

Please show **all** your work! Answers without supporting work will not be given credit. Write answers in spaces provided. You have 20 minutes to complete this Quiz. You can get MAXIMUM  $(8 + 7 + 5 =) 20$  marks.

Name: \_\_\_\_\_

1. Prove that the equation  $x^2 - x - 10 \sin x = 0$  has a positive solution.
2. Find the points on the curve  $y^2 = x(x^2 - 4)$  where it has a *vertical* tangent.
3. Does there exist a constant  $A$  such that the following function is continuous at  $x = 1$ ? If yes, find the value of  $A$ .

$$f(x) = \begin{cases} \frac{1}{Ax-2} & x \leq 1 \\ 3 - 2Ax + x^2 & x > 1 \end{cases}$$