

Full Name: _____

1. Consider the following 3×4 matrix:

$$A = \begin{bmatrix} 1 & 4 & 0 & -1 \\ 3 & 12 & 1 & -1 \\ 2 & 8 & 1 & 0 \end{bmatrix}$$

Let $T : \mathbb{R}^4 \rightarrow \mathbb{R}^3$ be a linear transformation defined as $T(\vec{x}) = A\vec{x}$.

- (a) What is the image of T ? Write it as span of some linearly independent vectors. 5
What kind of geometric object is it?

- (b) Find a basis of the kernel of T i.e. null space of A . 3

- (c) Is T one-to-one? Is T onto? 2

2. Suppose $\vec{v}_1 = \begin{bmatrix} 3 \\ 1 \\ 2 \end{bmatrix}$ and $\vec{v}_2 = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ form a basis \mathcal{B} of a vector space V . Suppose you are 5

given that $\vec{u} = \begin{bmatrix} 4 \\ -2 \\ 1 \end{bmatrix} \in V$. Find the coordinates of \vec{u} with respect to \mathcal{B} i.e. $[\vec{u}]_{\mathcal{B}}$.