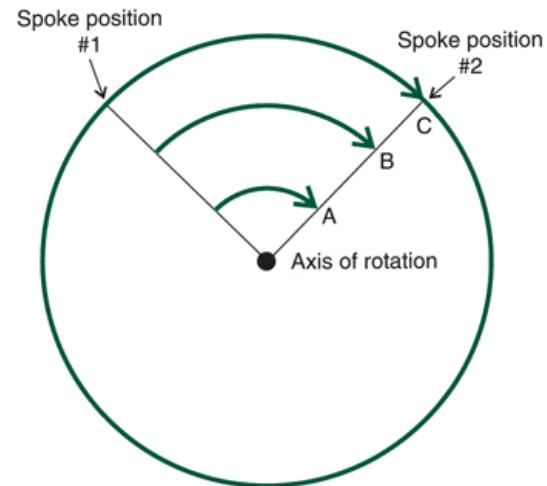


## Read a chapter on Angular Kinematics

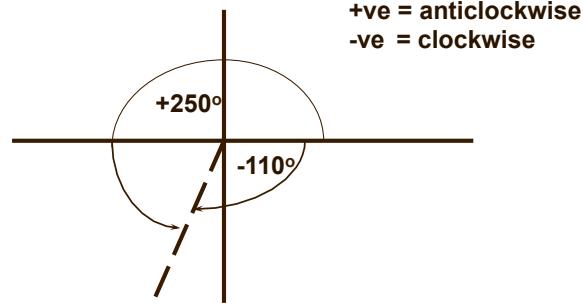
### Angular Kinematics

**Hamill & Knutzen (Ch 9)**

Hay (Ch. 4), Hay & Ried (Ch. 10), Kreighbaum  
& Barthels (Module I) or Hall (Ch. 11)



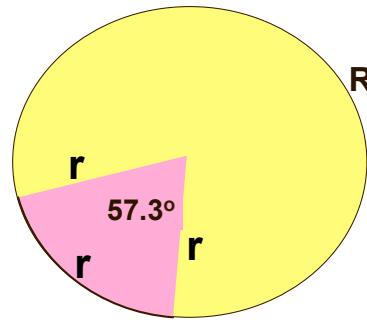
## Reporting Angles



## Measurement of Angles

- Degrees (arbitrary units)
- Radians (fundamental ratio)
- Revolutions

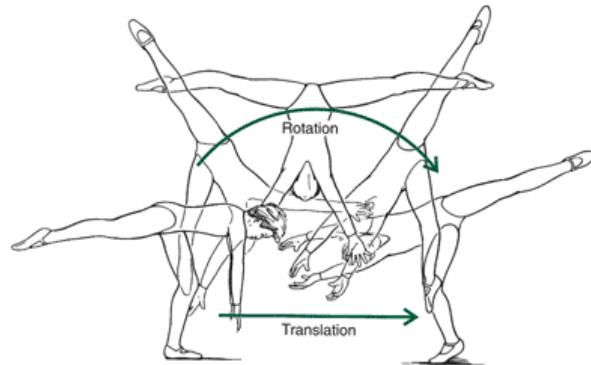
## Radians



**Circumference =  $2\pi r$**   
**therefore there are  $2\pi$  radians in  $360^\circ$**

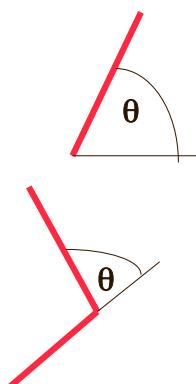
## General Motion

(a combination of both linear and angular translations)



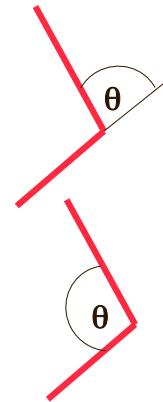
## Types of Angles

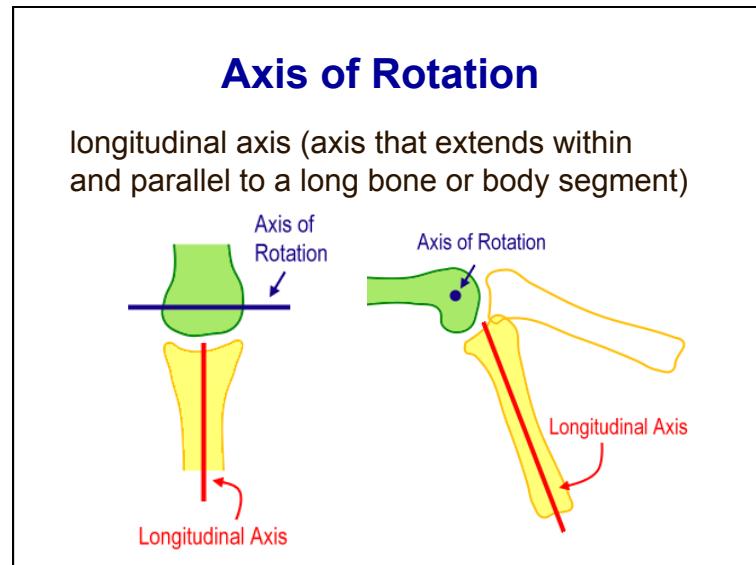
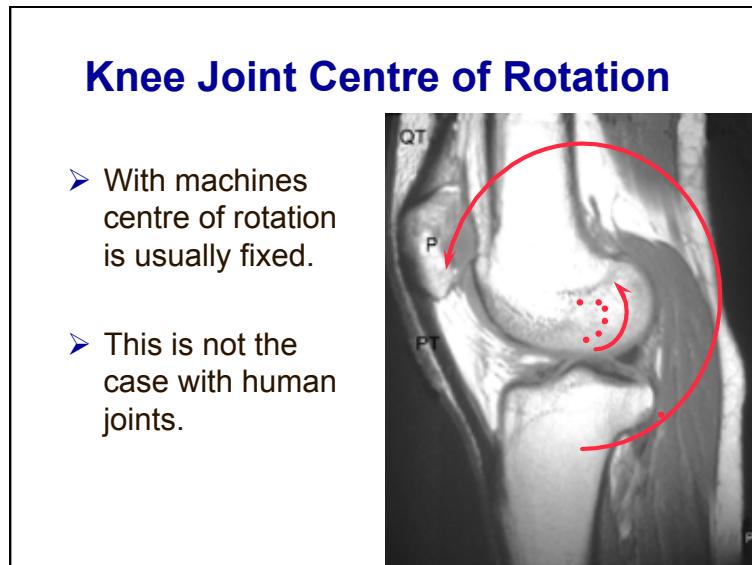
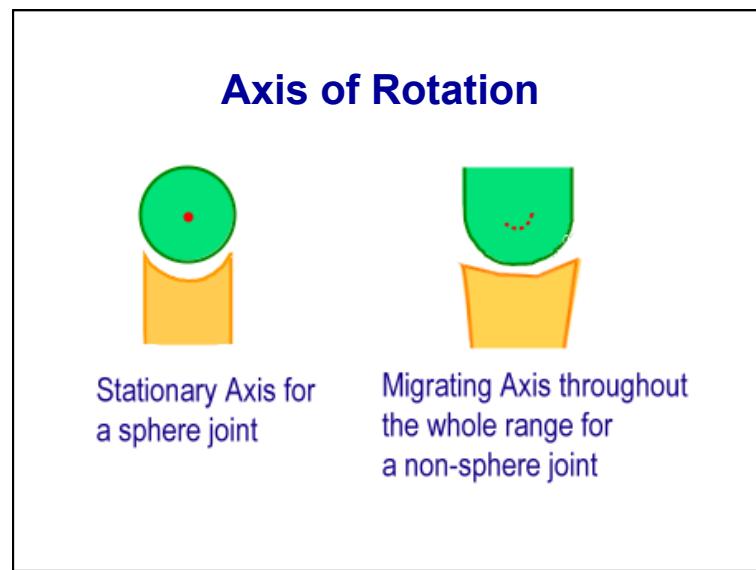
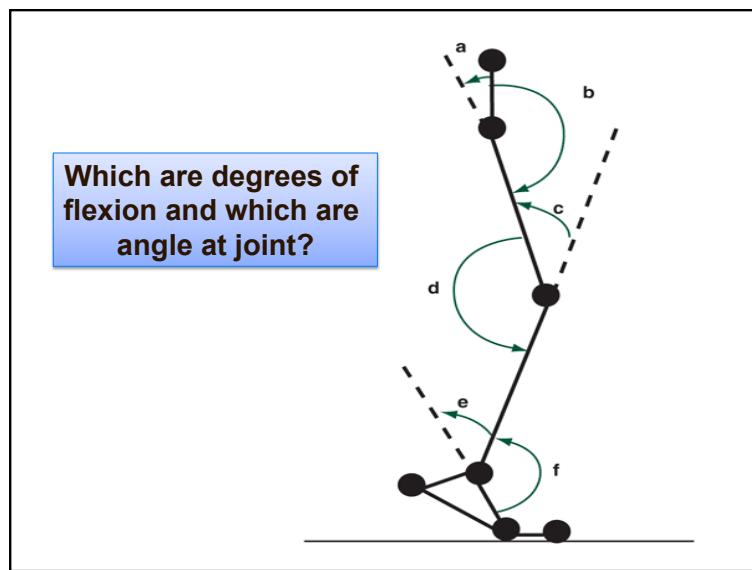
- An absolute angle is measured from an external frame of reference.
- A relative angle is the angle formed between two limb segments.



## Relative Angles

- A relative angle can be presented as degrees of flexion (opposite).
- or
- presented as the angle formed at the articulation (opposite)

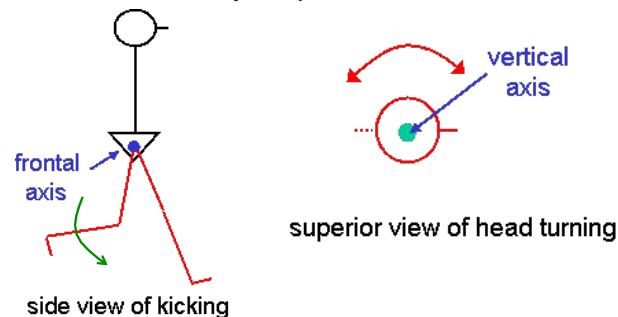




## Description of Motion

Kicking the leg (leg moves anticlockwise [shown] in the sagittal plane about a frontal axis)

Turning the head (the head moves around a vertical axis in the horizontal plane)

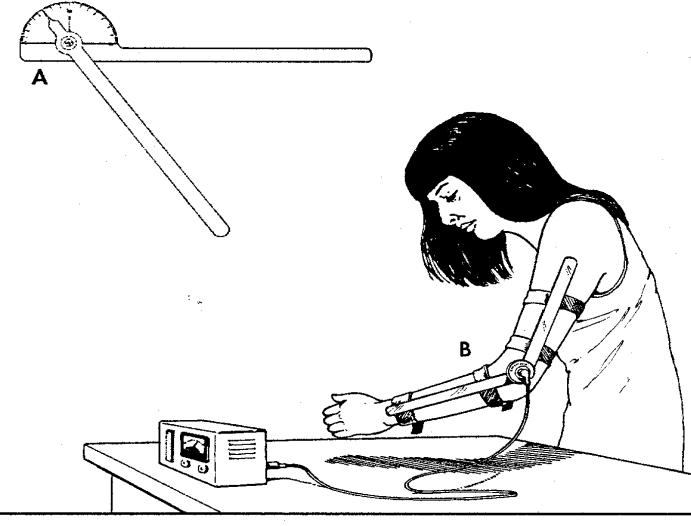
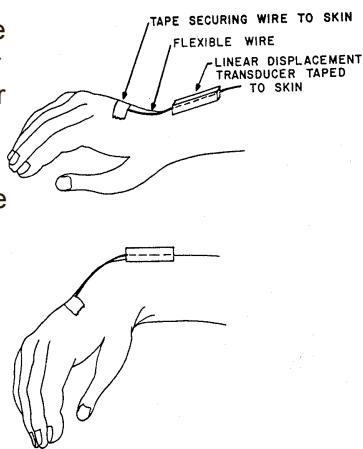


## Data Acquisition

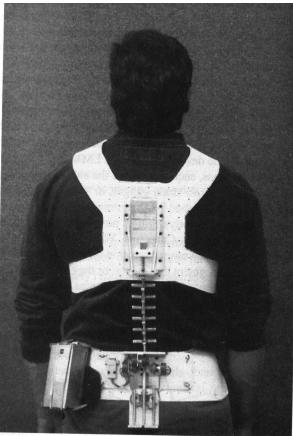
- If you really only need data for angular motion about a joint (pangle, angular velocity and angular acceleration) you do not need to collect data via an opto-electrical device.
- Electro-goniometers and other device are more portable.

## Goniometers

- Simple goniometers like the Leighton flexometer are really only useful for range of motion and static analysis.
- Electro-goniometers are easy to use and can follow changes in posture in dynamic situations (velocity & acceleration)

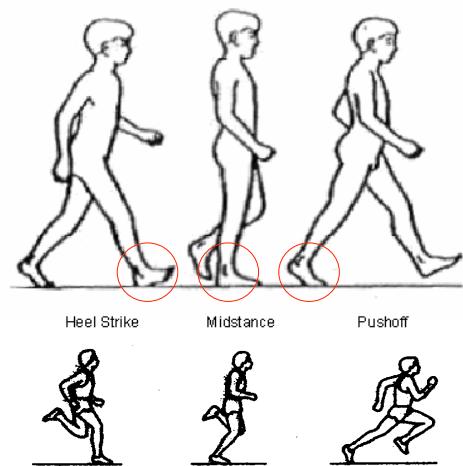
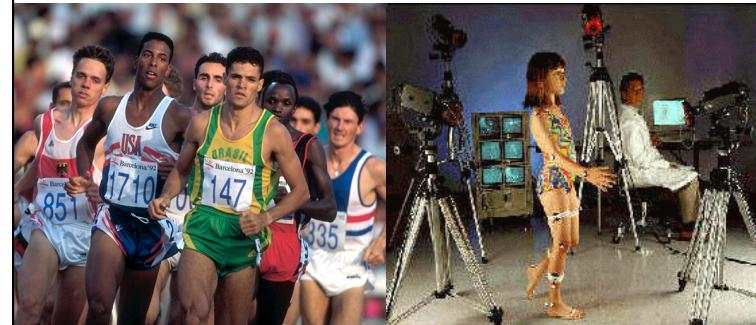


## Lumbar Motion Monitor



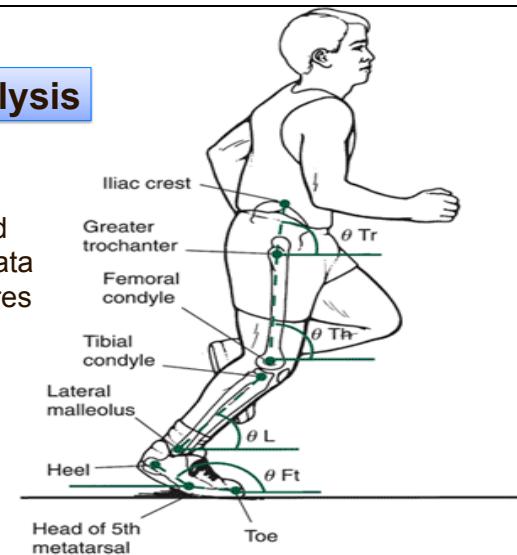
- The LMM™ lumbar motion monitoring system was developed in the Biodynamics Laboratory at Ohio State University (W. Marras)
- This system allows continuous monitoring of the trunk angle and subsequent analysis can quantify trunk velocities and accelerations.

## Gait and Running Analysis



### Gait Analysis

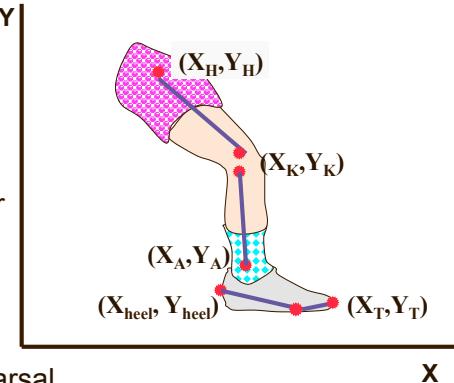
First we need coordinate data for joint centres



## Lower Extremity Joint Angles

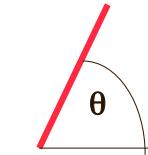
First we need coordinate data for joint centres

Marker locations:  
greater trochanter  
femoral condyle  
tibial condyle  
lateral malleolus  
heel  
head of 5<sup>th</sup> metatarsal  
toe

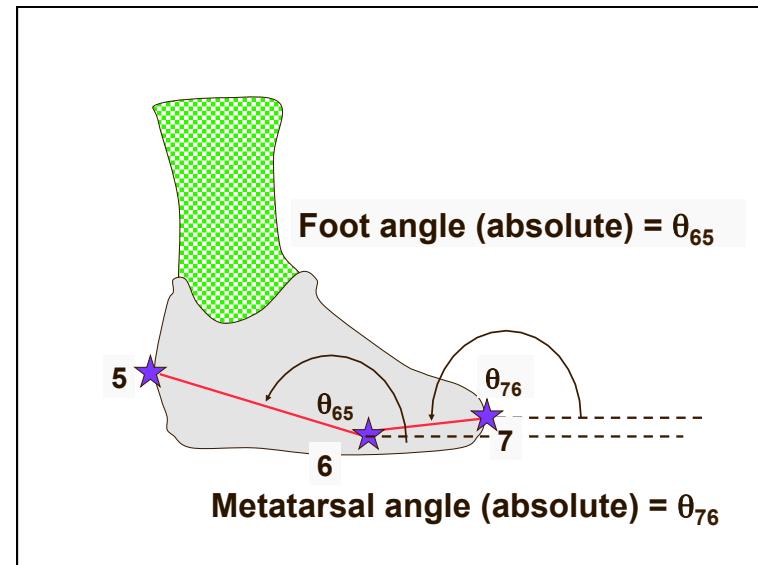
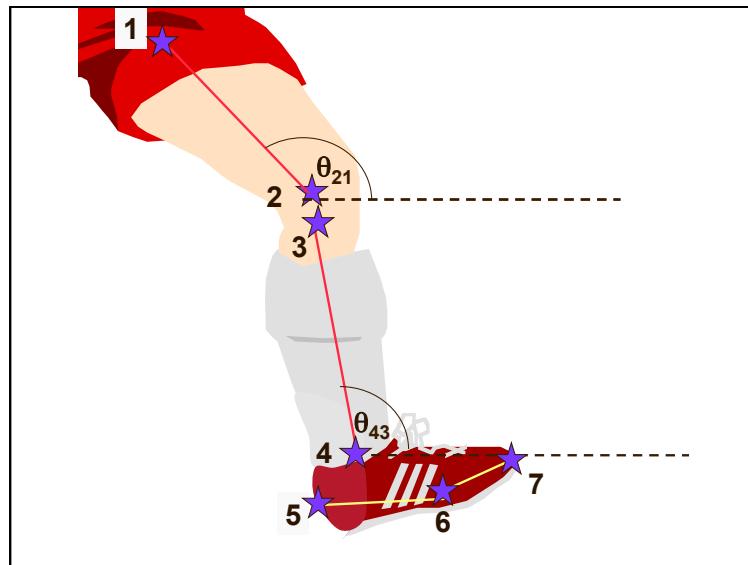
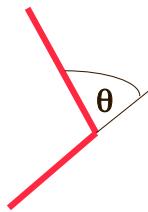


## Describing Angles

- An absolute angle is measured from an external frame of reference.

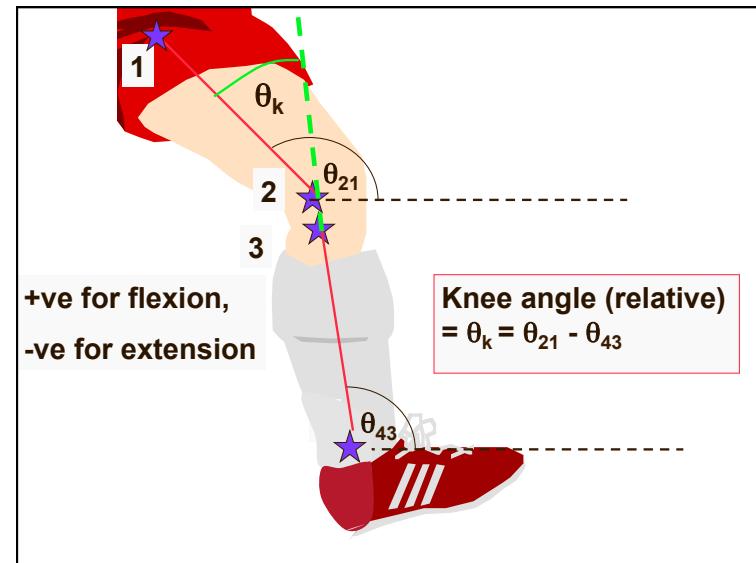


- A relative angle is the angle formed between two limb segments.



### Hamill text, Winter (1979) pages 39-44

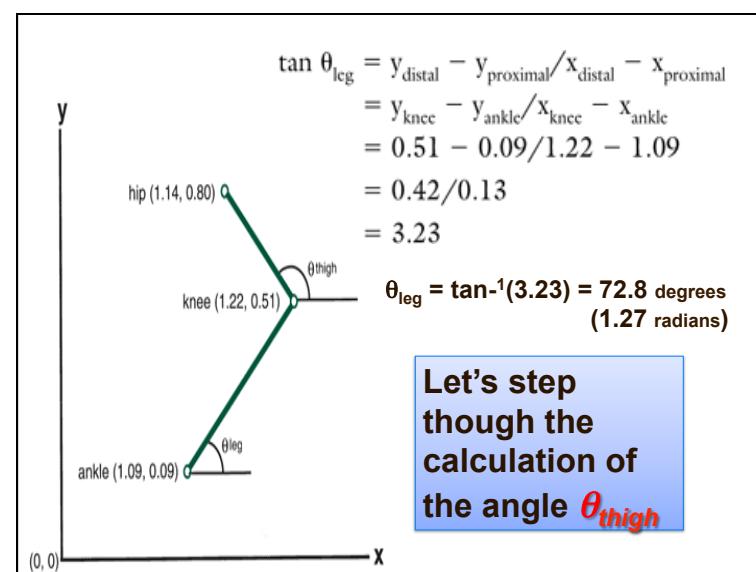
- Diagrams on the next two slides
- Thigh angle (absolute) =  $\theta_{21}$
- Shank angle (absolute) =  $\theta_{43}$
- Foot angle (absolute) =  $\theta_{65}$
- Metatarsal angle (absolute) =  $\theta_{76}$
- Knee angle (relative) =  $\theta_{21} - \theta_{43}$   
(+ve for flexion, -ve for extension)
- Ankle angle (relative) =  $\theta_{43} - \theta_{65} + 90^\circ$   
(+ve for plantarflexion, -ve for dorsiflexion)
- Metatarsal-phalangeal angle (relative) =  $\theta_{65} - \theta_{76}$



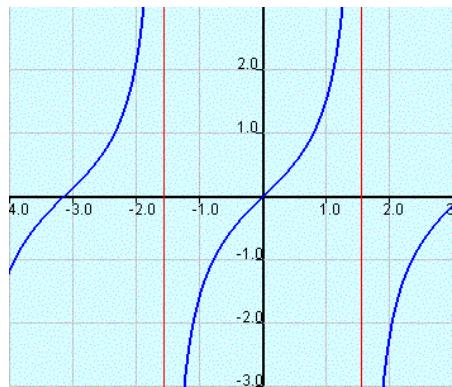
### Knee Angle (relative angle) from Co-ordinate Data

$$\theta_{43} = \tan^{-1}\left(\frac{y_3 - y_4}{x_3 - x_4}\right) \quad \theta_{21} = \tan^{-1}\left(\frac{y_1 - y_2}{x_1 - x_2}\right)$$

- Knee angle =  $\theta_k = \theta_{21} - \theta_{43}$
- if  $\theta_k$  is positive the knee is flexed
- if  $\theta_k$  is negative the knee is extended  
(dislocated?)



## Tangent Function



Absolute angle relative to the right horizontal  
 $= \theta_2 + 180^\circ$  (-----)

Absolute angle relative to the right horizontal  
 $= \theta_1$  (.....)

Absolute angle relative to the right horizontal  
 $= \theta_3 + 180^\circ$  (.....)

Absolute angle relative to the right horizontal  
 $= \theta_4 + 360^\circ$  (—)

$$\text{Angular Velocity} = \omega$$

$$\frac{\text{change in angular displacement}}{\text{change in time}}$$

$$\text{Angular Acceleration} = \alpha$$

$$\frac{\text{change in angular velocity}}{\text{change in time}}$$

$$\text{Angular Velocity \& Acceleration}$$

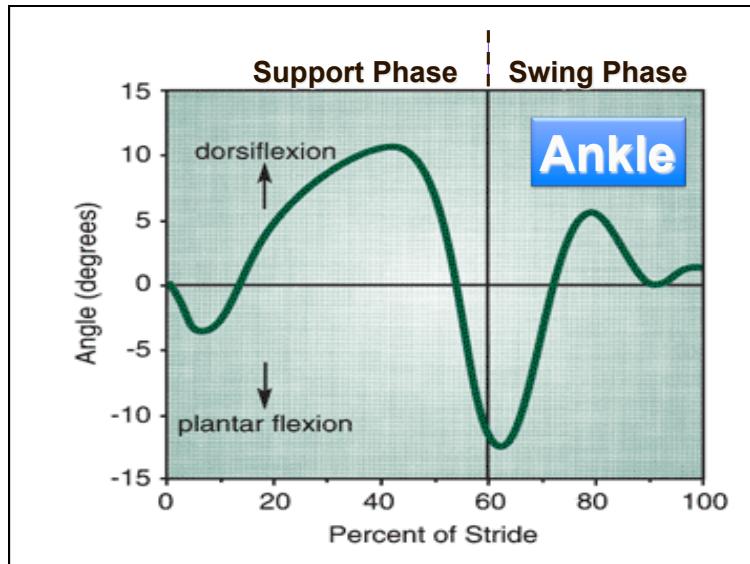
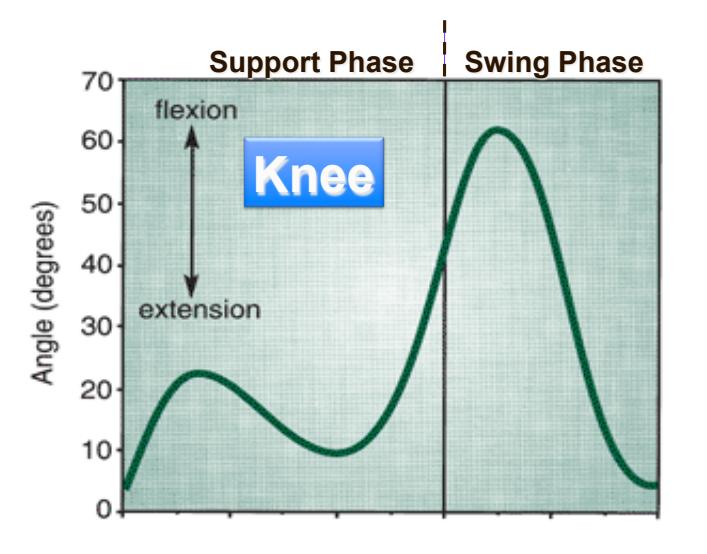
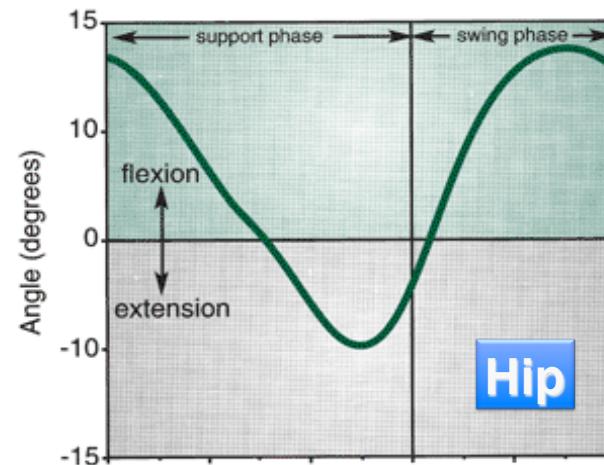
$$\omega_i = \frac{\theta_{i+1} - \theta_{i-1}}{2\Delta t}$$

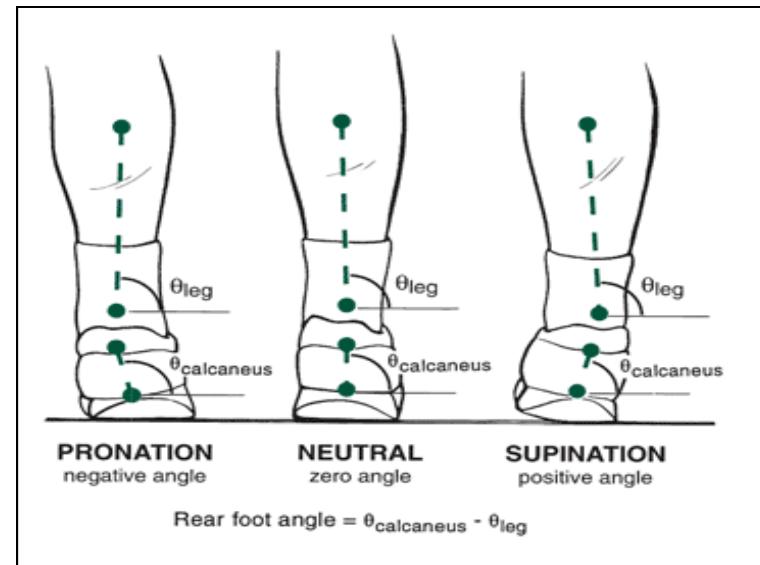
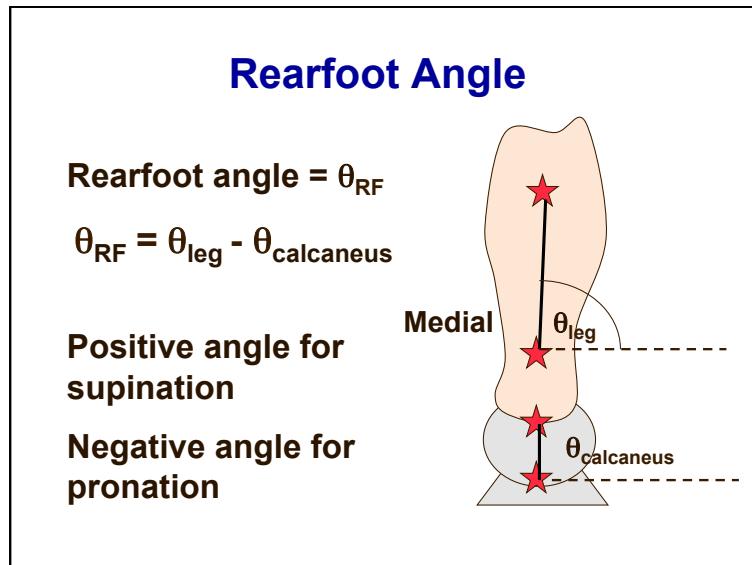
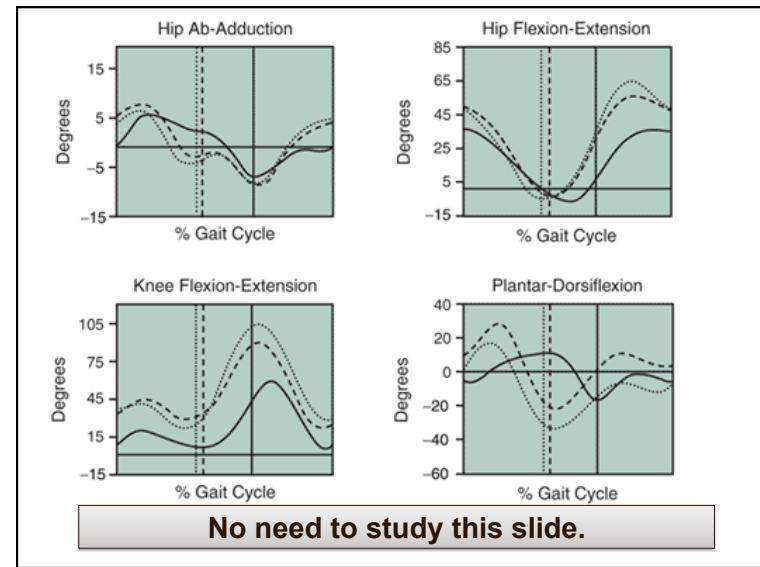
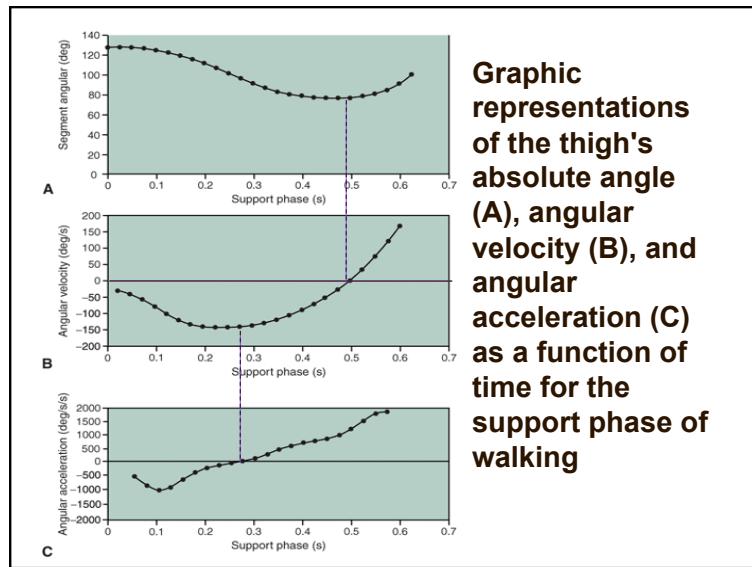
$$\alpha_i = \frac{\omega_{i+1} - \omega_{i-1}}{2\Delta t}$$

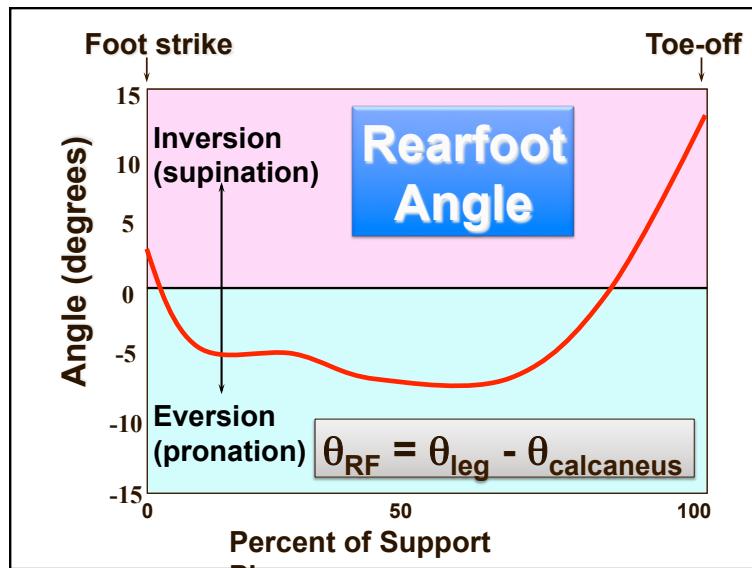
## Question

1. Calculate the angular velocity of the shank (lower leg) at frame 3. All values in are in cm. [6]

		greater trochanter		femoral condyle		tibial condyle		lateral malleolus		calcaneous /metatarsal		tarsal toe			
FRAME	TIME [s]	x	y	x	y	x	y	x	y	x	y	x	y		
2.0	0.0500	128.1	92.6	118.0	53.6	114.0	50.6	92.1	17.6	82.1	12.6	100.8	1.0	106.6	2.1
3.0	0.0667	130.9	92.2	121.3	53.2	117.4	50.3	93.7	18.6	83.4	14.6	100.7	1.1	106.5	2.0
4.0	0.0833	133.7	91.9	125.0	52.8	121.0	50.0	95.6	19.7	85.1	16.8	100.8	1.4	106.4	1.9
5.0	0.1000	136.6	91.7	129.0	52.4	125.0	49.7	97.9	20.9	87.2	19.1	101.1	1.8	106.6	1.8

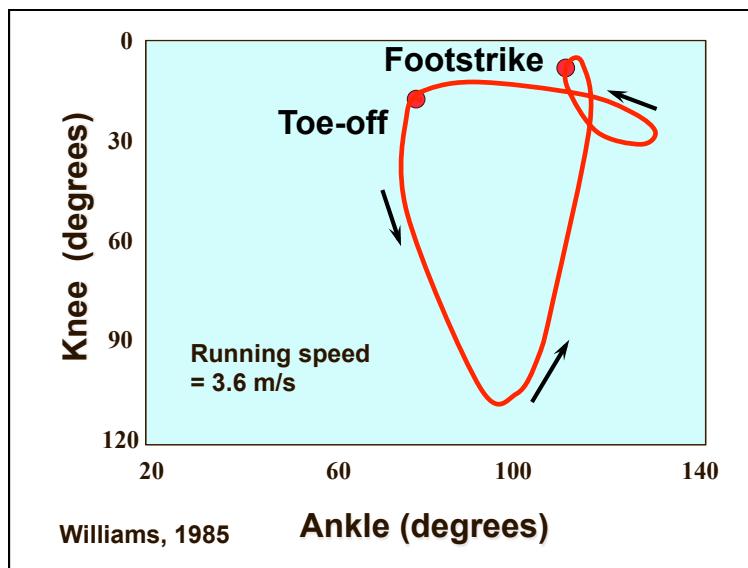
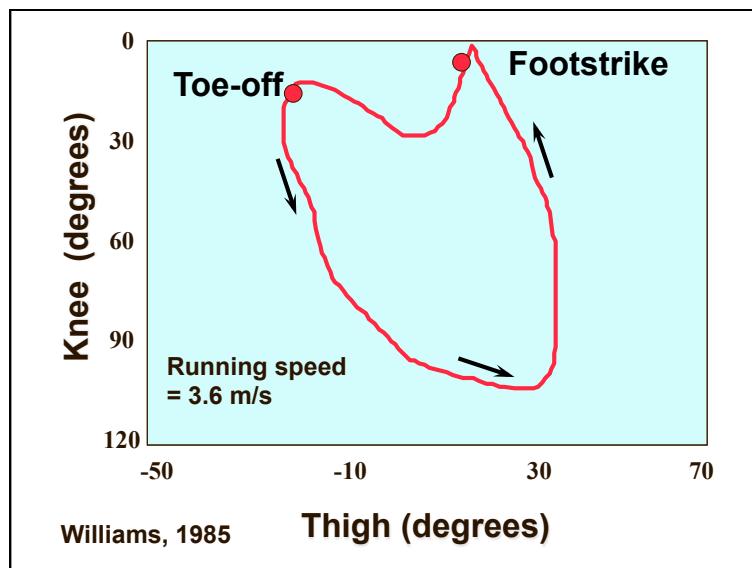


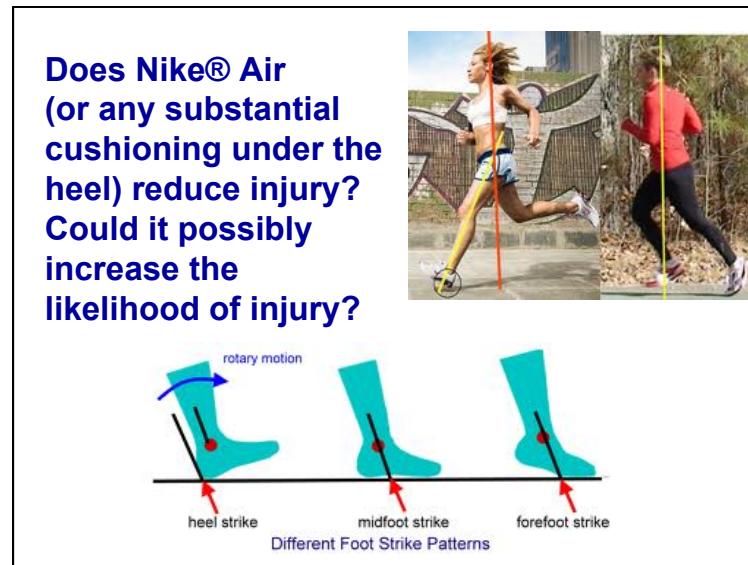
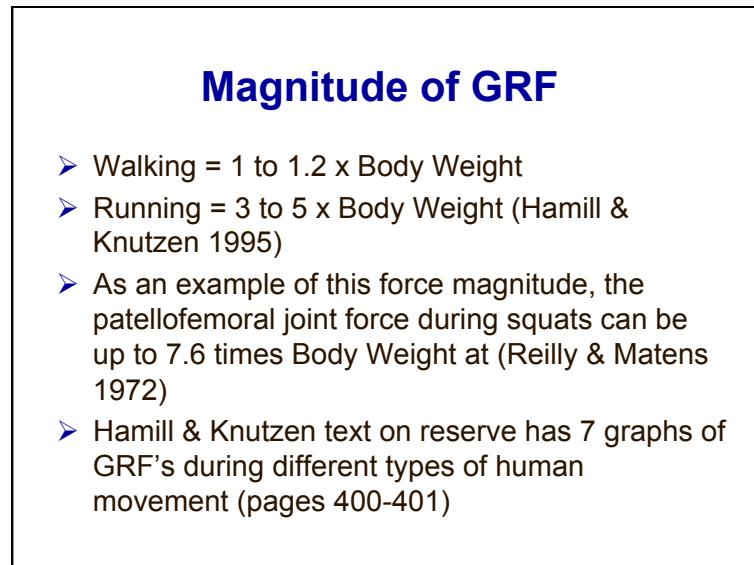
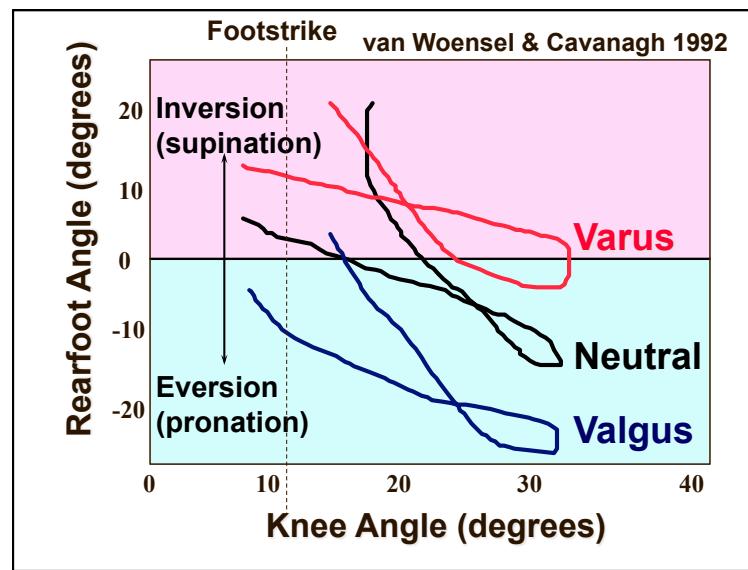
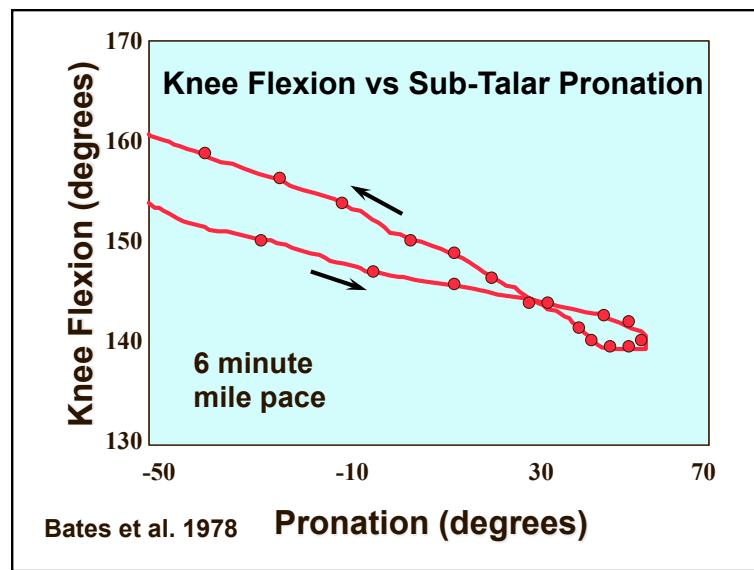




## Angle-Angle Diagrams

- Most graphical representations of human movement you will see, plot some parameter (e.g. position, angle, velocity, etc.) against time.
- However, activities like running are cyclic and often it is useful to plot the relationship between two angles during the movement.
- There should be a functional relationship between these angles.



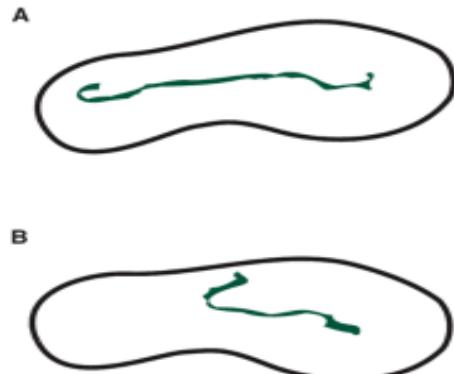


## Impact Forces While Running

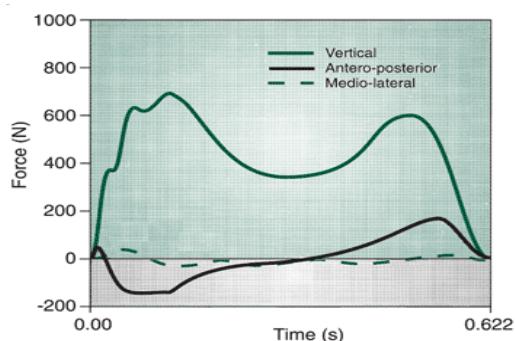
- The sport of running causes a relatively high injury rate
- Some argue this is due to overuse problems – basically too many foot strikes
- While this is definitely a causative factor, others suggest the heel strike is not a natural movement pattern and is a big contributing factor.

Center of pressure patterns for the left foot.

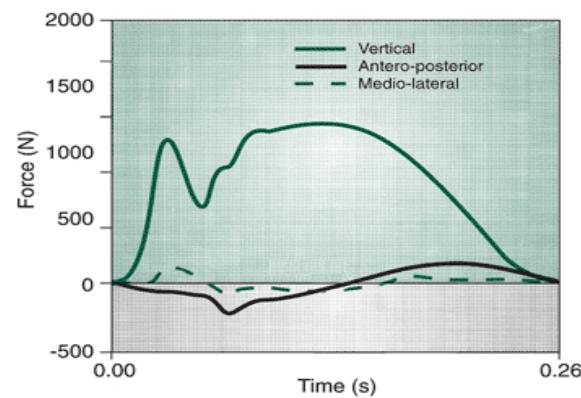
- A. Heel-toe footfall pattern runner.
- B. Mid-foot foot strike pattern runner.

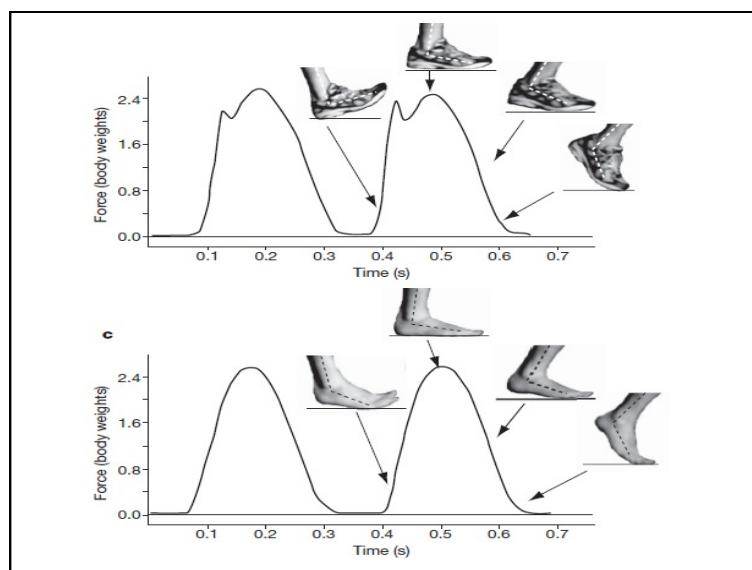
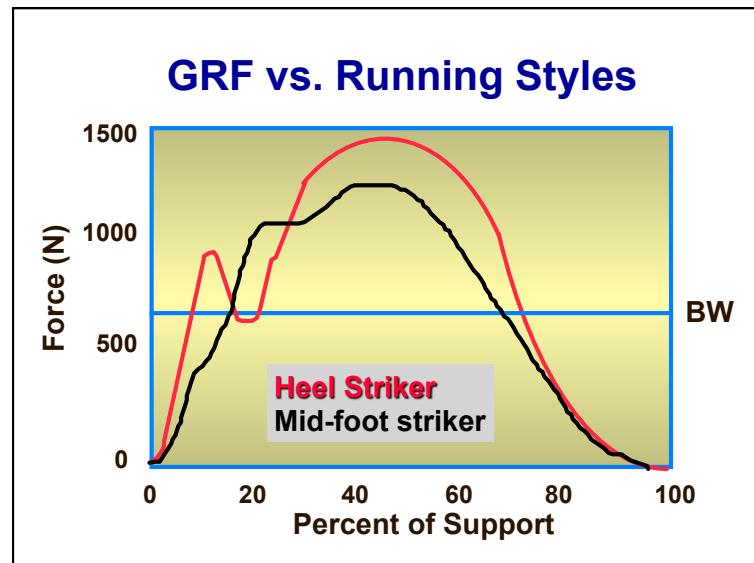
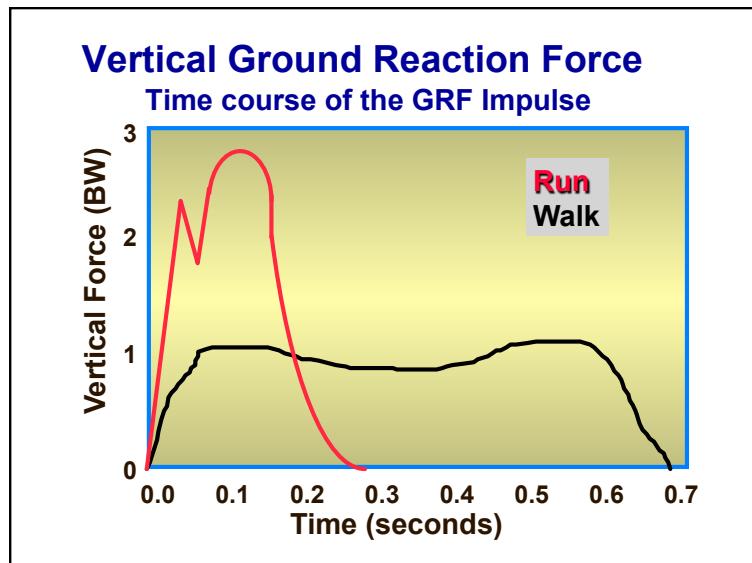


Ground reaction force for walking.  
Note the difference in magnitude between the vertical component and the shear components



Ground reaction force for running.  
Note the difference in magnitude between the vertical component and the shear components

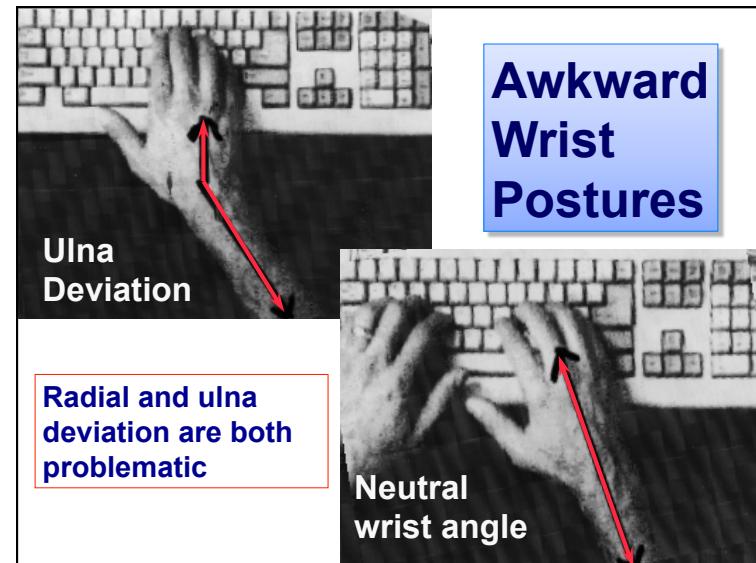




- ### Links of Interest
- The issue of what is a natural foot strike pattern is a relatively hot topic these days, resulting in a resurgence of interest in barefoot running.
  - <http://www.barefootrunning.fas.harvard.edu/4BiomechanicsofFootStrike.html>
  - <http://isiria.wordpress.com/2009/04/24/the-great-marketing-lie-expensive-runners-will-prevent-injury/>
  - <http://www.nytimes.com/2009/10/27/health/27well.html?r=2>
  - <http://www.vibramfivefingers.com/>
  - <http://www.posetech.com/>

## Other uses of Angular Kinematics.

(Angular Kinematics is used a lot in Ergonomics when trying to assess if the workers are having to adopt hazardous postures for too long?)

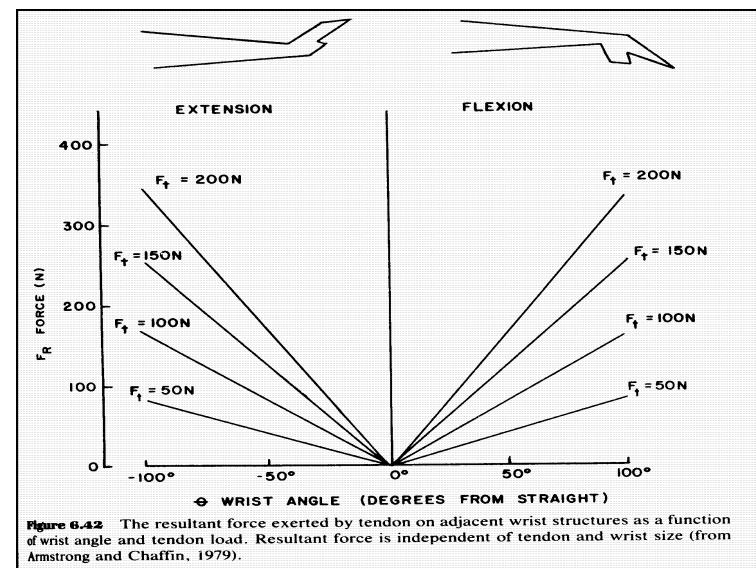


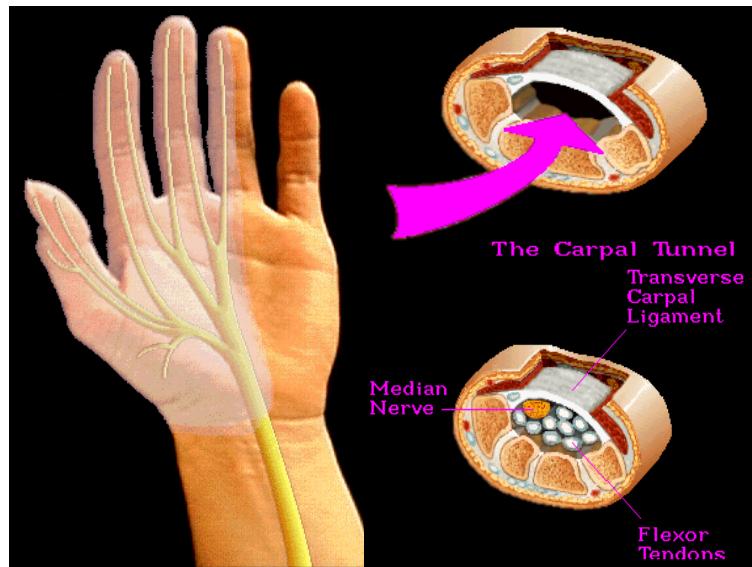
## Extreme wrist extension



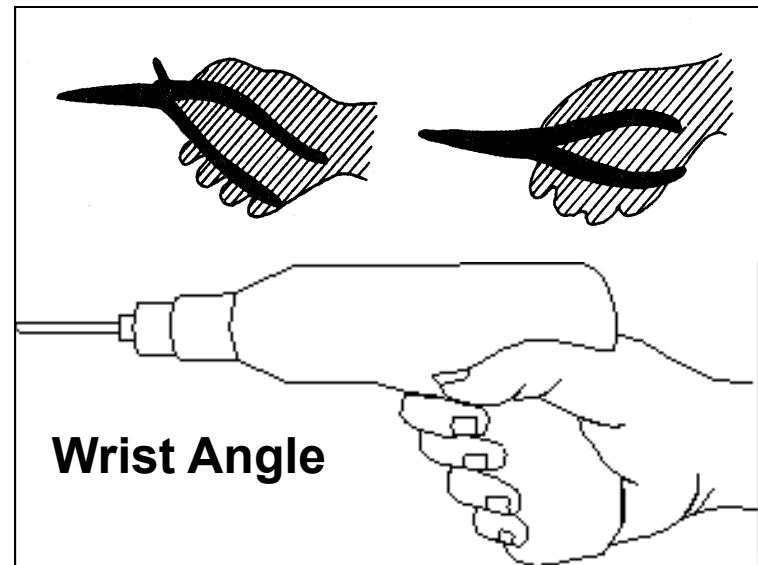
Kin 380 & Kin 481

Prolonged wrist extension is believed to be a significant risk factor for carpal tunnel syndrome (Rempel 1991).

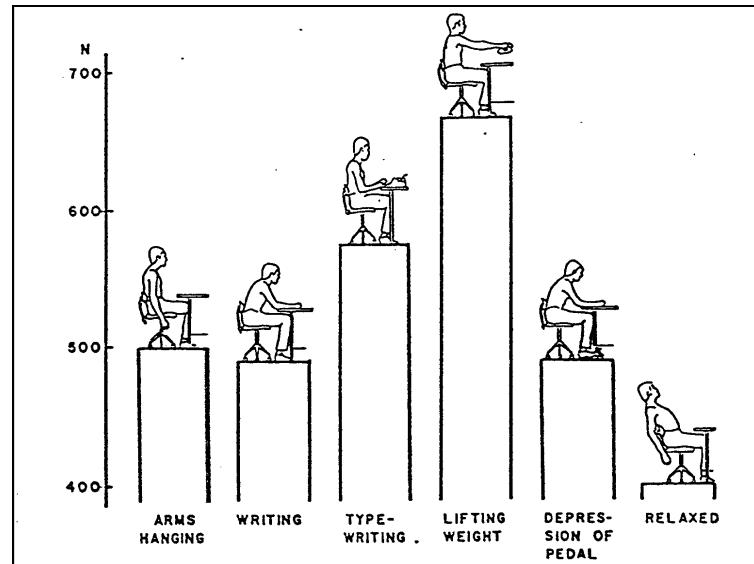
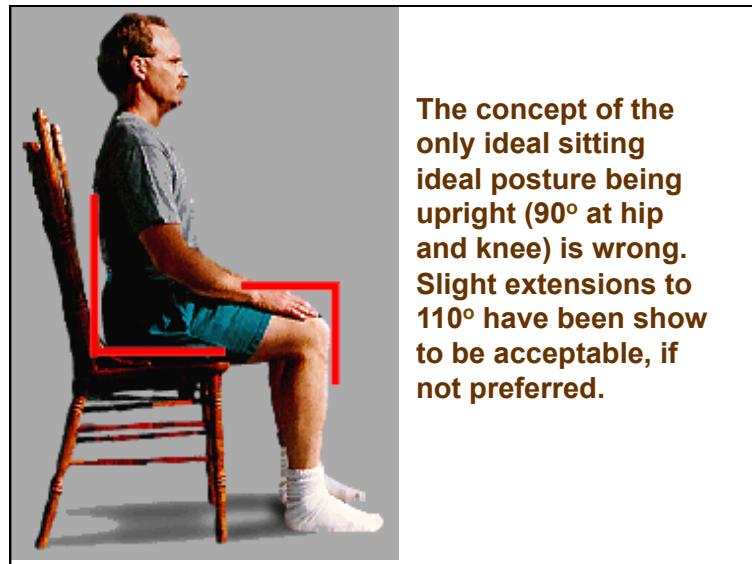
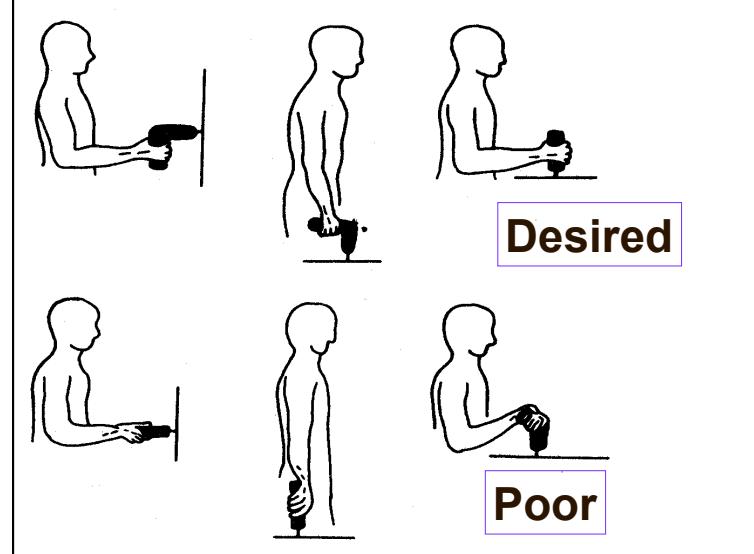
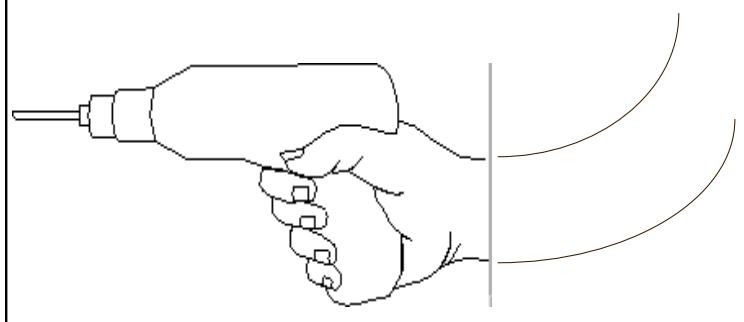


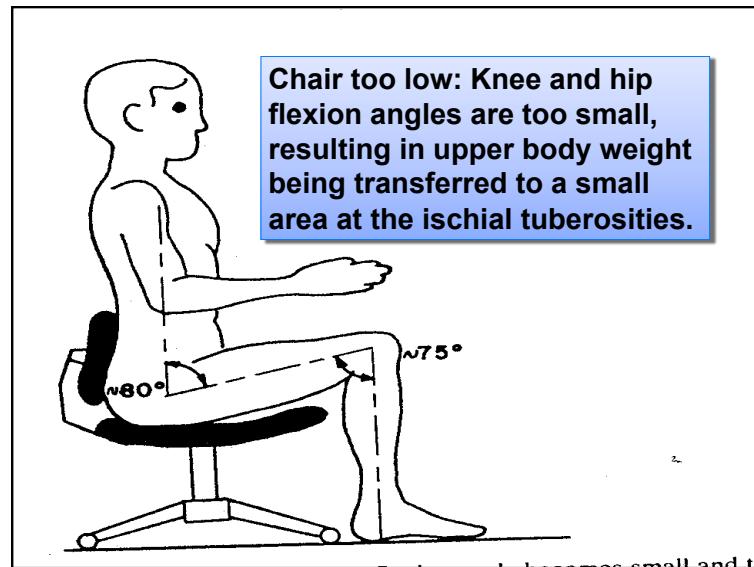


- Standard conservative treatment for CTS is splinting plus anti-inflammatory medication, for several weeks.
- Usually the splint should be worn at night only.

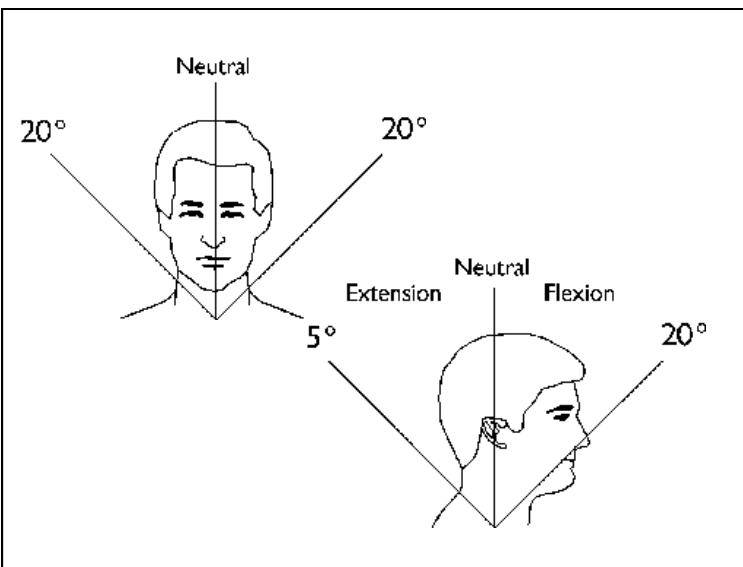
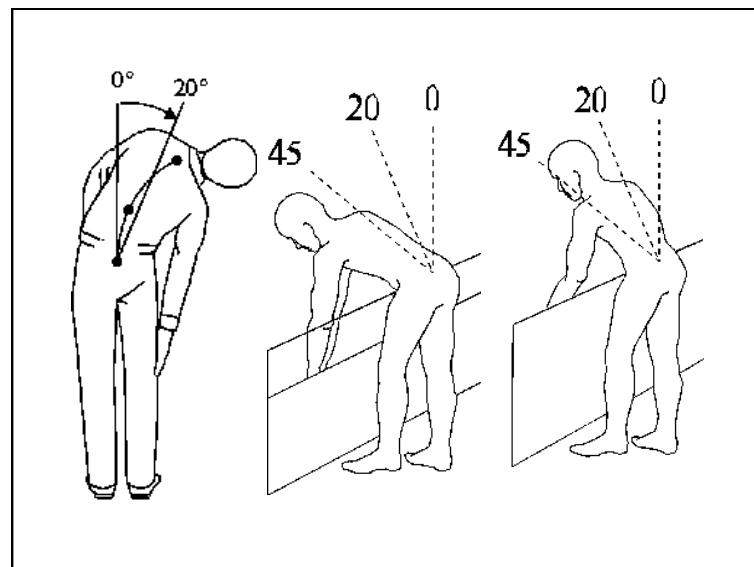
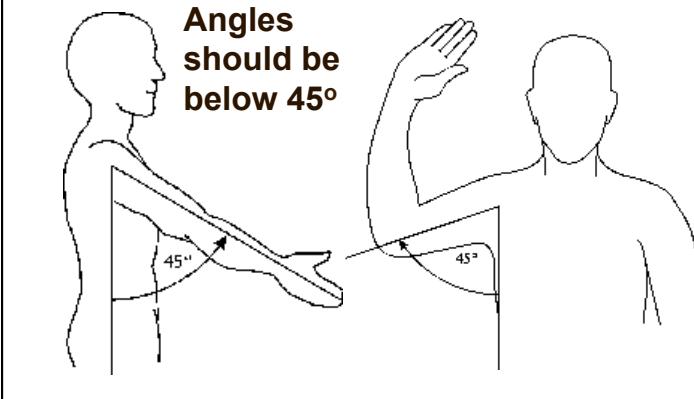


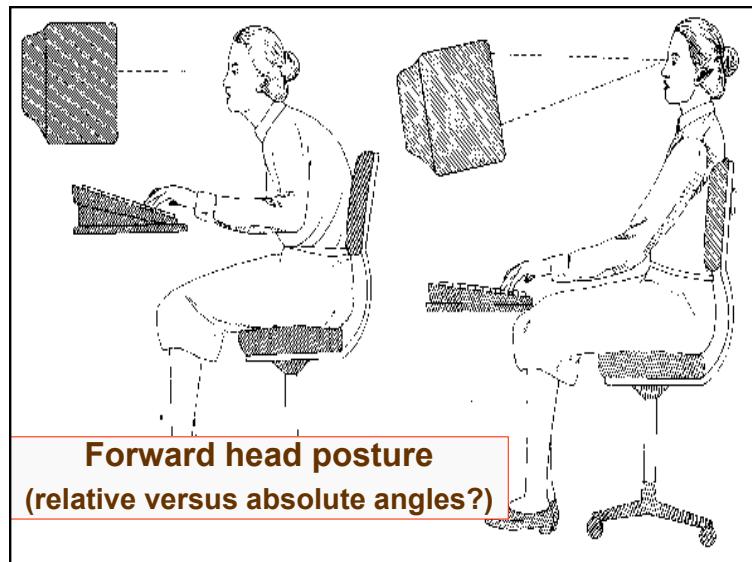
The preferred shape of the tool's handle depends the body alignment during use.





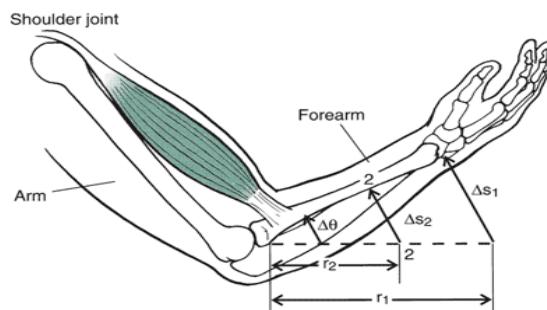
## Shoulder Postures





## Angular & Linear Motions

- All points on the forearm travel through the same angle (angular displacement).
- Each point travels through a different linear displacement



## Angular and Linear Displacement

- As we saw, a radian is defined as the ratio of the distance around the arc of the circle to the radius of the circle.

$$\theta = s/r$$

$$s = r\theta \quad (L \Rightarrow L \times \text{unitless ratio})$$

## Additional Relationships

- $v_t = r\omega \quad (LT^{-1} = L \times T^{-1})$
- $a_t = r\alpha \quad (LT^{-2} = L \times T^{-2})$

Note that the angular units must be in radians.

## Maximum Linear Velocity?



$$v_t = r\omega$$

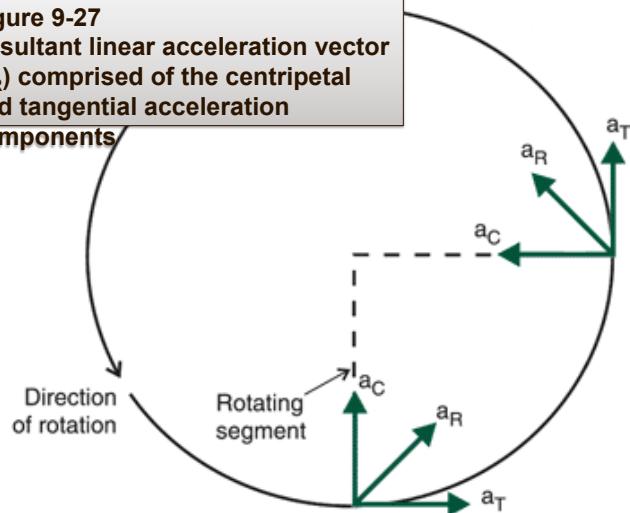


## Radial Acceleration

- What is radial acceleration?
- If velocity is a vector then even at a constant angular velocity (and hence constant linear speed) the linear velocity is changing as its directional component is changing. If velocity is changing then there must be acceleration.

$$a_r = v_t^2/r \quad \text{or} \quad r\omega^2$$

Figure 9-27  
Resultant linear acceleration vector ( $a_R$ ) comprised of the centripetal and tangential acceleration components



## Right Hand Thumb Rule

- The fingers of the right hand point in the direction of the rotation, and the right thumb points in the direction of the angular velocity vector.

