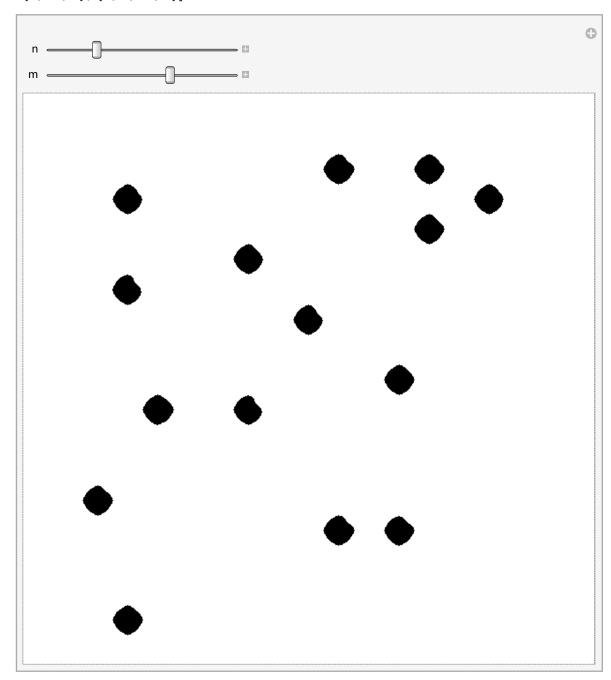
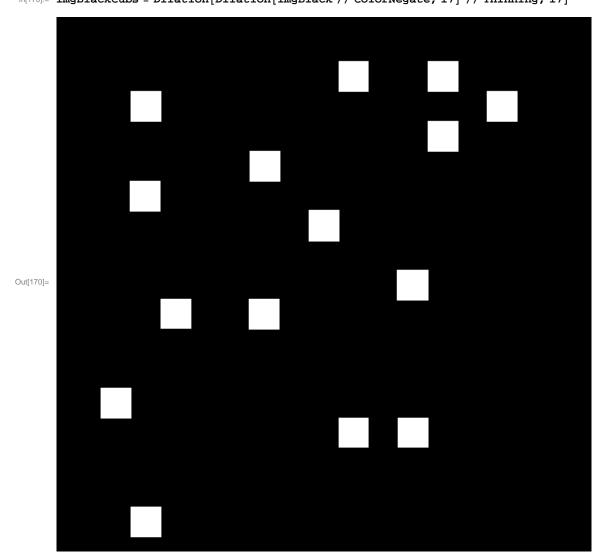
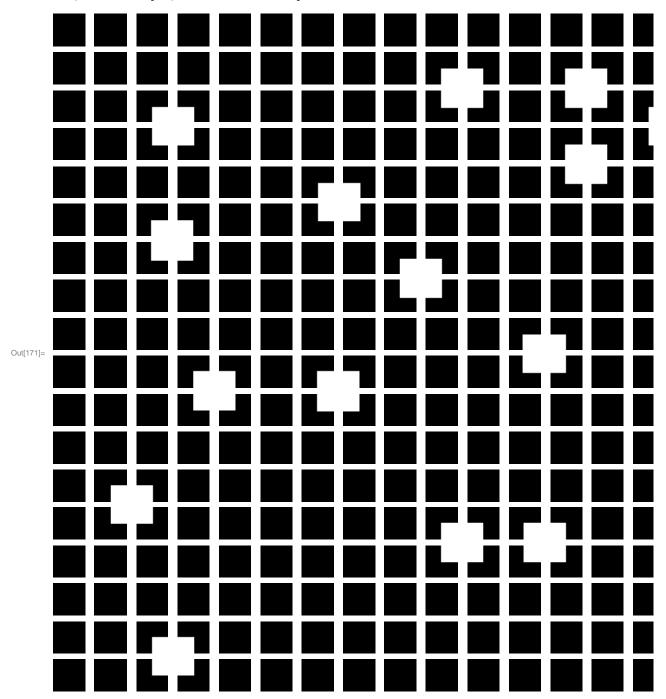


 $\label{lem:manipulate} $$ \mathtt{Manipulate[Closing[Opening[img1, DiskMatrix[n]], DiskMatrix[m]], } $$ \{n, 10, 1\}, \{m, 1, 10, 1\}]$$





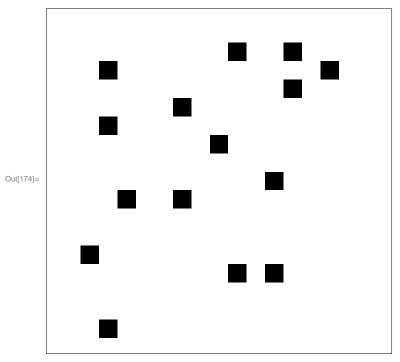
In[171]:= ImagePartition[imgBlackCubs, dim / 18] // Grid



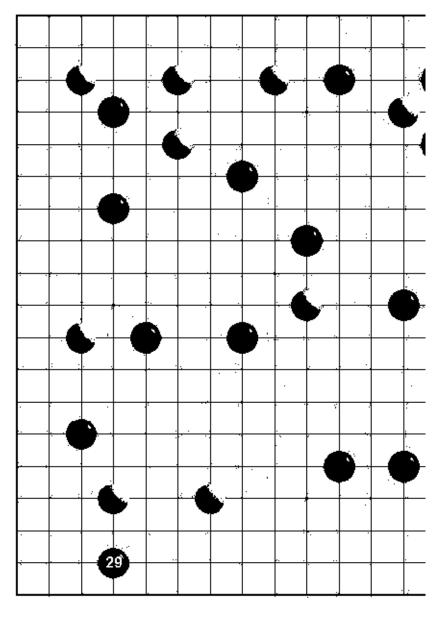
Out[173]//MatrixForm=

0 Ω Ω 0 0 0 0 Ω 0 0 0 0 1 0 0 0 0 1 Λ Ω 0 0 0 1 0 0 0 0 0 Ω 0 0 0 Ω 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 1 1 0 0 0 0 0 0 0 0 0 0 Ω Ω Ω Ω Ω 0 0 0 0 0 0 0 0 Ω Ω Ω 0 0 1 1 0 0 0 0 0 0 0 0 0 Ω 0 0 0 0 0 Ω Ω Ω Ω 0 0 0 Ω Ω Ω Ω Ω Λ 0 Λ 0 Ω 0 1 1 0 0 0 0 0 0 0 0 0 Ω 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 Ω Ω Λ $0 \ 0 \ 1$ Λ Λ Ω Λ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 1 1 0 0 0 0 0 0 0 Ω Ω Λ Ω 1 0 0 0 0 0 0 0 Ω 0

In[174]:= ArrayPlot[imageBlackMatrix]

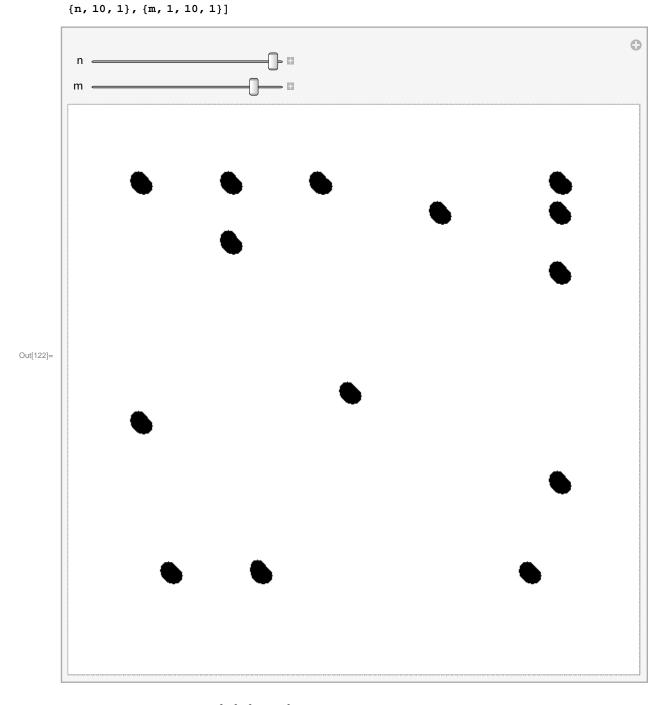


In[176]:= blackCoordinates = Total /@ Transpose@# / 4 & /@ clusters / 2 + 1 - 1 / 4;

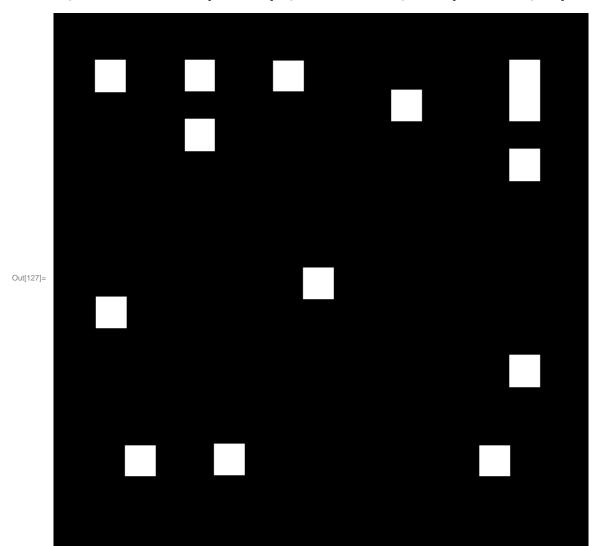


In[121]:= img2 = ImageAdd[ImageCrop@

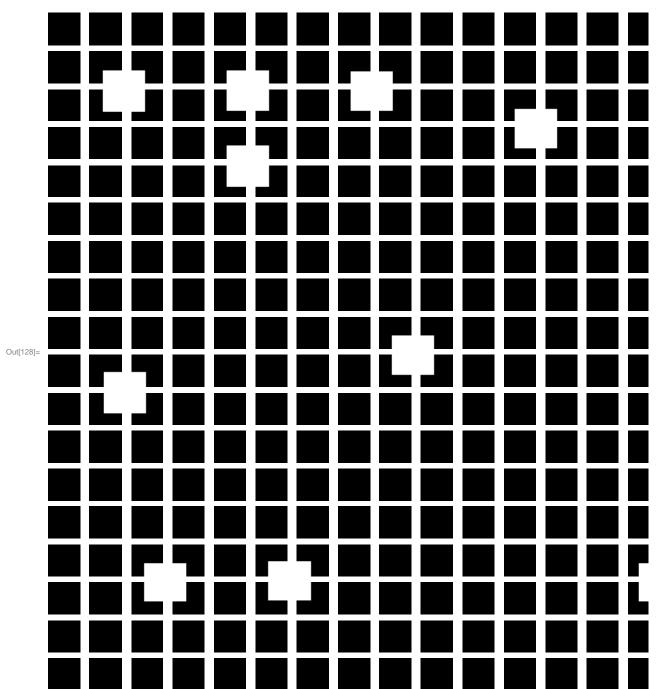
In[122]:= Manipulate[Closing[Opening[img2, DiskMatrix[n]], DiskMatrix[m]],



In[127]:= imgWhiteCubs = Dilation[Dilation[imgWhite // ColorNegate, 17] // Thinning, 17]



 $\label{eq:local_local_local_local} $$ \ln[128] := $$ $$ ImagePartition[imgWhiteCubs, dim / 18] // Grid$$$

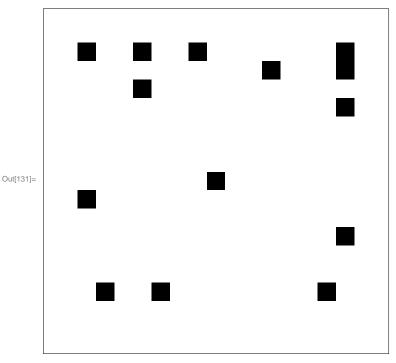


In[129]:= imageWhiteMatrix = ImageResize[imgWhiteCubs, {36, 36}] // ImageData; imageWhiteMatrix // MatrixForm

Out[130]//MatrixForm=

	AI OII																																				
(0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-	0	
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	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
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In[131]:= ArrayPlot[imageWhiteMatrix]



```
In[146]:= clusters = FindClusters[Position[imageWhiteMatrix, 1],
         14, Method \rightarrow {"Agglomerate", "Linkage" -> "Median"}]
```

```
 \text{Out}[146] = \left\{ \left\{ \left\{ 4, 4 \right\}, \left\{ 4, 5 \right\}, \left\{ 5, 4 \right\}, \left\{ 5, 5 \right\} \right\}, \left\{ \left\{ 4, 10 \right\}, \left\{ 4, 11 \right\}, \left\{ 5, 10 \right\}, \left\{ 5, 11 \right\} \right\}, \right. 
             \{\{4,\,16\}\,,\,\{4,\,17\}\,,\,\{5,\,16\}\,,\,\{5,\,17\}\}\,,\,\{\{4,\,32\}\,,\,\{4,\,33\}\,,\,\{5,\,32\}\,,\,\{5,\,33\}\}\,,
             \{\{6, 24\}, \{6, 25\}, \{7, 24\}, \{7, 25\}\}, \{\{6, 32\}, \{6, 33\}, \{7, 32\}, \{7, 33\}\},
             \{\{8,\,10\},\,\{8,\,11\},\,\{9,\,10\},\,\{9,\,11\}\},\,\{\{10,\,32\},\,\{10,\,33\},\,\{11,\,32\},\,\{11,\,33\}\},
             \{\{18,\,18\}\,,\,\{18,\,19\}\,,\,\{19,\,18\}\,,\,\{19,\,19\}\}\,,\,\{\{20,\,4\}\,,\,\{20,\,5\}\,,\,\{21,\,4\}\,,\,\{21,\,5\}\}\,,
             \{\{24,\,32\},\,\{24,\,33\},\,\{25,\,32\},\,\{25,\,33\}\},\,\{\{30,\,6\},\,\{30,\,7\},\,\{31,\,6\},\,\{31,\,7\}\},
             \{\{30, 12\}, \{30, 13\}, \{31, 12\}, \{31, 13\}\}, \{\{30, 30\}, \{30, 31\}, \{31, 30\}, \{31, 31\}\}\}
```

 $\ln[147]$: whiteCoordinates = Total /@ Transpose@# / 4 & /@ clusters / 2 + 1 - 1 / 4;

In[148]:= whiteCoordinates

```
\text{Out} [148] = \; \left\{ \left\{ \, 3 \,,\, 3 \,\right\} \,,\, \left\{ \, 3 \,,\, 6 \,\right\} \,,\, \left\{ \, 3 \,,\, 9 \,\right\} \,,\, \left\{ \, 3 \,,\, 17 \,\right\} \,,\, \left\{ \, 4 \,,\, 13 \,\right\} \,,\, \left\{ \, 4 \,,\, 17 \,\right\} \,,\, \left\{ \, 5 \,,\, 6 \,\right\} \,,
                      \{6, 17\}, \{10, 10\}, \{11, 3\}, \{13, 17\}, \{16, 4\}, \{16, 7\}, \{16, 16\}\}
```

```
In[178]:= linesColor = LightYellow; boardColor = LightGray;
                       board = {
                                    boardColor, Polygon[{{-10, -10}, {10, -10}, {10, 10}, {-10, 10}, {-10, 5}],
                                     linesColor,
                                     Table[Line[\{xx, -9\}, \{xx, 9\}\}], \{xx, -9, 9\}],
                                     Table[Line[\{\{-9, yy\}, \{9, yy\}\}\}], \{yy, -9, 9\}]
                        applycolor[{coordinates_, black}] := {Black, Disk[coordinates, .5]}
                        applycolor[{coordinates_, white}] := {White, EdgeForm[Black], Disk[coordinates, .5]}
                        showBlack[record_, movenumber_] :=
                           Graphics[
                                    board.
                                     Take[applycolor/@Partition[Riffle[record, black], 2, 2, 1, black],
                                         Min[Length[record], movenumber]]
                                }
                           ]
                        showWhite[record_, movenumber_] :=
                            Graphics[
                                    board,
                                     Take[applycolor/@Partition[Riffle[record, white], 2, 2, 1, white],
                                         Min[Length[record], movenumber]]
                                }
 In[218]:= showGame[whiteRecord_, blackRecord_, movenumber1_, movenumber2_] :=
                           Graphics[
                                    board.
                                     Take[applycolor /@ Partition[Riffle[whiteRecord, white], 2, 2, 1, white],
                                              Min[Length[whiteRecord], movenumber1]] ~Join ~
                                         Take[applycolor/@Partition[Riffle[blackRecord, black], 2, 2, 1, black],
                                              Min[Length[blackRecord], movenumber2]]
                                }
 In[219]:= coordinates = blackCoordinates ~ Join ~ whiteCoordinates
\text{Out}[219] = \left\{ \left\{ 3\,,\,11 \right\},\, \left\{ 3\,,\,14 \right\},\, \left\{ 4\,,\,4 \right\},\, \left\{ 4\,,\,16 \right\},\, \left\{ 5\,,\,14 \right\},\, \left\{ 6\,,\,8 \right\},\, \left\{ 7\,,\,4 \right\},\, \left\{ 8\,,\,10 \right\},\, \left\{ 10\,,\,13 \right\},\, \left\{ 11\,,\,5 \right\},\, \left\{ 1
                             \{11, 8\}, \{14, 3\}, \{15, 11\}, \{15, 13\}, \{18, 4\}, \{3, 3\}, \{3, 6\}, \{3, 9\}, \{3, 17\}, \{4, 13\},
                             \{4, 17\}, \{5, 6\}, \{6, 17\}, \{10, 10\}, \{11, 3\}, \{13, 17\}, \{16, 4\}, \{16, 7\}, \{16, 16\}\}
```

In[220]:= Manipulate[showGame[(blackCoordinates - 10).RotationMatrix[90 n Degree], (whiteCoordinates - 10).RotationMatrix[90 n Degree], movenumber1, movenumber2], ${\tt Button["NextMove", movenumber1 = movenumber1 + 1], \{n, 1, 4, 1\},}$ {movenumber1, 0, Length@whiteCoordinates, 1}, {movenumber2, 0, Length@blackCoordinates, 1}]

