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Solving the puzzle of discrepant variability on monthly time scales implied by SDSS and CRTS datasets

Krzysztof Suberlak,[1⋆] Željko Ivezić, [1] Chelsea L. MacLeod,[2] Matthew Graham,[3] Branimir Sesar[4]
[1] *Department of Astronomy, University of Washington, Seattle, WA, United States*
[2] *Institute for Astronomy, University of Edinburgh, Royal Observatory, Edinburgh, United Kingdom*
[3] *Center for Data-Driven Discovery, California Institute of Technology, Pasadena, CA, United States*
[4] *National Optical Astronomy Observatory, Tucson, AZ, United States.*

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ABSTRACT

We present improved error analysis for the 3,800 CRTS (Catalina Real-Time Transient Survey) optical light curves for quasars from the Sloan Digital Sky Survey Stripe 82 catalog. SDSS imaging survey has provided a time-resolved photometric dataset which greatly improved our understanding of the quasar optical continuum variability: data for monthly and longer timescales are consistent with a damped random walk. Recently, newer data obtained by CRTS provided puzzling evidence for enhanced variability, compared to SDSS results, on monthly time scales. Quantitatively, SDSS results predict about 0.06 mag root-mean-square variability for timescales below 50 days, while CRTS data show about a factor of two larger rms for spectroscopically confirmed SDSS quasars. Our analysis presented here has successfully resolved this discrepancy as due to slightly underestimated photometric uncertainties provided by the CRTS image processing pipelines. The photometric error correction factors, derived from detailed analysis of non-variable SDSS standard stars that were re-observed by CRTS, are about $20-30\%$, and result in a quasar variability behavior implied by the CRTS data that is fully consistent with earlier SDSS results.

1 INTRODUCTION

Variability can be used to both characterize and select quasars in sky surveys . Ahtough various timescales of variability can be linked to physical parameters, such as accretion disk viscosity, or corona geometry (Kelly+2011, Graham+2014), the physical mechanism remains elusive, and most viable explanations include accretion disk instabilities (Kawaguchi + 1998), surface thermal fluctuations from magnetic field turbulence (Kelly+2009), coronal x-ray heating (Kelly+2011) (see Kozlowski 2016 for review). The diversity of physical scenarios explaining the origin of quasar variability led to a plethore of ways to characterize the varying brightness. The two most widely used approaches to describe variability of quasars are damped random walk (DRW) and structure function. The DRW model is more suited for lightcurves with typical cadence of days (Zu+2013, Kozłowski+2016), whereas an ensemble SF analysis is better for sparsely sampled lightcurves (Hawkins 2002, Vanden Berk 2004 , de Vries 2005, Schmidt 2010, Graham 2014, or review in Kozlowski 2016). Although CRTS data has been used for both an SF and DRW analysis [CITE WHERE], we use the SF approach, as more robust for sparsely sampled lightcurves than the DRW. [For a recent overview of the context for variability studies, see Lawrence+2016.]

Although SF can be defined in a variety of ways, it can be characterized by a simple broken power law (Schmidt+2010). At short timescales, the variability amplitude increases, following a steeper power law index, until the power law index starts to flatten above the characteristic timescale τ. This knee in the power law description may correspond to a transition from the stochastic thermal process driving the variability, to the physical response of the disk that successfully dampens the amplitude on longer timescales (Lawrence+2016, Kelly+2007,2009,2011, Collier+Peterson 2001 (linking the amplitude to the black hole mass)). Indeed, in x-rays quasars are described by a broken power law, where the break timescale is linked to the size of x-ray emitting region (Kelly+2011 in Graham+2014).

Altough previous studies found that $\tau > 100$ days (MacLeod+2011, Kozłowski+2016), recently, Graham+2014 used the SF, DRW, and Slepian Wavelet Variance (SWV) analysis for CRTS and SDSS S82 lightcurves. Using SWV on CRTS data they found characteristic time scales at QSO rest frame of $\log_2(\tau) = 5.75$) 54 days, and ($\log_2(\tau) = 8.2$) - 294 days. Additionally, using this method on S82 data they found a peak at $\log_2(\tau) = 7.25$, and for OGLE at $\log_2(\tau) > 6$. The short timescale of $\tau = 54$ days is surprising, as it is shorter by a factor of two than any previous estimates (MacLeod+2011, Zu+2013). We set out to reanalyze the CRTS data, and investigate the plausibility of this discrepant timescale.

2 DATA SETS

We study stars and quasars from Stripe 82, using the Sloan Digital Sky Survey and the Catalina Real-time Transient Survey data. Stripe 82 is a large (over 100 $\deg^2$), repeatedly observed reqion of the equatorial sky ($22^h24^m < \mathrm{RA} < 04^h08^m$ and $|\mathrm{Dec}| < 1.27deg$) (Sesar+2007, Suveges+2012).

2.1 Sloan Digital Sky Survey (SDSS)

We use the SDSS catalog data with robust, five-band near-simultaneous photometry for 9258 quasars, and 1006849 standard stars - we use it for photometric color information and sample selection. The quasar catalog contains spectroscopically confirmed quasars from the SDSS Data Release 7 (Abazajian+2009), based on SDSS Quasar Catalog IV (Schneider+2008, VizieR Online Data Catalog, 7252, 0), and was compiled by Macleod+2011 (see [1]) . The standard stars catalog ver. 2.6 was compiled by Ivezic+2007 (see [2]) .

2.2 Catalina Real-time Transient Survey (CRTS)

The CRTS data consists of white light (no filter) lightcurves - it was designed to find near-Earth objects, hence short intra-night cadence, to allow a rapid follow up (Graham+2015). Three survey telescopes (0.7m Catalina Sky Survey Schmidt in Arizona, 1.5m Mount Lemmon Survey telescope in Arizona, and the 0.5m Siding Spring Survey Schmidt in Australia) were equipped with identical, 4kx4k CCDs (see Djorgovski+2011 for technical details CRTS), taking 4 exposures each night. Although in principle white light magnitudes can be calibrated to Johnson V-band zero point (Drake+2013), we found it a redundant step for our analysis.

For our study we used a sample of 7932 spectroscopically confirmed S82 quasars, prepared by B. Sesar, from the Data Release 2, based on the list by MacLeod+2011. The majority (96%) of CRTS quasar lightcurves span the time of 7-9 years, with a mean sampling of 1 to 4 times per night, on 70 nights on average (see Fig.1, upper-left panel). Mean interval between epochs is 209 days (Fig.1 bottom-right panel), and the mean quasar magnitude is 19.5 mag.

Our comparison sample consists of CRTS lightcurves of 52133 randomly chosen 10% of the S82 standard stars catalog ver.2.6 (Ivezic+2007), extracted by B. Sesar from the CRTS DR2.

2.3 Catalog Matching

To enrich the information about each CRTS object with SDSS color information, we matched positionally CRTS data to SDSS data within S82 using astropy

[1] http://www.astro.washington.edu/users/ivezic/cmacleod/qso_dr7/Southern.html
[2] http://www.astro.washington.edu/users/ivezic/sdss/catalogs/stripe82.html

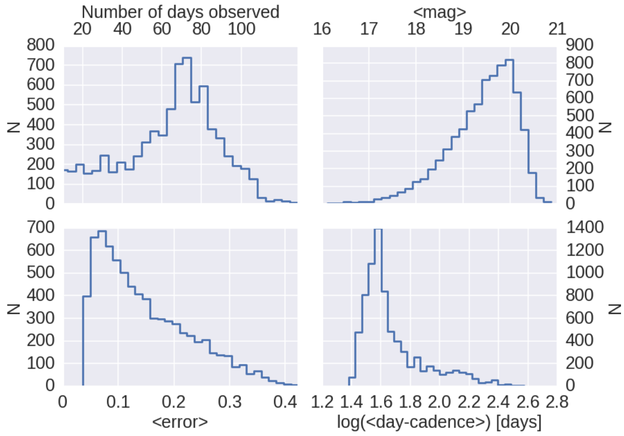

Figure 1. The sample of 7601 day-averaged quasar light-curves. The upper-left panel shows the distribution of the observations time span, i.e. $max(MJD) - min(MJD)$. The upper-right panel shows the average light curve magnitude. The bottom-left panel shows the light curve averaged error. The bottom-right panel shows the average number of days between epochs. Within that sample , 96% observations of quasars span the time of 7-9 years. 91.2% of quasars were observed between 1 to 4 times per night. We use only quasars with light curve averaged error smaller than 0.3, leaving 7108 quasars in the sample.

`match_to_catalog_sky` routine[3]. Given that the SDSS catalog has 100 times more stars than CRTS, we found an SDSS counterpart to all CRTS stars within 0.01 arcsec matching radius. However, since there is less SDSS quasars in the S82 catalog, and we found an SDSS counterpart to 7586 CRTS quasars within 0.36 arcsec. We ignored 15 quasars for which no SDSS counterpart was found within 1 arcsec.

2.4 Preprocessing

It is common to bin data to reduce noise, by averaging over timescales shorter than what is required by the science goals. In this study, the intra-night variability of CRTS lightcurves, with ≈ 4 epochs each night, is much shorter than considered timescales of order of tens of days. Thus, prior to analysis we day-averaged all CRTS light curves, following a procedure similar to Charisi+2016, replacing the magnitudes from the j-th night by their mean weighted by the inverse square of error:

$$m_j = \langle m_{ij} \rangle = \frac{\sum_{i=1}^{N} w_{i,j} m_{i,j}}{\sum_{i=1}^{N} w_{i,j}} \quad (1)$$

where $i = 1 \ldots N$, is the number of observations per night, with weights $w_{i,j} = e_{i,j}^{-2}$. We estimate the error on the weighted mean by the inverse square of the sum of weights:

$$\sigma_j(m_j) = \frac{1}{\sqrt{\sum_i w_{i,j}}} \quad (2)$$

[any CITATION ? is it a standard thing to do ?] Finally, to avoid unphysically small errors, we added in quadrature 0.01 mag to σ_j if $\sigma_j < 0.02\,mag$.

[3] http://docs.astropy.org/en/stable/coordinates/matchsep.html#matching-catalogs

2.5 Selection

We selected both quasars and stars using a combination of information from SDSS and CRTS. To find magnitude difference between different days we first required that the raw lightcurve has more than 10 epochs, which from initial 52131 stars and 7932 quasars left 49385 stars and 7707 quasars. We thus also removed those lightcurves with less than 10 days of observations, leaving 7601 quasars and 48250 stars. We also required that the lightcurve-average of day-error ($\langle \sigma_j(m_j) \rangle$) be less than 0.3^{mag} (see Fig.1). Since the raw distribution of errors peaks at lower values (mean of 0.19 for stars and 0.22 for quasars) than the distribution of the weighted mean errors (mean of 0.13 for stars and 0.15 for quasars), this cut only removes less than 10% of lightcurves. Our final sample consists of 7108 quasars and 42864 stars.

3 ANALYSIS METHODS

To analyze the quasar and stellar lightcurves we consider a relationship between measured data m_j at times t_j, and its "copy" shifted by Δt (Kozłowski+2016). We bin the data in bins of Δt, and calculate statistics that characterize the variability of stars and quasars. By splitting our sample of stars by color into "blue" and "red" we compare their variability properties to those of quasars in three magnitude bins.

3.1 Structure Function

The structure function is a well-studied approach to characterizing lightcurves (Vanden Berk +2004, de Vries+ 2005, Kozłowski+2016, Graham+2015) . To avoid the uncertain redshift estimate based on SDSS spectra that would be required to correct to the rest-frame variability, we use the observed frame time lags (like Schmidt+2010) (see Kozlowski+2016). The magnitude difference $\Delta m_{j,k} = m_j - m_k$ for $\Delta t_{j,k} = |t_j - t_k|$, and the errors added in quadrature : $\sigma_{j,k}^2 = \sigma_j^2 + \sigma_k^2$.

To study the statistical distribution of time-lag magnitude differences in an ensemble of quasars or stars we bin the data in bins of $\Delta t_{j,k}$, or for brevity Δt. For each object we prepared 'master' files containing $\Delta m_{j,k}$, Δt, $\sigma_{j,k}$. Even after day-averaging, with a median lightcure length of 70 days, each object contributes on average $\sum_{i=2}^{70}(i-1) = 2415$ $\Delta m_{j,k}$ points . Thus we have sufficient amount of pairwise time differences to study their statistical properties by splitting them into 200 linearly spaced bins of Δt. Bin number does not affect significantly the shape of the structure function, and 200 bins provide best resolution in affordable computational time, with a sizable number of $\Delta m_{j,k}$ in each bin.

With various theoretical definitions of structure function (see Kozłowski+2016 for overview), we adopt a view from Ivezic+2014, that *SF* corresponds to the intrinsic width of the $\delta m_{j,k}$ distribution $\mathcal{N}(\sigma,\mu)$. Each $\delta m_{j,k}$ has an error, assumed to be drawn from the Gaussian distribution with a known width e_i. Thus each $\delta m_{j,k}$ (called x_i in Ivezic+2014, and here for brevity), is drawn from a distribution with a total width $\sigma_{tot} = \sqrt{\sigma^2 + e_i^2}$.

Then the likelihood for a set of measurements $\{x_i\}$ is given by a product of likelihoods for each value of x_i:

$$p(\{x_i\}|\mu,\sigma,I) = \prod_{i=1}^{N} \frac{1}{\sqrt{2\pi}\sigma_{tot}} \exp\left(\frac{-(x_i-\mu)^2}{2\sigma_{tot}^2}\right) \tag{3}$$

Using uniform priors, the logarithm of the posterior pdf becomes :

$$L_p = const - \frac{1}{2}\sum_{i=1}^{N}\left(\ln(\sigma_{tot}^2) + \frac{(x_i-\mu)^2}{\sigma_{tot}}\right) \tag{4}$$

To find $SF = \sigma$, we would evaluate L_p on a grid of μ, σ, and marginalize over μ to find likelihood for σ:

$$p(\sigma|\{x_i\},I) = \int_0^\infty p(\mu,\sigma|\{x_i\},I)d\mu \tag{5}$$

The zero point of the first derivative of this likelihood - σ_0 - is the most likely value of σ. An alternative way is to find the $2D$ maximum of $\exp(L_p)$ to obtain simultaneously both μ_0 and σ_0.

However, this procedure is computationally expensive without any prior constraint on the bounds of μ_0 or σ_0.

Fortunately, it is possible to quickly find approximate values of σ_0 and μ_0. It turns out that sample median is a good estimator of μ_0, and σ_0 can be estimated by:

$$\sigma_0^2 = \zeta^2\sigma_G^2 - e_{50}^2 \tag{6}$$

where:

$$\zeta = median(\tilde{\sigma}_i)/mean(\tilde{\sigma}_i), \tag{7}$$

$$\tilde{\sigma}_i = (\sigma_G^2 + e_i^2 - e_{50}^2)^{1/2}, \tag{8}$$

$$\sigma_G = 0.741(Z_{75\%} - Z_{25\%}), \tag{9}$$

with Z is the sorted $\Delta m_{j,k}$ per bin, and $e_{50} = median(\sigma_{j,k})$.

Now, if errors were all equal ($e_i = e$), then $e_{50} = e$, and $\tilde{\sigma}_i = \sigma_G$, so that $\zeta = 1$, and thus $\sigma_0^2 = \sigma_G^2 - e^2$.

If errors were not all equal, but very small compared to σ_G, then $\tilde{\sigma}_i \rightarrow \sigma_G$, and $\zeta \rightarrow 1$, so that $\sigma_0^2 = \sigma_G^2 - e_{50}^2$, but since $e_{50} \ll \sigma_G$, $\sigma_0^2 \approx \sigma_G^2$. This explains why σ_G can be seen as an approximation of *SF* (see Kozłowski+16, eq.10).

Therefore, to find the best estimate of $SF = \sigma_0$, we evaluate 1000 boostrapped resamples of $\delta m_{j,k}$ in each δt bin, and thus find upper and lower limits on the approximate value of σ_0. We use these values as limits on our grid of μ, σ, on which we evaluate the full solution from L_p.

3.2 Statistics, sample construction

As described above, σ, σ_G and μ are all related in describing the structure function and variability of quasars, and thus we include them in Fig.2, as a function of Δt. As a guide to the width of the $\Delta m_{j,k}$ distribution, we also plot its standard deviation, i.e. the square root of the average of the squared deviations from the mean:

$$\sigma_{stdev} = \sqrt{\frac{\sum(\Delta m_{j,k} - \overline{\Delta m_{j,k}})^2)}{N_{bin}}} \tag{10}$$

Table 1. Count of stars and quasars, selected by their SDSS r-magnitude. For all objects we also required that the CRTS lightcurve error is smaller than 0.3*mag*

r-mag	red stars	blue stars	quasars
17-18	2993	2795	185
18-18.5	2087	1400	333
18.5-19	1496	2327	747

To consider the effect of stellar color on variability we divided stars into two SDSS g-i color bins: "red" stars with $1 < g-i < 3$, and "blue" stars with $-1 < g-i < 1$. We expect blue stars to be preferentially brighter, and have smaller variability than the red stars. See Table 1 for the number of stars and quasars in each color-magnitude bin.

4 RESULTS

5 CONCLUSIONS

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The SDSS is managed by the Astrophysical Research Consortium for the Participating Institutions. The Participating Institutions are the American Museum of Natural History, Astrophysical Institute Potsdam, University of Basel, University of Cambridge, Case Western Reserve University, University of Chicago, Drexel University, Fermilab, the Institute for Advanced Study, the Japan Participation Group, Johns Hopkins University, the Joint Institute for Nuclear Astrophysics, the Kavli Institute for Particle Astrophysics and Cosmology, the Korean Scientist Group, the Chinese Academy of Sciences (LAMOST), Los Alamos National Laboratory, the Max-Planck-Institute for Astronomy (MPIA), the Max-Planck-Institute for Astrophysics (MPA), New Mexico State University, Ohio State University, University of Pittsburgh, University of Portsmouth, Princeton University, the United States Naval Observatory, and the University of Washington.

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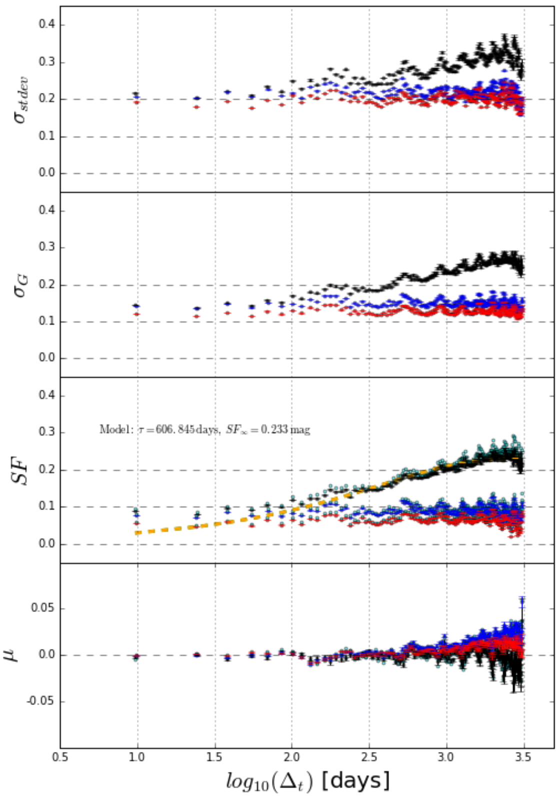

Figure 2. The four panels show statistics calculated for the subsample of 333 CRTS quasars (black points), 1400 "blue" stars (blue points), and 2087 "red" stars (red points), all chosen according to the SDSS r magnitude $18.5 < \mathrm{m} < 19$. Red and blue stars have $1 < \mathrm{g} - \mathrm{i} < 3$ and $-1 < \mathrm{g} - \mathrm{i} < 1$ respectively. All pairwise brightness differences in white light ($\Delta m_{i,j}$) are binned in linearly spaced 200 bins in $\Delta t_{i,j}$. For each bin, we calculate different statistics, from top to bottom panels: the standard deviation σ_{stdev}, the robust Gaussian deviation based on the interquartile range σ_G, the structure function SF, and the mean value of $\Delta m_{i,j}$ per bin:μ. Both μ and σ are found from the 2D maximum of the log-likelihood L_p on the $[\mu, \sigma]$ grid (see eq. 4, and Ivezic+2004). The signal modulation reflects differences in the number of $\Delta m_{i,j}$ points in each bin (from tens to hundreds of thousands per bin) - bigger number of points corresponds to larger spread of $\Delta m_{i,j}$ per bin (and thus slightly larger σ_{stdev}, σ_G, and SF). Yellow dashed line on the third panel traces the fiducial Damped Random Walk model. Note how both blue and red stars do not exhibit signs of variability as expected, whereas quasars (black) clearly show an intrinsic variability. At the low timescales $\log \tau < 1.7$ CRTS quasar SF departs from the fiducial model of Structure Function.

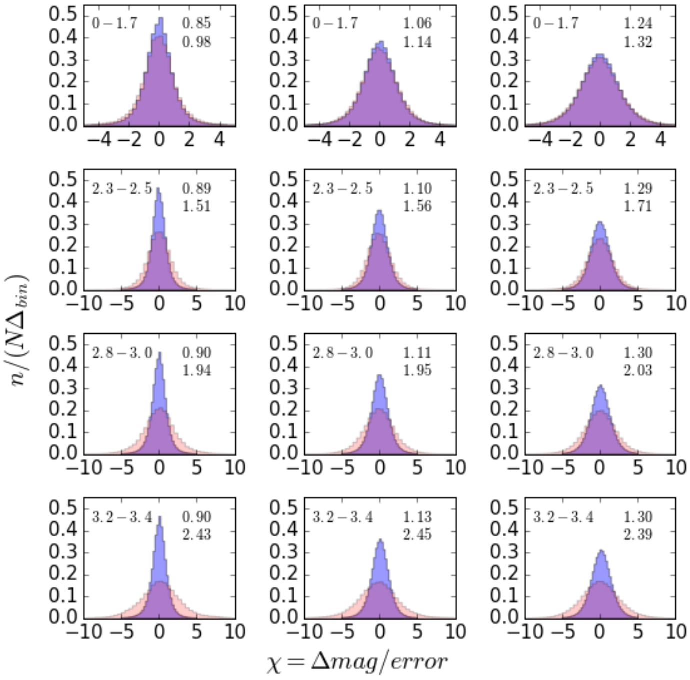

Figure 3. This grid of histograms shows $\chi = \Delta m/\mathrm{error}$ for CRTS blue stars (blue shading) and quasars (red shading), for bins of $\log\Delta t$- SDSS r magnitude. Vertically, from top to bottom, we iterate over bins of $\log\Delta t$: $0 < \log\Delta t < 1.7$ ($t < 50$ days) ,$2.3 < \log\Delta t < 2.5$, $2.8 < \log\Delta t < 3.0$, and $3.2 < \log\Delta t < 3.4$ (indicated by numbers in the upper left corner of each subplot). Horizontally, from left to right, we iterate over SDSS r-magnitude bins $17-18$, $18-18.5$, and $18.5-19$. Objects in each vertical strip were chosen according to the same magnitude cut, and all Δm points in a given $\log\Delta t$ range were binned together. The implied small quasar variability at short timescales is at the level measured by SDSS (indistinguishable from blue, non-variable stars). Numbers in the upper-right corner of each subplot are the robust width of stellar and quasar distributions of χ. Blue, bright stars in the left strip ($17-18$ r mag) have low σ_G, at the level of 0.9, and fainter blue stars (eg. right vertical strip, $18.5-19$ r mag) have higher $\sigma_G \approx 1.3$. Part of that increase is due to larger errors at fainter magnitude end. However, in each bin we expect that if errors for blue stars are correct, then $\sigma_G(\chi) = 1$. We use correction factors $f_c = \sigma_G(\chi_{blue}(\Delta t, mag))$ to correct for that effect. This implies that magnitude-difference errors $\sigma_{corr}(\Delta m) = f_c\sigma(\Delta m)$. If all raw errors were identical, it would also correspond to the linear correction of raw photometric errors by f_c. Quasars as intrinsically variable sources have a larger spread of χ than non-variable blue stars, but after applying the f_c correction their short-timescale χ at $t < 50$ days becomes much closer to 1, consistent with lack of variability (see Fig.4 for an illustration of the impact of f_c on SF of stars and quasars).

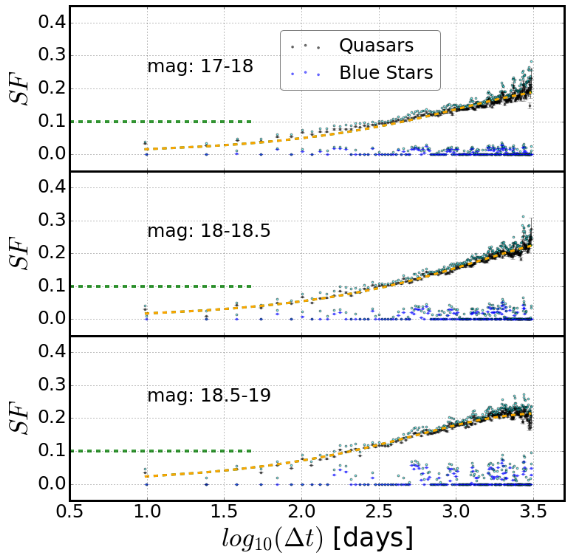

Figure 4. Three panels depict the impact that applying correction factors $f_c(\Delta t, mag)$ to errors $\sigma(\Delta m)$ has on the structure function (σ) for quasars and blue stars. In the middle of each panel we list the SDSS r-magnitude used to select quasars and stars for that magnitude bin. Note that with f_c the apparently discrepant variability of non-variable standard stars vanishes (the residual SF is consistent with the noise rms of 0.05 mag). The variability of quasars is reduced . We plot the observed frame timelags - see Fig.5 for the effect of converting that to the restframe timelags using known quasar redshifts from SDSS. The corrected SF of quasars at short time scales ($\log(\Delta t) < 1.7$) is consistent with lack of variability, consistent with SDSS results (upper limits of 0.1 mag marked by green dashed lines) (see MacLeod+2011).