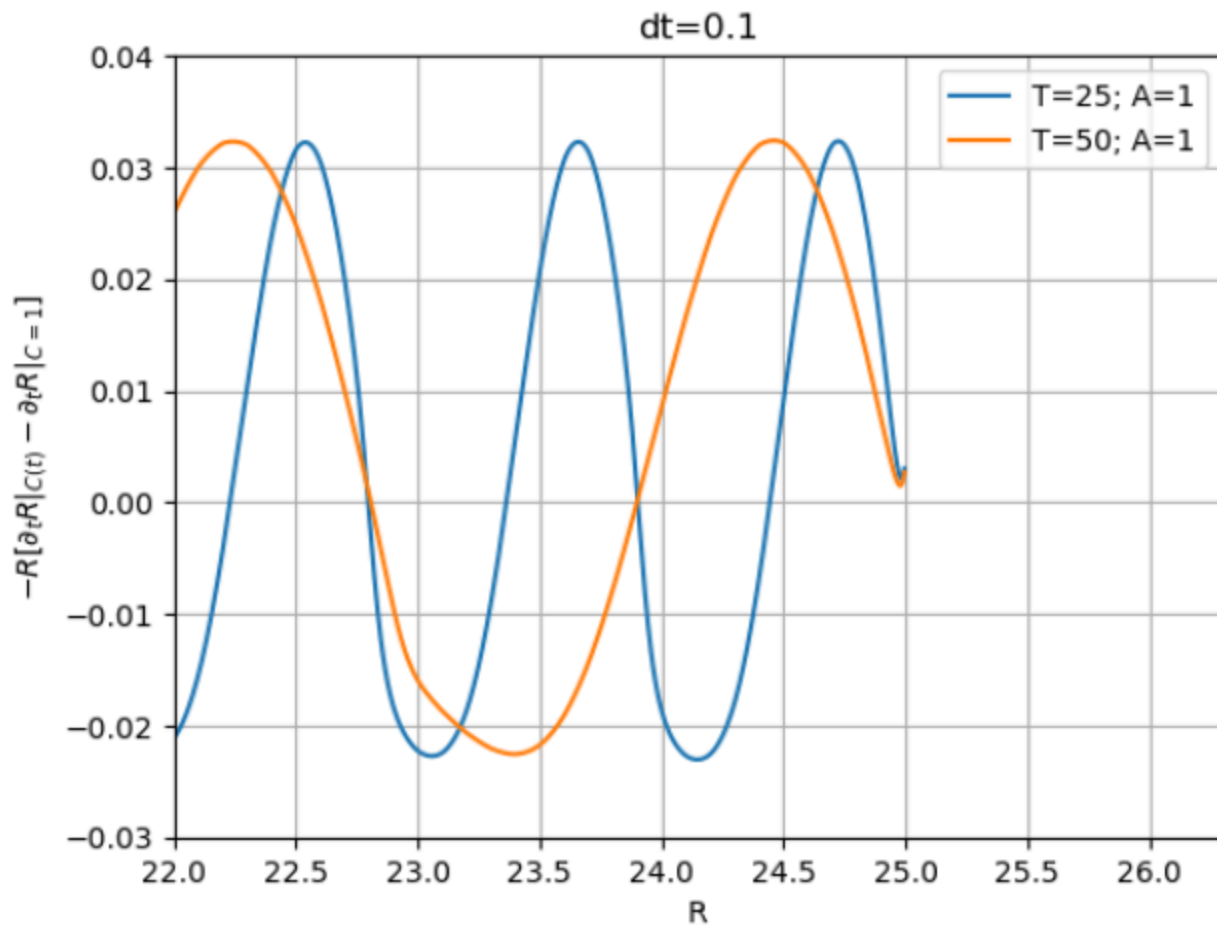


## 2D Slow oscillations ( $A \ll C_0$ ) (Numerical)

### Model-free analysis

Here we seek for the effect of oscillations on the dynamics of a circular domain, by **subtracting data** collected with  $C = 1$  constant to data collected with  $C(t) = 1 + A \sin\left(\frac{2\pi t}{T}\right)$ .

We see an oscillation of this quantity. Is it a **numerical effect**?



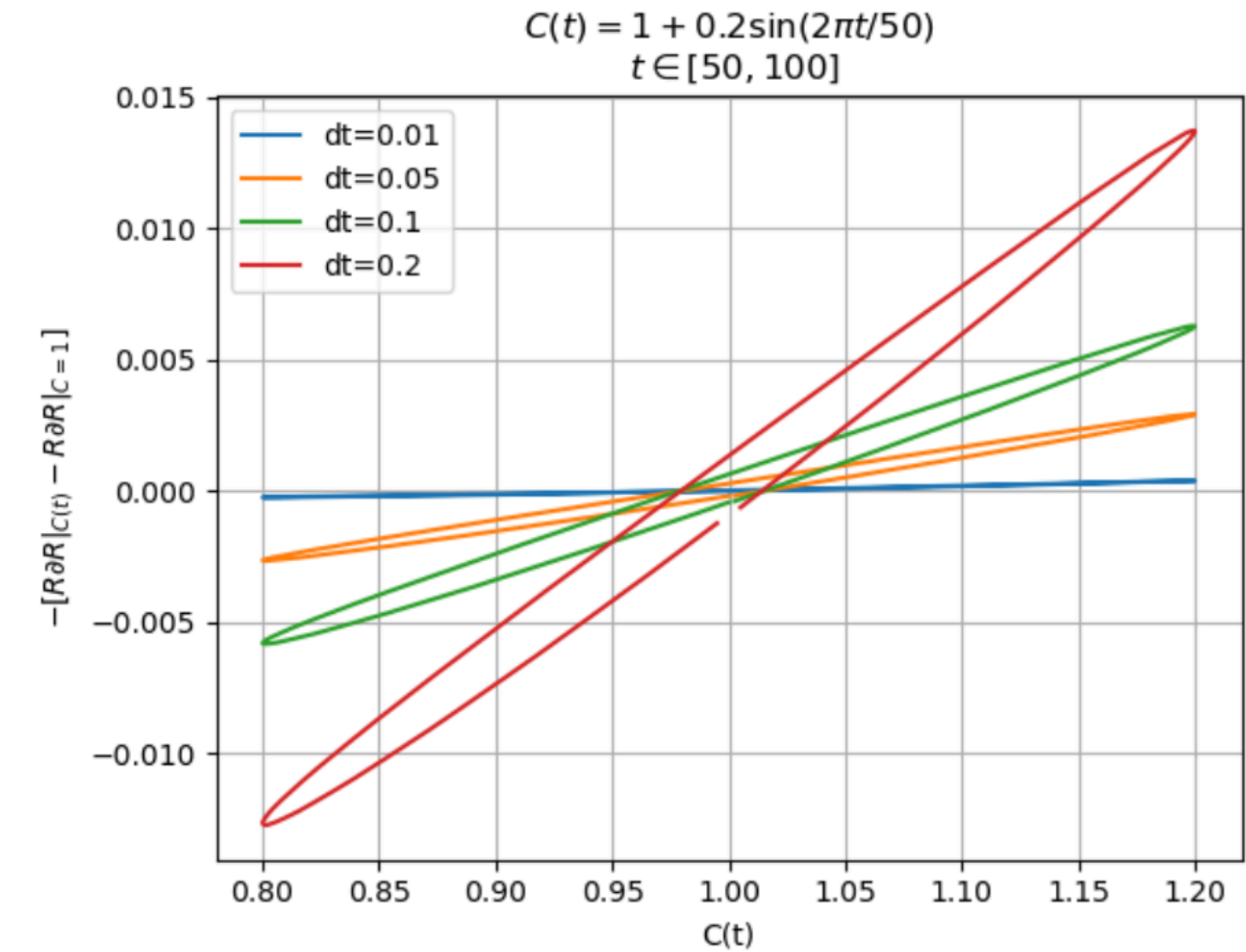
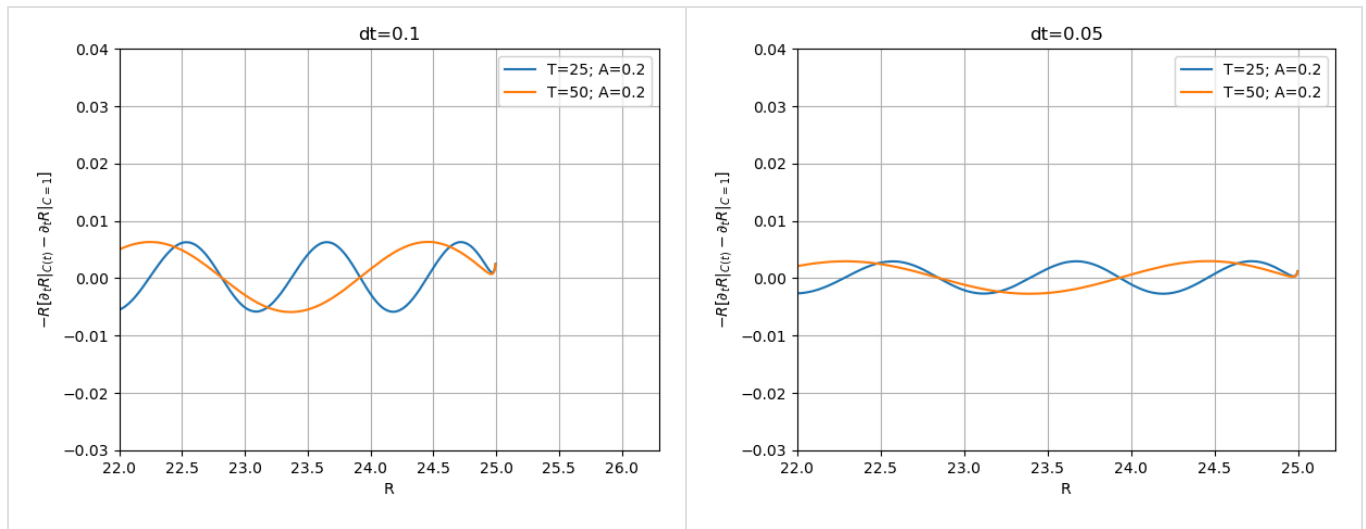
### Numerical error

Oscillations in  $C$  introduce an oscillation in the deviation from the constant  $C$  curve.

We look at the difference between the curves:

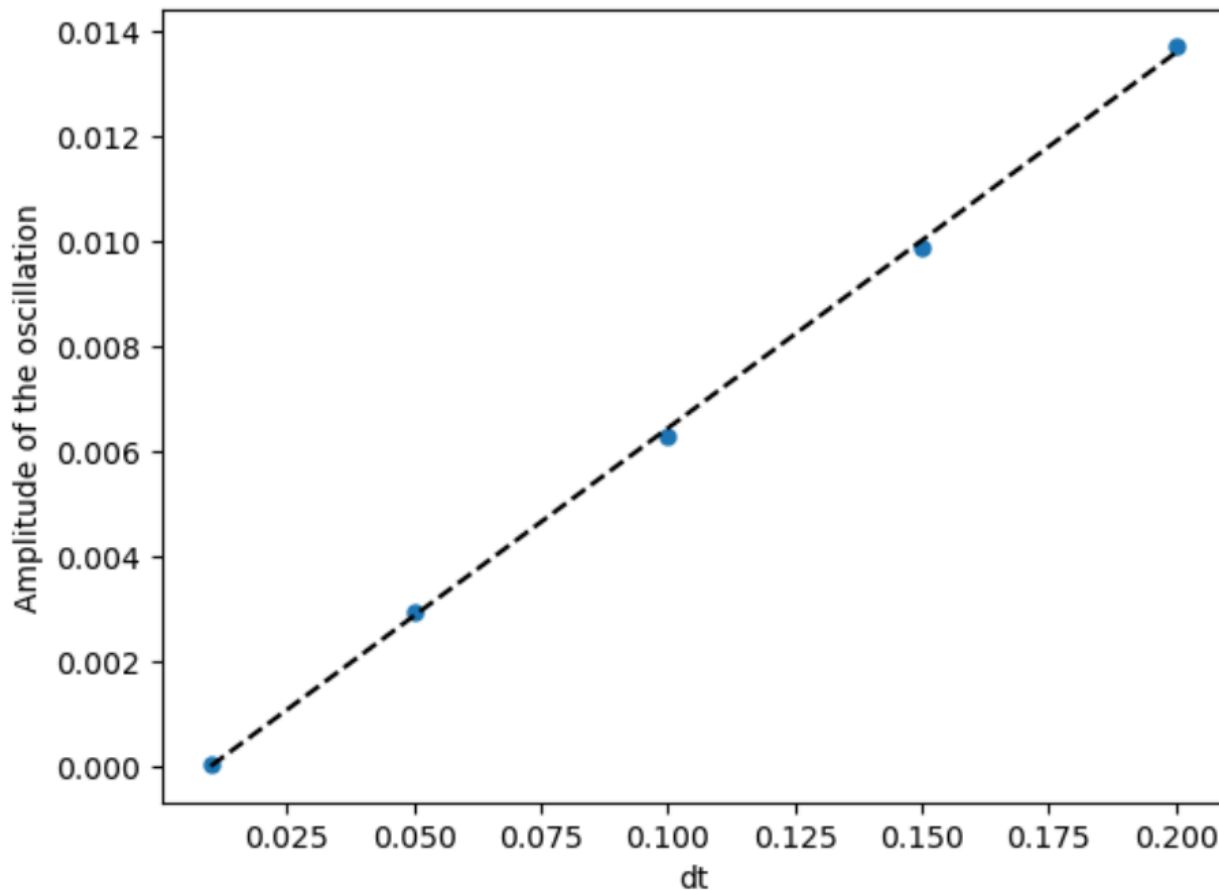
$$-[R\partial R]_{C(t)} - R\partial R|_{C=1}]$$

**A=0.2**



As the amplitude of the oscillation of this deviation increases with  $dt$ , we suspect it to be a numerical effect. We verify this:

Checking if the oscillations of  $R\partial_t R|_{C(t)}$  from  $R\partial_t R|_{C=1}$  seen at large  $R$  are just numerical effect. The amplitude of the oscillation is measured as the first maxima from the right (large  $R$ )  
 $dt=0$  extrapolation:  $-0.0007181671256673698$   
 $A=0.2$



The extrapolated value at  $dt = 0$  is the order of magnitude of the real (non-numerical) effect. Compared to the value of  $R\partial_t R|_{C=1}$  at large  $R$  (that is -1)

$$7 * 10^{-4} \ll 1$$

so we conclude this **is just a numerical effect** or, if there is an effect, it is 4 order of magnitude smaller than the limit value.

## Conclusion

The deviation we see in simulations from the "constant C" case goes to zero when  $dt$  goes to zero, so it is just a numerical error. As a consequence, we state that slow oscillations with **small amplitude** do not affect the dynamics of a circular domain.