

## HOMEWORK 16

**Note:** \* marked problems might be slightly more difficult or interesting than the unmarked ones.

- (1) Topology (Munkres), Chapter 4, Section 35, Exercise (1).
- (2) Topology (Munkres), Chapter 4, Section 35, Exercise (3).
- (3) Topology (Munkres), Chapter 4, Section 35, Exercise (4).
- (4) Topology (Munkres), Chapter 4, Section 35, Exercise (5).
- (5) Topology (Munkres), Chapter 4, Section 35, Exercise (7).
- (6)\* Show that a topological group  $G$  is  $T_0$  if and only if it is  $T_1$  if and only if it is  $T_2$ . (In fact you will see a stronger version of this problem in the last problem.)
- (7) Show that the following are topological groups.
  - (1)  $(\mathbb{R}_+, \times)$ .
  - (2)  $(S^1, \times)$ .
  - (3)  $\text{GL}_n(\mathbb{R})$  and  $\text{GL}_n(\mathbb{C})$ .
- (8) Topology (Munkres), Chapter 4, Section 22, Exercise (4).
- (9) Topology (Munkres), Chapter 4, Section 22, Exercise (5).
- (10) Topology (Munkres), Chapter 4, Section 22, Exercise (7).