### Kai (Steve) Fan

Contact Max Planck Institute for Mathematics

Vivatsgasse 7 53111 Bonn Germany **2**: (603) 667-5475

➤: steve.fan.1024@gmail.com

∴ https://stvfan.github.io

RESEARCH INTERESTS Analytic number theory: the distribution of primes, zeta and L-functions, asymptotic and statistical behaviors of arithmetic functions

EDUCATION

#### Dartmouth College

Ph.D. Candidate, Mathematics, November 2023 M.A. in Mathematics, February 2020

### Southeast University

B.S. in Mathematics and Applied Mathematics, June 2015

#### EMPLOYMENT

#### Max Planck Institute for Mathematics

Postdoctoral fellow, starting January 2024

# Publications and Preprints

- [1] LCM products and  $\kappa$ -colossally abundant numbers (with Mitsuo Kobayashi and Grant Molnar), manuscript in preparation.
- [2] The shifted prime-divisor function over shifted primes, preprint, 2024. arXiv:2406.05217
- [3] Shifted-prime divisors (with Carl Pomerance), submitted, 2024. arXiv:2401.10427
- [4] Weighted Erdős–Kac theorems via computing moments, accepted by Acta Arith., 2023. arXiv:2306.11289v9
- [5] On a super telescoping sum representing binomial coefficients, to appear in Rocky Mountain J. Math., 2023.
- [6] Numerically explicit estimates for the distribution of rough numbers, J. Number Theory **260** (2024), 120–150.
- [7] An inequality related to the sieve of Eratosthenes (with Carl Pomerance), J. Number Theory **254** (2024), 169–183.
- [8] An inequality for the distribution of numbers free of small prime factors, Integers 22 (2022), #A26, 12 pp.
- [9] The second largest Balaban index (sum-Balaban index) of unicyclic graphs (with Wei Fang, Yubin Gao and Zhongshan Li), J. Math. Res. Appl. 37 (2017), 391–403.
- [10] A finite difference scheme for semilinear space-fractional diffusion equations with time delay (with Wanrong Cao, Zhaopeng Hao and Zhizhong Sun), Appl. Math. Comput. **275** (2016), 238–254.

# MISCELLANEOUS NOTES

- [1] The Davenport-Halberstam theorem for Möbius function
- [2] Harmonic sums in arithmetic progressions
- [3] The Erdős-Kac theorem
- [4] The asymptotic for the second moment of  $\zeta(s)$  on the critical line
- [5] On Selberg's proof of Dirichlet's theorem on arithmetic progressions
- [6] A short note on convex functions
- [7] The Copeland–Erdős theorem on normal numbers
- [8] On geometric proofs of theorems on sums of squares
- [9] Vinogradov's estimate for the least quadratic non-residues
- [10] Note on chapter 26 of Davenport's multiplicative number theory
- [11] The Erdős-Ginzburg-Ziv theorem
- [12] Summability and the closed graph theorem

TALKS	May	2024	Counting shifted-prime divisors, Intercity Number Theory Seminar, Utrecht University
	May	2024	Geometry of numbers with applications to linear forms, The Circle Method Seminar, MPIM
	Mar	2024	The singular series in Waring's problem (II), The Circle Method Seminar, MPIM
	Mar	2024	The singular series in Waring's problem $(I)$ , The Circle Method Seminar, MPIM
	Feb	2024	Counting shifted-prime divisors, Algebra and Number Theory Seminar (virtual), Dartmouth College
	Feb	2024	$\label{lem:counting_shifted-prime_divisors} Counting \ shifted-prime \ divisors, \ {\tt Number\ Theory\ Lunch\ Seminar}, \ {\tt MPIM}$
	Oct	2023	$\label{lem:arithmetic combinatorics: integer partitions and sequences}, Graduate Student Seminar, Dartmouth College$
	Apr	2023	$\label{eq:Building finite fields through counting} Building finite fields through counting, Graduate Student Seminar, Dartmouth College$
	Feb	2023	Quadratic reciprocity via linear algebra, Graduate Student Seminar, Dartmouth College
	Nov	2022	Roth's theorem on arithmetic progressions, Graduate Student Seminar, Dartmouth College
	May	2022	Gaps between consecutive primes, Graduate Student Seminar, Dartmouth College
	Apr	2022	$LCM$ products and $\kappa\text{-}colossally$ abundant numbers, Algebra and Number Theory Seminar, Dartmouth College
	Mar	2022	The Prime Number Theorem: From the classical method to the pre-

tentious approach, Graduate Student Seminar, Dartmouth College

TALKS	Nov	2021	Zeros of the Riemann zeta-function and Hardy's theorem, Graduate Student Seminar, Dartmouth College			
	Apr	2021	The transcendence of $e$ and $\pi$ , Graduate Student Seminar, Dartmouth College			
Undergraduate Talks & Reports	June	2015	Ruled surfaces and isometric correspondence, Southeast University			
	March	2015	Semilinear space-fractional diffusion equations with time delay and numerical modeling, Southeast University			
Teaching at Dartmouth	Fall	2022	Instructor, Math 11: Accelerated Multivariable Calculus			
	Fall	2021	Instructor, Math 1: Introduction to Calculus			
	Summer	2020	Lecturer, Math Camp: Exploring Mathematics			
	Spring	2020	TA, Math 13: Multivariable Calculus			
	Fall	2019	TA, Math 23: Differential Equations			
	Winter	2019	TA, Math 3: Calculus			
	Fall	2018	TA, Math 3: Calculus			
ATTENDED	Jan 2023		Joint Mathematics Meetings			
Number Theory	$2021\mathrm{-Present}$		Number Theory Web Seminar			
Courses and Seminars	$2018\mathrm{-Present}$		Algebra and Number Theory Seminar, Dartmouth College			
DEMINARD	Nov 2021–Present		nt Webinar in Additive Combinatorics			
	Oct 2021		2021 Maine-Quebec Number Theory Conference			
	May-Au	g 2021	Harmonic Analysis and Analytic Number Theory (Dual Trimester Program), Hausdorff Center for Mathematics			
	Feb 2021	-Preser	nt Virtual Brazilan Number Theory Seminar			
	$June-July\ 2021$		Summer School in Analytic Number Theory (Virtual Sessions)			
	May 2021		Rational Points and Galois Representations (Online Workshop)			
	Winter 2021		Math 790: Introduction to Transcendence Theory, Duke University			
	Winter 2021		Math 105: Topics in Number Theory, Dartmouth College			
	Fall 2020		Math 249A: Topics in Number Theory (virtual), Stanford University			
	Spring 2019		Math 105: Topics in Number Theory, Dartmouth College			
Honors and Awards	2018–2023 D		Dartmouth Graduate Fellowship, Dartmouth College			
			National Undergraduate Scholarship (Nationally Top 1%), Minstry of Education of China			
	2011–2014 U		Undergraduate Academic Scholarship, Southeast University			
SKILLS AND	Languages: Mandarin Chinese (Native Speaker), English (Fluent)					
ACTIVITIES	Computer Skills: C, C++, Python, HTML, $\+ \!$					
	Assisted in reviewing problems for 2020–2021 Utah Math Olympiads					