

STAT 522 — Assignment 3

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1 Exercise 4.1

(a)

```
df_tot = 29
df_err = 20
df_treat = 4
df_block = df_tot - df_treat - df_err
df_block

## [1] 5

m <- rbind(df_treat, df_block, df_err, df_tot)
m

##           [,1]
## df_treat     4
## df_block     5
## df_err      20
## df_tot      29

ss_tot = 1503.71
ss_err = 169.33
ss_treat = 1010.56
ss_block = ss_tot - ss_treat - ss_err
ss_block

## [1] 323.8

n <- rbind(ss_treat, ss_block, ss_err, ss_tot)
n

##           [,1]
## ss_treat 1010.6
## ss_block  323.8
## ss_err   169.3
## ss_tot   1503.7

ms_treat = ss_treat/df_treat
ms_err = ss_err/df_err
ms_treat

## [1] 252.6

ms_err

## [1] 8.466
```

```

ms_block = 64.765

n1 <- rbind(ms_treat, ms_block, ms_err)
n1

##           [,1]
## ms_treat 252.640
## ms_block  64.765
## ms_err    8.466

F_treat = 29.84
F_block = ms_block/ms_err
F_block

## [1] 7.65

p_treat = 1 - pf(F_treat, df_treat, df_err)
p_treat

## [1] 3.545e-08

p_block = 1 - pf(F_block, df_block, df_err)
p_block

## [1] 0.0003689

```

The ANOVA Table:

Source	DF	SS	MS	F	P
Treatment	4	1010.56	252.64	29.84	0.0000
Block	5	323.83	64.765	7.65	0.0004
Error	20	169.33	8.4665		
Total	29	1503.71			

(b) Six blocks are used in this experiment.

(c) Based on the p-value, we can make decision on the null hypothesis. As for both treatment and block, the p-values are much smaller, we can reject the null hypothesis.

2 Exercise 4.3

```

## RANDOMIZED BLOCK DESIGN
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
chemist_RBD <- read.csv("4.3.csv")
head(chemist_RBD)

## Chemist Bolt Strength
## 1      C1      B1      73
## 2      C1      B2      68
## 3      C1      B3      74
## 4      C1      B4      71
## 5      C1      B5      67
## 6      C2      B1      73

```

```

topplot = matrix(chemist_RBD$Strength, byrow = TRUE, nrow = 4)
topplot

##      [,1] [,2] [,3] [,4] [,5]
## [1,]   73   68   74   71   67
## [2,]   73   67   75   72   70
## [3,]   75   68   78   73   68
## [4,]   73   71   75   75   69

library(lme4)

## Loading required package: lattice
## Loading required package: Matrix

modelRE = lmer(Strength ~ (1 | Bolt) + Chemist, data = chemist_RBD) #Random effects
summary(modelRE)

## Linear mixed model fit by REML ['lmerMod']
## Formula: Strength ~ (1 | Bolt) + Chemist
## Data: chemist_RBD
##
## REML criterion at convergence: 73.69
##
## Random effects:
## Groups Name Variance Std.Dev.
## Bolt (Intercept) 9.36 3.06
## Residual 1.82 1.35
## Number of obs: 20, groups: Bolt, 5
##
## Fixed effects:
## Estimate Std. Error t value
## (Intercept) 70.600 1.495 47.2
## ChemistC2 0.800 0.852 0.9
## ChemistC3 1.800 0.852 2.1
## ChemistC4 2.000 0.852 2.3
##
## Correlation of Fixed Effects:
## (Intr) ChmsC2 ChmsC3
## ChemistC2 -0.285
## ChemistC3 -0.285 0.500
## ChemistC4 -0.285 0.500 0.500

anova(modelRE, ddf = "lmer4")

## Analysis of Variance Table
## Df Sum Sq Mean Sq F value
## Chemist 3 12.9 4.32 2.38

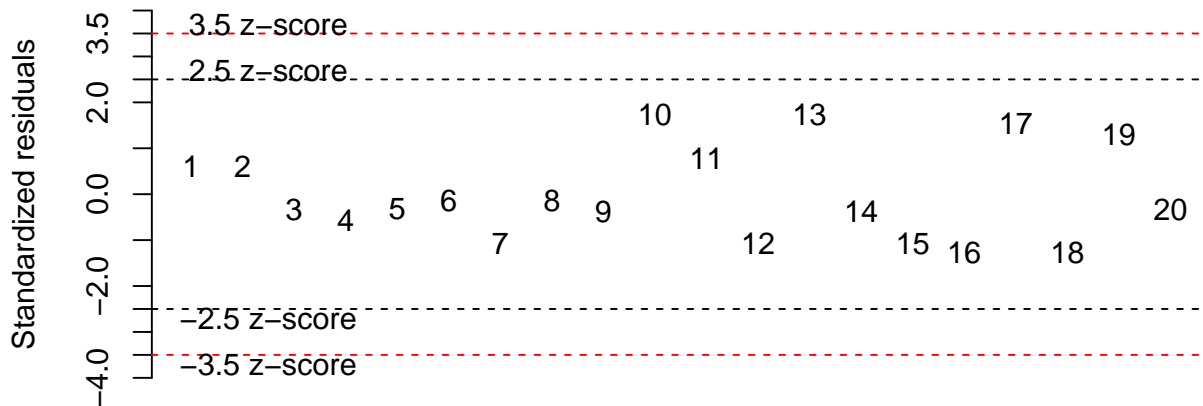
##### ALTERNATIVE METHOD BY USING LIBRARY 'easyanova'
library(easyanova)

## Loading required package: car
## Loading required package: MASS
## Loading required package: nnet
## Loading required package: nlme
##
## Attaching package: 'nlme'
## The following object is masked from 'package:lme4':
##
## lmList

chemist_RBD_anova <- ea1(chemist_RBD, design = 2)

```

Standardized residuals vs Sequence data



Sequence data

```
chemist_RBD_anova
```

```
## $`Analysis of variance`
##           df type III SS mean square F value    p>F
## treatments  3      12.95      4.317  2.3761 0.1211
## blocks      4      157.00     39.250 21.6055 <0.001
## Residuals   12       21.80      1.817      -      -
##
## $`Adjusted means`
## treatment adjusted.mean standard.error tukey snk duncan  t scott_knott
## 1          C4           72.6        0.6028    a  a      a  a          a
## 2          C3           72.4        0.6028    a  a      ab ab         a
## 3          C2           71.4        0.6028    a  a      ab ab         a
## 4          C1           70.6        0.6028    a  a      b  b         a
##
## $`Multiple comparison test`
##      pair contrast p(tukey) p(snk) p(duncan)  p(t)
## 1 C4 - C3        0.2   0.9952 0.8185    0.8185 0.8185
## 2 C4 - C2        1.2   0.5183 0.3679    0.2050 0.1846
## 3 C4 - C1        2.0   0.1418 0.1418    0.0497 0.0370
## 4 C3 - C2        1.0   0.6540 0.2635    0.2635 0.2635
## 5 C3 - C1        1.8   0.2043 0.1291    0.0668 0.0564
## 6 C2 - C1        0.8   0.7853 0.3665    0.3665 0.3665
##
## $`Residual analysis`
##                               values
## p.value Shapiro-Wilk test    0.0405
## p.value Bartlett test       0.7648
## coefficient of variation (%)  1.8800
## first value most discrepant  10.0000
## second value most discrepant 13.0000
## third value most discrepant  17.0000
```

From the R code values, the F-value for the treatment is 2.38 with a corresponding p-value of 0.1211. So, null hypothesis can not be rejected. No significant difference is visible among the chemical types at $\alpha = 0.05$ level. But the p-value for the blocks is very small. So, significant difference is visible for blocking.

3 Exercise 4.4

```
## RANDOMIZED BLOCK DESIGN
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
bacteria_RBD <- read.csv("4.4.csv")
head(bacteria_RBD)

##      Solution Days Growth
## 1      S1      D1      13
## 2      S1      D2      22
## 3      S1      D3      18
## 4      S1      D4      39
## 5      S2      D1      16
## 6      S2      D2      24

toplot = matrix(bacteria_RBD$Growth, byrow = TRUE, nrow = 3)
toplot

##      [,1] [,2] [,3] [,4]
## [1,]   13   22   18   39
## [2,]   16   24   17   44
## [3,]    5    4    1   22

modelRE = lmer(Growth ~ (1 | Days) + Solution, data = bacteria_RBD)
summary(modelRE)

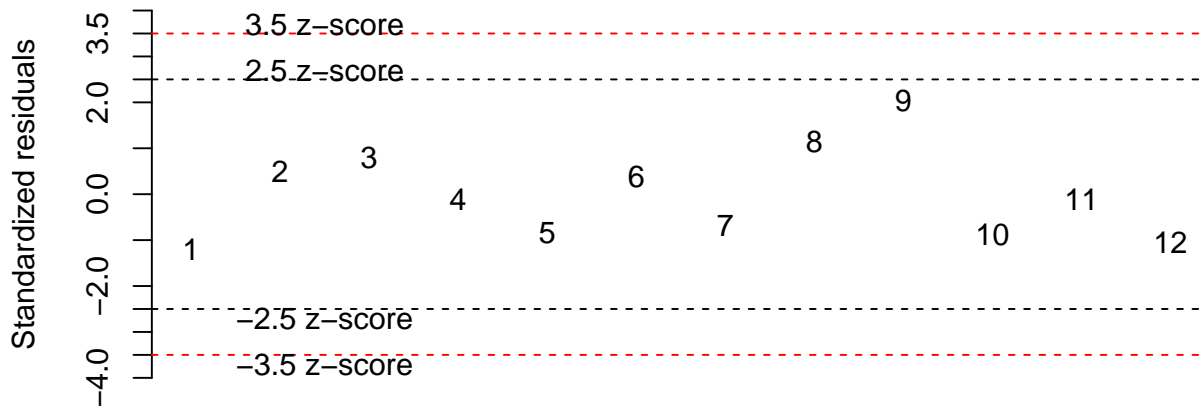
## Linear mixed model fit by REML ['lmerMod']
## Formula: Growth ~ (1 | Days) + Solution
##      Data: bacteria_RBD
##
## REML criterion at convergence: 60.37
##
## Random effects:
##      Groups      Name      Variance Std.Dev.
##      Days      (Intercept) 120.11   10.96
##      Residual              8.64    2.94
## Number of obs: 12, groups: Days, 4
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)    23.00     5.67    4.05
## SolutionS2      2.25     2.08    1.08
## SolutionS3    -15.00     2.08   -7.22
##
## Correlation of Fixed Effects:
##              (Intr) SltnS2
## SolutionS2 -0.183
## SolutionS3 -0.183  0.500

anova(modelRE, ddf = "lmer4")

## Analysis of Variance Table
##              Df Sum Sq Mean Sq F value
## Solution    2     703     352    40.7

##### ALTERNATIVE METHOD BY USING LIBRARY 'easyanova'
bacteria_RBD_anova <- eal(bacteria_RBD, design = 2)
```

Standardized residuals vs Sequence data



Sequence data

```
bacteria_RBD_anova
```

```
## $`Analysis of variance`
##           df type III SS mean square F value    p>F
## treatments  2      703.50    351.750  40.717 <0.001
## blocks      3     1106.92    368.972  42.7106 <0.001
## Residuals   6       51.83     8.639      -      -
##
## $`Adjusted means`
## treatment adjusted.mean standard.error tukey snk duncan t scott_knott
## 1          S2          25.25          1.47    a  a      a a          a
## 2          S1          23.00          1.47    a  a      a a          a
## 3          S3           8.00          1.47    b  b      b b          b
##
## $`Multiple comparison test`
## pair contrast p(tukey) p(snk) p(duncan) p(t)
## 1 S2 - S1      2.25    0.5578 0.3206    0.3206 0.3206
## 2 S2 - S3     17.25    0.0004 0.0004    0.0002 0.0002
## 3 S1 - S3     15.00    0.0009 0.0004    0.0004 0.0004
##
## $`Residual analysis`
##
## p.value Shapiro-Wilk test    0.4027
## p.value Bartlett test       0.8803
## coefficient of variation (%) 15.6800
## first value most discrepant  9.0000
## second value most discrepant 1.0000
## third value most discrepant  8.0000
```

From the R code values, the F-value for the treatment is 40.72 with a corresponding very small p-value. So, null hypothesis can be rejected. So, a clear difference is visible between the means of the three solutions. The blocking also shows some effect with F-value of 42.71 with lower p-value. The multiple comparison test indicates that solution 3 is significantly different than the other two solutions.

4 Exercise 4.11

(a)

```
## RANDOMIZED BLOCK DESIGN
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
alg_RBD <- read.csv("4.11.csv")
head(alg_RBD)

##   Project Algorith Cost.Error
## 1      P1      SLM      1244
## 2      P2      SLM        21
## 3      P3      SLM        82
## 4      P4      SLM     2221
## 5      P5      SLM       905
## 6      P6      SLM       839

toplot = matrix(alg_RBD$Cost.Error, byrow = TRUE, nrow = 6)
toplot

##      [,1] [,2] [,3] [,4] [,5] [,6]
## [1,] 1244  21  82 2221  905  839
## [2,]  281 129 396 1306  336  910
## [3,]  220  84 458  543  300  794
## [4,]  225  83 425  552  291  826
## [5,]   19  11 -34  121   15  103
## [6,]  -20  35 -53  170  104  199

modelRE = lmer(Cost.Error ~ (1 | Project) + Algorith, data = alg_RBD)
summary(modelRE)

## Linear mixed model fit by REML ['lmerMod']
## Formula: Cost.Error ~ (1 | Project) + Algorith
##   Data: alg_RBD
##
## REML criterion at convergence: 451.5
##
## Random effects:
##   Groups   Name      Variance Std.Dev.
##   Project (Intercept) 57714    240
##   Residual              11183    333
## Number of obs: 36, groups: Project, 6
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)         560         168   3.34
## AlgorithCOCOMO-C     -159         192  -0.83
## AlgorithCOCOMO-R     -160         192  -0.83
## AlgorithESTIMALS     -487         192  -2.53
## AlgorithFUNCTION POINTS -520         192  -2.70
## AlgorithSLM          326         192   1.69
##
## Correlation of Fixed Effects:
##              (Intr) ACOCOMO-C ACOCOMO-R AESTIM AFUNCP
## AlgCOCOMO-C -0.574
## AlgCOCOMO-R -0.574  0.500
## AlgESTIMALS -0.574  0.500  0.500
## AFUNCTIONPO -0.574  0.500  0.500  0.500
## AlgorithSLM -0.574  0.500  0.500  0.500  0.500

anova(modelRE, ddf = "lmer4")
```

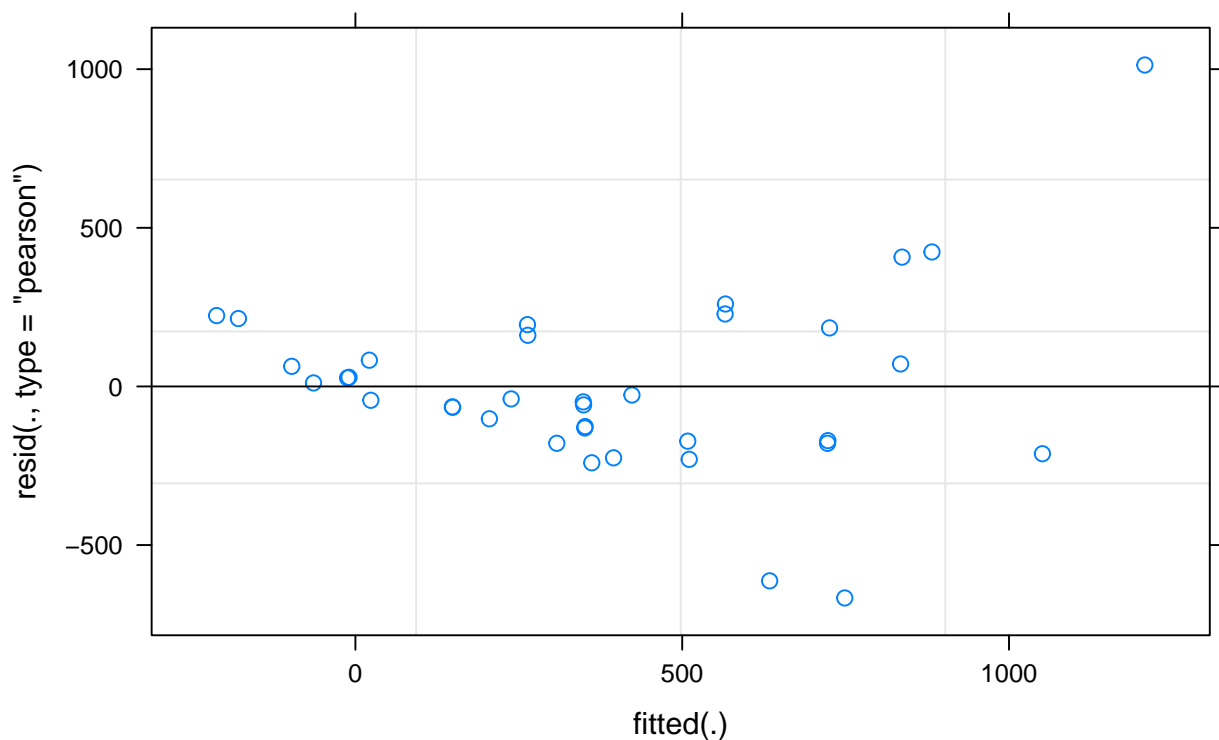
```
## Analysis of Variance Table
##      Df Sum Sq Mean Sq F value
## Algorithm  5 2989130  597826    5.38

p_value <- 1 - pf(5.38, 5, 25)
p_value

## [1] 0.001714
```

(b)

```
plot(modelRE)
```



(c)

```
modelRE

## Linear mixed model fit by REML ['lmerMod']
## Formula: Cost.Error ~ (1 | Project) + Algorithm
## Data: alg_RBD
## REML criterion at convergence: 451.5
## Random effects:
## Groups Name Std.Dev.
## Project (Intercept) 240
## Residual 333
## Number of obs: 36, groups: Project, 6
## Fixed Effects:
## (Intercept) AlgorithmCOCOMO-C AlgorithmCOCOMO-R
## 560 -159 -160
## AlgorithmESTIMALS AlgorithmFUNCTION POINTS AlgorithmSLM
## -487 -520 326
```

I will recommend Algorithm-SLIM for use in practice because it has only the positive effect.

5 Exercise 4.22

```
### LATIN SQUARE DESIGN
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
ingredient_LS <- read.csv("4.22.csv")
head(ingredient_LS)

##   Batch Day Catalyst Time
## 1    B1  D1         A    8
## 2    B2  D1         C   11
## 3    B3  D1         B    4
## 4    B4  D1         D    6
## 5    B5  D1         E    4
## 6    B1  D2         B    7

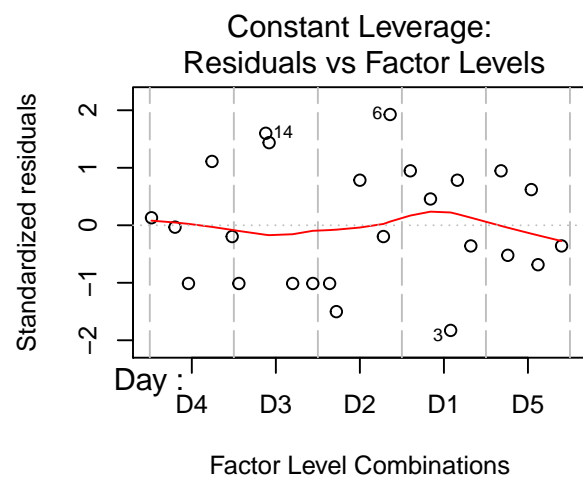
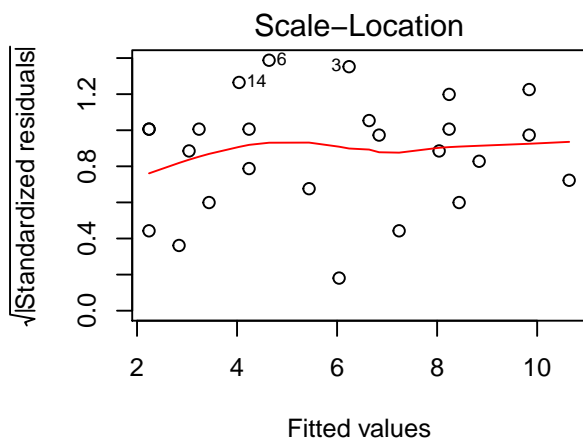
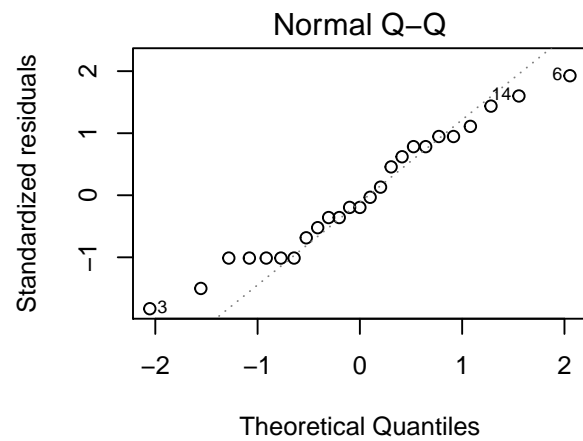
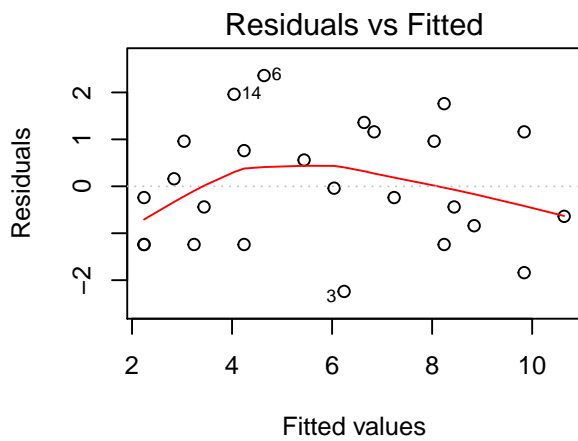
ingredient.lm <- lm(Time ~ Day + Batch + Catalyst, ingredient_LS)
anova(ingredient.lm)

## Analysis of Variance Table
##
## Response: Time
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Day         4   12.2      3.1    0.98 0.45501
## Batch        4   15.4      3.9    1.23 0.34762
## Catalyst     4  141.4     35.4   11.31 0.00049 ***
## Residuals   12   37.5      3.1
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ingredient.aov = aov(Time ~ Day + Batch + Catalyst, ingredient_LS)
anova(ingredient.aov)

## Analysis of Variance Table
##
## Response: Time
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Day         4   12.2      3.1    0.98 0.45501
## Batch        4   15.4      3.9    1.23 0.34762
## Catalyst     4  141.4     35.4   11.31 0.00049 ***
## Residuals   12   37.5      3.1
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

par(mfrow = c(2, 2))
plot(ingredient.aov)
```

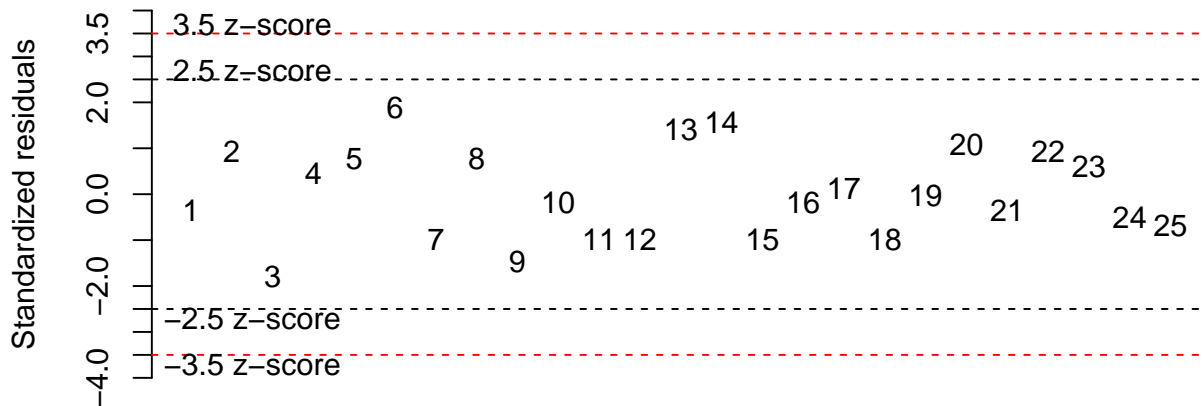


```
##### ALTERNATIVE METHOD BY USING LIBRARY 'easynova'
ingredient_LS1 <- ingredient_LS[c(3, 1, 2, 4)]
head(ingredient_LS1)

##   Catalyst Batch Day Time
## 1      A     B1  D1    8
## 2      C     B2  D1   11
## 3      B     B3  D1    4
## 4      D     B4  D1    6
## 5      E     B5  D1    4
## 6      B     B1  D2    7

alg_RBD_anova <- ea1(ingredient_LS1, design = 3)
```

Standardized residuals vs Sequence data



Sequence data

```
alg_RBD_anova
```

```
## $`Analysis of variance`
##           df type III SS mean square F value    p>F
## treatments  4      141.44      35.360 11.3092 <0.001
## rows        4       15.44       3.860  1.2345 0.3476
## columns     4       12.24       3.060  0.9787 0.455
## Residuals  12       37.52       3.127    -    -
##
## $`Adjusted means`
## treatment adjusted.mean standard.error tukey snk duncan t scott_knott
## 1          C           8.8         0.7908    a  a      a a          a
## 2          A           8.4         0.7908    a  a      a a          a
## 3          B           5.6         0.7908   ab  b      b b          b
## 4          D           3.4         0.7908    b  b      b b          b
## 5          E           3.2         0.7908    b  b      b b          b
##
## $`Multiple comparison test`
##      pair contrast p(tukey) p(snk) p(duncan)  p(t)
## 1  C - A         0.4  0.9960 0.7268    0.7268 0.7268
## 2  C - B         3.2  0.0864 0.0355    0.0179 0.0143
## 3  C - D         5.4  0.0031 0.0020    0.0007 0.0004
## 4  C - E         5.6  0.0023 0.0023    0.0006 0.0003
## 5  A - B         2.8  0.1540 0.0277    0.0277 0.0277
## 6  A - D         5.0  0.0056 0.0020    0.0010 0.0008
## 7  A - E         5.2  0.0041 0.0027    0.0009 0.0006
## 8  B - D         2.2  0.3366 0.0727    0.0727 0.0727
## 9  B - E         2.4  0.2632 0.1220    0.0630 0.0530
## 10 D - E         0.2  0.9997 0.8611    0.8611 0.8611
##
## $`Residual analysis`
##                               values
## p.value Shapiro-Wilk test    0.5476
## p.value Bartlett test       0.8170
## coefficient of variation (%) 30.0700
## first value most discrepant  6.0000
## second value most discrepant 3.0000
```

```
## third value most discrepant 14.0000
```

From the R code values, the F-value for the catalyst is 11.31 with a corresponding small p-value. So, null hypothesis can be rejected. So, the difference between the effect of five different ingredients on the reaction time of a chemical process is somewhat significant. But for day and batches, the p-values are higher in values which indicate that they have no effect on the experiment.

6 Exercise 4.24

```
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
bacteria_RBD <- read.csv("4.4.csv")
head(bacteria_RBD)

##   Solution Days Growth
## 1      S1   D1      13
## 2      S1   D2      22
## 3      S1   D3      18
## 4      S1   D4      39
## 5      S2   D1      16
## 6      S2   D2      24

modelRE = lmer(Growth ~ (1 | Solution) + Days, data = bacteria_RBD)
summary(modelRE)

## Linear mixed model fit by REML ['lmerMod']
## Formula: Growth ~ (1 | Solution) + Days
##   Data: bacteria_RBD
##
## REML criterion at convergence: 51.76
##
## Random effects:
##   Groups   Name      Variance Std.Dev.
##   Solution (Intercept) 85.78    9.26
##   Residual              8.64    2.94
## Number of obs: 12, groups: Solution, 3
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)   11.333     5.610    2.02
## DaysD2         5.333     2.400    2.22
## DaysD3         0.667     2.400    0.28
## DaysD4        23.667     2.400    9.86
##
## Correlation of Fixed Effects:
##      (Intr) DaysD2 DaysD3
## DaysD2 -0.214
## DaysD3 -0.214  0.500
## DaysD4 -0.214  0.500  0.500

anova(modelRE, ddf = "lmer4")

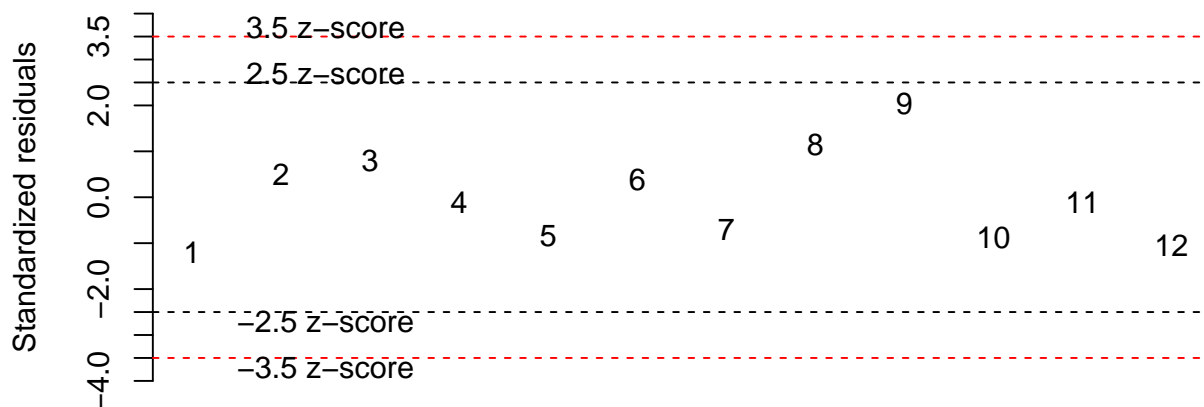
## Analysis of Variance Table
##      Df Sum Sq Mean Sq F value
## Days  3  1107      369    42.7

##### ALTERNATIVE METHOD BY USING LIBRARY 'easyanova'
bacteria_RBD1 <- bacteria_RBD[c(2, 1, 3)]
head(bacteria_RBD1)
```

```
## Days Solution Growth
## 1 D1 S1 13
## 2 D2 S1 22
## 3 D3 S1 18
## 4 D4 S1 39
## 5 D1 S2 16
## 6 D2 S2 24
```

```
bacteria_RBD_anova <- eal(bacteria_RBD1, design = 2)
```

Standardized residuals vs Sequence data



Sequence data

```
bacteria_RBD_anova
```

```
## $`Analysis of variance`
##          df type III SS mean square F value    p>F
## treatments  3      1106.92      368.972 42.7106 <0.001
## blocks      2       703.50      351.750 40.717 <0.001
## Residuals   6        51.83       8.639    -    -
##
## $`Adjusted means`
## treatment adjusted.mean standard.error tukey snk duncan t scott_knott
## 1 D4      35.00      1.697    a    a    a a    a
## 2 D2      16.67      1.697    b    b    b b    b
## 3 D3      12.00      1.697    b    b    b b    b
## 4 D1      11.33      1.697    b    b    b b    b
##
## $`Multiple comparison test`
##      pair contrast p(tukey) p(snk) p(duncan)  p(t)
## 1 D4 - D2 18.3333 0.0011 0.0003 0.0003 0.0003
## 2 D4 - D3 23.0000 0.0003 0.0002 0.0001 0.0001
## 3 D4 - D1 23.6667 0.0003 0.0003 0.0001 0.0001
## 4 D2 - D3 4.6667 0.3038 0.0998 0.0998 0.0998
## 5 D2 - D1 5.3334 0.2193 0.1455 0.0756 0.0680
## 6 D3 - D1 0.6667 0.9917 0.7905 0.7905 0.7905
##
## $`Residual analysis`
##
##          values
## p.value Shapiro-Wilk test 0.4027
```

```
## p.value Bartlett test      0.8369
## coefficient of variation (%) 15.6800
## first value most discrepant 9.0000
## second value most discrepant 1.0000
## third value most discrepant 8.0000
```

From the R output, the F-value for the treatment is 42.71 with a corresponding small p-value. So, null hypothesis can be rejected. So, treatment has some effect. The blocks also generate F-value of 40.72 with lower p-value. So, blocking also has some effect.

7 Exercise 4.35

```
### Graeco-Latin Square Design
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
chemical_GLS <- read.csv("4.35.csv")
head(chemical_GLS)

##   Batch Acid Time Catalyst Yield
## 1    B1   A1    A         a    26
## 2    B2   A1    B         c    18
## 3    B3   A1    C         e    20
## 4    B4   A1    D         b    15
## 5    B5   A1    E         d    10
## 6    B1   A2    B         b    16

chemical_GLS.aov = aov(Yield ~ Acid + Batch + Catalyst + Time, chemical_GLS)
anova(chemical_GLS.aov)

## Analysis of Variance Table
##
## Response: Yield
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Acid         4      24      6.1     1.04 0.44254
## Batch         4      10      2.5     0.43 0.78545
## Catalyst      4      12      3.0     0.51 0.72890
## Time         4     343     85.7    14.65 0.00094 ***
## Residuals    8       47      5.9
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

From the R output, the F-value of time is 14.65 with a corresponding p-value of 0.00094. So, null hypothesis can be rejected. We can say that time has some effect. But acid, batch and catalyst, the p-values are higher in value which indicate that they have no effect on the experiment.

8 Exercise 4.42

```
### Balanced Incomplete Block Design (BIBD)
setwd("C:/Users/Subasish/Dropbox/A Spring 2014/Dr Novelo/HW")
hardwood_BIBD <- read.csv("4.42_1.csv")
head(hardwood_BIBD)

##   Concen Days Strength
## 1     C2   D1      114
## 2     C2   D2       NA
## 3     C2   D3       NA
## 4     C2   D4       NA
```

```
## 5      C2   D5      120
## 6      C2   D6      NA

toplot = matrix(hardwood_BIBD$Strength, byrow = TRUE, nrow = 7)
toplot

##      [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## [1,] 114   NA   NA   NA  120   NA  117
## [2,] 126  120   NA   NA   NA  119   NA
## [3,]   NA  137  114   NA   NA   NA  134
## [4,] 141   NA  129  149   NA   NA   NA
## [5,]   NA  145   NA  150  143   NA   NA
## [6,]   NA   NA  120   NA  118  123   NA
## [7,]   NA   NA   NA  136   NA  130  127

ingredient.lm <- lm(Strength ~ Concen + Days, hardwood_BIBD)
anova(ingredient.lm)

## Analysis of Variance Table
##
## Response: Strength
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Concen      6   2040      340   13.52 0.00084 ***
## Days        6    442       74    2.93 0.08126 .
## Residuals   8     201       25
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

From the R output, the F-value for the concentration is 13.52 with a corresponding p-value of 0.00084. So, null hypothesis can be rejected. We can say that concentration has some effect. For days, the p-value is slightly higher than 0.05 for days. It indicates that days have no effect on the experiment.

9 Exercise 4.49

```
### Verify that a BIBD with the parameters a =8, r =8, k =4, and b =16
### does not exist.

a = 8
r = 8
k = 4
b = 16

lamda = r * (k - 1)/(a - 1)
lamda

## [1] 3.429
```

From the R output, it's found that the value of λ is not an integer. So, a BIBD with these parameters cannot exist.