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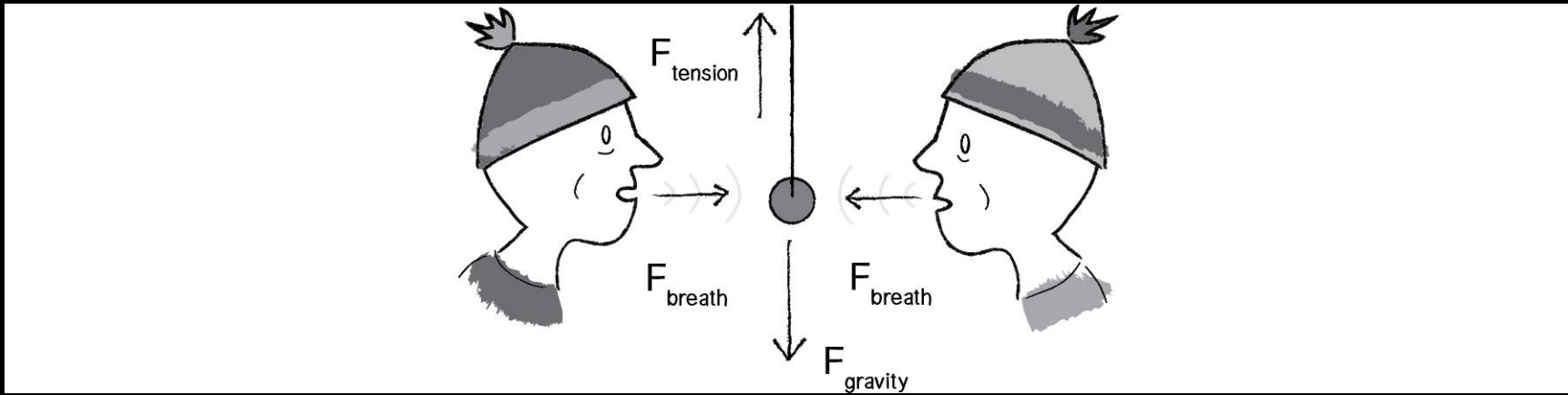
Forces and Newton's Laws of Motion

- A force is a vector that causes an object with mass to accelerate.
- 힘은 질량 있는 객체가 가속도를 갖게 하는 벡터.

Newton's First Law

- 다른 힘의 영향을 받지 않는다면 가만히 있는 물체는 계속 가만히 있고, 움직이는 물체는 같은 속도와 방향으로 계속 움직인다.

Newton's First Law



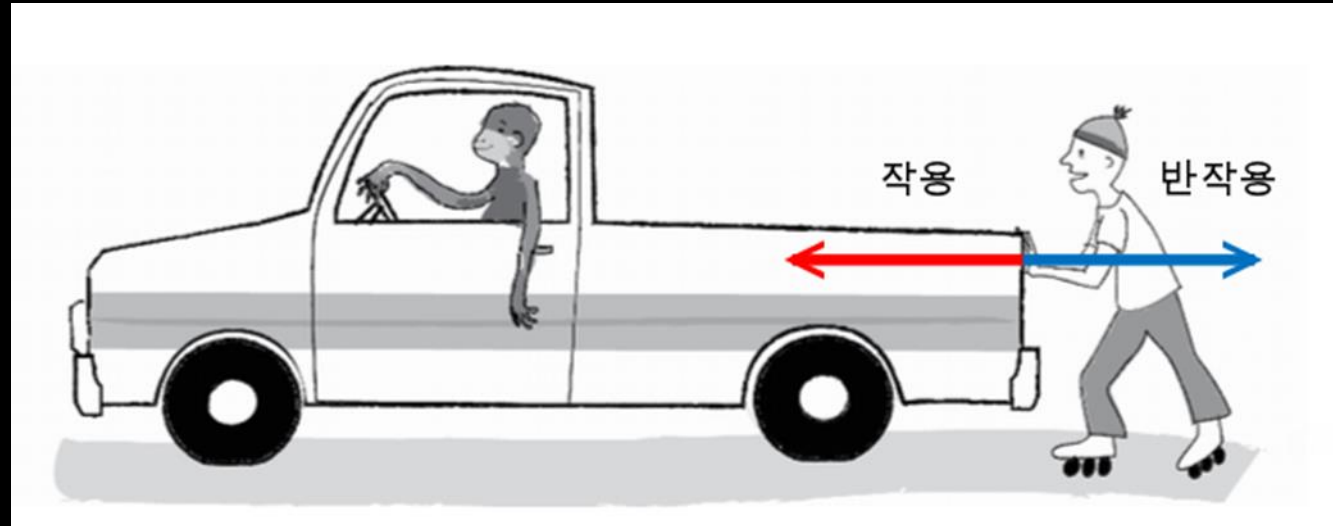
Newton's First Law

- An object's PVector velocity will remain constant if it is in a state of equilibrium.

Newton's Third Law

- 어떤 물체에 힘을 주면 반대 방향으로도 같은 힘이 일어난다.
- Forces always occur in pairs.
- The two forces are of equal strength, but in opposite directions.

Newton's Third Law



Newton's Third Law

- A라는 물체가 B라는 물체에 PVector f라는 힘을 준다면 B도 A에 PVector.mult(f,-1)만큼의 힘을 주어야 한다.

Newton's Second Law

- Force equals mass times acceleration.

$$F = ma$$



$$a = F/m$$

Newton's Second Law

- The acceleration of an object is equal to force.
- Location is adjusted by velocity, and velocity by acceleration.
- Acceleration was where it all began.
- Force is truly where it all begins.

Newton's Second Law

```
class Mover {  
    PVector location;  
    PVector velocity;  
    PVector acceleration;  
}
```

Newton's Second Law

```
void applyForce(PVector force) {  
    //Newton's second law at its simplest.  
    //But this function has problem.  
    //What's that?  
    acceleration = force;  
}
```

```
mover.applyForce(wind);  
mover.applyForce(gravity);
```

Force Accumulation

- `velocity.add(acceleration);`

```
void applyForce(PVector force) {  
    acceleration.add(force);  
}
```

Force Accumulation

```
if (mousePressed) {  
    PVector wind = new PVector(0.5,0);  
    mover.applyForce(wind);  
}
```

Since we're adding all the forces together at any given moment, we have to make sure that we clear acceleration (i.e. set it to zero) before each time `update()` is called.

Force Accumulation

```
void update() {  
    velocity.add(acceleration);  
    location.add(velocity);  
    acceleration.mult(0); // 가속도를 0으로  
}
```

Dealing with Mass

```
class Mover {  
    PVector location;  
    PVector velocity;  
    PVector acceleration;  
    float mass;  
}
```


Dealing with Mass

```
Mover() {  
    location = new  
        PVector(random(width),random(height));  
    velocity = new PVector(0,0);  
    acceleration = new PVector(0,0);  
    mass = 10.0;  
}
```

Creating Forces

- Make up a force.
- Model a force

Gravity on Earth and Modeling a Force

```
for (int i = 0; i < movers.length; i++) {  
  
    PVector wind = new PVector(0.001,0);  
    float m = movers[i].mass;  
        //Scaling gravity by mass to be more accurate  
    PVector gravity = new PVector(0,0.1*m);  
    movers[i].applyForce(wind);  
    movers[i].applyForce(gravity);  
  
    movers[i].update();  
    movers[i].display();  
    movers[i].checkEdges();  
}
```

Reference

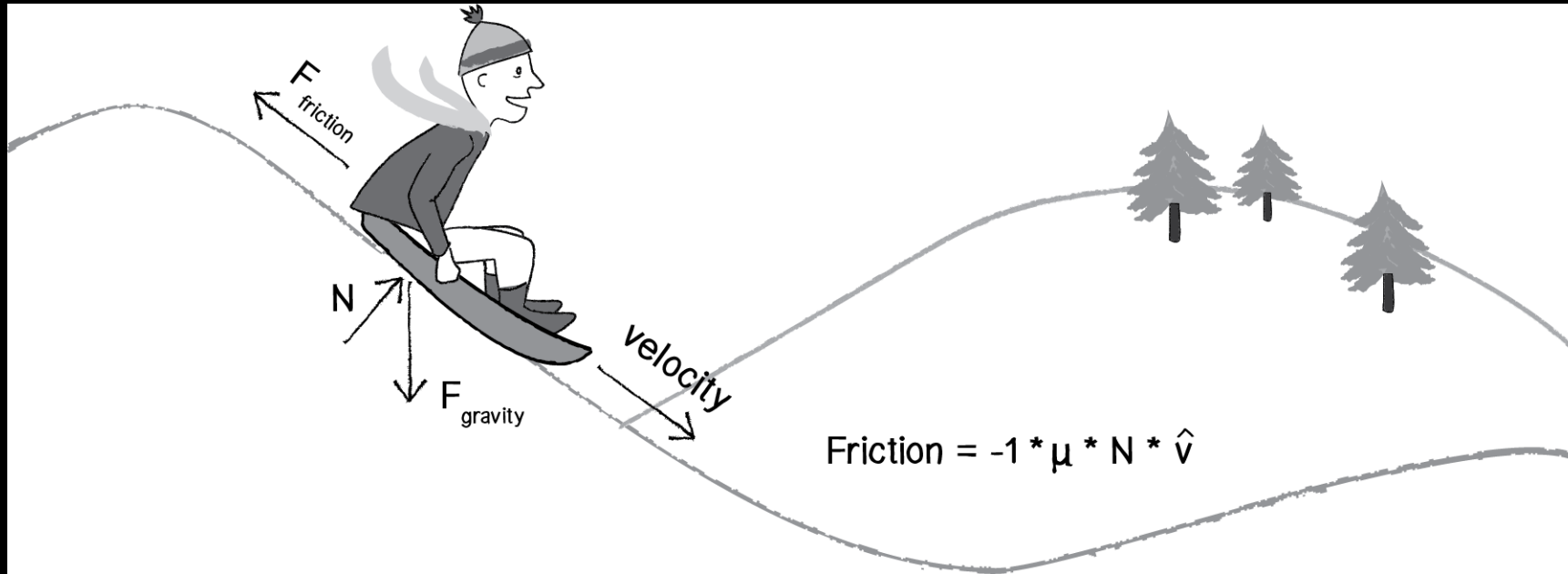
```
void applyForce(PVector force) {  
  //Making a copy of the PVector before //using it!  
  PVector f = force.get();  
  f.div(mass);  
  acceleration.add(f);  
}
```

Test

Friction

- 마찰력
 - 흠어지는 힘으로 물체가 움직일 때 전체 에너지를 감소 시키는 힘
- static friction
- kinetic friction

Friction



Friction

```
PVector friction = velocity.get();  
friction.normalize();  
friction.mult(-1);
```

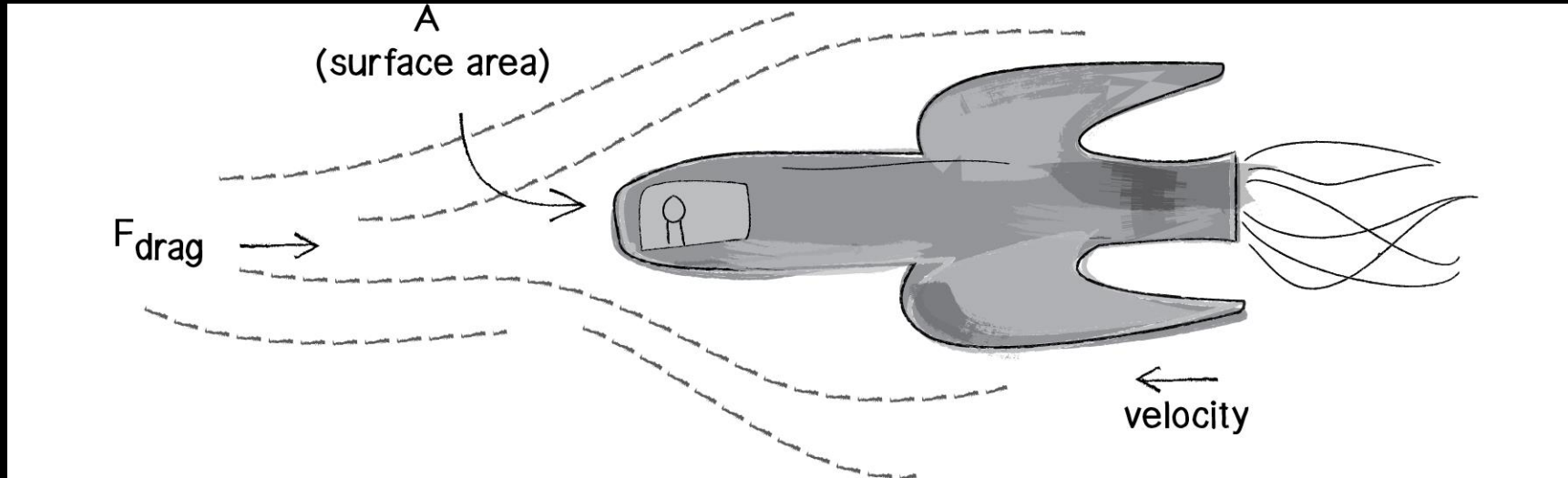

Friction

- $\mu * N$
- μ : coefficient of friction
- N : Normal force

```
float c = 0.01;  
float normal = 1;  
float frictionMag = c*normal;
```

```
PVector friction = velocity.get();  
friction.mult(-1);  
friction.normalize();  
friction.mult(frictionMag);
```

Air and Fluid Resistance



Air and Fluid Resistance

$$F_d = -\frac{1}{2}\rho v^2 A C_d \hat{v}$$

F_d = 저항력

ρ = 액체 밀도

v = 객체의 속도

A = 액체와 닿는 앞쪽 면적

C_d = 저항 계수

\hat{v} = 속도의 방향 단위 벡터

Air and Fluid Resistance

magnitude is speed squared * coefficient of drag

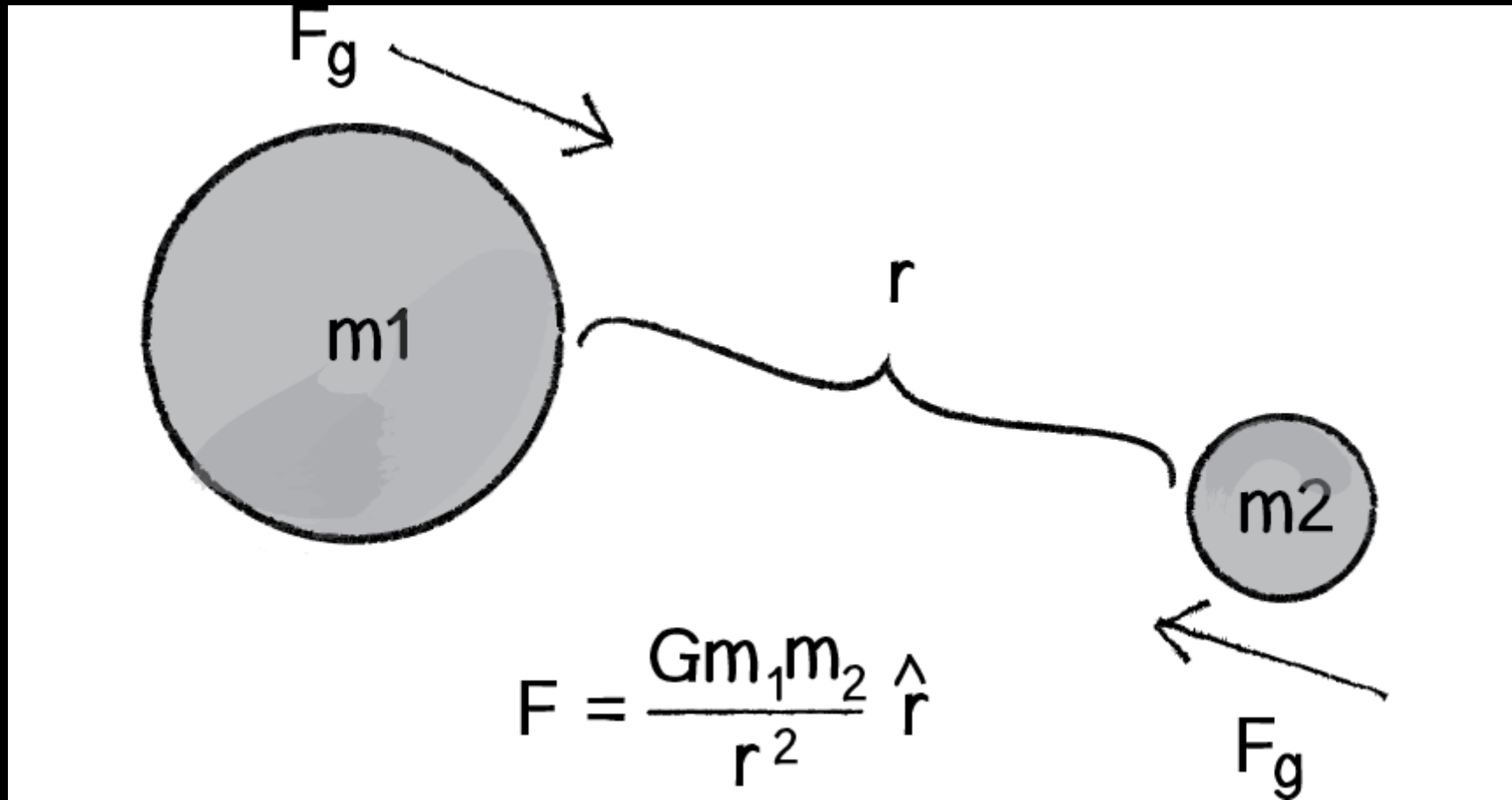
$$F_{\text{drag}} = \overbrace{\|v\|^2 * c_d}^{\text{magnitude is speed squared * coefficient of drag}} * \underbrace{\hat{v} * -1}_{\text{direction is opposite of } v \text{ (velocity)}}$$

direction is opposite of v (velocity)

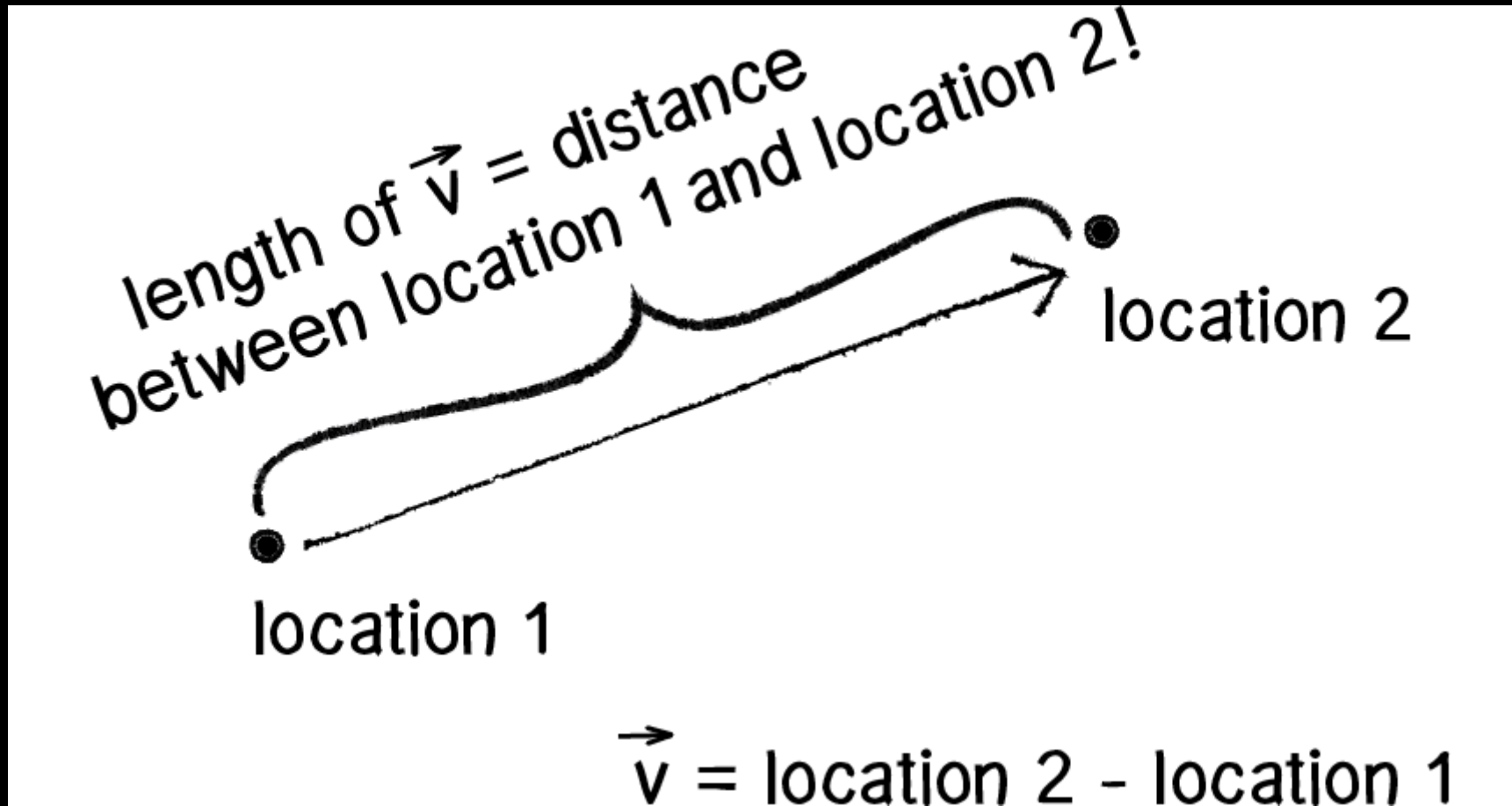
Air and Fluid Resistance

```
float c = 0.1;  
float speed = v.mag();  
float dragMagnitude = c * speed * speed;  
PVector drag = velocity.get();  
drag.mult(-1);  
drag.normalize();  
drag.mult(dragMagnitude);
```

Gravitational Attraction



Gravitational Attraction



Gravitational Attraction

```
PVector force = PVector.sub(location1,location2);
```

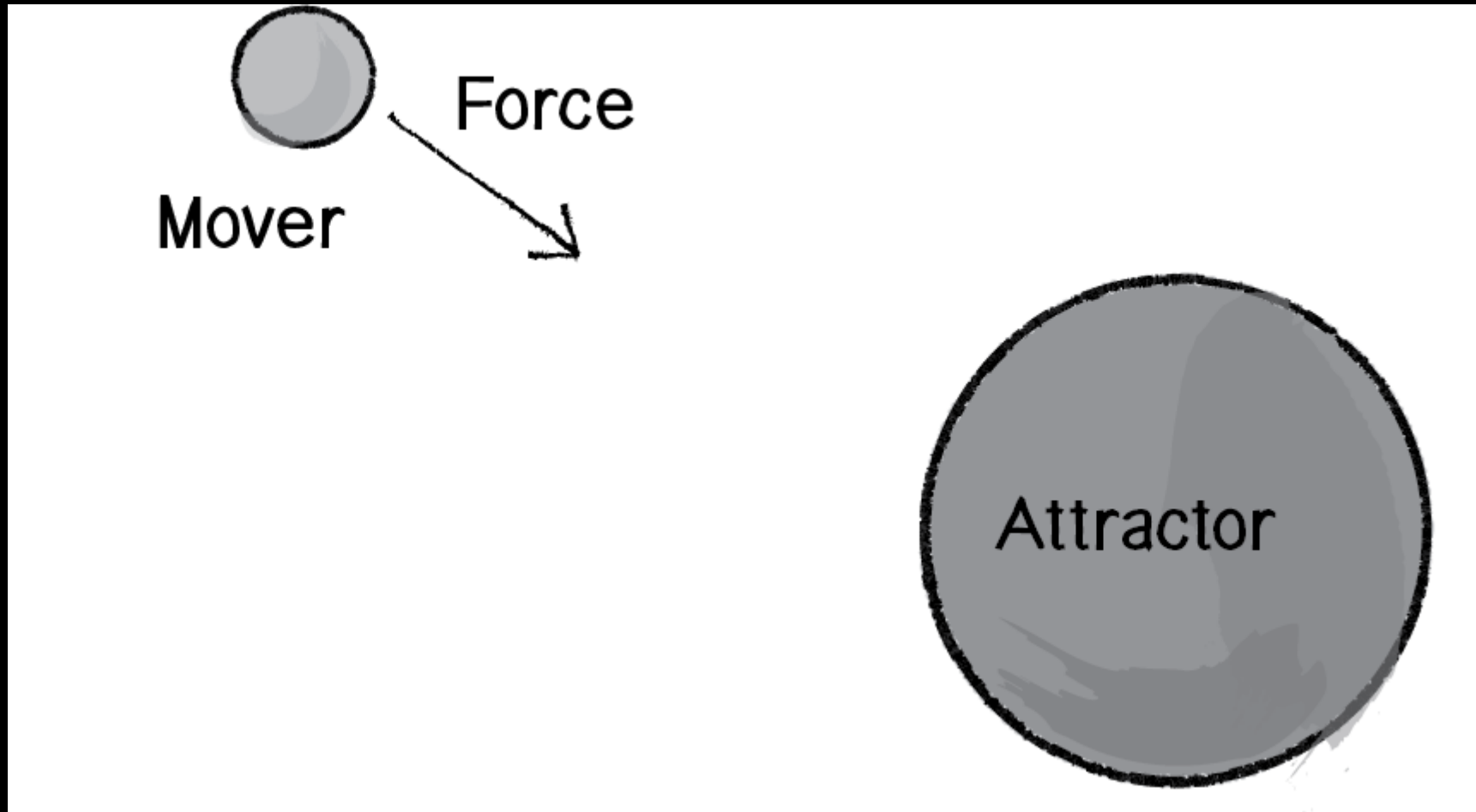
```
float distance = force.magnitude();
```

```
float m = (G * mass1 * mass2) / (distance * distance);
```

```
force.normalize();
```

```
force.mult(m);
```


Gravitational Attraction



Attractor

- Attractor is simple object that doesn't move.
- We just need a mass and a location.

Break...

- CU..