Exam Assistance Note

 X_0 = Value in the Base Year, X_n = Value in the Recent Year

 \hat{X}_{n+k} = Predicted Value in the Year n+k

CBR= Crude Brith Rate (out of 1000 population), CDR= Crude Death Rate (out of 1000 population)

Percentage of Change	$\frac{X_n - X_0}{X_0} \times 100\%$	
Average Annual Growth Rate	$AAGR\% = \left(\frac{X_n}{X_0}\right)^{\left(\frac{1}{n}\right)} \times 100 - 100\%$	
Prediction in the year $n + k$ based on AAGR% and X_n	$\widehat{X}_{n+\frac{\mathbf{k}}{\mathbf{k}}} = X_n \times \left(\frac{100 + AAGR}{100}\right)^{\mathbf{k}}$	
Average Growth Rate Percentage (AGR%) based on CBR and CDR	$AGR\% = \frac{CBR - CDR}{10}\%$	

Related to Human Development Index (HDI)

PcGNI = Percapita Gross National Product

General Dimension Index :=
$$\frac{Actual \ Value - Min}{Max - Min}$$

$$Income\ Index: I_{Income} = \frac{log(PcGNI) - log\left(Minimun\ PcGNI\right)}{log\left(Maximum\ PcGni\right) - log\left(Minimun\ PcGNI\right)}$$

$$Education\ Index: I_{Education} = \frac{\sqrt{\mathit{I}_1 \times \mathit{I}_2}}{0.951}, \ where$$

 I_1 = Dimension Index for the Variable 'Mean Years of Adult Education'

 I_2 = Dimension Index for the Variable 'Expected Years of Schooling'

$$\label{eq:Homogeneous} \text{Human Development Index}: \text{HDI} = \left(I_{Life} \times I_{Education} \times I_{Income}\right)^{(\frac{1}{3})}$$

Name of Attribute	Minimum Value	Maximum Value
Life Expetancy	20	83.2
Mean Years of Adult Education	0	13.2
Expected Years of Schooling	0	20.6
Combined Education Index	0	0.951
Percapita GNI (PcGNI)	163	108211

Related to World Reserve Life Index (WRLI)

'World Reserve Life Index' provides an estimate for the years remaining before a specific world resource is expected to be completely depleted based on certain assumptions. Below are the related formula:

World Reserve Life Index (WRLI): If the consumption remains fixed as it was in the year T, then the Number years of the year for a complete depletion of the Resource is:

$$WRLI_{\frac{}{T}} = \frac{World Reserve at the End of a Year}{World Consumption in the Year} \frac{T}{T}$$

$$WRBLI_{\frac{}{T}} = \frac{World \text{ Base } Reserve \text{ at the End of a Year } \frac{T}{T}}{World \text{ Consumption in the Year } \frac{T}{T}}$$

World Reserve Life Index (WRLI): If the the consumption **Increases** by a Annual Average Growth Rate of AAGR % from the year T, then the Number years of the year for a complete depletion of the Resource is:

$$WRLI_{\textcolor{red}{\textbf{T, AAGR}}}^* = \frac{log\left(1 + WRLI_{\textcolor{red}{\textbf{T}}} \times \frac{AAGR}{100 + AAGR}\right)}{log\left(\frac{100 + AAGR}{100}\right)}$$

World Reserve Life Index (WRLI): If the consumption **Decreases** by a Annual Average Rate of AAGR % from the year T, then the Number years of the year for a complete depletion of the Resource is:

If
$$\left(1 - \text{WRLI}_{\boxed{\textbf{T}}} \times \frac{\text{AAGR}}{100 - \text{AAGR}}\right) > 0$$
, then
$$\text{WRLI}_{\boxed{\textbf{T}, \text{AAGR}}}^* = \frac{\log\left(1 - \text{WRLI}_{\boxed{\textbf{T}}} \times \frac{\text{AAGR}}{100 - \text{AAGR}}\right)}{\log\left(\frac{100 - \text{AAGR}}{100}\right)}$$

• $\left(1 - \text{WRLI}_{\overline{\mathbf{T}}} \times \frac{\text{AAGR}}{100 - \text{AAGR}}\right) \leq 0$, then the World Reserve on the material is never going to be depleted if we continue to decrease consumption at the specified rate. Eventually (hypothetically) the consumption will be almost zero before the resource gets depleted.

^{*}The above calculation is based on the assumption that AAGR% < 100%