

September 19, 2019

1 model

$$f_1(x) = 3\exp(-30(x - 0.3)^2) + \exp(-50(x - 0.7)^2)$$

$$Y|\beta, \sigma^2, \gamma \sim N(Z\Gamma\beta, \sigma^2 I)$$

$$\sigma^2 \sim \text{Inverse} - \text{Gamma}(A, B)$$

$$\beta_j \sim N(0, \sigma_\beta^2)$$

$$\gamma_j \sim \text{Bernoulli}(\rho)$$

$$\rho \sim \text{Beta}(C, D)$$

2 Empirical Bayes

We need to calculate the likelihood $p(y|\rho)$ and select the hyper parameter ρ which maximize the likelihood

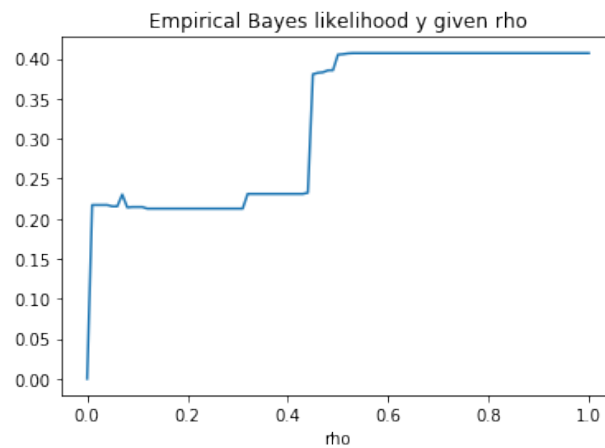


Figure 1: likelihood by changing of ρ

3 ρ with Beta prior

Sensitivity of variation family need to be checked. When sample size is small ($n=800$) variational distribution is sensitive by changing the distribution of $\rho \sim \text{Beta}(\alpha, \beta)$, but if sample size has enough size ($n=8000$) result is more robust.

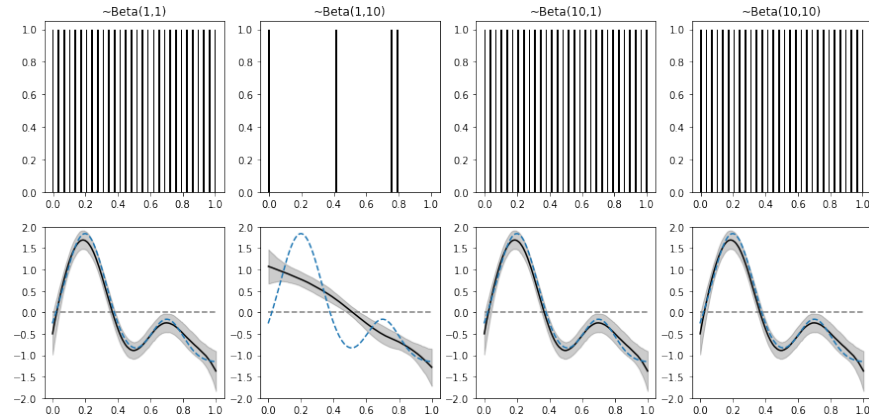


Figure 2: number of obs : 800 and posterior mean of ρ is 0.97, 0.12, 0.98, 0.8

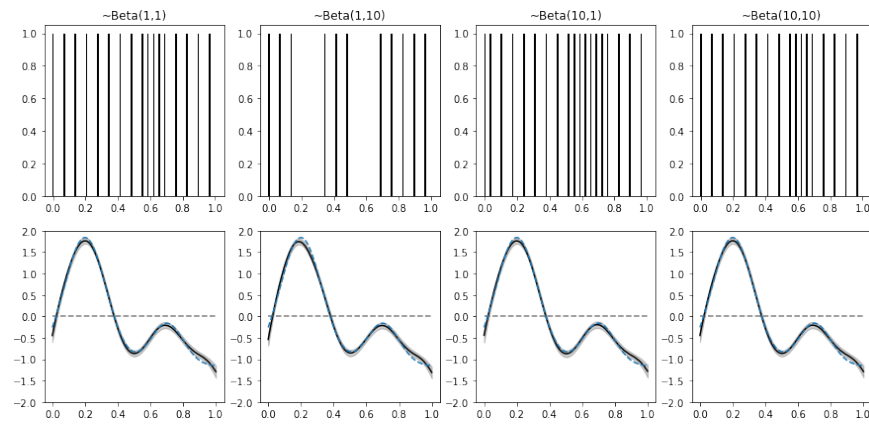


Figure 3: number of obs : 8000 and posterior mean of ρ is 0.56, 0.29, 0.70, 0.54