

# Solving the puzzle of discrepant variability on monthly time scales implied by SDSS and CRTS datasets

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## ABSTRACT

We present improved error analysis for the 3,800 CRTS (Catalina Real-Time Transient Survey) optical quasar light curves from the Sloan Digital Sky Survey Stripe 82 catalog. SDSS imaging survey has provided a time-resolved photometric dataset which greatly improved our understanding of the quasar optical continuum variability: data for monthly and longer timescales are consistent with a damped random walk. Recently, newer data obtained by CRTS (Catalina Real-Time Transient Survey) provided puzzling evidence for enhanced variability, compared to SDSS results, on monthly time scales. Quantitatively, SDSS results predict about 0.06 mag rms variability for timescales below 50 days, while CRTS data show about a factor of two larger root-mean-square for spectroscopically confirmed SDSS quasars. Our analysis presented here has successfully resolved this discrepancy as due to slightly underestimated photometric error estimates provided by the CRTS image processing pipelines. The photometric error correction factors, derived from detailed analysis of non-variable SDSS standard stars that were re-observed by CRTS, are about 20 – 30%, and result in a quasar variability behavior implied by the CRTS data fully consistent with earlier SDSS results.

**Key words:** keyword1 – keyword2 – keyword3

## 1 INTRODUCTION

Quasar variability is an important characteristic that has a potential to shed light on the structure of the innermost region of the accretion disk, and has been the subject of research for the past half century (Matthew, Sandage 1963, Vanden Berk + 2004, Grier+2012, Kozłowski+2016). The Sloan Digital Sky Survey (SDSS, Schmidt+2010, Sesar+2007) and Catalina Real-Time Transient Survey (CRTS, Djorgovski+2012, Drake+2009) allowed an unprecedented study of well-calibrated light curves.

Assuming that the observed variability of a lightcurve - discretely sampled time series - is caused by a continuous underlying physical phenomenon, to characterise it we can use a mathematical formalism of a stochastic process model (Kasliwal+2015). A one-parameter Auto-Regressive, AR(1), process may correspond to the physical situation

of an environment where a disturbance is diffused and returns to the median value. Various explanations exist for the nature of such disturbances, including supernovae, microlensing, accretion disk instabilities, and thermal fluctuations (Kelly+2009, Kelly+2011, Collier&Peterson 2001, Ruan+2014). Most likely, thanks to Reverberation Mapping studies (Peterson 2004, Fausnaugh+2016, Munoz+2016), we understand the accretion disk to be the main source of the underlying variability.

At the cadence of the CRTS survey (more than few days), the AR(1) process (Damped Random Walk model) describes well the quasar variability (Butler Bloom 2011, MacLeod+2010,2011,2012, Kelly+2009, Zu+2011,2013, Kozłowski+2010a, Ruan+2012). [A deviation from the DRW model at very short timescales, reported by Kasliwal+2015, is based on Kepler lightcurves at cadences shorter than a day, which is below the observational limit of CRTS. For this reason, in this paper DRW is assumed to be a good descriptor of the quasar stochastic variability].

The DRW model has two parameters - an amplitude

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of variability, and a characteristic timescale, that corresponds to the timescale of damping of thermal oscillations or orbital timescale (Kelly+2009). When the lightcurves are sparsely sampled, it is more meaningful to describe their ensemble properties, using the structure function (SF), which is well defined for a collection of variable objects driven by the DRW (Kozłowski+2010, 2016, Vanden Berk+2004, Schmidt+2010, Hawkins+2002)

Recent SDSS-based studies (MacLeod+2010, Kelly+2009) reflect the traditional timescale of  $\tau > 100$  days in quasar rest frame, supported by OGLE results of Zu+2014 with  $17 \leq \tau \leq 2700$  days. However, a CRTS-based study of Graham+2014 that used Slepian Wavelet Variance methodology found  $\tau$  54 days. The latter is consistent with the Kepler-based results of Kasliwal+2015 for cadences above a day, who found  $17 \leq \tau \leq 2700$  days. The aim of this paper is to revisit the analysis of the CRTS quasars using a well-tested approach of the Structure Function, and detailed error analysis (MacLeod+2010, MacLeod+2012, Simonetti+1984, Vanden Berk+2004, Sumi+2005, Bauer+2009).

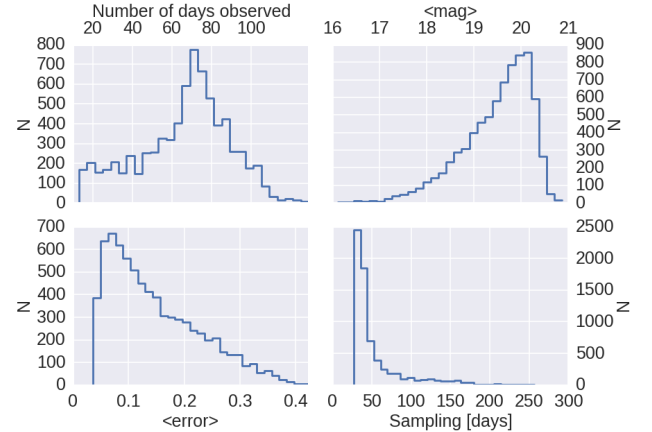
In section 2 we describe the properties of our dataset, all selection criteria, and the structure function analysis. In section 3 we explain the results of our analysis of the small timescale subset of the structure function. This is followed by discussion of the impact of our result, and conclusions in sections 4 and 5.

## 2 DATA ANALYSIS

### 2.1 Data overview

Catalina Real-time Transient Survey (CRTS) employed three telescopes (0.7 m Catalina Sky Survey Schmidt and 1.5 m Mount Lemmon Survey telescopes in Arizona, and the 0.5 m Siding Springs Survey Schmidt in Australia” Graham+2015), each with a 4kx4k CCD detector (Djorgovski+2011). All observations are taken in an unfiltered white light, calibrated to Johnson V-band zero point (Drake+2013). Our quasar sample consists of 7932 Quasars from the equatorial region of the sky ( $22^h24^m < R.A. < 04^h08^m$  and  $|Dec| < 1.27deg$ ) known as the Stripe 82 (Branimir Sesar, priv comm.). We also use a sample of 52133 stars from the CRTS Stripe 82. Our sampling criterion : more than 10 measurements in the lightcurve, leaves 7707 quasars and 50723 stars. (See Fig.2.1) We also require more than 10 individual days of observations, leaving 7601 quasars and 49387 stars. We further perform day-averaging to

As a control sample we use CRTS observations of standard stars in Stripe 82. Both CRTS stars and quasars are positionally matched to SDSS targets, and thus to their CRTS white light photometry we add the SDSS photometric information. For stars we used the SDSS Stripe 82 standard stars catalog ver. 2.6 (Ivezic+2007), and for quasars the SDSS DR7 stripe 82 catalog with 2-MASS cross-matched 8974 quasars.



**Figure 1.** Statistical information about the CRTS Quasar sample including 7601 day-averaged light curves. The upper-left panel shows the number of days that a given quasar was observed, i.e.  $\max(MJD) - \min(MJD)$  per light curve. The upper-right panel shows the average light curve magnitude. The bottom-left panel shows the light curve averaged error. If  $i, i+1$  are two consecutive day-averaged observations in the light curve, then  $MJD_i - MJD_{i+1}$  is the sampling interval. The bottom-right panel shows light curve - averaged sampling intervals. The light curve and sample-averaged mean and median error is 0.22. The mean brightness is 19.50, and the mean number of individual observations per light curve is 209. Within that sample, 96% observations of quasars span the time of 7-9 years. 91.2% of quasars were observed between 1 to 4 times per night.

### 2.2 Day-averaging and selection

To improve signal-to-noise ratio we day-average light curve points. The day-average error  $e_w$  is the weighted sum of individual errors  $e_i$ : (see eq.1)

$$e_w = \frac{1}{\sqrt{\sum_i w_i}} \quad (1)$$

where  $w_i = 1/e_i^2$  is the weight assigned to each point. To avoid unphysically small error values ( $\infty$ ), we added 0.01 mag to  $e_w$  in quadrature if  $e_w < 0.02$  mag. A typical sampling interval of day-averaged CRTS Quasar lightcurves is  $\approx 20$  days.

In the structure function analysis, we use CRTS standard stars as the reference objects that exhibit no intrinsic variability (SF=0). We define our sample in a following way: for CRTS stars and quasars, we require SDSS r-band  $17 < m_{SDSS,r} < 20$ , and the CRTS lightcurve-averaged error to be  $0.05 < \langle e_w \rangle < 0.3$ . To assess the influence of colors on variability, we divide the comparison stars into two color bins: "red" with  $1 < g - i < 3$  and "blue"  $-1 < g - i < 1$ , using SDSS  $g$  and  $i$  filters.

### 2.3 Structure Function

[The structure function is a well-studied approach to characterising quasar light curves. It describes the relationship between the time lag and the amplitude of brightness variability (Cristiani+1996, Schmidt+2010, Vanden Berk+2004, de Vries + 2005, Rengstorf + 2006).]

Similarly to Schmidt+2010, we calculate the structure function for a given object using the magnitude difference  $\Delta m_{i,j}$  between light curve points  $i$  and  $j$ , separated by a time lag  $\Delta t_{i,j}$ . To avoid the additional uncertainty of redshift estimates based on the SDSS spectra, we also use time lags in the observed frame. We add the error information in quadrature:  $e_{ij} = \sqrt{e_i^2 + e_j^2}$ .

To analyze the magnitude difference we bin the  $\Delta m_{i,j}$  points from all objects in logarithmic  $\Delta t_{i,j}$  space. The number of chosen bins is a choice of convenience between very coarse grid (a small number of bins) or a very fine grid, risking a small number of points per bin. Having performed tests with 50, 100, 200, 400 bins we find that  $N = 200$  is the right choice between computational efficiency and information content.

We calculate the  $SF$  using an exact prescription involving marginalizing the log-likelihood of the probability in  $p(SF)$  and  $p(\mu)$  space per bin, after [Ivezic+2013], chapter 5:

$$\left. \frac{dp(SF)}{dSF} \right|_{SF=mode} = 0 \quad (2)$$

For each bin we calculate four statistical descriptors, shown on Fig. 2.3 - standard deviation from the mean ( $\sigma$ ), Gaussian robust deviation from the mean  $\sigma_G = 0.7414(q_{75} - q_{25})$ , the Structure Function ( $SF$ ) and the mean ( $\mu$ ).

To show the departure of the CRTS quasars from the DRW model we fit to the  $SF$  a fiducial DRW model:

$$SF(\Delta t) = SF_\infty \cdot (1 - e^{-\Delta t/\tau})^{1/2} \quad (3)$$

with model error  $\sqrt{SF(\Delta t)^2 + err_{SF}^2}$ .

### 3 RESULTS OF DETAILED SAMPLE ERROR ANALYSIS

As seen on Fig. 2.3, the quasar variability on short timescales departs from the DRW model, and non-variable stars show a non-zero variability on a level larger than allowed by photometric errors. To analyze the error properties of the short timescale points we select  $\log \tau < 1.7$  points for both quasars and stars, which includes 721283 time-lag points based on quasars, and 314248 time-lag stellar points. To disentangle the magnitude sensitivity, we further split the sample into three magnitude bins:  $17 - 18$ ,  $18 - 18.5$  and  $18.5 - 19$  mag.

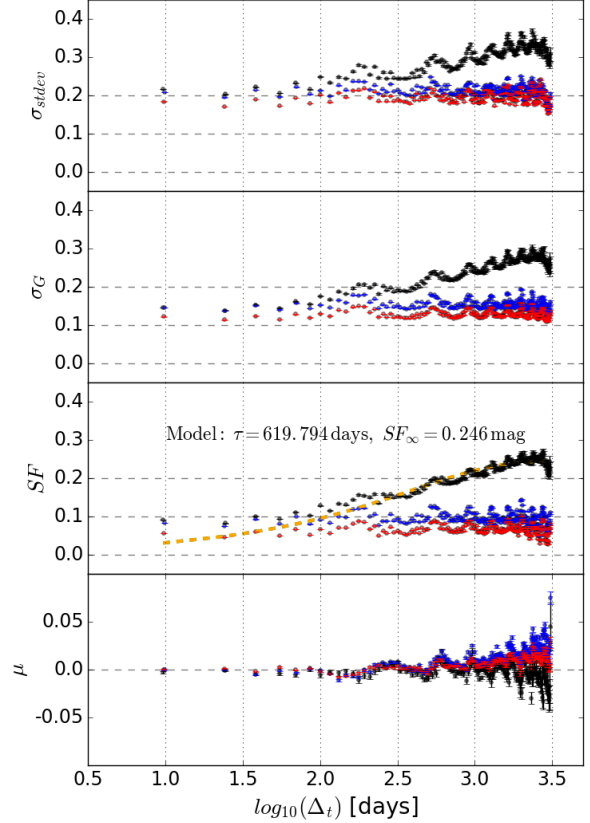
Assuming that each  $\delta m$  data point originates from a homoscedastic Gaussian distribution, with a standard deviation  $\sigma_{com}$  (that includes all intrinsic variability  $\sigma$  and error-related  $f_c * e_i$ ):

$$\sigma_{com} = \sqrt{\sigma^2 + (f_c \cdot e_i)^2} \quad (4)$$

and the mean  $\mu$ , then the distribution of all magnitude difference points in our sample is a sum of Gaussians:

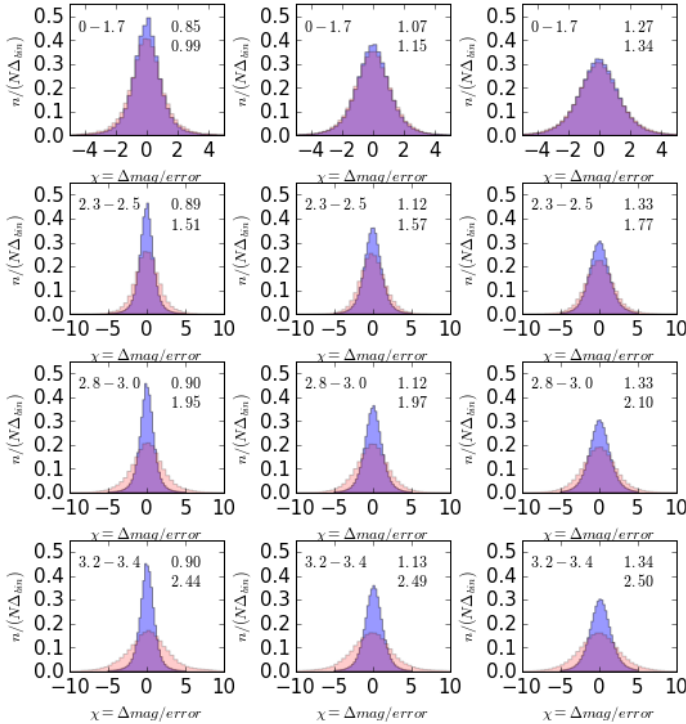
$$\frac{1}{N} \cdot \sum_{i=0}^N \frac{1}{\sqrt{2\pi}\sigma_{com}} \cdot e^{-(x_i - \mu)^2 / (2\sigma_{com}^2)} \quad (5)$$

Since standard stars do not vary on level above  $0.02\text{mag}$  [reference], it is reasonable to assume for stars  $\sigma = 0$ , and a



**Figure 2.** The four panels show statistics calculated for the subsample of 333 CRTS quasars (black points), 1400 "blue" stars (blue points), and 2087 "red" stars (red points), all chosen according to the SDSS  $r$  magnitude  $18.5 < m < 19$ . For "red" stars we require that SDSS colors are  $1 < g - i < 3$  and for "blue" stars  $-1 < g - i < 1$ . Lightcurve-derived pairwise brightness differences for all objects of a given type are binned according to linearly spaced 200 bins in  $\Delta t$ . The binning was not found to affect the main features of the plot. The sine-like modulation reflects differences in number of points in each bin (from tens to hundreds of thousands per bin). For each bin, we calculated for each type of object the standard deviation  $\sigma_{sdev}$ , the robust Gaussian standard deviation  $\sigma_G$  (from the interquartile range  $0.7414(q_{75} - q_{25})$ , Structure Function and the mean (using eqs. 5.67 – 5.68 in Ivezic + 2004 (the AstroML book)). Yellow dashed line on the SF panel traces the fiducial Damped Random Walk model. Note how both blue and red stars do not exhibit signs of variability as expected, whereas quasars (black) clearly show an intrinsic variability. At the low timescales  $\log \tau < 1.7$  CRTS quasar  $SF$  departs from the fiducial model of Structure Function.

distribution centered around  $\mu = 0$ . With these parameters we fit the ensemble of Gaussian distributions per magnitude bin to a histogram of "blue" stars to recover an error correction factor that would explain the variability ( $\sigma_{com} = f_c \cdot e_i$ ). Those factors applied to quasar distribution explain their variability (see Figs. 3 and ??).



**Figure 3.** The top panels show how the histogram of  $\chi = \Delta_m / \text{error}$  for small timescales ( $\log \Delta_t < 1.7$ ,  $t < 50$  days) for quasars (red) overlaps almost perfectly with blue stars (blue). The implied small quasar variability is at the level measured by SDSS. From left to right, we iterate over the magnitude bins : 17 – 18, 18 – 18.5, and 18.5 – 19 mag. From top to bottom we change the  $\log \Delta_t$  range. Note how the stars, being nonvariable, maintain the same spread of  $\chi$ , due to their lack of intrinsic variability. The quasars spread more thanks to their intrinsic variability, but at small timescales their spread is same as that of stars, consistent with their lack of short timescale variability. On each plot numbers in the upper-left corner indicate the  $\log \Delta_t$  range, and in the upper-right the robust width of stellar and quasar distributions of  $\chi$ .

#### 4 DISCUSSION

#### 5 CONCLUSIONS

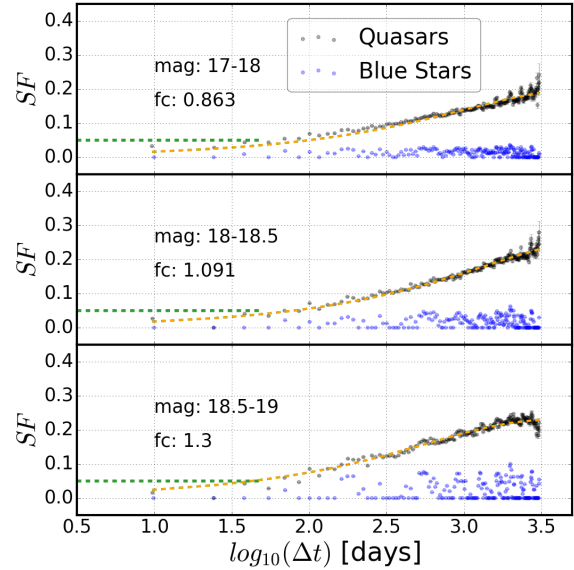
CRTS errors were underestimated at the 20-30 % level.

Implications: \* information from correspondence with M. Graham \* other recent findings that are based on short timescale CRTS variability - all would be called into question

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**Figure 4.** Three panels compare the Structure Function (SF) for quasars and blue stars in three bins based on their mean SDSS  $r$  magnitude. We correct CRTS errors using listed  $fc$  factors. Stars have a flat SF consistent with their lack of variability, whereas quasars have a nonzero variability. At short time scales, the quasar variability seen in CRTS data is consistent with that from SDSS, shown by horizontal green lines.

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