 4a)(3a - 5b)$$

Question 10.**Solution:**

$$\begin{aligned}(x+5)^2 - 4(x+5) \\&= (x+5)\{(x+5)-4\} \\&= (x+5)(x+1)\end{aligned}$$

Question 11.**Solution:**

$$\begin{aligned}3(a-2b)^2 - 5(a-2b) \\&= (a-2b)\{3(a-2b)-5\} \\&= (a-2b)(3a-6b-5)\end{aligned}$$

Question 12.**Solution:**

$$\begin{aligned}2a+6b-3(a+3b)^2 \\&= 2(a+3b)-3(a+3b)^2 \\&= (a+3b)\{2-3(a+3b)\} \\&= (a+3b)(2-3a-9b)\end{aligned}$$

Question 13.**Solution:**

$$\begin{aligned}16(2p-3q)^2 - 4(2p-3q) \\&= (2p-3q)\{16(2p-3q)-4\} \\&= (2p-3q)(32p-48q-4)\end{aligned}$$

Question 14.**Solution:**

$$\begin{aligned}x(a-3)+y(3-a) \\&= x(a-3)-y(a-3) \\&= (a-3)(x-y)\end{aligned}$$

Question 15.**Solution:**

$$\begin{aligned}12(2x-3y)^2 - 16(3y-2x) \\&= 12(2x-3y)^2 + 16(2x-3y) \\&= (2x-3y)\{12(2x-3y)+16\} \\&= (2x-3y)(24x-36y+16)\end{aligned}$$

Question 16.**Solution:**

$$\begin{aligned}(x+y)(2x+5) - (x+y)(x+3) \\&= (x+y)\{(2x+5) - (x+3)\} \\&= (x+y)(2x+5-x-3) \\&= (x+y)(x+2)\end{aligned}$$

Question 17.**Solution:**

$$\begin{aligned}ar + br + at + bt \\&= (ar + br) + (at + bt) \\&= r(a+b) + t(a+b) \\&= (a+b)(r+t)\end{aligned}$$

Question 18.**Solution:**

$$\begin{aligned}x^2 - ax - bx + ab \\&= (x^2 - bx) - (ax - ab) \\&= x(x-b) - a(x-b) \\&= (x-b)(x-a)\end{aligned}$$

Question 19.**Solution:**

$$\begin{aligned}ab^2 - bc^2 - ab + c^2 \\&= (ab^2 - ab) - (bc^2 - c^2) \\&= ab(b-1) - c^2(b-1) \\&= (b-1)(ab - c^2)\end{aligned}$$

Question 20.**Solution:**

$$\begin{aligned}x^2 - xz + xy - yz \\&= (x^2 + xy) - (xz + yz) \\&= x(x+y) - z(x+y) \\&= (x+y)(x-z)\end{aligned}$$

Question 21.**Solution:**

$$\begin{aligned} & 6ab - b^2 + 12ac - 2bc \\ &= (6ab + 12ac) - (b^2 + 2bc) \\ &= 6a(b + 2c) - b(b + 2c) \\ &= (b + 2c)(6a - b) \end{aligned}$$

Question 22.**Solution:**

$$\begin{aligned} & (x - 2y)^2 + 4x - 8y \\ &= (x - 2y)^2 + 4(x - 2y) \\ &= (x - 2y)\{(x - 2y) + 4\} \\ &= (x - 2y)(x - 2y + 4) \end{aligned}$$

Question 23.**Solution:**

$$\begin{aligned} & y^2 - xy(1 - x) - x^3 \\ &= y^2 - xy + x^2y - x^3 \\ &= y(y - x) + x^2(y - x) \\ &= (y - x)(y + x^2) \end{aligned}$$

Question 24.**Solution:**

$$\begin{aligned} & (ax + by)^2 + (bx - ay)^2 \\ &= (a^2x^2 + b^2y^2 + 2axby) + (b^2x^2 + a^2y^2 - 2bxay) \\ &= a^2x^2 + a^2y^2 + b^2y^2 + b^2x^2 + 2axby - 2bxay \\ &= a^2(x^2 + y^2) + b^2(x^2 + y^2) \\ &= (x^2 + y^2)(a^2 + b^2) \end{aligned}$$

Question 25.**Solution:**

$$\begin{aligned} & ab^2 + (a - b)b - 1 \\ &= ab^2 + ba - b - 1 \\ &= ab(b + 1) - 1(b + 1) \\ &= (b + 1)(ab - 1) \end{aligned}$$

Question 26.**Solution:**

$$\begin{aligned} & x^3 - 3x^2 + x - 3 \\ &= (x^3 - 3x^2) + (x - 3) \\ &= x^2(x - 3) + 1(x - 3) \\ &= (x - 3)(x^2 + 1) \end{aligned}$$

Question 27.**Solution:**

$$\begin{aligned} & ab(x^2 + y^2) - xy(a^2 + b^2) \\ &= abx^2 + aby^2 - a^2xy - b^2xy \\ &= abx^2 - a^2xy + aby^2 - b^2xy \\ &= ax(bx - ay) + by(ay - bx) \\ &= ax(bx - ay) - by(bx - ay) \\ &= (bx - ay)(ax - by) \end{aligned}$$

Question 28.**Solution:**

$$\begin{aligned} & x^2 - x(a + 2b) + 2ab \\ &= x^2 - ax - 2bx + 2ab \\ &= x^2 - 2bx - ax + 2ab \\ &= (x^2 - 2bx) - (ax - 2ab) \\ &= x(x - 2b) - a(x - 2b) \\ &= (x - 2b)(x - a) \end{aligned}$$

Page number: 100**Exercise 7B****Question 1.****Solution:**

$$\begin{aligned} & x^2 - 36 \\ &= x^2 - (6)^2 \\ &= (x + 6)(x - 6) \end{aligned}$$

Question 2.**Solution:**

$$\begin{aligned} &4a^2 - 9 \\ &= (2a)^2 - (3)^2 \\ &= (2a + 3)(2a - 3) \end{aligned}$$

Question 3.**Solution:**

$$\begin{aligned} &81 - 49x^2 \\ &= (9)^2 - (7x)^2 \\ &= (9 + 7x)(9 - 7x) \end{aligned}$$

Question 4.**Solution:**

$$\begin{aligned} &4x^2 - 9y^2 \\ &= (2x)^2 - (3y)^2 \\ &= (2x + 3y)(2x - 3y) \end{aligned}$$

Question 5.**Solution:**

$$\begin{aligned} &16a^2 - 225b^2 \\ &= (4a)^2 - (15b)^2 \\ &= (4a + 15b)(4a - 15b) \end{aligned}$$

Question 6.**Solution:**

$$\begin{aligned} &9a^2b^2 - 25 \\ &= (3ab)^2 - (5)^2 \\ &= (3ab + 5)(3ab - 5) \end{aligned}$$

Question 7.**Solution:**

$$\begin{aligned} &16a^2 - 144 \\ &= (4a)^2 - (12)^2 \\ &= (4a + 12)(4a - 12) \end{aligned}$$

Question 8.**Solution:**

$$\begin{aligned} &63a^2 - 112b^2 \\ &= 7(9a^2 - 16b^2) \\ &= 7\{(3a)^2 - (4b)^2\} \\ &= 7\{(3a + 4b)(3a - 4b)\} \end{aligned}$$

Question 9.**Solution:**

$$\begin{aligned} &20a^2 - 45b^2 \\ &= 5(4a^2 - 9b^2) \\ &= 5\{(2a)^2 - (3b)^2\} \\ &= 5\{(2a + 3b)(2a - 3b)\} \end{aligned}$$

Question 10.**Solution:**

$$\begin{aligned} &12x^2 - 27 \\ &= 3(4x^2 - 9) \\ &= 3\{(2x)^2 - (3)^2\} \\ &= 3\{(2x + 3)(2x - 3)\} \end{aligned}$$

Question 11.**Solution:**

$$\begin{aligned} &x^3 - 64x \\ &= x\{(x)^2 - (8)^2\} \\ &= x\{(x + 8)(x - 8)\} \end{aligned}$$

Question 12.**Solution:**

$$\begin{aligned} &16x^5 - 144x^3 \\ &= x^3(16x^2 - 144) \\ &= x^3\{(4x)^2 - (12)^2\} \\ &= x^3\{(4x + 12)(4x - 12)\} \end{aligned}$$

Question 13.**Solution:**

$$\begin{aligned} & 3x^5 - 48x^3 \\ &= 3x^3(x^2 - 16) \\ &= 3x^3\{(x)^2 - (4)^2\} \\ &= 3x^3\{(x+4)(x-4)\} \end{aligned}$$

Question 14.**Solution:**

$$\begin{aligned} & 16p^3 - 4p \\ &= 4p(4p^2 - 1) \\ &= 4p\{(2p)^2 - (1)^2\} \\ &= 4p\{(2p+1)(2p-1)\} \end{aligned}$$

Question 15.**Solution:**

$$\begin{aligned} & 63a^2b^2 - 7 \\ &= 7(9a^2b^2 - 1) \\ &= 7\{(3ab)^2 - (1)^2\} \\ &= 7\{(3ab+1)(3ab-1)\} \end{aligned}$$

Question 16.**Solution:**

$$\begin{aligned} & 1 - (b-c)^2 \\ &= (1)^2 - (b-c)^2 \\ &= (1+b-c)(1-b+c) \end{aligned}$$

Question 17.**Solution:**

$$\begin{aligned} & (2a+3b)^2 - 16c^2 \\ &= (2a+3b)^2 - (4c)^2 \\ &= (2a+3b+4c)(2a+3b-4c) \end{aligned}$$

Question 18.**Solution:**

$$\begin{aligned}(l+m)^2 - (l-m)^2 \\&= (l+m+l-m)(l+m-l+m) \\&= (2l)(2m)\end{aligned}$$

Question 19.**Solution:**

$$\begin{aligned}(2x+5y)^2 - 1 \\&= (2x+5y)^2 - (1)^2 \\&= (2x+5y+1)(2x+5y-1)\end{aligned}$$

Question 20.**Solution:**

$$\begin{aligned}36c^2 - (5a+b)^2 \\&= (6c)^2 - (5a+b)^2 \\&= (6c+5a+b)(6c-5a-b)\end{aligned}$$

Question 21.**Solution:**

$$\begin{aligned}(3x-4y)^2 - 25z^2 \\&= (3x-4y)^2 - (5z)^2 \\&= (3x-4y+5z)(3x-4y-5z)\end{aligned}$$

Question 22.**Solution:**

$$\begin{aligned}x^2 - y^2 - 2y - 1 \\&= x^2 - (y^2 + 2y + 1) \\&= x^2 - (y+1)^2 \\&= (x+y+1)(x-y-1)\end{aligned}$$

Question 23.**Solution:**

$$\begin{aligned}25 - a^2 - b^2 - 2ab \\&= (5)^2 - (a^2 + 2ab + b^2) \\&= (5)^2 - (a+b)^2 \\&= (5+a+b)(5-a-b)\end{aligned}$$

Question 24.**Solution:**

$$\begin{aligned} & 25a^2 - 4b^2 + 28bc - 49c^2 \\ &= (5a)^2 - (4b^2 - 28bc + 49c^2) \\ &= (5a)^2 - (2b - 7c)^2 \\ &= (5a + 2b - 7c)(5a - 2b + 7c) \end{aligned}$$

Question 25.**Solution:**

$$\begin{aligned} & 9a^2 - b^2 + 4b - 4 \\ &= (3a)^2 - (b^2 + 4b + 4) \\ &= (3a)^2 - (b + 2)^2 \\ &= (3a + b + 2)(3a - b - 2) \end{aligned}$$

Question 26.**Solution:**

$$\begin{aligned} & 100 - (x - 5)^2 \\ &= (10)^2 - (x - 5)^2 \\ &= (10 + x - 5)(10 - x + 5) \\ &= (5 + x)(15 - x) \end{aligned}$$

Question 27.**Solution:**

$$\begin{aligned} & \{(405)^2 - (395)^2\} \\ &= (405 + 395)(405 - 395) \\ &= 800 \times 10 \\ &= 8000 \end{aligned}$$

Question 28.**Solution:**

$$\begin{aligned} & \{(7.8)^2 - (2.2)^2\} \\ &= (7.8 + 2.2)(7.8 - 2.2) \\ &= 10 \times 5.6 \\ &= 56 \end{aligned}$$

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Exercise 7C

Factorise:

Question 1.

Solution:

$$\begin{aligned}x^2 + 8x + 16 \\&= x^2 + 4x + 4x + 16 \\&= x(x + 4) + 4(x + 4) \\&= (x + 4)(x + 4)\end{aligned}$$

Question 2.

Solution:

$$\begin{aligned}x^2 + 14x + 49 \\&= x^2 + 7x + 7x + 49 \\&= x(x + 7) + 7(x + 7) \\&= (x + 7)(x + 7)\end{aligned}$$

Question 3.

Solution:

$$\begin{aligned}1 + 2x + x^2 \\&= x^2 + 2x + 1 \\&= x^2 + x + x + 1 \\&= x(x + 1) + 1(x + 1) \\&= (x + 1)(x + 1)\end{aligned}$$

Question 4.

Solution:

$$\begin{aligned}9 + 6z + z^2 \\&= z^2 + 6z + 9 \\&= z^2 + 3z + 3z + 9 \\&= z(z + 3) + 3(z + 3) \\&= (z + 3)(z + 3)\end{aligned}$$

Question 5.**Solution:**

$$\begin{aligned} & x^2 + 6ax + 9a^2 \\ &= 9a^2 + 6ax + x^2 \\ &= (3a + x)^2 \\ &= (3a + x)(3a + x) \end{aligned}$$

Question 6.**Solution:**

$$\begin{aligned} & 4y^2 + 20y + 25 \\ &= (2y + 5)^2 \\ &= (2y + 5)(2y + 5) \end{aligned}$$

Question 7.**Solution:**

$$\begin{aligned} & 36a^2 + 36a + 9 \\ &= (6a + 3)^2 \\ &= (6a + 3)(6a + 3) \end{aligned}$$

Question 8.**Solution:**

$$\begin{aligned} & 9m^2 + 24m + 16 \\ &= (3m + 4)^2 \\ &= (3m + 4)(3m + 4) \end{aligned}$$

Question 9.**Solution:**

$$\begin{aligned} & z^2 + z + \frac{1}{4} \\ &= \left(z + \frac{1}{2}\right)^2 \\ &= \left(z + \frac{1}{2}\right)\left(z + \frac{1}{2}\right) \end{aligned}$$

Question 10.**Solution:**

$$\begin{aligned} &49a^2 + 84ab + 36b^2 \\ &= (7a + 6b)^2 \\ &= (7a + 6b)(7a + 6b) \end{aligned}$$

Question 11.**Solution:**

$$\begin{aligned} &p^2 - 10p + 25 \\ &= (p - 5)^2 \\ &= (p - 5)(p - 5) \end{aligned}$$

Question 12.**Solution:**

$$\begin{aligned} &121a^2 - 88ab + 16b^2 \\ &= (11a - 4b)^2 \\ &= (11a - 4b)(11a - 4b) \end{aligned}$$

Question 13.**Solution:**

$$\begin{aligned} &1 - 6x + 9x^2 \\ &= 9x^2 - 6x + 1 \\ &= (3x - 1)^2 \\ &= (3x - 1)(3x - 1) \end{aligned}$$

Question 14.**Solution:**

$$\begin{aligned} &9y^2 - 12y + 4 \\ &= (3y - 2)^2 \\ &= (3y - 2)(3y - 2) \end{aligned}$$

Question 15.**Solution:**

$$\begin{aligned} &16x^2 - 24x + 9 \\ &= (4x - 3)^2 \\ &= (4x - 3)(4x - 3) \end{aligned}$$

Question 16.**Solution:**

$$\begin{aligned} & m^2 - 4mn + 4n^2 \\ &= (m - 2n)^2 \\ &= (m - 2n)(m - 2n) \end{aligned}$$

Question 17.**Solution:**

$$\begin{aligned} & a^2b^2 - 6abc + 9c^2 \\ &= (ab - 3c)^2 \\ &= (ab - 3c)(ab - 3c) \end{aligned}$$

Question 18.**Solution:**

$$\begin{aligned} & m^4 + 2m^2n^2 + n^4 \\ &= (m^2 + n^2)^2 \\ &= (m^2 + n^2)(m^2 + n^2) \end{aligned}$$

Question 19.**Solution:**

$$\begin{aligned} & (l + m)^2 - 4lm \\ &= l^2 + m^2 + 2lm - 4lm \\ &= (l^2 + m^2 - 2lm) \end{aligned}$$

Page number: 102**Exercise 7D****Factorise:****Question 1.****Solution:**

$$\begin{aligned} & x^2 + 5x + 6 \\ &= x^2 + 2x + 3x + 6 \\ &= x(x + 2) + 3(x + 2) \\ &= (x + 2)(x + 3) \end{aligned}$$

Question 2.**Solution:**

$$\begin{aligned} & y^2 + 10y + 24 \\ &= y^2 + 4y + 6y + 24 \\ &= y(y + 4) + 6(y + 4) \\ &= (y + 4)(y + 6) \end{aligned}$$

Question 3.**Solution:**

$$\begin{aligned} & z^2 + 12z + 27 \\ &= z^2 + 3z + 9z + 27 \\ &= z(z + 3) + 9(z + 3) \\ &= (z + 3)(z + 9) \end{aligned}$$

Question 4.**Solution:**

$$\begin{aligned} & p^2 + 6p + 8 \\ &= p^2 + 2p + 4p + 8 \\ &= p(p + 2) + 4(p + 2) \\ &= (p + 2)(p + 4) \end{aligned}$$

Question 5.**Solution:**

$$\begin{aligned} & x^2 + 15x + 56 \\ &= x^2 + 7x + 8x + 56 \\ &= x(x + 7) + 8(x + 7) \\ &= (x + 7)(x + 8) \end{aligned}$$

Question 6.**Solution:**

$$\begin{aligned} & y^2 + 19y + 60 \\ &= y^2 + 4y + 15y + 60 \\ &= y(y + 4) + 15(y + 4) \\ &= (y + 4)(y + 15) \end{aligned}$$

Question 7.**Solution:**

$$\begin{aligned} & x^2 + 13x + 40 \\ &= x^2 + 5x + 8x + 40 \\ &= x(x + 5) + 8(x + 5) \\ &= (x + 5)(x + 8) \end{aligned}$$

Question 8.**Solution:**

$$\begin{aligned} & q^2 - 10q + 21 \\ &= q^2 - 3q - 7q + 21 \\ &= q(q - 3) - 7(q - 3) \\ &= (q - 3)(q - 7) \end{aligned}$$

Question 9.**Solution:**

$$\begin{aligned} & p^2 + 6p - 16 \\ &= p^2 - 2p + 8p - 16 \\ &= p(p - 2) + 8(p - 2) \\ &= (p - 2)(p + 8) \end{aligned}$$

Question 10.**Solution:**

$$\begin{aligned} & x^2 - 10x + 24 \\ &= x^2 - 4x - 6x + 24 \\ &= x(x - 4) - 6(x - 4) \\ &= (x - 4)(x - 6) \end{aligned}$$

Question 11.**Solution:**

$$\begin{aligned} & x^2 - 23x + 42 \\ &= x^2 - 2x - 21x + 42 \\ &= x(x - 2) - 21(x - 2) \\ &= (x - 2)(x - 21) \end{aligned}$$

Question 12.**Solution:**

$$\begin{aligned} & x^2 - 17x + 16 \\ &= x^2 - x - 16x + 16 \\ &= x(x-1) - 16(x-1) \\ &= (x-1)(x-16) \end{aligned}$$

Question 13.**Solution:**

$$\begin{aligned} & y^2 - 21y + 90 \\ &= y^2 - 6y - 15y + 90 \\ &= y(y-6) - 15(y-6) \\ &= (y-6)(y-15) \end{aligned}$$

Question 14.**Solution:**

$$\begin{aligned} & x^2 - 22x + 117 \\ &= x^2 - 9x - 13x + 117 \\ &= x(x-9) - 13(x-9) \\ &= (x-9)(x-13) \end{aligned}$$

Question 15.**Solution:**

$$\begin{aligned} & x^2 - 9x + 20 \\ &= x^2 - 4x - 5x + 20 \\ &= x(x-4) - 5(x-4) \\ &= (x-4)(x-5) \end{aligned}$$

Question 16.**Solution:**

$$\begin{aligned} & x^2 - x - 132 \\ &= x^2 + 12x - 11x - 132 \\ &= x(x+12) - 11(x+12) \\ &= (x+12)(x-11) \end{aligned}$$

Question 17.**Solution:**

$$\begin{aligned} & x^2 + 5x - 104 \\ &= x^2 + 13x - 8x - 104 \\ &= x(x + 13) - 8(x + 13) \\ &= (x + 13)(x - 8) \end{aligned}$$

Question 18.**Solution:**

$$\begin{aligned} & y^2 + 7y - 144 \\ &= y^2 + 16y - 9y - 144 \\ &= y(y + 16) - 9(y + 16) \\ &= (y + 16)(y - 9) \end{aligned}$$

Question 19.**Solution:**

$$\begin{aligned} & z^2 + 19z - 150 \\ &= z^2 + 25z - 6z - 150 \\ &= z(z + 25) - 6(z + 25) \\ &= (z + 25)(z - 6) \end{aligned}$$

Question 20.**Solution:**

$$\begin{aligned} & y^2 + y - 72 \\ &= y^2 + 9y - 8y - 72 \\ &= y(y + 9) - 8(y + 9) \\ &= (y + 9)(y - 8) \end{aligned}$$

Question 21.**Solution:**

$$\begin{aligned} & a^2 + 6a - 91 \\ &= a^2 + 13a - 7a - 91 \\ &= a(a + 13) - 7(a + 13) \\ &= (a + 13)(a - 7) \end{aligned}$$

Question 22.**Solution:**

$$\begin{aligned} & p^2 - 4p - 77 \\ &= p^2 + 7p - 11p - 77 \\ &= p(p + 7) - 11(p + 7) \\ &= (p + 7)(p - 11) \end{aligned}$$

Question 23.**Solution:**

$$\begin{aligned} & x^2 - 7x - 30 \\ &= x^2 + 3x - 10x - 30 \\ &= x(x + 3) - 10(x + 3) \\ &= (x + 3)(x - 10) \end{aligned}$$

Question 24.**Solution:**

$$\begin{aligned} & x^2 - 11x - 42 \\ &= x^2 - 14x + 3x - 42 \\ &= x(x - 14) + 3(x - 14) \\ &= (x - 14)(x + 3) \end{aligned}$$

Question 25.**Solution:**

$$\begin{aligned} & x^2 - 5x - 24 \\ &= x^2 + 3x - 8x - 24 \\ &= x(x + 3) - 8(x + 3) \\ &= (x + 3)(x - 8) \end{aligned}$$

Question 26.**Solution:**

$$\begin{aligned} & y^2 - 6y - 135 \\ &= y^2 - 15y + 9y - 135 \\ &= y(y - 15) + 9(y - 15) \\ &= (y - 15)(y + 9) \end{aligned}$$

Question 27.**Solution:**

$$\begin{aligned} & z^2 - 12z - 45 \\ &= z^2 - 15z + 3z - 45 \\ &= z(z - 15) + 3(z - 15) \\ &= (z - 15)(z + 3) \end{aligned}$$

Question 28.**Solution:**

$$\begin{aligned} & x^2 - 4x - 12 \\ &= x^2 - 6x + 2x - 12 \\ &= x(x - 6) + 2(x - 6) \\ &= (x - 6)(x + 2) \end{aligned}$$

Question 29.**Solution:**

$$\begin{aligned} & 3x^2 + 10x + 8 \\ &= 3x^2 + 6x + 4x + 8 \\ &= 3x(x + 2) + 4(x + 2) \\ &= (x + 2)(3x + 4) \end{aligned}$$

Question 30.**Solution:**

$$\begin{aligned} & 3y^2 + 14y + 8 \\ &= 3y^2 + 12y + 2y + 8 \\ &= 3y(y + 4) + 2(y + 4) \\ &= (y + 4)(3y + 2) \end{aligned}$$

Question 31.**Solution:**

$$\begin{aligned} & 3z^2 - 10z + 8 \\ &= 3z^2 - 12z + 2z + 8 \\ &= 3z(z - 4) + 2(z - 4) \\ &= (z - 4)(3z + 2) \end{aligned}$$

Question 32.**Solution:**

$$\begin{aligned} &2x^2 + x - 45 \\ &= 2x^2 + 10x - 9x - 45 \\ &= 2x(x + 5) - 9(x + 5) \\ &= (x + 5)(2x - 9) \end{aligned}$$

Question 33.**Solution:**

$$\begin{aligned} &6p^2 + 11p - 10 \\ &= 6p^2 - 4p + 15p - 10 \\ &= 2p(3p - 2) + 5(3p - 2) \\ &= (3p - 2)(2p + 5) \end{aligned}$$

Question 34.**Solution:**

$$\begin{aligned} &2x^2 - 17x - 30 \\ &= 2x^2 - 12x - 5x - 30 \\ &= 2x(x - 6) - 5(x - 6) \\ &= (x - 6)(2x - 5) \end{aligned}$$

Question 35.**Solution:**

$$\begin{aligned} &7y^2 - 19y - 6 \\ &= 7y^2 - 21y + 2y - 6 \\ &= 7y(y - 3) + 2(y - 3) \\ &= (y - 3)(7y + 2) \end{aligned}$$

Question 36.**Solution:**

$$\begin{aligned} &28 - 31x - 5x^2 \\ &= 5x^2 + 31x - 28 \\ &= 5x^2 + 35x - 4x - 28 \\ &= 5x(x + 7) - 4(x + 7) \\ &= (x + 7)(5x - 4) \end{aligned}$$

Question 37.**Solution:**

$$\begin{aligned} & 3 + 23z - 8z^2 \\ &= 8z^2 - 23z - 3 \\ &= 8z^2 - 24z + z - 3 \\ &= 8z(z - 3) + 1(z - 3) \\ &= (z - 3)(8z + 1) \end{aligned}$$

Question 38.**Solution:**

$$\begin{aligned} & 6x^2 - 5x - 6 \\ &= 6x^2 + 4x - 9x - 6 \\ &= 2x(3x + 2) - 3(3x + 2) \\ &= (3x + 2)(2x - 3) \end{aligned}$$

Question 39.**Solution:**

$$\begin{aligned} & 3m^2 + 24m + 36 \\ &= 3(m^2 + 8m + 12) \\ &= 3(m^2 + 6m + 2m + 12) \\ &= 3[m(m + 6) + 2(m + 6)] \\ &= 3[(m + 6)(m + 2)] \end{aligned}$$

Question 40.**Solution:**

$$\begin{aligned} & 4n^2 - 8n + 3 \\ &= 4n^2 - 2n - 6n + 3 \\ &= 2n(2n - 1) - 3(2n - 1) \\ &= (2n - 1)(2n - 3) \end{aligned}$$

Question 41.**Solution:**

$$\begin{aligned} & 6x^2 - 17x - 3 \\ &= 6x^2 - 18x + x - 3 \\ &= 6x(x - 3) + 1(x - 3) \\ &= (x - 3)(6x + 1) \end{aligned}$$

Question 42.**Solution:**

$$\begin{aligned} & 7x^2 - 19x - 6 \\ &= 7x^2 - 21x + 2x - 6 \\ &= 7x(x-3) + 2(x-3) \\ &= (x-3)(7x+2) \end{aligned}$$

Page number: 103**Exercise 7E****Question 1.****Solution:** (d) $7(a-3b)(a+3b)$

$$\begin{aligned} & (7a^2 - 63b^2) \\ &= 7(a^2 - 9b^2) \\ &= 7[(a+3b)(a-3b)] \end{aligned}$$

Question 2.**Solution:** (d) $2x(1-4x)(1+4x)$

$$\begin{aligned} & (2x - 32x^3) \\ &= 2x(1 - 16x^2) \\ &= 2x[(1+4x)(1-4x)] \end{aligned}$$

Question 3.**Solution:** (c) $x(x-12)(x+12)$

$$\begin{aligned} & x^3 - 144x \\ &= x(x^2 - 144) \\ &= x[(x+12)(x-12)] \end{aligned}$$

Question 4.**Solution:** (d) $2(1-5x)(1+5x)$

$$\begin{aligned} & (2 - 50x^2) \\ &= 2(1 - 25x^2) \\ &= 2[(1+5x)(1-5x)] \end{aligned}$$

Question 5.**Solution:** (a) $(a + b)(a + c)$

$$a^2 + bc + ab + ac$$

$$= a^2 + ab + ac + bc$$

$$= a(a + b) + c(a + b)$$

$$= (a + b)(a + c)$$

Question 6.**Solution:** (a) $(pq + 1)(q - 1)$

$$pq^2 + q(p - 1) - 1$$

$$= pq^2 + qp - q - 1$$

$$= pq(q - 1) + 1(q - 1)$$

$$= (q - 1)(pq + 1)$$

Question 7.**Solution:** (b) $(a - m)(b + n)$

$$ab - mn + an - bm$$

$$= ab + an - bm - mn$$

$$= a(b + n) - m(b + n)$$

$$= (b + n)(a - m)$$

Question 8.**Solution:** (a) $(a - 1)(b - 1)$

$$ab - a - b + 1$$

$$= a(b - 1) - 1(b - 1)$$

$$= (b - 1)(a - 1)$$

Question 9.**Solution:** (c) $(x + y)(x - z)$

$$x^2 - xz + xy - yz$$

$$= x(x - z) + y(x - z)$$

$$= (x - z)(x + y)$$

Question 10.**Solution:** (c) $3(2m - 3)(2m + 3)$

$$\begin{aligned}
 &(12m^2 - 27) \\
 &= 3(4m^2 - 9) \\
 &= 3[(2m + 3)(2m - 3)]
 \end{aligned}$$

Question 11.

Solution: (d) $x(x+1)(x-1)$

$$\begin{aligned}
 &x^3 - x \\
 &= x(x^2 - 1) \\
 &= x(x+1)(x-1)
 \end{aligned}$$

Question 12.

Solution: (d) $(1+a-b)(1-a+b)$

$$\begin{aligned}
 &1 - 2ab - (a^2 + b^2) \\
 &= 1 - 2ab - a^2 - b^2 \\
 &= 1 - (a^2 + 2ab + b^2) \\
 &= (1)^2 - (a+b)^2 \\
 &= (1+a+b)(1-a-b)
 \end{aligned}$$

Question 13.

Solution: (c) $(x+2)(x+4)$

$$\begin{aligned}
 &x^2 + 6x + 8 \\
 &= x^2 + 4x + 2x + 8 \\
 &= x(x+4) + 2(x+4) \\
 &= (x+4)(x+2)
 \end{aligned}$$

Question 14.

Solution: (b) $(x+7)(x-3)$

$$\begin{aligned}
 &x^2 + 4x - 21 \\
 &= x^2 + 7x - 3x - 21 \\
 &= x(x+7) - 3(x+7) \\
 &= (x+7)(x-3)
 \end{aligned}$$

Question 15.

Solution: (a) $(y-1)(y+3)$

$$\begin{aligned}
& y^2 + 2y - 3 \\
&= y^2 + 3y - y - 3 \\
&= y(y + 3) - 1(y + 3) \\
&= (y + 3)(y - 1)
\end{aligned}$$

Question 16.

Solution: (a) $(x + 5)(x - 8)$

$$\begin{aligned}
& 40 + 3x - x^2 \\
&= x^2 - 3x - 40 \\
&= x^2 - 8x + 5x - 40 \\
&= x(x - 8) + 5(x - 8) \\
&= (x - 8)(x + 5)
\end{aligned}$$

Question 17.

Solution: (b) $(x + 1)(2x + 3)$

$$\begin{aligned}
& 2x^2 + 5x + 3 \\
&= 2x^2 + 2x + 3x + 3 \\
&= 2x(x + 1) + 3(x + 1) \\
&= (x + 1)(2x + 3)
\end{aligned}$$

Question 18.

Solution: (c) $(3a - 2)(2a - 3)$

$$\begin{aligned}
& 6a^2 - 13a + 6 \\
&= 6a^2 - 9a - 4a + 6 \\
&= 3a(2a - 3) - 2(2a - 3) \\
&= (2a - 3)(3a - 2)
\end{aligned}$$

Question 19.

Solution: (a) $(2z - 1)(2z - 3)$

$$\begin{aligned}
& 4z^2 - 8z + 3 \\
&= 4z^2 - 2z - 6z + 3 \\
&= 2z(2z - 1) - 3(2z - 1) \\
&= (2z - 1)(2z - 3)
\end{aligned}$$

Question 20.

Solution: (b) $(1+8y)(3-y)$

$$3+23y-8y^2$$

$$=8y^2-23y-3$$

$$=8y^2-24y+y-3$$

$$=8y(y-3)+1(y-3)$$

$$=(y-3)(8y+1)$$