

## **Lab 1**

**Stuti Patel**

### **Section 15**

1. a) -112

b) 4

c) -4

2. a) 3841

b) 0

c) 17

d) 15

3. a) 0000 0000 0000 0000 0000 0000 1001 1101

b) 0000 0000 0000 0000 0000 0000 1100 1111

c) 1111 1111 1111 1111 1111 1111 0110 1010

d) 1111 1111 1111 1111 1111 1111 1100 1001

e) 1111 1111 1111 1111 1111 1111 1111 1101

f) 0000 0000 0000 0000 0000 0000 0100 0001

4. a) 0100 0001 0110 0000 0000 0000 0000 0000

b) 0100 0010 0000 0000 0000 0000 0000 0000

c) 1100 0000 0100 0000 0000 0000 0000 0000

d) 0100 0011 0000 0000 0000 0000 0000 0000

e) 1100 0000 1100 0000 0000 0000 0000 0000

f) 1100 0001 0111 0000 0000 0000 0000 0000

5. a) A0B2C3E5

b) FAA157E8

6. a) 0110 0110 1100 1100 1111 1111

b) 0011 0011 0110 0110 1111 1111

c) 1111 1111 1111 1111 1111 1111

d) 0001 0010 0011 0100 0101 0110

e) 1010 1011 1100 1101 1110 1111

7. a) 3368601

b) 16763938

c) 3430008

d) 10066329

e) 0

8. a) 2C

b) 26E

c) 61F

d) 3E8

e) 2A5

CPS 125 - Lab 1

Q1. 1100 0010 1110 0000 0000 0000 0000,  
 -vc EXP bits fraction bit

a) Negative Decimal.

b)  $(0000|01)_2 \rightarrow 2^0 + 2^3 + 2^7$  Exp Bias. = 127  
 $= 1 + 8 + 128 = 133$   $e = 133 - 127 = 6$

c)  $m = 110.0000 \dots$

$$= 2^{-1} + 2^{-2} = \frac{3}{4} = 0.75$$

$$\begin{aligned} & (-1)^s (1+m) \times 2^e \\ & (-1)^1 (1+0.75) \times 2^6 \\ & -(1.75) \times 2^6 \\ & -1.75 \times 2^6 \\ & = \underline{\underline{-112}} \end{aligned}$$

Q2. 100 000 0 1000.0000 0000 0000 0000 0000

a) Positive Decimal.

b)  $(10000001)_2 \rightarrow 2^0 + 2^7$  Exp base = 127  
 $= 1 + 128 = 129$   $e = 129 - 127 = 2$

c)  $m = 0$

$$\begin{aligned} & (-1)^s (1+m) \times 2^e \\ & (-1)^0 (1+0) \times 2^e \\ & 1 \times 2^2 \\ & = \underline{\underline{4}} \end{aligned}$$

1100 0000 1000 0000 0000 0000 0000 \* (should be -4 b/c it is the same  
 check: as previous question) ✓

a) Negative Decimal

b)  $(10000001)_2 \rightarrow 2^0 + 2^7$  Exp Base = 127  
 $= 1 + 128 = 129$   $e = 129 - 127 = 2$

c)  $m = 0$

$$\begin{aligned} & (-1)^s (1+m) \times 2^e \\ & (-1)^1 (1+0) \times 2^2 \\ & -1 \times 2^2 \\ & = \underline{\underline{-4}} \end{aligned}$$

Q2. 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000

$$\begin{aligned} & = 2^0 + 2^8 + 2^9 + 2^{10} + 2^{11} \\ & = 1 + 256 + 512 + 1024 + 2048 \\ & = 3841 \end{aligned}$$

$$\begin{array}{r} 0048 \\ 1024 \\ 512 \\ 256 \\ + 1 \\ \hline 3841 \end{array}$$

0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000

= zero

$$\begin{aligned} & 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 0000 \\ & \quad \downarrow 2^4 \\ & \quad 0001 \\ & = 2^0 + 2^4 \\ & = 1 + 16 \\ & = \underline{\underline{17}} \end{aligned}$$

0000 ... 0000 1111

$$= 2^0 + 2^1 + 2^2 + 2^3$$

$$= 1 + 2 + 4 + 8$$

$$= \underline{\underline{15}}$$

Q3.  $157 \quad 256 \quad \underline{128} \quad 64 \quad 32 \quad \underline{\underline{16}} \quad \underline{\underline{8}} \quad \underline{\underline{4}} \quad \underline{\underline{2}} \quad \underline{\underline{1}}$       12-bit Representation:  
 $157 - 128 = 29 - 16 = 13 - 8 = 5 - 4 = 1$        $\downarrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$        $\left. \begin{array}{l} \\ \\ \\ \\ \end{array} \right\}$   $0000 \ 1001 \ 1101$   
 $207 \quad 256 \quad \underline{128} \quad 64 \quad 32 \quad 16 \quad \underline{\underline{8}} \quad \underline{\underline{4}} \quad \underline{\underline{2}} \quad \underline{\underline{1}}$       16-bit Representation:  
 $207 - 128 = 79 - 64 = 15 - 8 = 7 - 4 = 3 - 2 = 1$        $\downarrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$        $0000 \ 1100 \ 1111$   
~~128 - 150~~  
 $\underline{128} \quad 64 \quad 32 \quad \underline{\underline{16}} \quad \underline{\underline{8}} \quad \underline{\underline{4}} \quad \underline{\underline{2}} \quad \underline{\underline{1}}$   
 $150 - 128 = 22 - 16 = 6 - 4 = 2$        $\uparrow \quad \uparrow \quad \uparrow \quad \uparrow$   
~~-55~~  
 $128 \quad 64 \quad \underline{32} \quad \underline{\underline{16}} \quad \underline{\underline{8}} \quad \underline{\underline{4}} \quad \underline{\underline{2}} \quad \underline{\underline{1}}$   
 $55 - 32 = 23 - 16 = 7 - 4 = 3 - 2 = 1$        $\uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow$   
 $-3$   
 $3 - 2 = 1$   
 $\uparrow \quad \uparrow$   
 $2^1 \quad 2^0$   
 $65$   
 $128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1$   
 $65 - 64 = 1$   
 $\uparrow \quad \uparrow$   
 $2^6 \quad 2^0$   

2's complement: (10-bit representation)  
 $0000 \ 1001 \ 0110 \quad \text{complement} \rightarrow 1111 \ 0110 \ 1001 \quad + \frac{1}{1111 \ 0110 \ 1010}$   
 2's complement: 1111 0110 1010

2's complement: (8-bit)  
 $0011 \ 0 \ 111 \quad \text{complement} \rightarrow 1100 \ 1000 \quad + \frac{1}{1100 \ 1001}$

2's complement: (4-bit)  
 $0011 \quad \text{complement} \rightarrow 1100 \quad + \frac{1}{1101}$

2's complement: (8-bit)  
 $0100 \ 0001 \quad \text{complement} \rightarrow 1011 \ 1110 \quad + \frac{1}{1011 \ 1111}$   
 2's complement: 1011 1111

128 - 0      2's complement  
 $(128)_{10} \rightarrow 2^7 \rightarrow 1000 \ 0000 \ . 0$

-6 - 0  
 $(6)_{10} \rightarrow 2^2 + 2^1 \rightarrow 0110 \ 0000 \ . 0$   
 $(-6)_{10} \rightarrow 1001 \quad + \frac{1}{1110}$   
 1110.0

-3 - 0  
 $(3)_{10} \rightarrow 00011$   
 $(-3)_{10} \rightarrow 11100 \quad + \frac{1}{1101 \ . 0}$

-15 - 0  
 $(15)_{10} \rightarrow 2^3 + 2^2 + 2^1 + 2^0 \rightarrow 1111 \ . 0$   
 $(-15)_{10} \rightarrow 00000 \quad + \frac{1}{00001}$   
 0001.0

5. 1010 0000 1011 ~~0010~~  
0010 1100 0011 1110 0101

$$(1010)_2 \rightarrow 2^3 + 2^1 = \underline{\underline{10}} \text{ (A)}$$

$$(0000)_2 \rightarrow \underline{\underline{0}}$$

$$(1011)_2 \rightarrow 2^3 + 2^1 + 2^0 = \underline{\underline{11}} \text{ (B)}$$

$$(0010)_2 \rightarrow 2^1 = \underline{\underline{2}}$$

$$(1100)_2 \rightarrow 2^3 + 2^2 = \underline{\underline{12}} \text{ (C)}$$

$$(0011)_2 \rightarrow 2^1 + 2^0 = \underline{\underline{3}}$$

$$(1110)_2 \rightarrow 2^3 + 2^2 + 2^1 = \underline{\underline{14}} \text{ (E)}$$

$$(0101)_2 \rightarrow 2^2 + 2^0 = \underline{\underline{5}}$$

A0B2C3E5

1111 1010 1010 0001 0101 0111 1110 1000

$$(1111)_2 \rightarrow 2^3 + 2^2 + 2^1 + 2^0 = \underline{\underline{15}} \text{ (F)}$$

$$(1010)_2 \rightarrow 2^3 + 2^1 = \underline{\underline{10}} \text{ (A)}$$

$$(1010)_2 \rightarrow \underline{\underline{10}} \text{ (A)}$$

$$(0001)_2 \rightarrow 2^0 = \underline{\underline{1}}$$

$$(0101)_2 \rightarrow 2^2 + 2^0 = \underline{\underline{5}}$$

$$(0111)_2 \rightarrow 2^0 + 2^1 + 2^2 = \underline{\underline{7}}$$

$$(1110)_2 \rightarrow 2^1 + 2^2 + 2^3 = \underline{\underline{14}} \text{ (E)}$$

$$(1000)_2 \rightarrow 2^3 = \underline{\underline{8}}$$

FAA157E8

Q6. 66CCFF 108 32 16 8 4 2 1

$$\begin{array}{l} (6)_{10} \rightarrow 2^2 + 2^1 = 0110 \\ (C)_{16} \rightarrow (12)_{10} \rightarrow 1100 \\ (F)_{16} \rightarrow (15)_{10} \rightarrow 1111 \end{array} \quad \left. \begin{array}{l} 0110 \\ 0110 \\ 1100 \\ 1100 \\ 1111 \\ 1111 \end{array} \right\}$$

3366FF

$$\begin{array}{l} (3)_{10} \rightarrow 0011 \\ (6)_{10} \rightarrow 0110 \\ (F)_{16} \rightarrow (15)_{10} \rightarrow 1111 \end{array} \quad \left. \begin{array}{l} 0011 \\ 0011 \\ 0110 \\ 0110 \\ 1111 \\ 1111 \end{array} \right\}$$

FFFFFFFFFF → 1111 1111 1111 1111 1111  
 $(F)_{16} \rightarrow (15)_{10} \rightarrow 1111$

123456

$$\begin{array}{l} (1)_{10} \rightarrow 0001 \\ (2)_{10} \rightarrow 0010 \\ (3)_{10} \rightarrow 0011 \end{array} \quad \left. \begin{array}{l} (4)_{10} \rightarrow 0100 \\ (5)_{10} \rightarrow 0101 \\ (6)_{10} \rightarrow 0110 \end{array} \right\} 0001 0010 0011 0100 0101 0110$$

A B C D E F

$$\begin{array}{l} (A)_{16} \rightarrow (10)_{10} \rightarrow 1010 \\ (B)_{16} \rightarrow (11)_{10} \rightarrow 1011 \\ (C)_{16} \rightarrow (12)_{10} \rightarrow 1100 \\ (D)_{16} \rightarrow (13)_{10} \rightarrow 1101 \\ (E)_{16} \rightarrow (14)_{10} \rightarrow 1110 \\ (F)_{16} \rightarrow (15)_{10} \rightarrow 1111 \end{array} \quad \left. \begin{array}{l} 1010 \\ 1011 \\ 1100 \\ 1101 \\ 1110 \\ 1111 \end{array} \right\}$$

Q7. 336699  
 $\downarrow$   
 $16^5 \dots 16^0$

$$\begin{array}{l} 3 \times 16^5 = 3145728 \\ 3 \times 16^4 = 194608 \\ 6 \times 16^3 = 34576 \\ 6 \times 16^2 = 1536 \\ 9 \times 16^1 = 144 \\ 9 \times 16^0 = 9 \end{array}$$

3368601

$$\begin{array}{l} 543210 \\ FFCC22 \\ \downarrow \\ 16^5 \\ 16^4 \\ 15 \times 16^5 = 15728640 \\ 15 \times 16^4 = 983040 \\ 18 \times 16^3 = 49152 \\ 12 \times 16^2 = 3072 \\ 2 \times 16^1 = 32 \\ 2 \times 16^0 = 2 \end{array}$$

16763938

$$\begin{array}{l} 543210 \\ 345678 \\ \downarrow \\ 999999 \\ 999999 \\ 9 \times 16^5 = 9437184 \\ 9 \times 16^4 = 589824 \\ 9 \times 16^3 = 36864 \\ 9 \times 16^2 = 2304 \\ 9 \times 16^1 = 144 \\ 9 \times 16^0 = 9 \end{array}$$

3430008

999999

0000000

$$\begin{array}{l} 3 \times 16^5 = 3145728 \\ 4 \times 16^4 = 262144 \\ 5 \times 16^3 = 20480 \\ 6 \times 16^2 = 1536 \\ 7 \times 16^1 = 112 \\ 8 \times 16^0 = 8 \end{array}$$

10066329

Q8. 44 4096 256 16 1

$$\begin{array}{l} 44 \div 16 = 2.75 \text{ R } 2 \\ 2.75 \div 16 = 0.171 = 0 \underline{R} 2 \\ 1567 \end{array}$$

12C

$$1567 \div 16 = 97.9375 = 97 \underline{R} 15$$

$$97 \div 16 = 6.0625 = 6 \underline{R} 1$$

61F

$$6 \div 16 = 0.375 = 0 \underline{R} 6$$

677

$$677 \div 16 = 42.3125 = 42 \underline{R} 5$$

$$42 \div 16 = 2.625 = 2 \underline{R} 10$$

$$2 \div 16 = 0.125 = 0 \underline{R} 2$$

2A5

622

$$622 \div 16 = 38.875 = 38 \underline{R} 14$$

$$\begin{array}{r} 38 \div 16 = 2.375 = 2 \underline{R} 6 \\ 2 \div 16 = 0.125 = 0 \underline{R} 2 \end{array}$$

26E

1000

$$1000 \div 16 = 62.5 = 62 \underline{R} 8$$

$$62 \div 16 = 3.875 = 3 \underline{R} 14$$

3E8

$$3 \div 16 = 0.1875 = 0 \underline{R} 3$$