

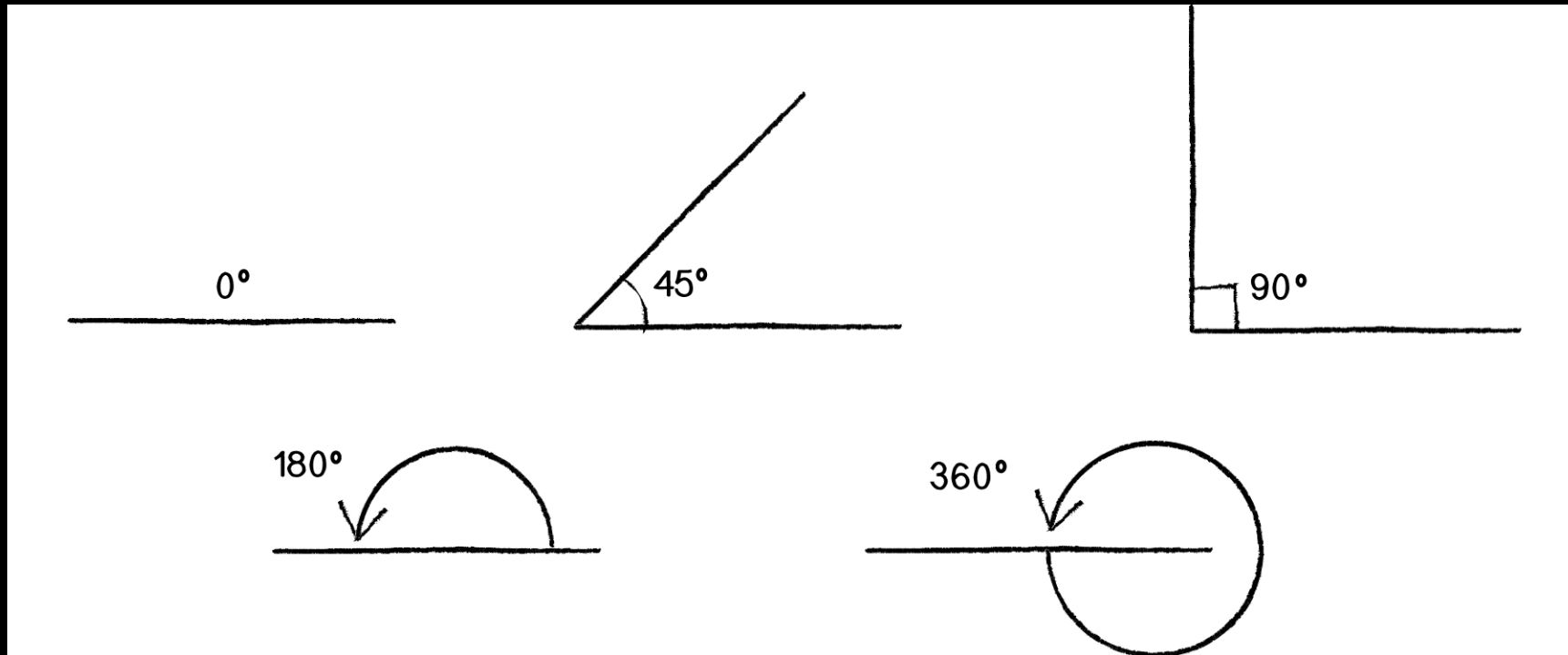
20170923 Ajou2

Jonghwa Park

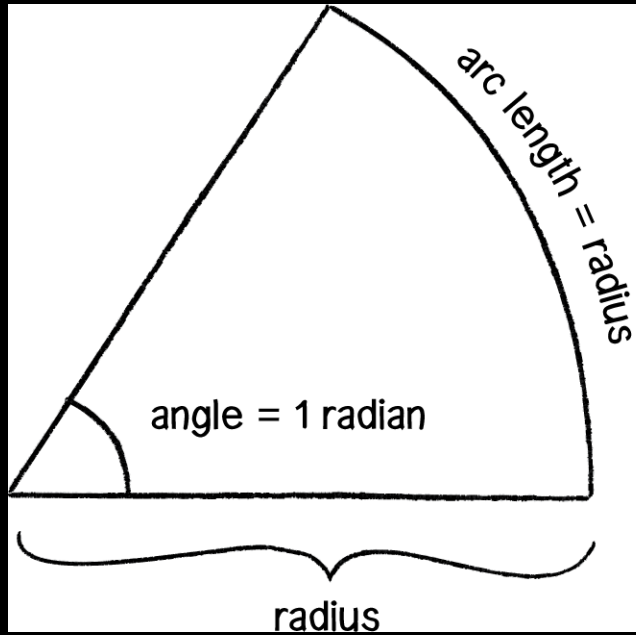
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GYEONGGI SCIENCE HIGH SCHOOL

# Angles



# Angles



# Angular Motion

- $\text{location} = \text{location} + \text{velocity}$
- $\text{velocity} = \text{velocity} + \text{acceleration}$
- $\text{angle} = \text{angle} + \text{angular velocity}$
- $\text{angular velocity} = \text{angular velocity} + \text{angular acceleration}$

# Angular Motion

```
float angle = 0;  
float aVelocity = 0;  
float aAcceleration = 0.0001;
```

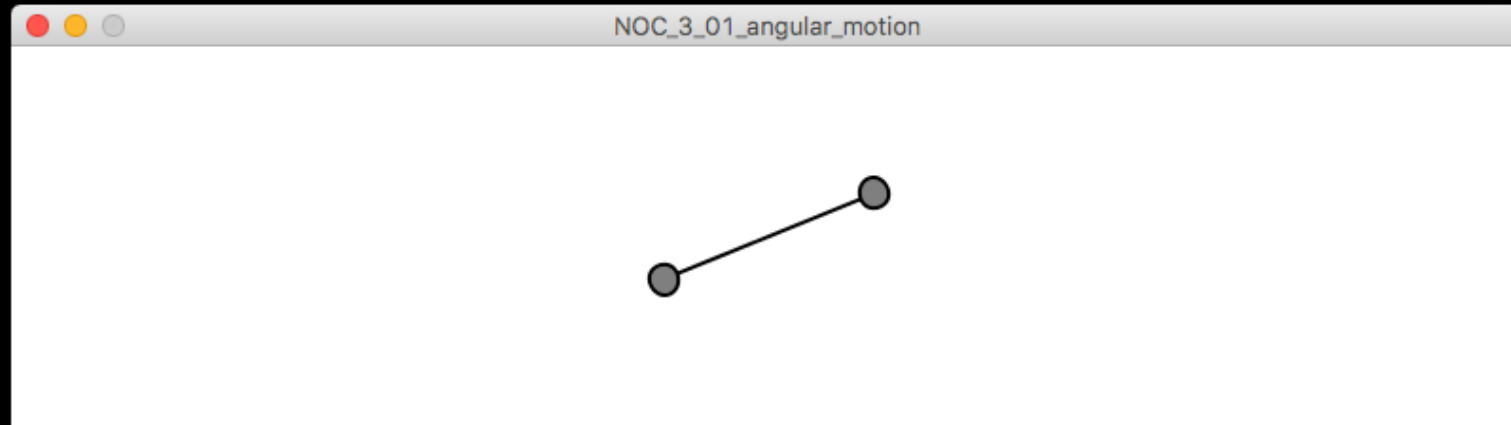
```
void setup() {  
  size(800, 200);  
  smooth();  
}
```

```
void draw() {  
  background(255);
```

```
  
  fill(127);  
  stroke(0);
```

```
  
  translate(width/2, height/2);  
  rectMode(CENTER);  
  rotate(angle);  
  stroke(0);  
  strokeWeight(2);  
  fill(127);  
  line(-60, 0, 60, 0);  
  ellipse(60, 0, 16, 16);  
  ellipse(-60, 0, 16, 16);
```

# Angular Motion



# Angular Motion - Mover

```
void update() {  
    velocity.add(acceleration);  
    location.add(velocity);  
    aVelocity += aAcceleration;  
    angle += aVelocity;  
    acceleration.mult(0);  
}
```

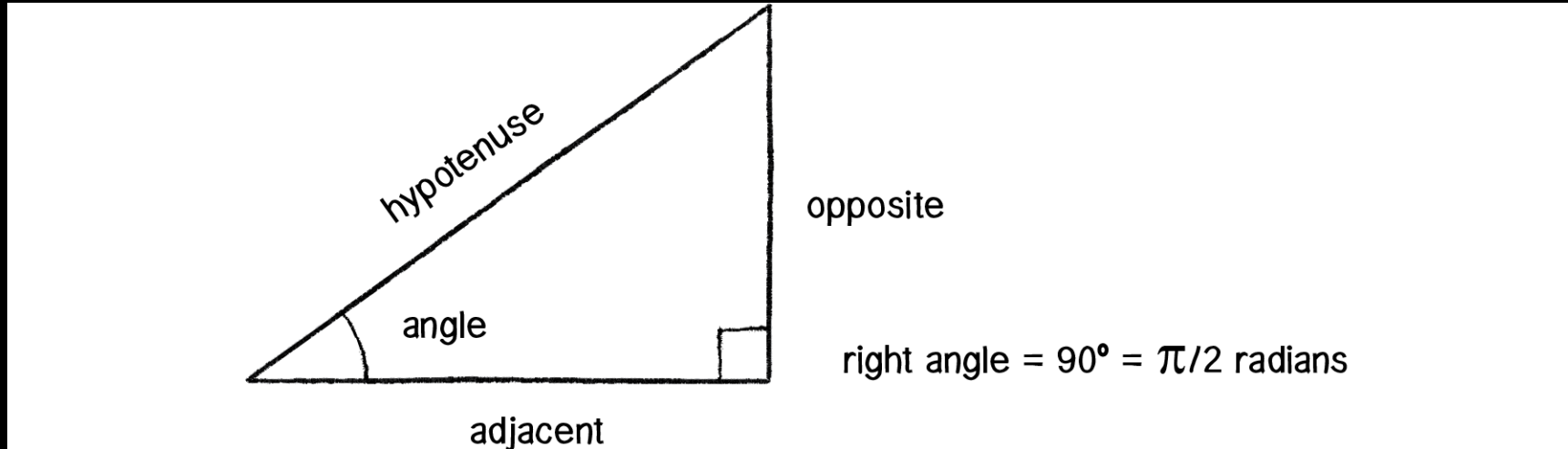
# Angular Motion - Mover

```
void display() {  
    stroke(0);  
    fill(175,200);  
    rectMode(CENTER);  
    pushMatrix();  
        translate(location.x,location.y);  
        rotate(angle);  
        rect(0,0,mass*16,mass*16);  
    popMatrix();  
}
```

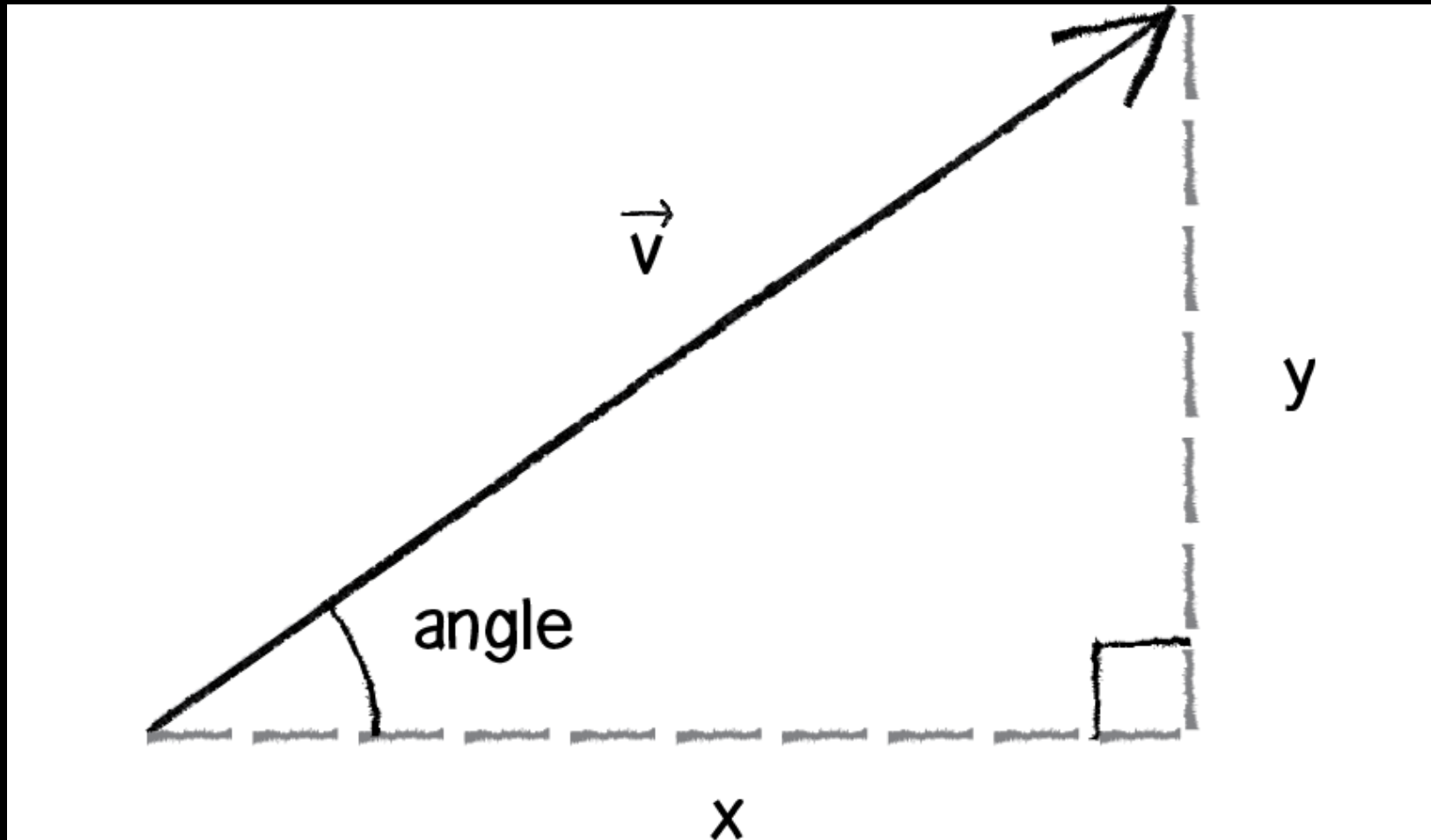


# Canon Example

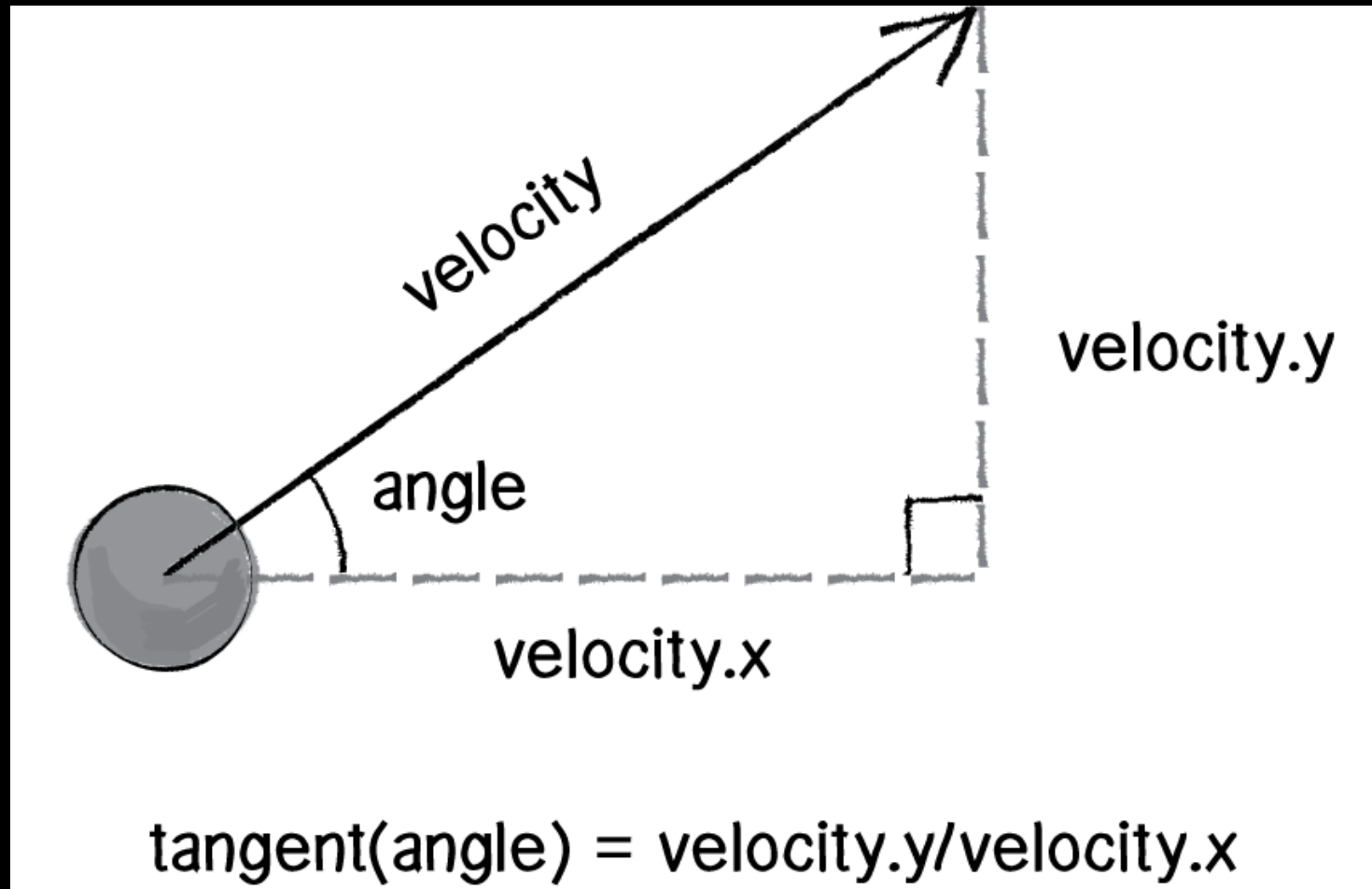
# Trigonometry



# Trigonometry



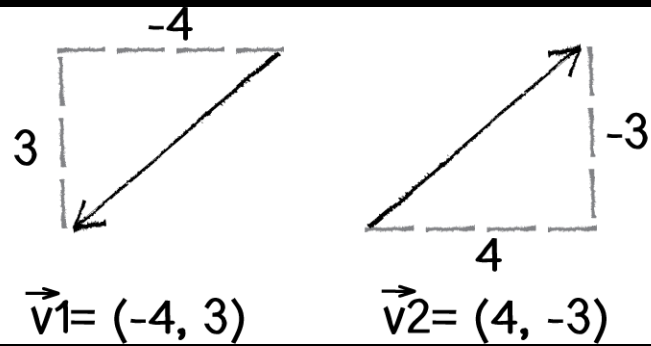
# Pointing in the Direction of Movement



# Pointing in the Direction of Movement

```
void display() {  
    //Solve for angle by using atan().  
    float angle = atan(velocity.y/velocity.x);  
    stroke(0);  
    fill(175);  
    pushMatrix();  
        rectMode(CENTER);  
        translate(location.x,location.y);  
        //Rotate according to that angle.  
        rotate(angle);  
        rect(0,0,30,10);  
    popMatrix();  
}
```

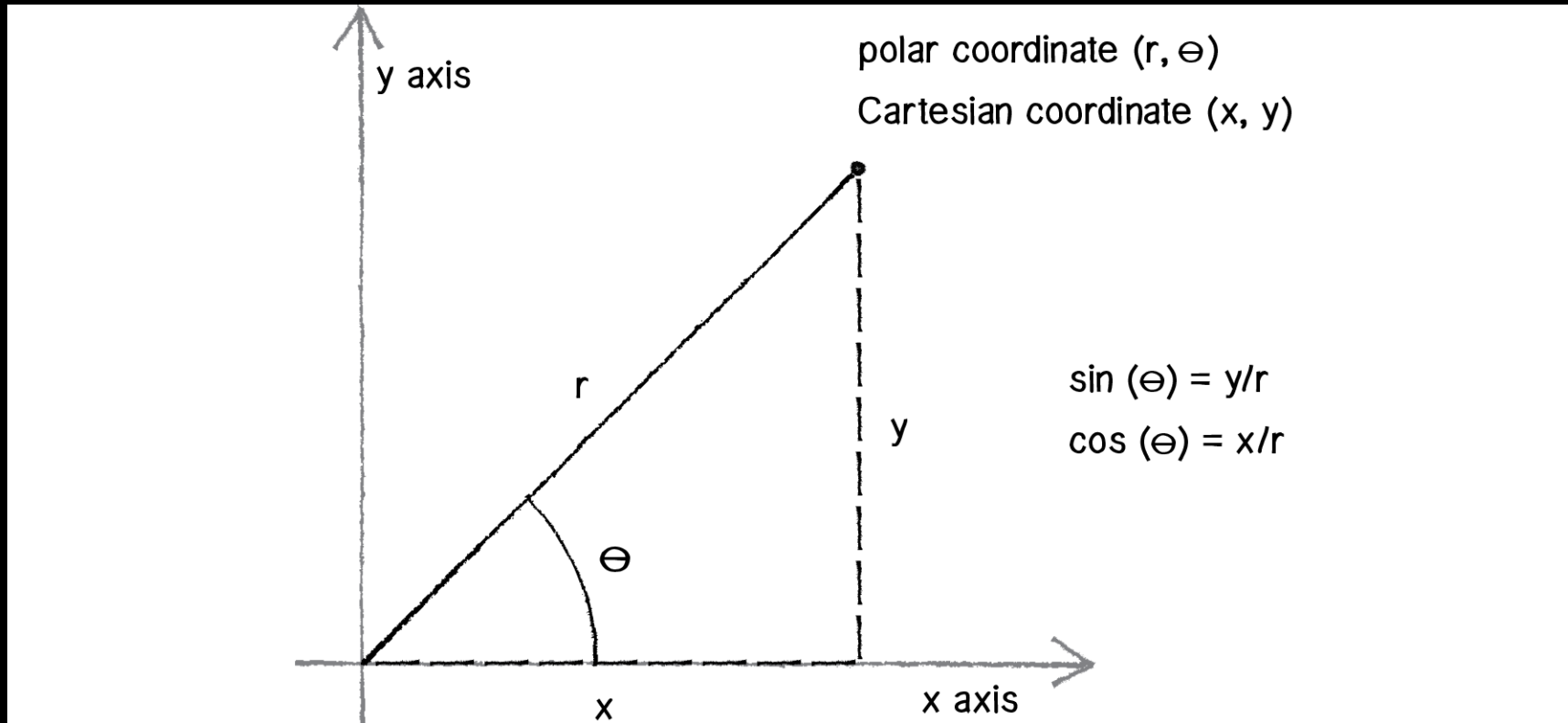
# Actan Problem



# Actan2 or Heading()

```
void display() {  
    //Using atan2() to account for all possible directions  
    float angle = atan2(velocity.y,velocity.x);  
    //angle = velocity.heading();  
    stroke(0);  
    fill(175);  
    pushMatrix();  
        rectMode(CENTER);  
        translate(location.x,location.y);  
        //Rotate according to that angle.  
        rotate(angle);  
        rect(0,0,30,10);  
    popMatrix();  
}
```

# Polar vs Cartesian Coordinates





# Polar to Cartesian

```
float r = 75;
```

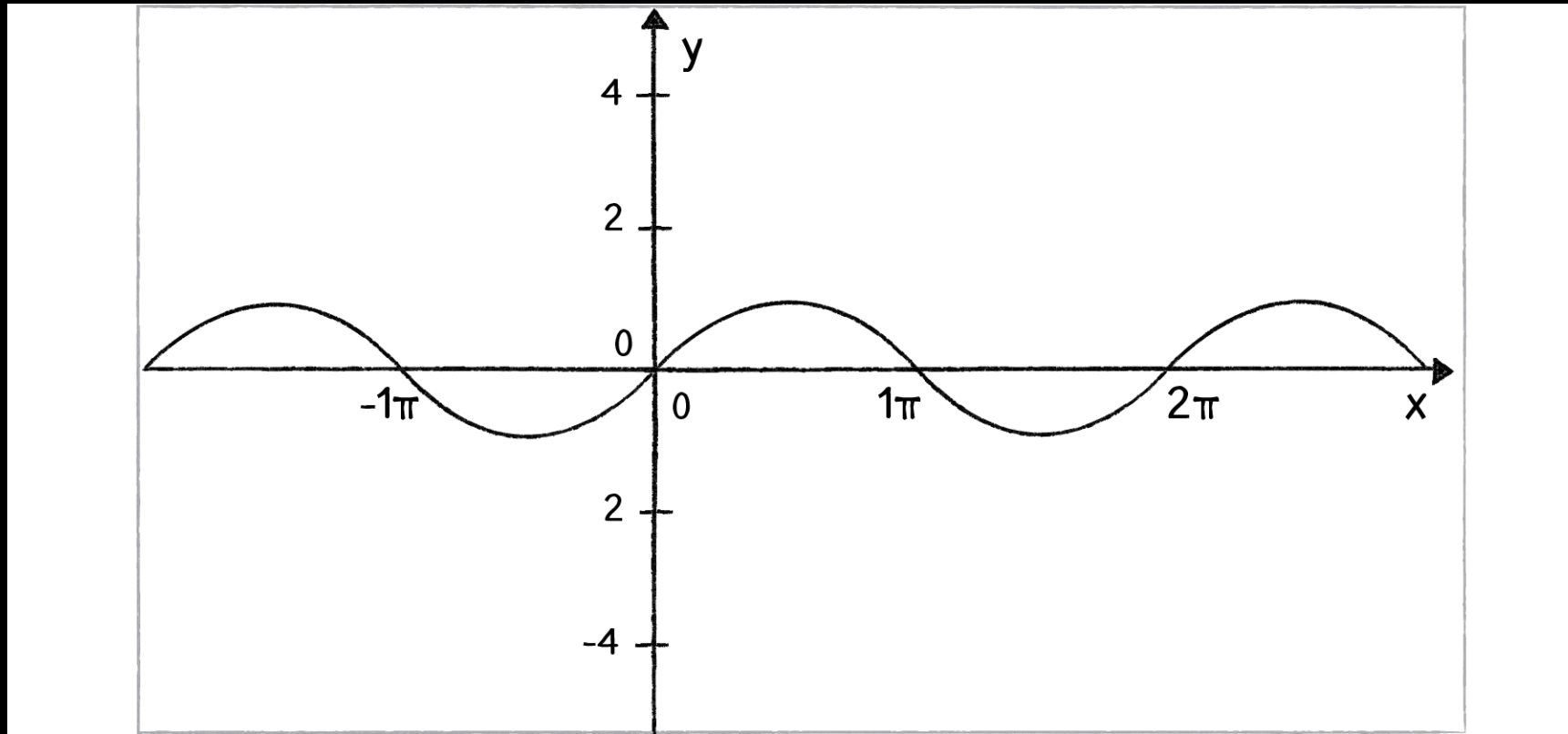
```
float theta = PI / 4;
```

```
//Converting from polar (r,theta) to //Cartesian (x,y)
```

```
float x = r * cos(theta);
```

```
float y = r * sin(theta);
```

# Oscillation Amplitude and Period



# Simple Harmonic Motion

```
void setup() {  
  size(640,360);  
}  
void draw() {  
  background(255);  
  float period = 120;  
  float amplitude = 100;  
  //Calculating horizontal location according to the formula for simple harmonic motion  
  float x = amplitude * cos(TWO_PI * frameCount/ period);  
  stroke(0);  
  fill(175);  
  translate(width/2,height/2);  
  line(0,0,x,0);  
  ellipse(x,0,20,20);  
}
```

# Simple Harmonic Motion

frameCount	frameCount / period	TWO_PI * frameCount / period
0	0	0
60	0.5	PI
120	1	TWO_PI
240	2	2 * TWO_PI (or 4* PI)
etc.		

# Oscillation with Angular Velocity

```
float angle = 0;
float aVelocity= 0.05;
void setup() {
  size(640,360);
}
void draw() {
  background(255);
  float amplitude = 100;
  float x = amplitude * cos(angle);
  //Using the concept of angular velocity to increment an angle variable
  angle += aVelocity;
  ellipseMode(CENTER);
  stroke(0);
  fill(175);
  translate(width/2,height/2);
  line(0,0,x,0);
  ellipse(x,0,20,20);
}
```

# Waves



# Waves

- 여러 개의 원을 나열하고 진동
- `float angle = 0;`
- `float angleVel = 0.2;`
- `float amplitude = 100;`
- 너비를 기준으로 주기를 만들어 보자.

# Waves

```
for (int x = 0; x <= width; x += 24) {
```

```
    1) Calculate the y location according to amplitude  
    the angle.
```

```
    float y = amplitude*sin(angle);
```

```
    2) Draw a circle at the (x,y) location.
```

```
    ellipse(x,y+height/2,48,48);
```

```
    3) Increment the angle according to angular velocity.
```

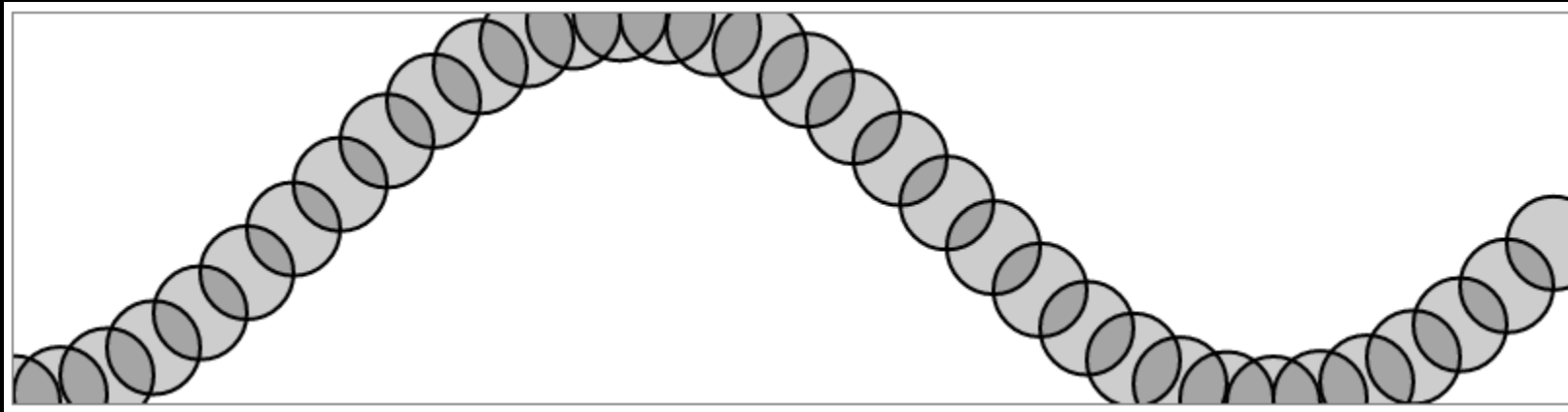
```
    angle += angleVel;
```

```
}
```

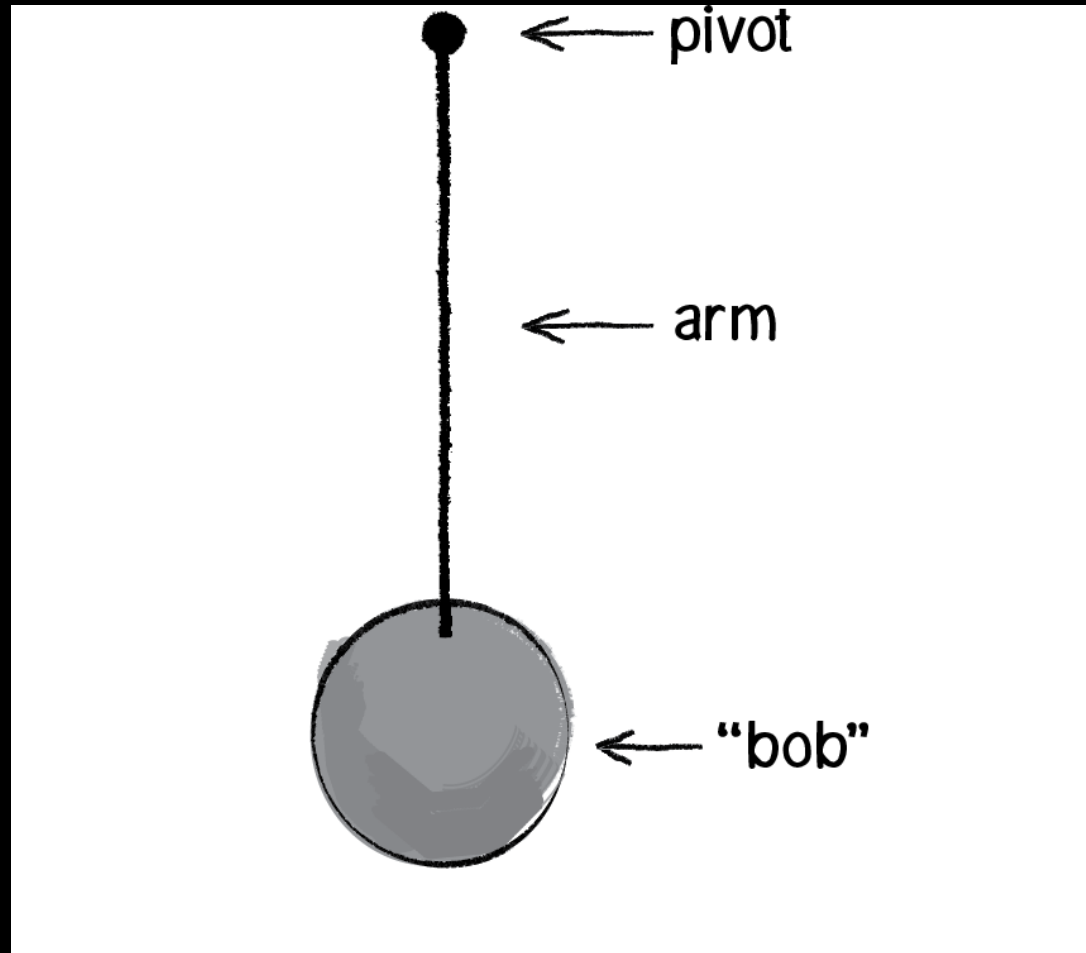
and sine of



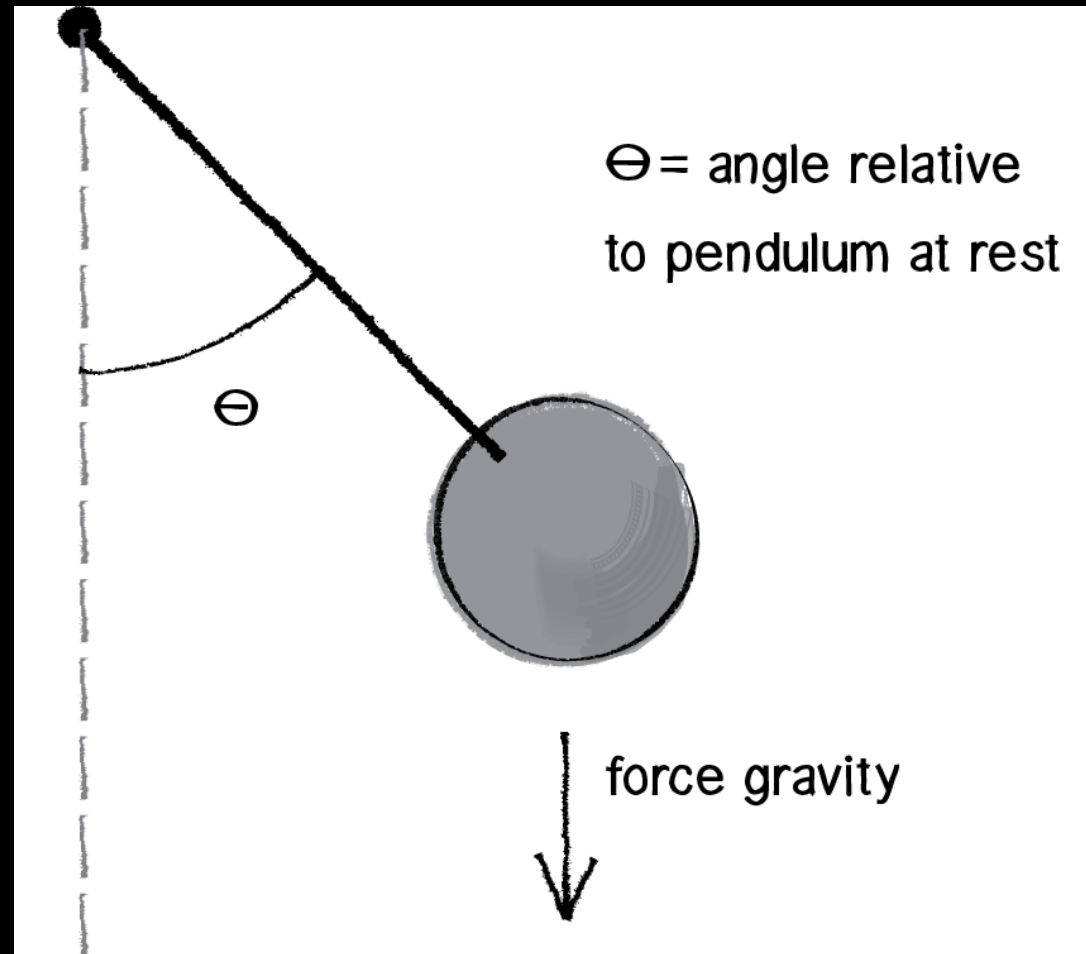
# Moving Waves



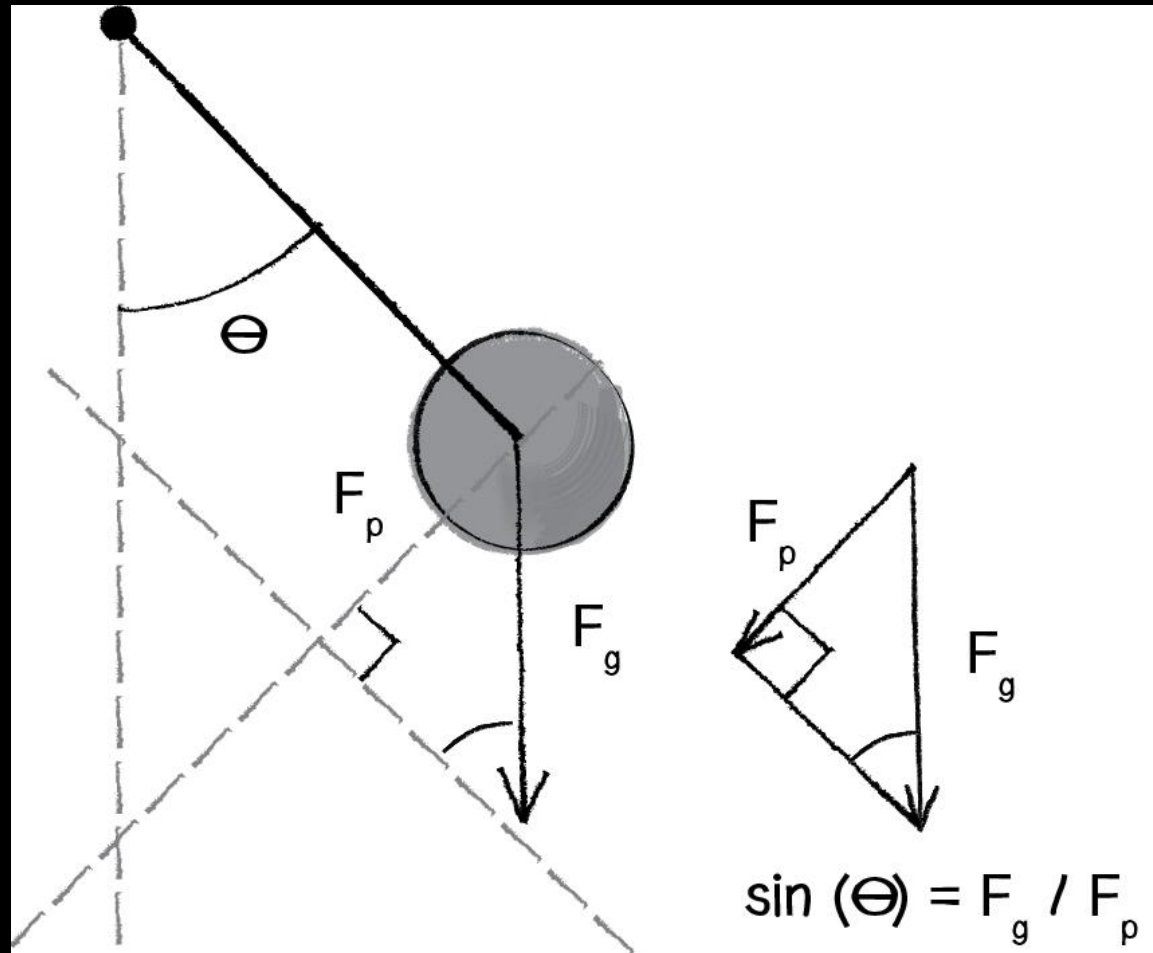
# Trigonometry and Forces: The Pendulum



# Trigonometry and Forces: The Pendulum



# Trigonometry and Forces: The Pendulum



# Trigonometry and Forces: The Pendulum

- $\sin(\theta) = F_p / F_g$
- $F_p = F_g \sin(\theta)$
- pendulum angular acceleration = acceleration due to gravity \*  $\sin(\theta)$
- angular acceleration = gravity \*  $\sin(\theta)$

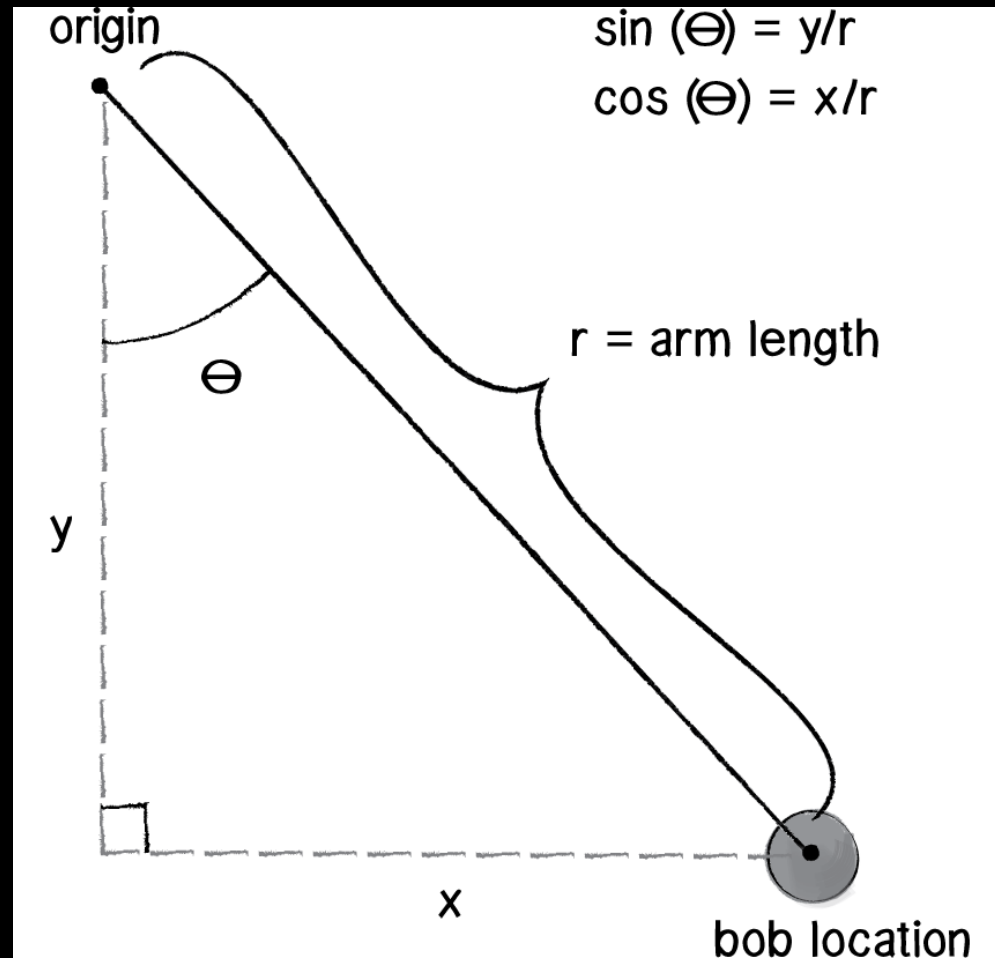
# Pendulum Class

```
class Pendulum {  
    float r;//Length of arm  
    float angle;//Pendulum arm angle  
    float aVelocity;//Angular velocity  
  
    float aAcceleration;//Angular acceleration
```

# Pendulum Class

```
void update() {  
    float gravity = 0.4;  
    aAcceleration= -1 * gravity * sin(angle);  
    aVelocity+= aAcceleration;  
    angle += aVelocity;  
}
```

# Pendulum Class

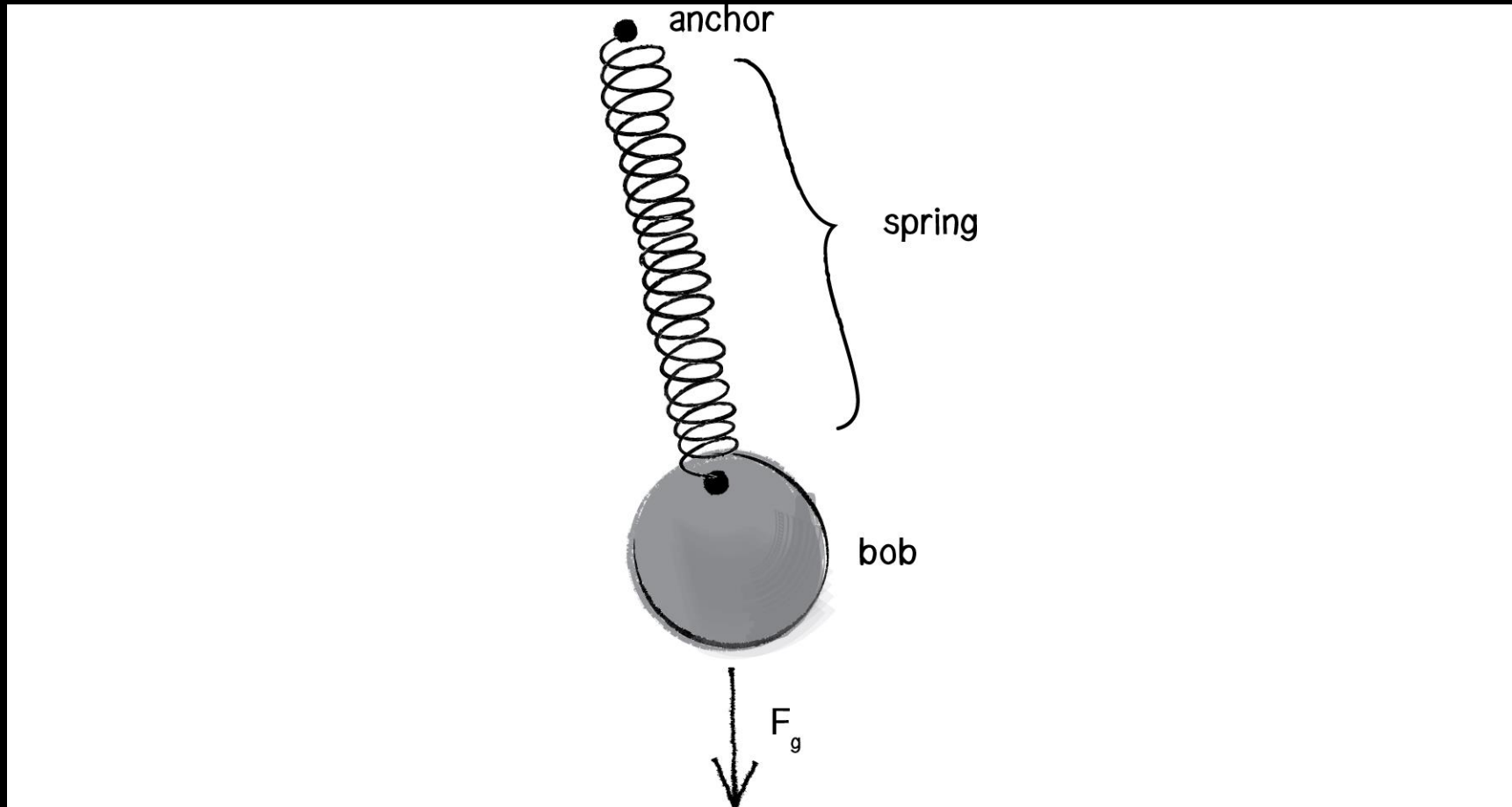




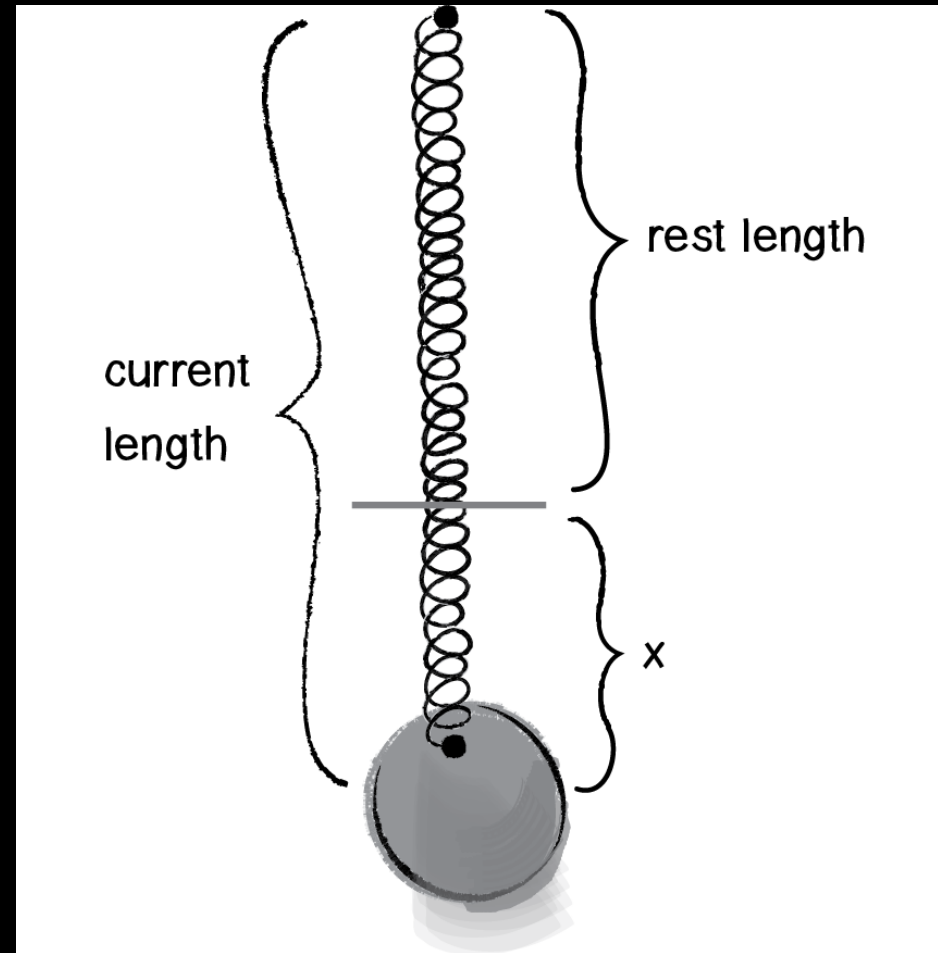
# Pendulum Class

```
PVectororigin = new PVector(100,10);  
float r = 125;  
PVectorlocation = new PVector(r*sin(angle),r*cos(angle));  
location.add(origin);  
aAcceleration= (-1 * G * sin(angle)) / r;
```

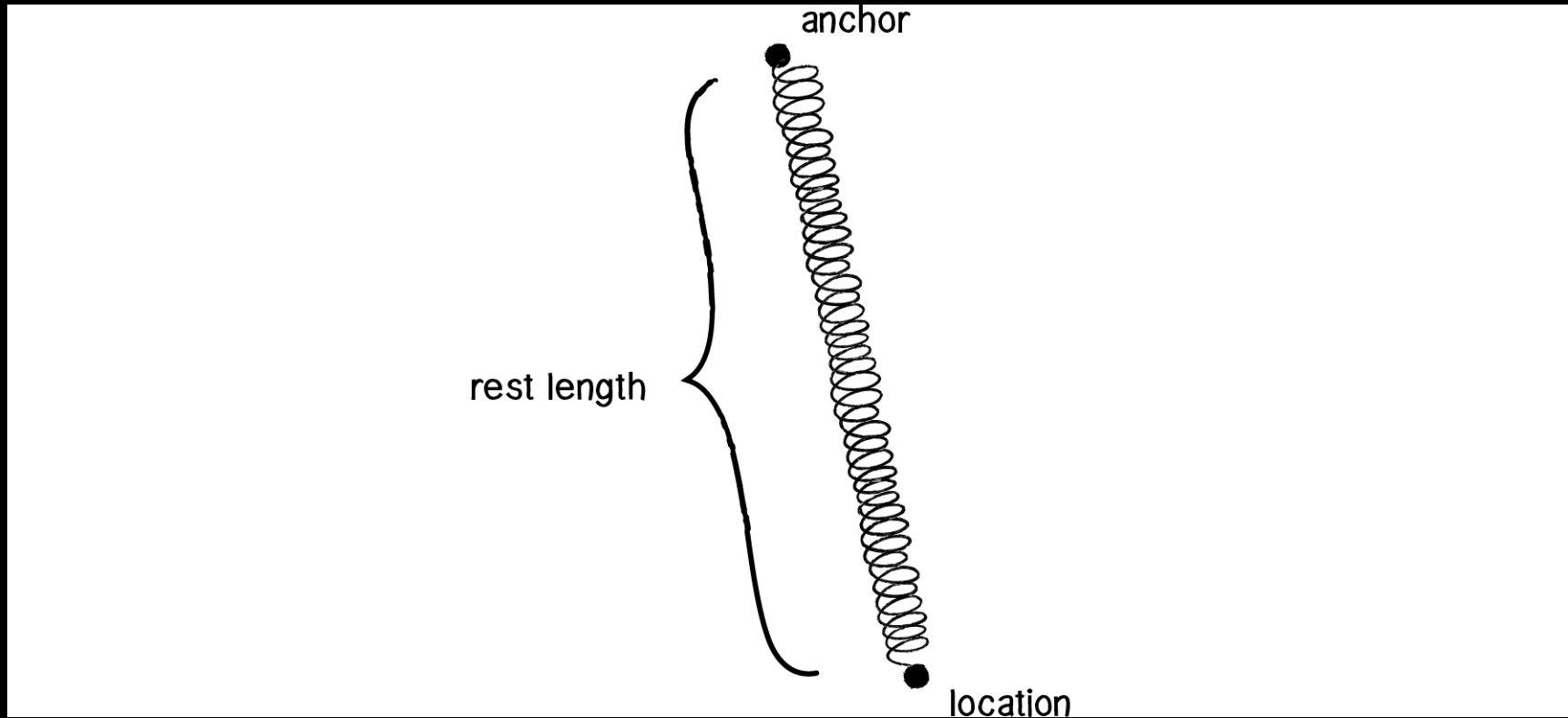
# Spring Forces



Hooke's law :  $F_{\text{spring}} = -k * x$



# Spring Forces



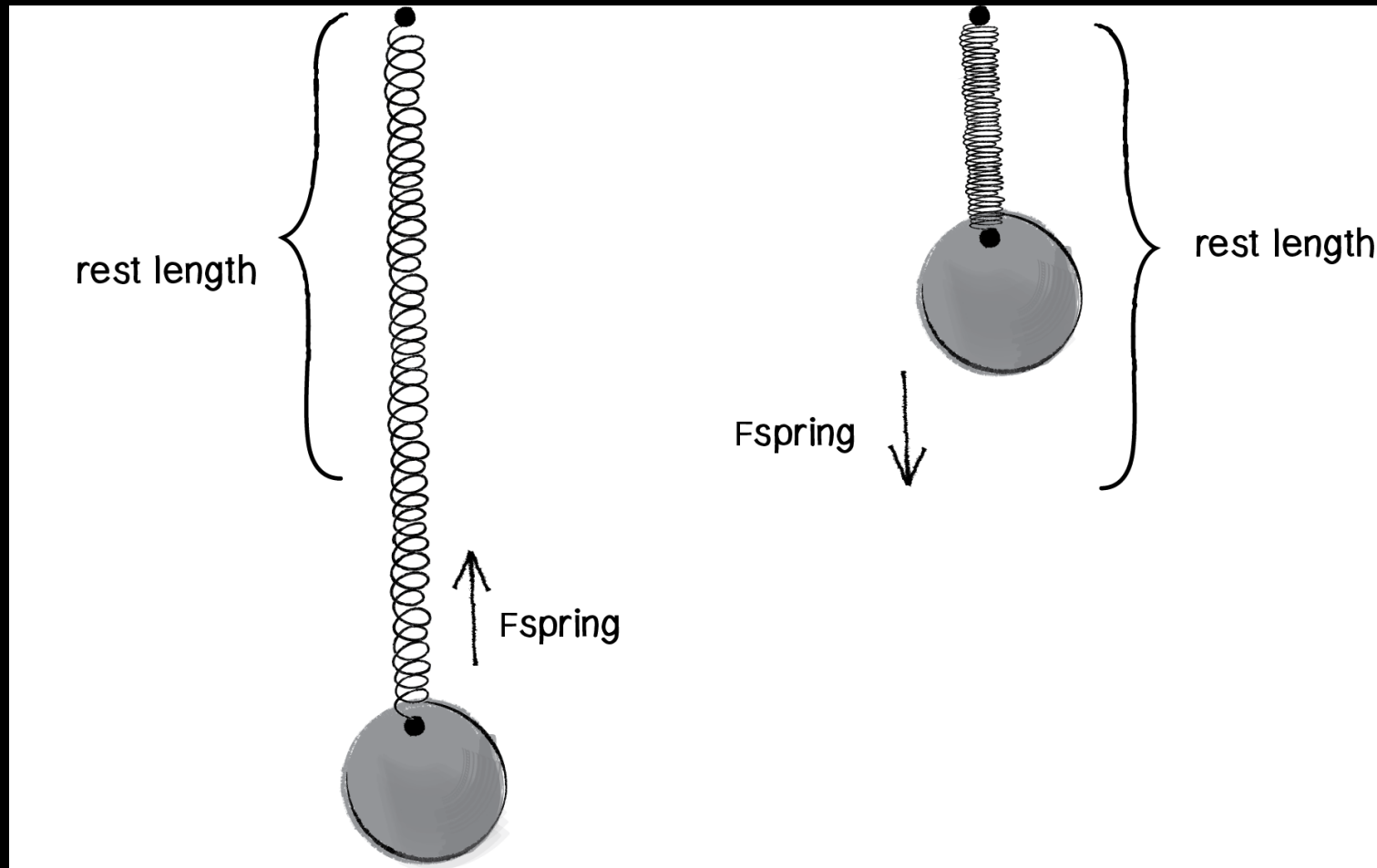
# Spring Forces

- PVector anchor;
- PVector location;
- float restLength;
- float k = 0.1

# Spring Forces

- `PVector rdir= PVector.sub(bob,anchor);`
- `float currentLength= dir.mag();`
- `float x = restLength - currentLength;`

# Spring Forces

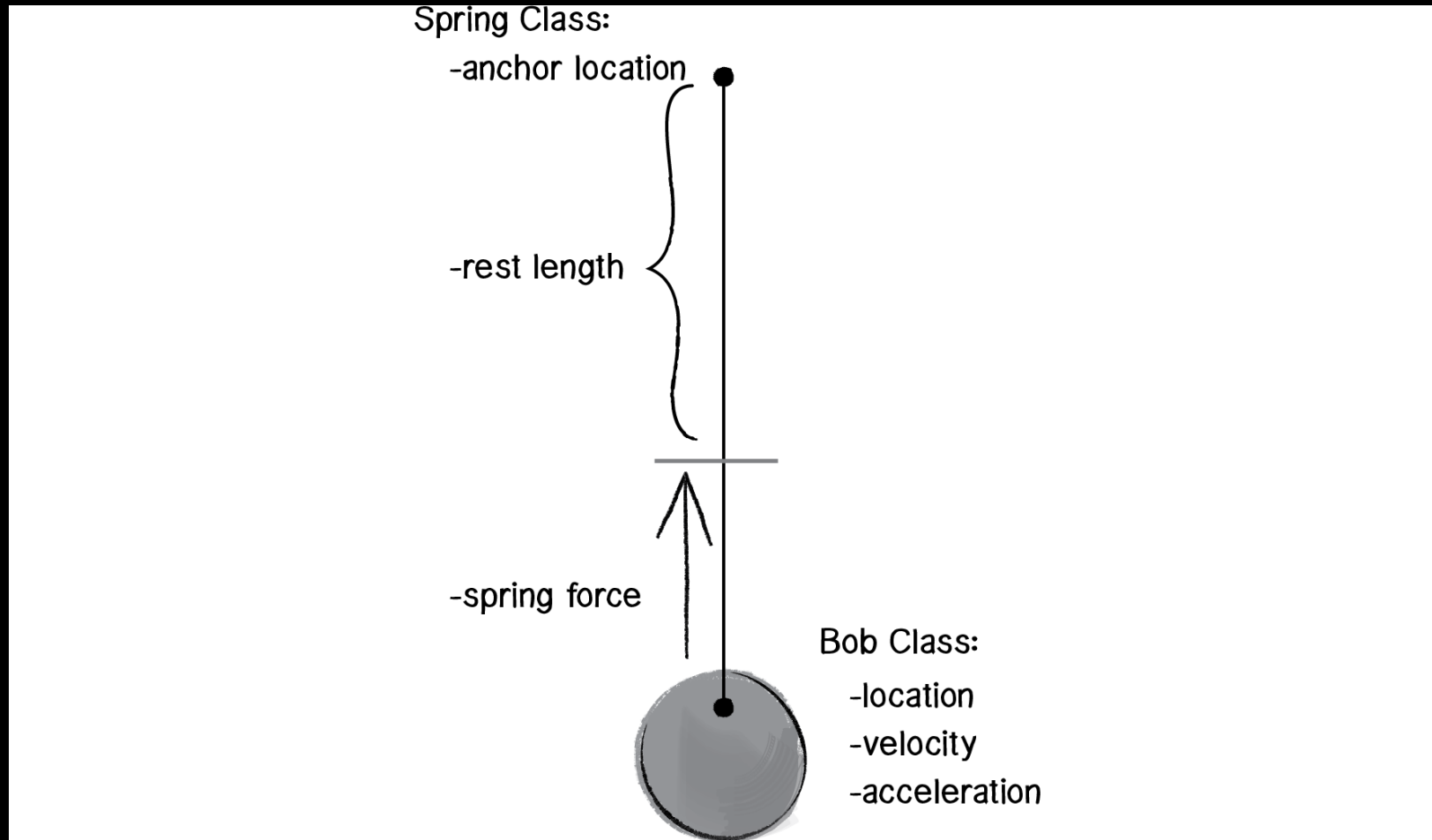


# Spring Forces

```
float k = 0.1;  
PVector force = PVector.sub(bob, anchor);  
float currentLength = dir.mag();  
float x = restLength - currentLength;  
//Direction of spring force (unit vector)  
force.normalize();  
//Putting it together: direction and magnitude!  
force.mult(-1 * k * x);
```



# Spring Class



QA