

Full Name: \_\_\_\_\_

1. Consider the matrices

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$$A = \begin{bmatrix} -1 & 3 & 0 \\ 2 & 0 & 4 \end{bmatrix} \text{ and } B = \begin{bmatrix} 1 & 0 \\ 2 & 2 \\ 0 & 0 \end{bmatrix}$$

Find the matrix product  $AB$ .

2. Let
- $A$
- be a
- $3 \times 4$
- matrix. For the vector
- $\vec{b} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$
- , suppose that:

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(a) the vector  $\vec{v} = \begin{bmatrix} 2 \\ 0 \\ 4 \\ 3 \end{bmatrix}$  is a solution to  $A\vec{x} = \vec{b}$ , and(b)  $A$  has a reduced echelon form equal to  $\begin{bmatrix} 1 & 0 & 7 & 3 \\ 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 0 \end{bmatrix}$ Using this information, find all solutions to the homogeneous equation  $A\vec{x} = \mathbf{0}$ , as well as the nonhomogeneous equation  $A\vec{x} = \vec{b}$ , both written in parametric vector form.