



Software Testing & Quality Assurance

Boundary Value Testing

- ❖ Boundary value analysis
- ❖ Single fault assumption
- ❖ Robustness testing
- ❖ Worst case testing
- ❖ Special value testing
- ❖ Random testing



Credits & Readings

The material included in these slides are mostly adopted from the following books:

- *Software Testing: A Craftsman's Approach*, by Paul Jorgensen, CRC PRESS, third edition, ISBN: 0-8493-7475-8
- Cem Kaner, Jack Falk, Hung Q. Nguyen, *“Testing Computer Software”* Wiley (see also <http://www.testineducation.org/>)
- Cem Kaner, James Bach, Bret Pettichord, *“Lessons Learned in Software Testing”*, Wiley
- Paul Ammann and Jeff Offutt, *“Introduction to Software Testing”*, Cambridge University Press
- Kent Beck, *“Test-driven Development by Example”* Addison-Wesley
- Robert Binder, *“Testing Object-Oriented Systems: Models, Patterns, and Tools”* Addison-Wesley
- Glen Myers, *“The Art of Software Testing”*



Introduction

- Input domain testing is the most commonly taught (and perhaps the most commonly used) software testing technique
- We will see a number of approaches to boundary value analysis
- We will then study some of the limitations of domain testing

What is Boundary Value Analysis?

- Many programs can be viewed as a function F that maps values from a set A (its domain) to values in another set B (its range)

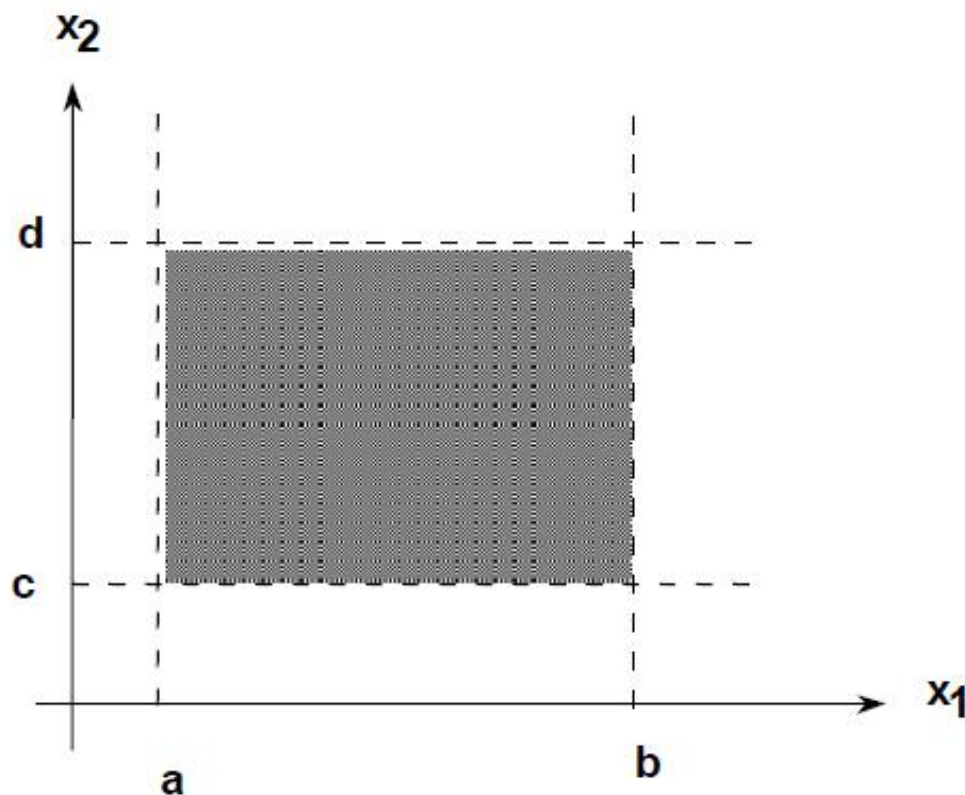
$$F : A \rightarrow B$$

- The input variables of F will have some (possibly unstated) boundaries:

$$a \leq x_1 \leq b$$

$$c \leq x_2 \leq d$$

Input domain for variables x_1 and x_2





What does BVA focus on?

- It focuses on the boundary of the input space to identify test cases
- The rationale behind this is that errors tend to occur near the extreme values of an input variable
 - Many times when a system is tested the function result is “off by one”



What is the basic idea?

- To use input variable values at their...
 - Minimum
 - Just above the minimum
 - A nominal value
 - Just below their maximum
 - At their maximum



The “single fault” assumption

- Failures are only rarely the result of the simultaneous occurrence of two (or more) faults



How does BVA work?

- Boundary value analysis test cases are obtained by
 - holding the values of all but one variable at their nominal values, and
 - letting that variable assume its extreme values i.e.
 - Minimum
 - Just above the minimum
 - Nominal
 - Just below the maximum
 - Maximum

Example: BVA test cases for a two-variable function

$\langle X_{1nom}, X_{2min} \rangle$

$\langle X_{1nom}, X_{2min+} \rangle$

$\langle X_{1nom}, X_{2nom} \rangle$

$\langle X_{1nom}, X_{2max-} \rangle$

$\langle X_{1nom}, X_{2max} \rangle$

$\langle X_{1min}, X_{2nom} \rangle$

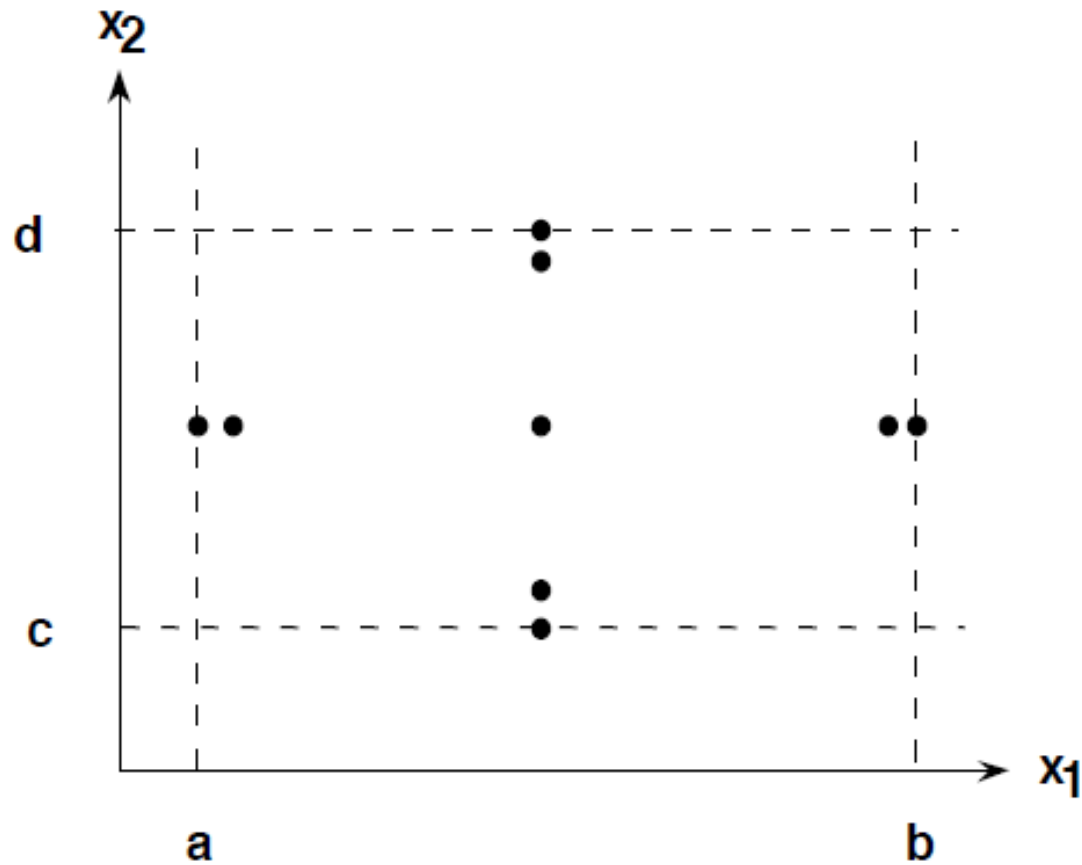
$\langle X_{1min+}, X_{2nom} \rangle$

$\langle X_{1nom}, X_{2nom} \rangle$

$\langle X_{1max-}, X_{2nom} \rangle$

$\langle X_{1max}, X_{2nom} \rangle$

BVA test cases for x_1 and x_2





In-class activity

- Let's apply BVA to the
 - Adder program
 - Input domain: 2 integers (2-digits each)
 - Triangle problem
 - Input domain: 3 sides (values 1-200 each)



Limitations

- Boundary value analysis works well when the program is a function of several independent variables that represent bounded physical quantities
 - Physical boundaries can be extremely important
 - Airport in Phoenix shut down
 - Air temperature was 122 degrees
 - Instruments could only accept up to 120 degrees
- It won't work for the *NextDate* program because
 - dependencies exist among the *month, day* and *year* variables
- It does not work well for logical variables
 - Customer's PIN in ATM, transaction type
- It does not work well for Boolean variables
 - Boolean variables lend themselves to *decision table-based* testing (we will discuss later)



How can BVA be generalized?

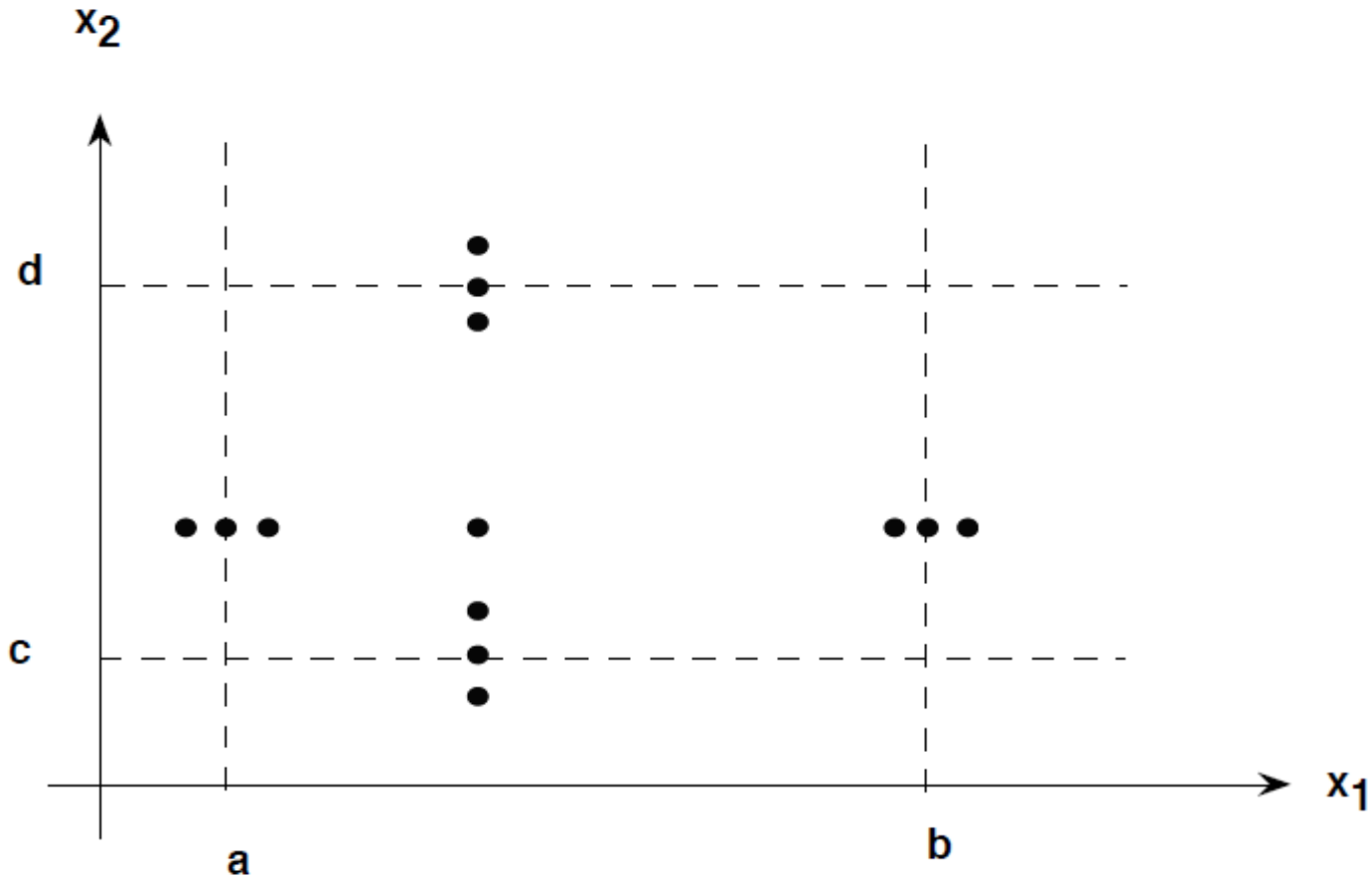
- It can be generalized in 2 ways:
 - By the number of variables
 - By the number of ranges
- Generalizing the number of variables is easy
 - Function of n variables, we hold all but one at the nominal values and let remaining variable assume min, min+, nom, max-, and max
 - It makes $4n+1$ test cases



Robustness testing

- A simple extension to boundary value analysis
- Add two more values per variable
 - Slightly greater than the maximum
 - Slightly less than the minimum
- What is the expected output?
 - Hopefully error message, system recovers

Robust testing: test cases for x_1 and x_2





In-class activity

- Let's apply robust testing to the
 - Adder program
 - Input domain: 2 integers (2-digits each)
 - Triangle problem
 - Input domain: 3 sides (values 1-200 each)



Worst case testing

- Rejects the single fault assumption and tests all combinations of values
- Instead of $5n$ test cases, we have 5^n
- Often leads to a large number of test cases with low bug-finding power
 - Usually better to apply special value testing (i.e. test cases based on the tester's intuition)
- Best application for worst-case testing when
 - physical variables have numerous interactions
 - failure of the function is extremely costly
 - Use of automated testing tools



Special value testing

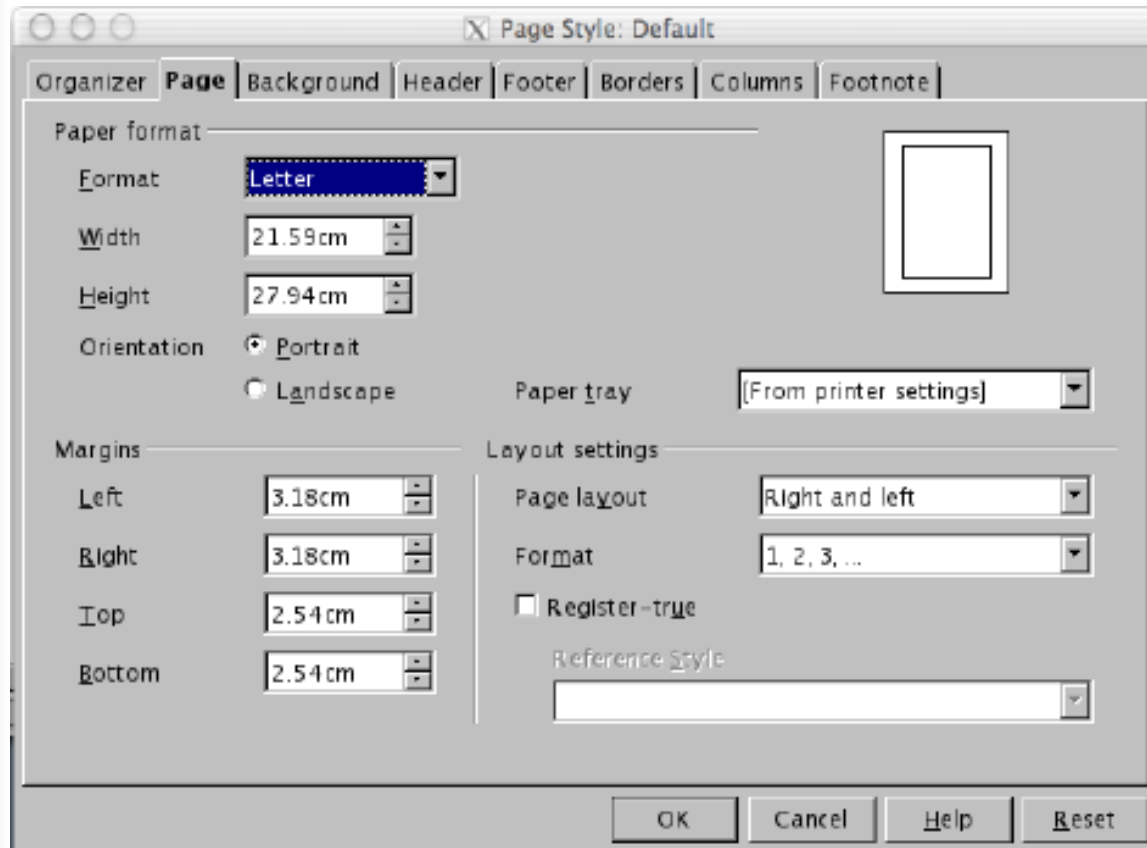
- Most widely practiced form of functional testing
- Most intuitive and least uniform
- Occurs when a tester uses his/her domain knowledge, experience with similar programs, and information about “soft spots” to devise test cases
 - Also called “ad hoc testing” or “seat-of-the-pants” testing
 - No guidelines used other than best engineering judgment
 - Can be very useful, often more effective in revealing error results



Random testing

- Besides always choosing min, max, min+....
 - Use a random number generator to pick test case values
 - Avoids biases in testing

In class activity



- Do a domain analysis on page width and height
 - BVA
 - Robust testing
 - Special value
- Assume the spec mentions that
 - Width values between 10cm and 60cm should be handled
 - Height values between 20cm and 100cm
- Can you identify any weaknesses of BVA?