

## RECAP Functions and Pattern matching

```
+trait Function1 [-A, +R] {  
    def apply (x:A): R  
}
```

The pattern matching block...

```
{ case (key,value) => key ++ " " + value }
```

expands to the Function1 instance

```
+new Function1 [ ]Binding, String] {  
    def apply (x: ]Binding) = x match {  
        case (key,value) => key ++ " " + value   
                                strawbsline)  
    }  
}
```

```
{ case "ping" => "pong" }
```

can be given type  $\text{String} \rightarrow \text{String}$

We need to give it a type from outside

```
val F: String  $\Rightarrow$  String = { case "ping" => "pong" }  
F ("ping") we get "pong"  
F ("abc") we get match error
```

We can make it a partial function

```
val F: PartialFunction[String, String] =  
{ case "ping" => "pong" }  
F.isDefinedAt ("ping") true
```

A partial function is defined as follows

trait PartialFunction[-A, +R] extends

def apply(x: A): R

def isDefinedAt(x: A): Boolean

Function &  
[-A, +R]

}

{ case "ping" => "pong" } extended to...

new PartialFunction[String, String] {

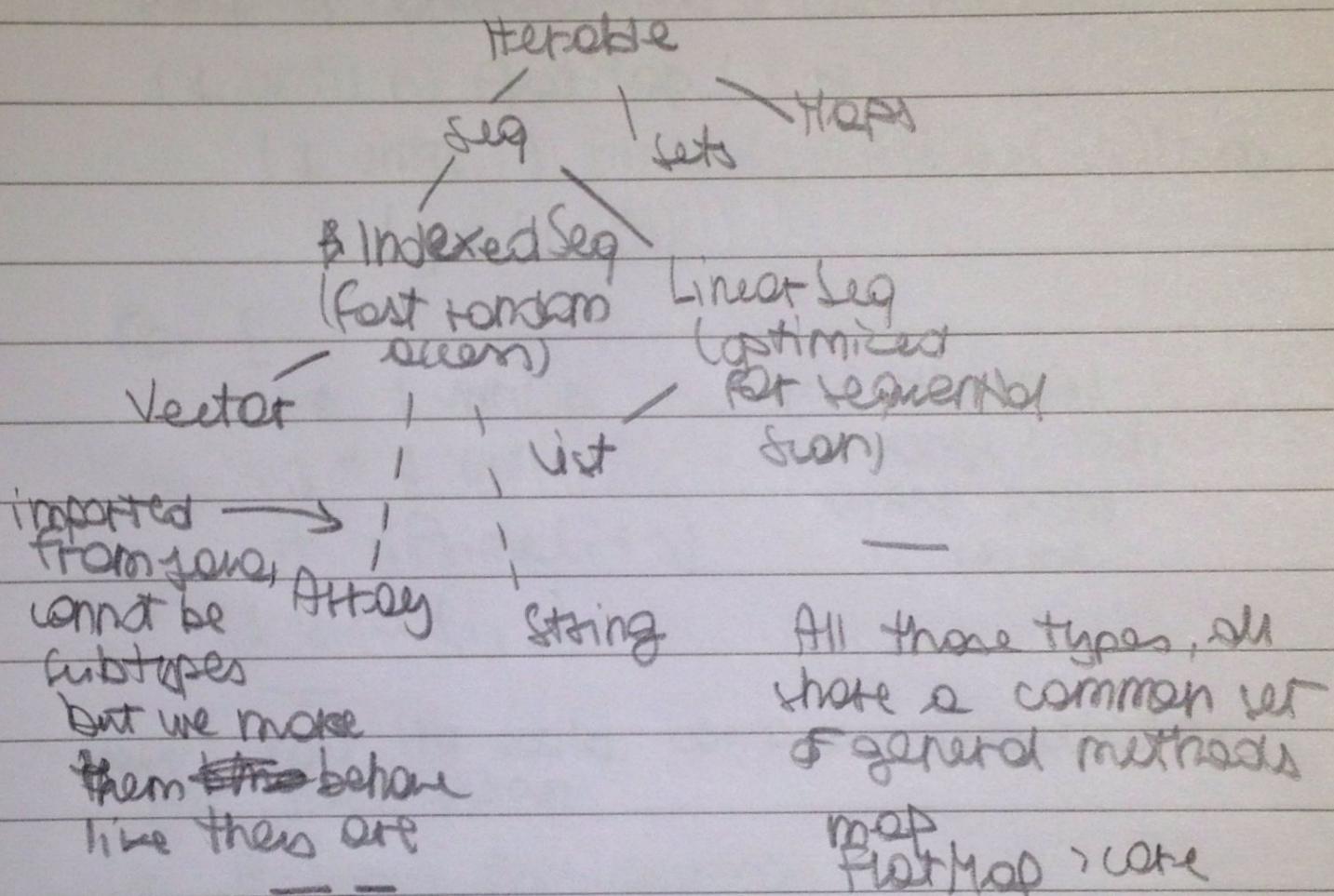
def apply - ...

def isDefinedAt(x: String) = x match {

case "ping" => true

case \_ => false

## RECAP Collections



~~def~~ map

~~def~~ def ~~map~~ [U]

(F : T  $\rightarrow$  U) : List[U] = ~~match~~

this match { case x :: xs  $\Rightarrow$  F(x) :: xs.map(F)  
case Nil  $\Rightarrow$  Nil }

{ }

def flatMap[U](F : T  $\rightarrow$  List[U]) : List[U] =

this match { case x :: xs  $\Rightarrow$  F(x) ++ xs.flatMap(F)  
case Nil  $\Rightarrow$  Nil }

def filter(p : T  $\rightarrow$  Boolean) : List[T] = this match {

case x :: xs  $\Rightarrow$  if p(x) then x :: xs.filter(p)  
case Nil  $\Rightarrow$  Nil }

## For expressions

Simplify combinations of core methods

( $\$$  until  $n$ ) flatMap ( $i \Rightarrow$

( $\$$  until  $i$ ) filter ( $j \Rightarrow \text{isPrime}(i+j)$ ) map  
( $j \Rightarrow (i, j)$ )

For {

$i \in \$$  until  $n$  yield the pair

$j \in \$$  until  $i$  in range  $1$  to  $n$

if  $\text{isPrime}(i+j)$  whose sum

is prime

$\$$  yield  $(i, j)$

—

Here's how the Scala compiler translates  
for expressions

1 A simple for-expression

for ( $x \leftarrow e1$ ) yield  $e2$

becomes  $\text{et}. \text{map} (x \Rightarrow e2)$

2 For-expression with a filter

for ( $x \leftarrow e1 \text{ if } F; s$ ) yield  $e2$

where  $F$  is a filter and  $s$  is a sequence  
of generators and filters ...

becomes for ( $x \leftarrow e1.$  withFilter ( $x \Rightarrow F$ );  $s$ ) yield  $e2$

withFilter can be thought of a variant of  
filter that doesn't produce an intermediate  
list, but instead filter map or flatmap  
function ~~without~~ application

3. With two generators in sequence

`for(x ← e1; y ← e2; i)` yield e3

where i is a sequence of generation and filters

becomes `e1.flatMap(x ⇒ for(y ← e2; i) yield e3)`

-

Each of these rules translates to `for-expression` with one fewer element between the parentheses:

1 eliminates a single generator

2 eliminates a filter

3 eliminates the leading generator

The lhs of a generator in a `for expression` can also be a pattern.

They'll get ~~converted~~ as implicit filters  
so does

map, flatMap, filter can be defined in terms of for

def mapFun[T, V](xs: List[T], f: T  $\Rightarrow$  Iterable[V])

: List[V] = for(x  $\in$  xs) yield f(x)

def flatMap[T, V](xs: List[T], f: T  $\Rightarrow$  Iterable[V])

: List[V] = for(x  $\in$  xs; y  $\in$  f(x)) yield y

def filter[T](xs: List[T], p: T  $\Rightarrow$  Boolean): List[T] =

for(x  $\in$  xs if p(x)) yield x

-

In reality, the Scala compiler translates  
for expression to combinations of  
map, flatMap and a variant of filter

↓  
lazy

for(x  $\in$  e1) yield e2

et. map(x  $\Rightarrow$  e2) 1. Simple for expr!

for(x  $\in$  e1 if f; s) yield e2

↓ translated  
to,

more filters

s can be  
empty!

for(x  $\in$  e1 withFilter  
(x  $\Rightarrow$  f); s) yield e2

↑ generators

2. for expr

↑ filter absorbed  
by generator

where f is a

↑ generator reduced  
to elements that  
pass condition f

filter and s is  
a sequence  
of generators,

for(x  $\in$  e1; y  $\in$  e2; s) yield e3

↓ translated to

et. flatMap(x  $\Rightarrow$  for(y  $\in$  e2; s)  
yield e3)

3. A for expr  
where s is a  
sequence of  
generators  
and filter is  
translated to

1 → Direct translation into a map

2 / 3 → for expression to another with one less element ~~one less element~~

It will then translate into a map once we hit 1 after 2/3 simplifications!

For expr are not limited to collections.

They can be used with any type with map, withFilter, flatMap defined

## Functional Random Generation

~~Random value generation~~

(get random values for other domains  
~~other than~~

```
trait Generator[L + T] {  
    def generate: T
```

}

```
val integers = new Generator[Int] {  
    val rand = new java.util.Random  
    def generate = rand.nextInt()
```

```
val booleans = new Generator[Boolean] {  
    def generate = integers.generate > 0
```

```
val pairs = new Generator[(Int, Int)] {  
    def generate = (integers.generate,  
                  integers.generate)
```

}

~~THEORY~~

Ideally, we can write

~~not~~ `bodeoms = For(x < integers) yield x`  
~~def~~ `points [T, U] (T: Generator[T], U: Generator[U])`  
`= for {x < T; y < U} yield points(x, y)`

We need to define map and flatMap

```
trait Generator[T] {  
    self => // methods on others for this  
    def generate: T  
    def map[S] (F: T  $\rightarrow$  S): Generator[S] =  
        new Generator[S] {  
            def generate = F(self.generate)  
        }  
}
```

```
def flatMap[S] (F: T  $\rightarrow$  Generator[S]): Generator[S] =  
    new Generator[S] {  
        def generate = F(self.generate).generate  
    }
```

---

```
def single[T] (x: T): Generator[T] = new Generator[T] {  
    def generate = x  
}
```

```
def choose (lo: Int, hi: Int): Generator[Int] =  
    for (x < integers) yield lo + x % (hi - lo)
```

## List generator

```
def lists: (gen[List[int]]) = for { isEmpty < boolean }  
    list <- if (isEmpty) emptyLists else nonEmptyLists  
    } yield list
```

```
def emptyLists = single(Nil)
```

```
def nonEmptyLists = for { head < integer }  
    tail <- lists } yield head :: tail
```

## Tree generator

```
def leafs: (gen[Leaf]) = for { x < integers }  
    } yield Invert(x)
```

```
def trees: (gen[Tree]) = for { isLeaf < boolean }  
    tree <- if (isLeaf) leafs else invert  
    } yield tree
```

## RANDOM TESTING!

### Unit Tests

- You come up with some test inputs to program functions and a postcondition
- The postcondition is a property of the expected result
- Verify that ~~the~~ the program satisfies the postcondition

There may be other test inputs on which the program could fail

We can do it without finding the test inputs if we can generate random test inputs!

```

def test[T](g: Gen[T], numTimes: Int = 100)
  (test: T => Boolean): Unit =
    for (i < 0 until numTimes) {
      val value = g.generate
      assert(test(value)), "test failed
                            for " + value)
    }
    println(s"passed $numTimes tests")
}

```

The idea of random tests ~~generator~~ and random value generators is embodied in a tool called ScalaCheck

It would come up with random value generators, sometimes just by giving the type, and then run tests.

↗ test domains!

```

forAll { (l1: List[Int], l2: List[Int]) =>
  l1.size + l2.size == (l1 ++ l2).size
}

```

If a test fails, it can minimize the counter example, ~~if~~ if it tries to repeatedly find smaller and smaller examples until the ~~small~~ example is small enough to be easy to understand as a counterexample

## Monads

Date structures with map and flatMap seem to be quite common.

In fact there's a name that describes this class of date structures together with some algebraic laws that they should have, called monads.

A monad is a parametric type  $M[T]$  with two operations: FlatMap and unit  
that  $M[T] \{$  (should bind)  
 $\text{def FlatMap}[U](f:T \Rightarrow M[U]): M[U]$   
3     $\text{def unit}[T](x:T): M[T]$

List is a monad with unit  $\text{List}(x)$ , same for set, option and generator ( $\text{single}(x)$ )

FlatMap is an operation if each  $f$  has unit  
there, whereas unit is different for each monad  
 $m \text{ map } f \rightsquigarrow m \text{ FlatMap } (x \rightarrow \text{unit}(f(x)))$

To qualify as a monad, /m FlatMap (F and Then unit)  
a type has to satisfy those laws

$$\begin{array}{c} (x) \quad \text{unit!} \\ \text{unit}' \text{ FlatMap } F = F(x) \end{array}$$

$m \text{ FlatMap } F \text{ FlatMap } g =$   
 $\rightarrow m \text{ FlatMap } (F \text{ FlatMap } g)$        $m \text{ FlatMap } \text{unit} = m$   
Associativity!  
Right unit!

Significance of ~~the~~ the ~~lawn~~ for for expr.

1 Associativity says that one can inline nested for expressions

For(  $y \in$  For(  $x \in m ; y \in F(x)$  ) yield  $y$

$z \in Q(y))$  yield  $z =$

for(  $x \in m ; y \in F(x) ; z \in Q(y)$  ) yield  $z$

2 Right unit says  $\text{For}(x \in m) \text{ yield } x = m$

3 left unit does not have an analogue for for expr

Try is another type that resembles Option, except that there's two different cases, Success and Failure that contains an exception.

Try is used when we want to propagate exception between different threads or processes

abstract class Try [+T]

use class Success [T] ( $x : T$ ) extends Try [T]

use class Failure (ex: Exception)

extends Try [Nothing]

Bottom up type

~~What are~~ static types!

Types allow you to denote function domains and codomains

Given types the compiler can now statically verify that the program is valid

With increasing expressiveness in type systems we can produce more reliable code

All type information is stored at compile time

## Types in Scala

- parametric polymorphism, roughly generic programming
- (local) type inference, you know ~~that~~ one
- existential quantification, roughly, defining something for some unnamed type
- views, roughly, "castability" of values of one type or another

You can wrap up an arbitrary computation in a try  $\bullet$  Try(expt)

Here's an implementation of Try

Object Try {

def apply[T](expt:  $\Rightarrow T$ ): Try[T] =

try Success(expt) catch {

case NonFatal(ex)  $\Rightarrow$  Failure(ex)}

expt passed  
by name  
because  
otherwise it  
wouldn't be a  
computation that could  
throw an exception!

Just like with option, try-valued computation can be composed in for extensions

```
for { x ← computeX; y ← computeY }  
    yield F(x, y)
```

IF compute X and compute Y both succeed with Success(x) and Success(y), that will return Success(F(x, y)). But if either computation fails, this will return Failure(ex)

flatMap and map on Try

```
def flatMap[U](F: T ⇒ Try[U]): Try[U] = this match {  
  case Success(x) ⇒ Try(F(x))  
  case NonFatal(ex) ⇒ Failure(ex)  
  case Fail ⇒ Fail}
```

```
def map[TU](F: T ⇒ U): Try[U] = this match {  
  case Success(x) ⇒ Try(F(x))  
  case NonFatal(ex) ⇒ Failure(ex)  
  case Fail ⇒ Fail}
```

~~Try is not a monad!~~

~~I could be with unit Try constructor but we want the to never throw a non fatal exception in a statement like Try.map(flatMap!)~~

~~that fails the first law!~~

~~An exception with Try.map flatMap with never throw a non fatal exception~~

Streams!

We've seen a number of immutable collections that provide powerful operations for combinatorial search

~~Task 2~~

((100 to 1000) filter isPrime) ~~(1)~~ (1)

2nd prime between 100 and 1000

which is more elegant than ~~the~~

nthPrime (from: Int, to: Int, n: Int): Int =

  IF (from)  $\geq$  to throw new error

  else IF (isPrime (from))

    IF (n = 1) from else (from + 1,  
      + to, n - 1)

  else nthPrime (from + 1, to, n)

But the shorter expression is inefficient because we construct all primes between 1000 and 10000 only to get the second element!

Reducing the bound would speed up but you ~~can't~~ won't be ~~sure~~ ~~sure~~ whether the bound is too low and you would miss the prime number

Idea, avoid computing tail of a sequence until it is needed for evaluation result <sup>the</sup>

Stream is a class ~~similar~~ to lists which tail is evaluated on demand

Streams can be build from Stream.empty and a constructor Stream.cons

val xs = Stream.cons(1, Stream.cons(Stream.empty))

or Stream(1, 2, 3), like other<sup>2)</sup> collections

toStream will turn a collection into a stream  
(1 to 1000).toStream

→ res0: Stream = Stream(1, ?)

map Function that returns (lo until hi).toStream

```
def listRange (lo:Int, hi:Int): List[Int] =  
  if (lo >= hi) Nil  
  else lo :: listRange (lo + 1, hi)
```

compose  
to ↓

```
def StreamRange (lo:Int, hi:Int): Stream[Int] =  
  if (lo >= hi) Stream.empty  
  else Stream.cons (lo, StreamRange (lo + 1, hi))
```

Streams support all the methods of List  
((1000 to 10000).toStream filter isPrime) (91)

:: always produces a list, never a stream

#:: produces a stream! x#::x1 =

↳ can be used in patterns!

Stream.cons (x, xs)

## Implementation of streams

```
trait Stream[+A] extends Seq[A] {  
    def isEmpty: Boolean; def head: A; def tail:  
        Stream[A] }  
    ONLY Stream[A]  
object Stream {  
    def cons[T](hd: T, tl: Stream[T]): Stream[T] =  
        new Stream[T] { def isEmpty = false  
            def head = hd; def tail = tl }  
}
```

```
val empty = new Stream[Nothing] {  
    def isEmpty = true  
    def head = Error; def tail = Error }  
}
```

\* When I first construct a cons cell for a ~~to~~ stream, the tail is not evaluated, it is the first time somebody dereferences it! (calls def tail!)

The other methods are implemented analogously to their list counterpart

Lazy evaluation!

The proposed implementation of streams solves the problem of enabling unnecessary computation, but it suffers from another performance problem!

If tail is called several times, the corresponding stream will be recomputed each time

Idea, store the result of the first evaluation of tail, and re-use the stored result instead of recomputing it

~~We will be a purely functional language.~~  
~~BY EXPERT~~

We call this ~~the~~ scheme lazy evaluation (as opposed to by-name evaluation where everything is recomputed and strict evaluation for normal parameters and val definitions)

Haskell uses it by default!

Scheme doesn't do it as lazy val can be unpredictable

so it uses strict evaluation by default but allows lazy evaluations with ~~lazy~~ of value definition with "lazy val" pattern

lazy val x = ~~exp~~  $\uparrow$  not evaluated here at def x = ~~exp~~  $\downarrow$  definition but after all its name when x is accessed

- the difference is that ~~def~~ it is then reevaluated each time, while, lazy val ~~lets~~ the expr is reevaluated everytime except for the first one

~~def~~ Using lazy val for tail,  
~~Stream~~ Stream can be more efficient

~~def~~ cons ... => new ~~Stream~~{  
  ~~def~~ head = hd  
  ~~lazy val~~ tail = tl}

def cons[T](hd: T, tl: ~~Stream~~[T]) =  
  new ~~Stream~~[T] {  
    ~~def~~ head = hd  
    ~~def~~ tail = tl  
    ...  
    3

~~the~~ infinite streams?

All ints starting from a given number

def from(n: Int): Stream[Int] =

n #:: From(n+1)

=

Sieve of Eratosthenes

- start w/ all integers starting from  $\frac{1}{2}$
- Eliminate multiples of 2 prime
- The first ~~number~~ of the resulting list is 3, prime
- Eliminate all multiples of 3
- iterate. At each step, the first number in the list is prime and eliminate its multiples

def sieve(s: Stream[Int]): Stream[Int] =

s.head #:: sieve(s.tail filter (\_ % s.head != 0))

val primes = sieve(From(2))

(primes take(100)).toList

Square roots

Our previous square root algorithm used is GoodEnough to tell when to terminate the iteration.

With streams we express the concept of a converging series without having to worry about when to terminate it

sqrt Stream ( $x$ : Double) : Stream[Double] = {

def improve (guess: Double) =

$$(guess + x / guess) / 2$$

lazy val guesses : Stream[Double] =

1#::(guesses map improve)

3 guesses

=

val xs = from(1) map (\_ \* N)

val x1 = from(1) filter (\_ % N == 0)

map does not generate unnecessary stream elements and therefore

it's ~~more~~ efficient

more

## Functions and state

Until now our programs have been  
side effect free

For all programs that terminate  
only ~~if~~ sequence of output give  
the same result

if ( $t == 0$ ) 3 else iterate ( $t - 1$ , square,  
square( $t$ ))

iterate(0, square  
square(3))

if (i == 0) 3  
else iterate(1-1, count, 3+3)

→ 19 ←

Confluence, discovered by Church and Russell,  
also called Church-Russell theorem.

That holds for pure functional programming,  
but we now want to introduce state

Some objects have state that changes over the course of time

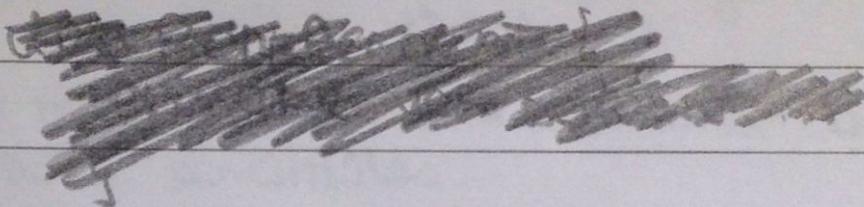
"An object has state if its behaviour is influenced by its history"

Every form of mutable state is constructed from some variables

To define a variable use var!

~~The value~~ A variable can be reassigned

Objects with state are usually represented by objects that have some variable members



## Identity and change

$\text{val } x = E ; \text{ val } y = E$   $E \rightarrow \text{expression}$

then  $x$  and  $y$  are the same

$\text{val } x = E ; \text{ val } y = x$  is same as above

~~Equivalent~~ operational equivalence defines the property of being the same

suppose you have  $x$  and  $y$ , they are operational equivalent if no possible test can distinguish between them

$\text{val } x = \text{new} \dots$   
 $\text{val } y = \text{new} \dots \leftarrow$   $f$  is every possible test  
 $f(x, y) = f(x, x)$

IF  $f(x, y)$  is different from  $f(x, x)$  the objects are different

$\text{val } x = \text{new BankAcc}$   $\text{val } x = \text{new BankAcc}$   
 $\text{val } y = \text{new BankAcc}$   $\text{val } y = \text{new BankAcc}$   
 $x \text{ deposit } 30$   $x \text{ deposit } 30$   
 $y \text{ withdraw } 20$   $\rightarrow x \text{ withdraw } 20$

the final results are different, they're not equal!

`val x = new BankAcc`

`val y = x`  $\xrightarrow{\text{NO sequence of operations}} \text{can't distinguish between them}$

The model of substitution cannot be used in those examples.

According to this model, one can always replace the ~~the~~ name of a value by the expression that defines it. For example

`val x = new BankAcc`  $\xrightarrow{\text{val x = new BankAcc}}$   
`val y = x`  $\xrightarrow{\text{val y = new BankAcc}}$

The `x` in the definition of `y` could be replaced by `new BankAcc`, but we've seen that this change leads to a different program.

The substitution model is not valid with assignments

It is possible to adapt the substitution model, but that becomes more complicated

Variables are enough to model all imperative programs

Loops are not essential for imperative languages,  
and can be modelled ~~using~~ functions

def WHILE (condition:  $\rightarrow$  Boolean) (command:  $\rightarrow$  Unit)  
: Unit = if (condition) {  
    command  
    WHILE (condition) (command)  
} else ()

- conditions are passed by value so that they are translated in each iteration
- WHILE is tail recursive

def REPEAT (command:  $\rightarrow$  Unit) (condition:  $\rightarrow$  Boolean) =  
    command  
    if (condition) ()  
    else REPEAT (command) (condition)

The classical For loop cannot be modeled simply by a higher order function

Scala has a similar kind of for loop

for (i < 1 until 3) print(i)

For loops translate quite similarly to for expressions, but for expressions translate into combinations of map and flatmap,

for loops into combinations of function foreach

foreach ( $F: T \rightarrow$  Unit): Unit =  $\lambda$

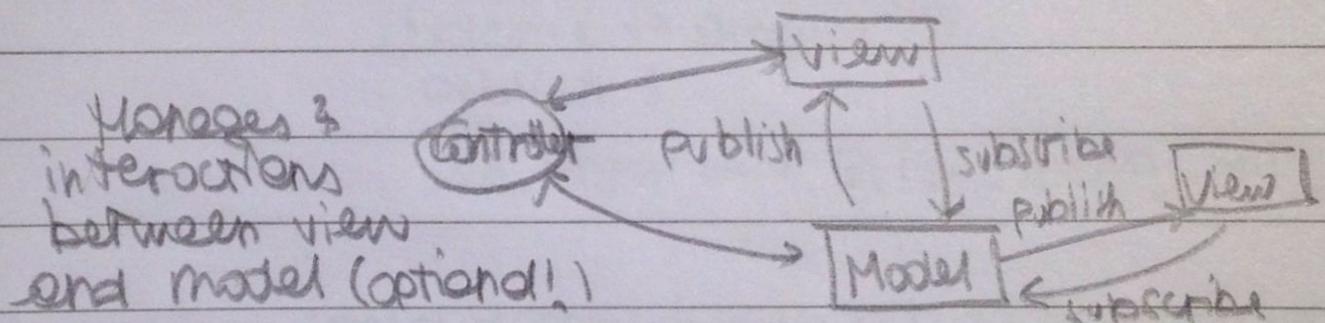
\* apply  $F$  to each element of the collection

```

for (i < 1 until 3 ; j < "abc") println(i + " " + j)
(1 until 3) foreach (i => "abc" foreach (j => println
Timely effects = (i + " " + j))

```

The observer pattern is widely used when views need to react to changes in a model present the properties of the model in some way maintains the logic of an application



trait Publisher {

```

private var subscribers: Set[Subscriber] =
def subscribe(subscriber: Subscriber) = {
  subscribers += subscriber
}

```

```

def unsubscribe(subscriber: Subscriber) =
  subscribers -= subscriber
}

```

```

def publish() = subscribers.foreach(_.handle(this))
}

```

trait Subscriber {

```

def handle(pub: Publisher)
}
```

```
class BankAccount extends Publisher {  
    private var balance = 0  
    def withdraw(amount: Int) =  
        def deposit(amount: Int) =  
            if (amount > 0) {  
                balance += amount  
                publish  
            }  
}
```

```
def withdraw(amount: Int) =  
    if (0 < amount & amount <= balance) {  
        balance -= amount  
        publish  
    }  
    else throw new Error("Insufficient funds")  
}
```

```
class Consolidator(observed: List[BankAccount])  
    extends Subscriber {  
    observed.foreach(_.subscribe)  
    private var total: Int = 0  
    def handle(pub: Publisher) =  
        compute()  
    private def compute() =  
        total = observed.map(_.currentBalance).sum  
    def totalBalance = total  
}  
=
```

~~Crosscutting pattern~~

## Observer pattern, The good

- Decouples view from state
- varying number of views for a given state
- simple to set up

## The bad

- Forces imperative style, since handlers return Unit  
(so they must be imperative)
- Many moving parts that need to be coordinated
- Concurrency makes things more complicated
- Views are still tightly bound to the state, view updates happens immediately

## Functional Reactive Programming

Reactive programming is all about reacting to sequences of events that happen in time

Functional view: Aggregate an event sequence into a signal

- A signal is a value that changes over time
- Represented as a function from the time domain to the value domain
- Instead of propagating updates to mutable state, we define new signals in terms of existing ones

Example: Mouse positions

## Event-based view:

Whenever the mouse moves, an event  
Mouse Moved (to for. Position)

... it fixed I will update current state (imperative)

FPP view:

A signal mouse position: `signal[Position]`  
which at any point in time represents  
the current mouse position

## Origins of FRP

started in 1997 with the paper Functional Reactive Animation by Elliott, Hudspeth

There have been many FRP systems since

We will introduce FPR with a minimal class FPR light, which we'll define ourselves

FIFO signal is modeled after scale reset, ~~which~~ in the first Defecting the Observer pattern

## Fundamental Signal Operations

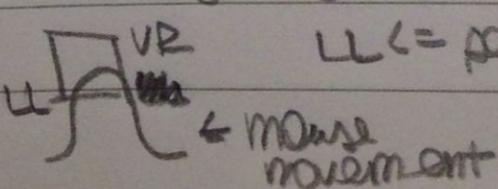
- Obtain the value of a signal at the current time.  
In our library it is expressed by ()

e.g. mousePosition() //the current mouse position

- Define a signal in terms of other signals  
In our library expressed by the signal constructor

eg def isRectangle (LL:Position, UR:Position): Signal

= Signal { vol for = maniforion ()



## Constant Signals

The signal(::) syntax can also be used to define a signal that has always the same value

```
val sig = Signal(3)
```

## Time-Varying Signals

- We can use externally defined signals (such as multiplication) and map over them to have new ~~value~~ time-varying signals
- Or we can use a Var (mutation of Signal)

## = Variable Signals

Values of type Signal are immutable

But our library defines a mutable Var of Signal that can change

Var provides an update operation, which allows to redefine the value of a Signal from the current time on

```
val sig = Var(3)
```

```
sig.update(5) // From now on, sig is 5
```

In Scala, code to update can be written as assignments

```
arr(i) = 0 really is arr.update(i, 0)
```

```
class Array[T] { def update(idx:Int, value:T) = ... }
```

Indexed assignment like  $f(E_1, \dots, E_n) = E$

is translated to  $f.update(E_1, \dots, E_n, E)$

For  $n=0$ ,  $F()=E$  is shorthand for  $f.update(E)$

e.g.  $update(s)$  really is  $f(g(), s) = s$

Var look like mutable variables, but there's a crucial difference

We can map over signals, which gives us a relation between two signals that is maintained automatically at all future points in time

$$\begin{aligned} a &= 2 \\ b &= a * 2 \\ a &= a + 1 \end{aligned}$$

↑  
b is not updated!

$$\begin{aligned} a(1) &= 2 \\ b(1) &= 2 * a(1) \end{aligned}$$

$$a(1) = 3$$

↑ b is updated!

class BankAccount {

private var balance = Var(0)

def deposit(amount: Int) =

if (amount > 0)

val b = balance()

balance() = b - amount

def withdraw(amount: Int) = balance()

if (amount > 0 && amount < balance())

val b = balance()

balance() = amount + b

else throw new Error("Insufficient funds")

def consolidated(accounts: List[BankAccount]): Signal[Int] =

: Signal[Int] =

Signal(accounts.map(-balance)).sum

def exchange = Signal(246.00) ← Add exchange dollar with bitcoins

val inDollar = Signal(c() \* exchange())

## A Simple FRP Implementation

```
class Signal[T] (expr: => T) {  
    def apply (): T = ??? }
```

object Signal {

```
    def apply [T] (expr: => T) = new Signal(expr) }
```

class Var[T] (expr: => T) extends Signal[T]

```
    def update (expr: => T): Unit = ??? }
```

object Var {

```
    def apply [T] (expr: => T) = new Var(expr) }
```

Each signal maintains

- The current value
- The expression that defines the signal
- A set of observers: other signals that depend on the value of the current signal

If signal changes, all observers need to be re-evaluated

How do we record dependencies in observers?

- When evaluating a signal-valued ~~expr~~ expression, we need to know which signal's value gets defined or updated by the expression
- If we know that, then executing `sig()` means sending a value to the observers of `sig`
- When signal changes, all previously observing signals are re-evaluated and the observers in sig are alerted
- Re-evaluation will re-enter a calling signal's value in sig's observers, as long as value still depends on sig

How do we find out on ~~who's~~ who's behalf a signal expression is evaluated

One simple way to do this is to maintain a global structure referring to the current collector

That data structure is stored in a stack-like fashion because one evaluation of a signal might trigger others

```
class StackableVariable [T] (init:T) {  
    private var values: List[T] = List(init)  
    def value: T = values.head  
    def withValue [R] (newValue: T) (op: T ⇒ R): R =  
        { values = newValue :: values  
          try { finally values = values.tail }  
        }  
}
```

object Nofignal extends Signal[Nothing] (???){...}

object Signal {

```
    private val collect = new StackableVariable  
    def apply [T] (expr: ⇒ T) = [Signal[-]](Nofignal)  
        new Signal(expr)  
}
```

class Signal [T] (expr: ⇒ T) {

import Signal.\_

private var myExpr: () ⇒ T = \_

private var myValue: T = \_

private var observers: Set[Signal[-]] = Set()  
 update(expr)

protected def update (expr: ⇒ T): Unit = {

myExpr = () ⇒ ~~Expr~~ expr

computeValue()

```

protected def computeValue(): Unit = {
    myValue = collector.withValue(this)(myExpr)
}

def apply() = {
    observers += collector.value
    assert(!collector.value.observers.contains
        (this), "cyclic signal definition")
    myValue
}

} ← close Signal class
=

```

- A signal's current value can change when
- somebody calls an update operation on a var or
  - the value of a dependent signal changes

propagating requires a more refined implementation of computeValue

```

protected def computeValue: Unit = {
    val newValue = collector.withValue(this)(myExpr)
    if !newValue.equals(myValue) = newValue {
        myValue = newValue
        val obs = observerH
        observerH = Set()
        obs.foreach(_ -> computeValue())
    }
}

```

```

object NoSignal extends Signal[Nothing](???) {
    override def computeValue() = ()
}

→
enable computeValue for NoSignal

```

all functionalities for Var is already present in Signal class. Var[T](expr: > T) extends Var0[T](expr)?  
override off update(expr: > T): Unit =  
    update(expr).  
override update to make it public  
(was protected)

object Var {  
 def apply[T](expr: > T) = new Var[expr]  
}

~~The other might be to have multiple global state~~

One way to get around the problem of concurrent access to global state is to use synchronization

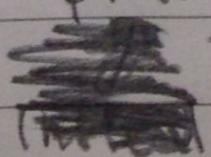
But this blocks threads, can be slow and can lead to deadlocks

Another solution is to replace global state by a thread local state

- Thread local state means that each thread accesses a separate copy of a variable
- It is supported by Scala through `scala.util.DynamicVariable`

object Signal {

private val collar = new DynamicVariable[



signal[-]](NoSignal)

}

Instead of  
SelectableVariable

thread-local stores have a number of disadvantages

- It is imperative relative, often produces dependencies which are hard to manage
- Its implementation on the JRE involves a hash-table lookup which can be a performance problem
- It does not play well in situations where threads are multiplexed between several tasks

Another solution, Implicit Parameter

- Instead of maintaining a thread-local variable, we pass its current value into a word extension as an implicit parameter
- This is purely functional. But it currently requires more boilerplate than the thread-local solution
- Future versions of scob might solve that problem

Latency is an effect

"Computation ~~on time~~ time"

val socket = Socket()

val packet = ~~Random~~ → Socket.readFromMemory()

// block for 50,000 ns

val confirmation = socket.sendToEurope()

// block for 150,000,000 ns

Both blockings would throw an exception

~~Callback~~, if a computation takes a lot of time, we introduce a callback that will be called when the computation terminates either successfully or with an exception

=

Future[T] is a monad that handles both exceptions and latency

~~import~~

trait Future[T] { ... }

def onComplete(callback: Try[T] ⇒ Unit)

(implicit executor: ExecutionContext)

}

: Unit

You can pattern match it like

ts match {

case Success(t) ⇒ onNext(t)

case Failure(e) ⇒ onError(e)

}

```
trait Socket {
```

```
  def readFromMemory(): Future[Array[Byte]]
```

```
  def sendToEurope(socket: Socket, bytes: Byte):
```

```
}
```

```
Future[Array[Byte]]
```

```
val socket = Socket()
```

```
val port = Future[Array[Byte]] =
```

```
socket.readFromMemory
```

↪ ~~confirmation~~

```
port.onComplete {
```

```
  case Success(p) => {
```

```
    val confirmation: Future[Array[Byte]]
```

```
    3       socket.sendToEurope(p)
```

```
  case Failure(t) => ...
```

```
3
```

↪ Not great...

# Starts an asynchronous computation and returns a Future object to which you can ~~subscribe~~ subscribe to be notified when the Future completes

```
object Future {
```

```
  def apply[T](body: => T)
```

```
    (implicit context: ExecutionContext): Future[T]
```

```
3
```

## Combinators on Future:

(FlatMap, map, filter)

Future has common higher-order operations and specific ones such as recoverWith

= Better:

val socket: Socket()

val packet: Future[Array[Byte]] = socket.

val confirmation: Future[Array[Byte]] =  
socket.readFromMemory() =  
socket.flatMap(p => socket.sendToEurope(p))

=  
def recover(f: PartialFunction[Throwable, T]): Future[T]

def recoverWith(f: PartialFunction[Throwable, Future[T]]): Future[T]

↑ FLATMAP FOR  
ERROR CASE

↓ Map for the error case

↓ error case

def fullBcastTo(that: => Future[T]): Future[T] = {  
 this recoverWith {  
 case \_ => that recoverWith (case \_ => this)  
 }  
}

def sendToSafe(packet: Array[Byte]): Future[Array[Byte]] =  
sendTo(mailServer.europe, packet) +> {  
 .fullBcastTo { sendTo(mailServer.usa, packet) } +> {  
 case \_ not= mailServer.usa.getMessage.  
 }  
}

case \_ not= mailServer.usa.getMessage.  
} +> {  
 .fullBcastTo { sendTo(mailServer.usa, packet) } +> {  
 case \_ not= mailServer.usa.getMessage.  
 }  
}

Sometimes you want to block (like printing),  
there's a method that allows to block on a  
Future with a timeout duration.

~~The result is not guaranteed~~

```
xf → val socket = Socket()  
val socket Future[Array[Byte]] =  
  socket.readFromMemory()  
val confirmation: Future[Array[Byte]] =  
  socket.write("socket.sendToSelf(-)")  
val c = Await.result(confirmation, 2 seconds)  
println(c.toNext)
```

You always want asynchronous and never  
block! except for little scripts.

(You might as well not use asynchrony)

### composing futures

We can rewrite the code xf wh  
for comprehension like

post fix operator  
(3 minutes wh  
import scala.  
longer postfix)

```
val socket = Socket()  
val confirmation: Future[Array[Byte]] = for {  
  packet ← socket.readFromMemory()  
  confirmation ← socket.writeToSelf(packet)  
} yield confirmation
```

```
def retry(notimes: Int)(block: ⇒ Future[T]): Future[T] =  
  if (notimes == 0) Future.failed(  
    new Exception("Sorry"))  
  else block.rollbackTo {  
    retry(notimes - 1) { block ⇒
```

3 3 3  
3 3 3

Closer look at flatMap in terms of onComplete:

trait Future[T] {

def onComplete (callback: Try[T] => Unit): Unit = ...

def flatMap[S](f: T => Future[S]): Future[S] = ???

}

def flatMap[S] = newFuture[S] {

def onComplete (callback: Try[S] => Unit): Unit =

self onComplete {

case Success(x) => f(x).onComplete(callback)

case Failure(e) => callback(Failure(e))

3

=  
3

"When we do things wh recursion, it often needs to  
do it wh  $\in$  fold"

↳ neutral element

List(a, b, c). foldRight(e)(f) ← function

Folds the list from right to left

f(a, f(b, f(c, e)))

List(a, b, c). foldLeft(e)(f)

Folds ... from the left

f(f(f(f(e, a), b), c))

The recursion is  
elected, and the  
way to go

def retry(n: Int)(block: => Future[T]): Future[T] = {

val ms = (1 to n).toList

val attempts = ms.map(\_ => () => block)

val failed = Future.failed(new Exception("boom"))

val result = attempts.foldLeft(failed) {

((e, block) => e.recoverWith { block(1) })

3

// ok val result = attempts.foldRight((1) => failed) {

((block, e) => (1) => { block.flatMapTo { e } })

result(1)