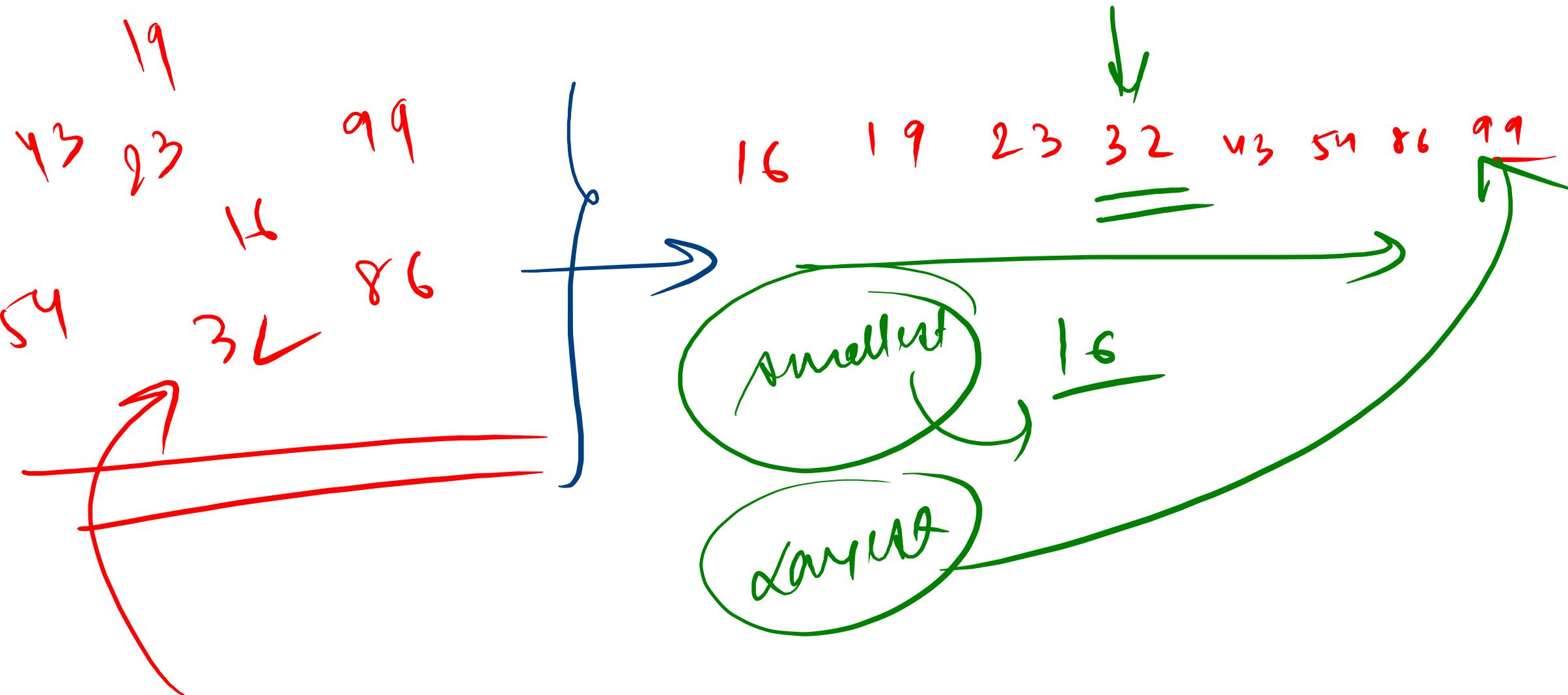


Morning

Arranging  
reading)

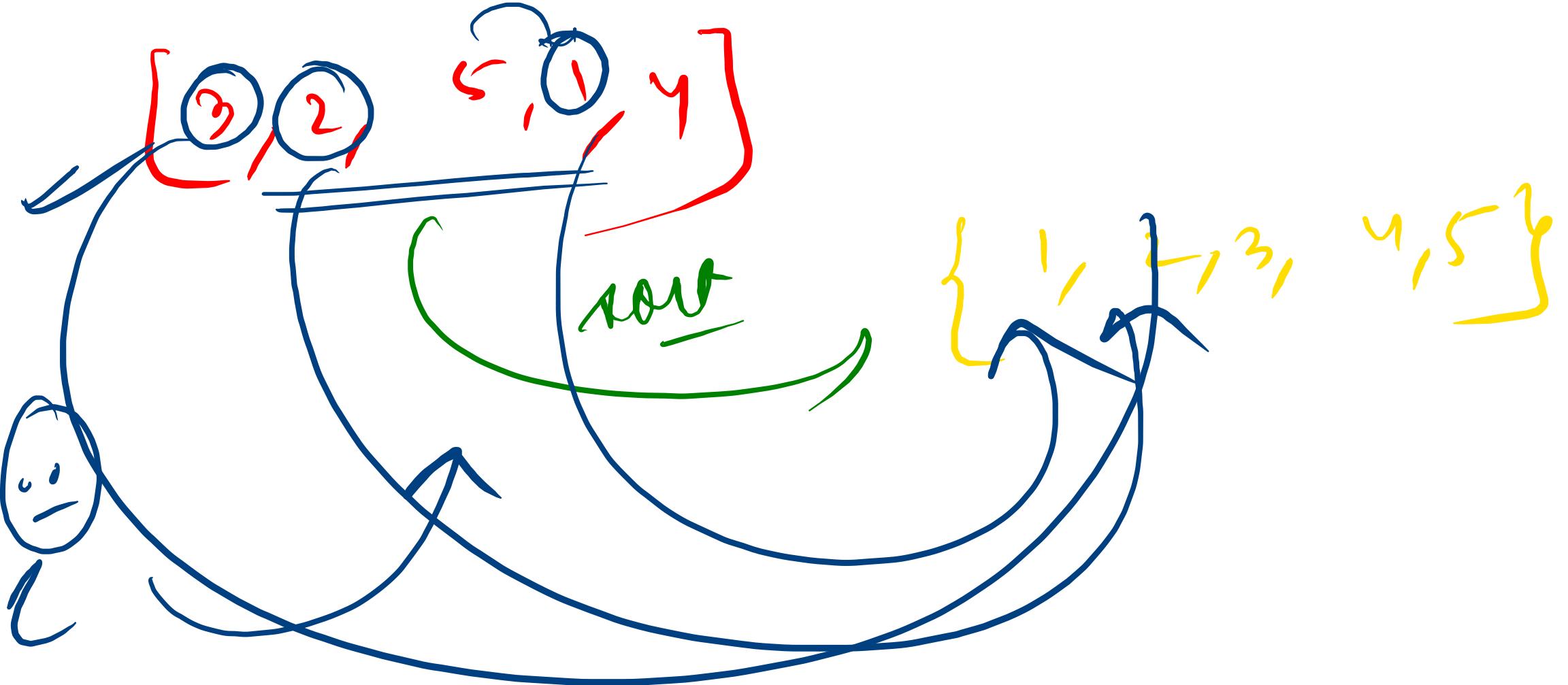
?



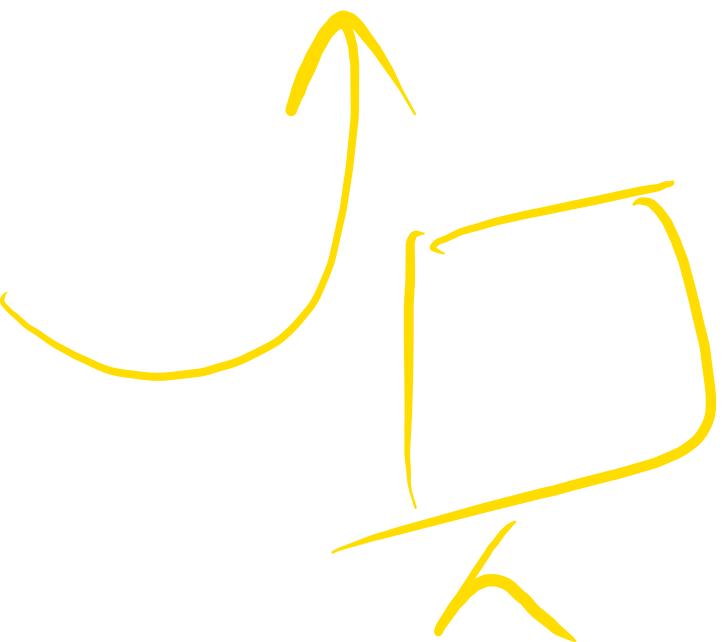
pointing)  data information]

~~join~~ what way?

How do we do it?



[ 3, 4, 1, 5, 9 -



connected

of grammaticality

will

$$\{ 3, 1, 2, 5, 4 \}$$

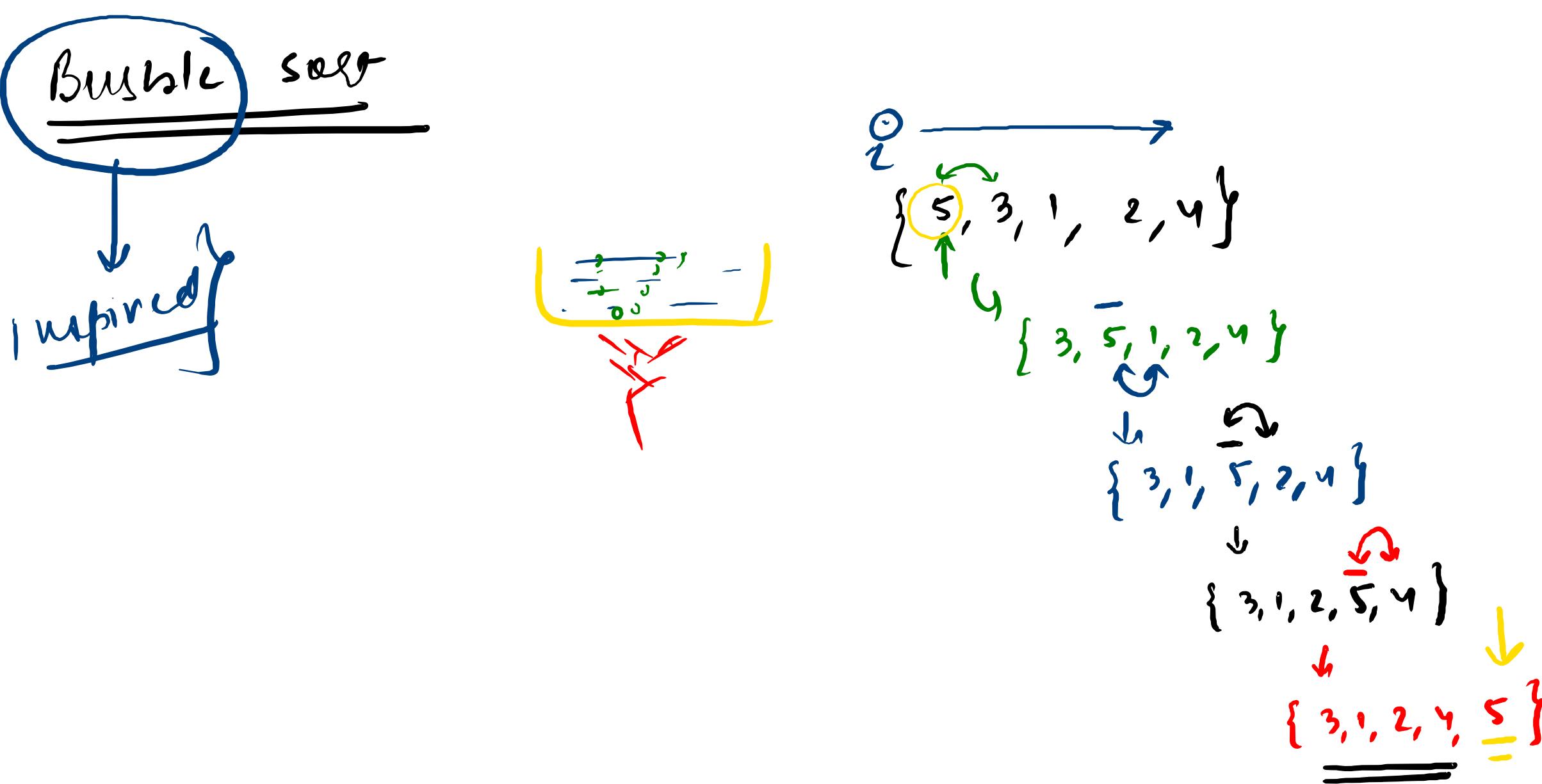

Three basic  
yrthm algorithms

- ① Bubble sort
- ② Selection sort
- ③ Insertion sort

Bubble sort

Tweak

smart



$2 \mid 3 \mid 4 \mid 1$

```
def bubbleSort(arr):  
    for i in range(len(arr)-1, 0, -1):  
        for j in range(i):  
            if(arr[j]>arr[j+1]):  
                arr[j], arr[j+1] = arr[j+1], arr[j]
```

swapping

$\{ 2, 3, 1, 4 \}$

$j \uparrow \quad \{ 2, 3, 1, 4 \}$

$j \uparrow \quad \{ 2, 1, 3, 4 \}$

$\underline{\{ 1, 2, 3, 4 \}}$

$j \uparrow \{ 4, 2, 3, 1 \}$

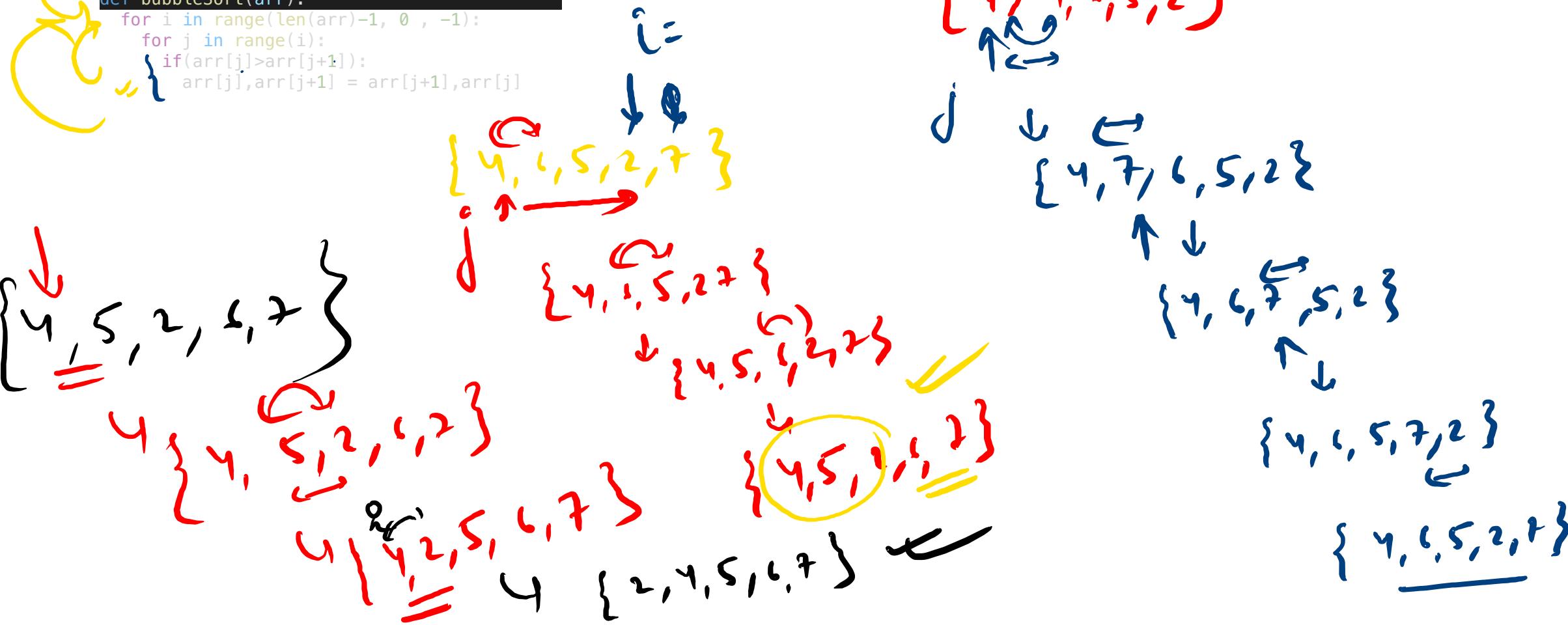
$j \uparrow \{ 4, 2, 3, 1 \}$

$\{ 2, 4, 3, 1 \}$

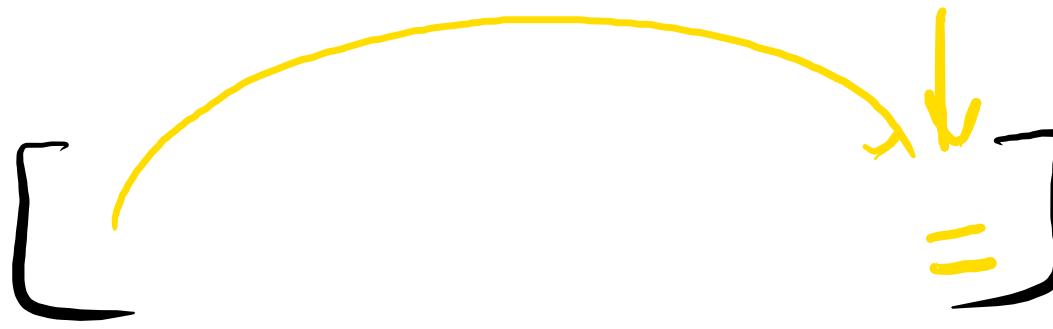
$\{ 2, 3, 4, 1 \}$

$\{ 2, 3, 1, 4 \}$

 def bubbleSort(arr):  
 for i in range(len(arr)-1, 0, -1):  
 for j in range(i):  
 if(arr[j]>arr[j+1]):  
 arr[j], arr[j+1] = arr[j+1], arr[j]



Bürolese



```
def bubbleSort(arr):  
    for i in range(len(arr)-1, 0, -1):  
        for j in range(i):  
            if(arr[j]>arr[j+1]):  
                arr[j], arr[j+1] = arr[j+1], arr[j]
```

$$T_C \underset{\sim}{=} O(n^2)$$

worst case?

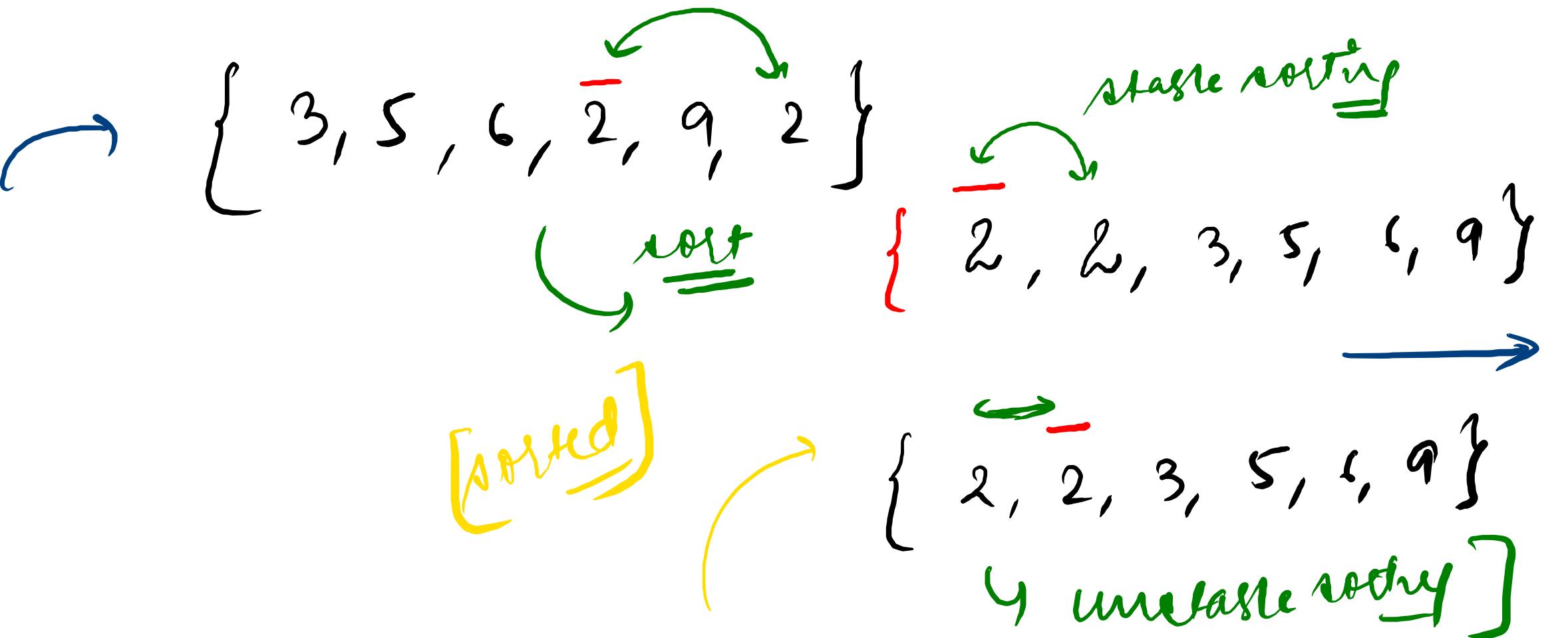
$$\{5, 4, 3, 2, 1\}$$

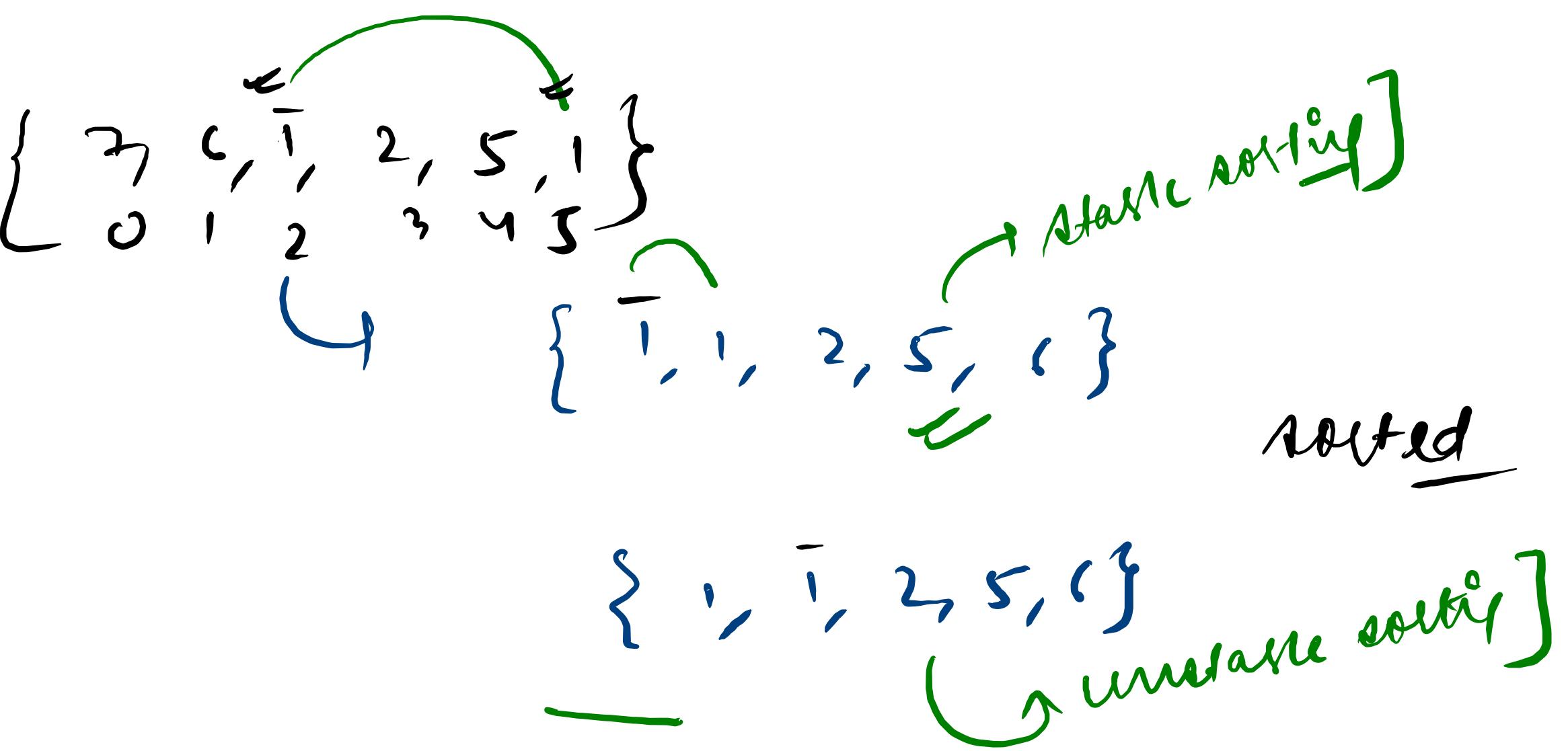
g

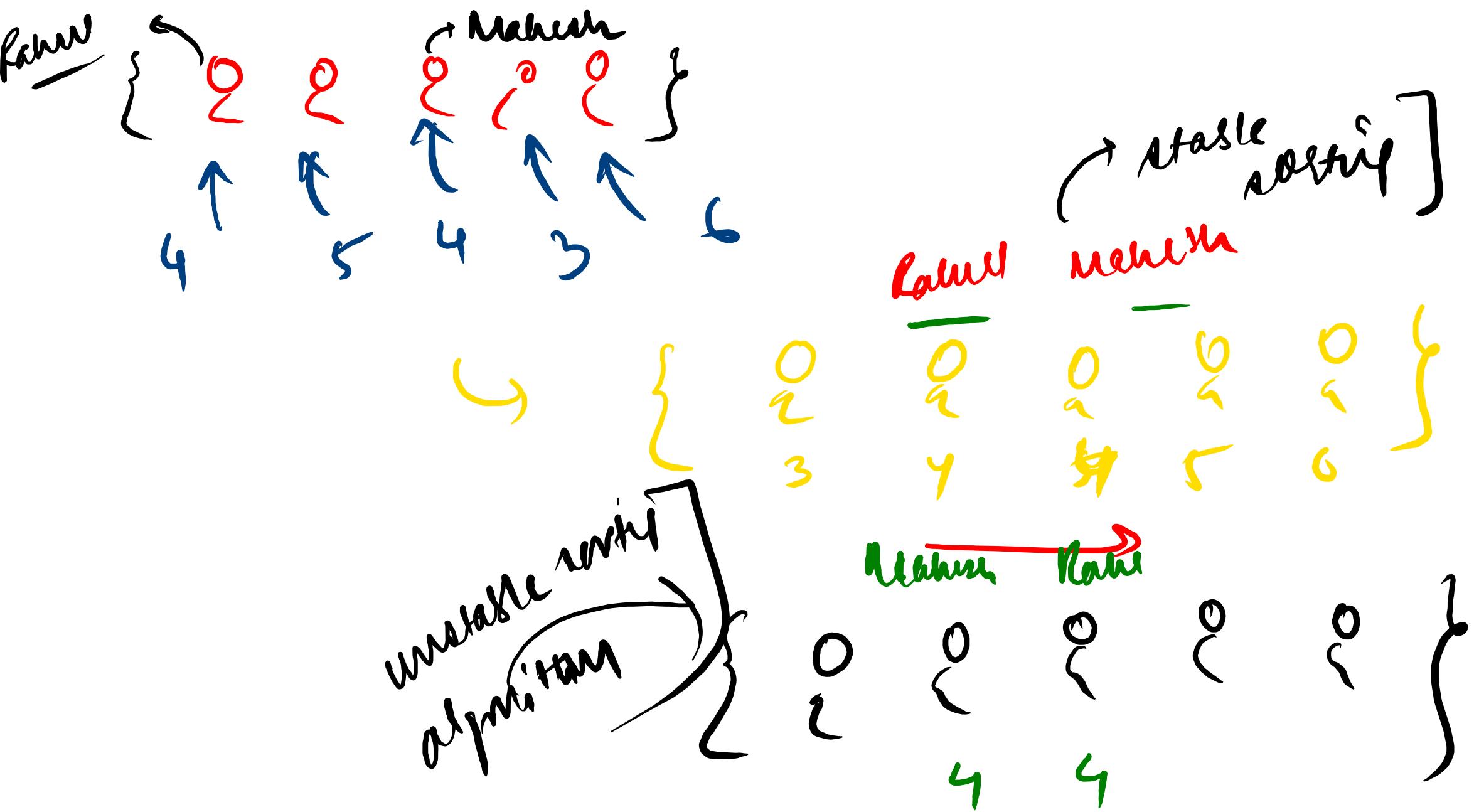
time complexity

worst case:  
comparisons ?  $\rightarrow n^2$   
swapping  $\propto n^2$

solving}      ↗ stable sorting  
                        ]      ↗  
                        Unstable sorting





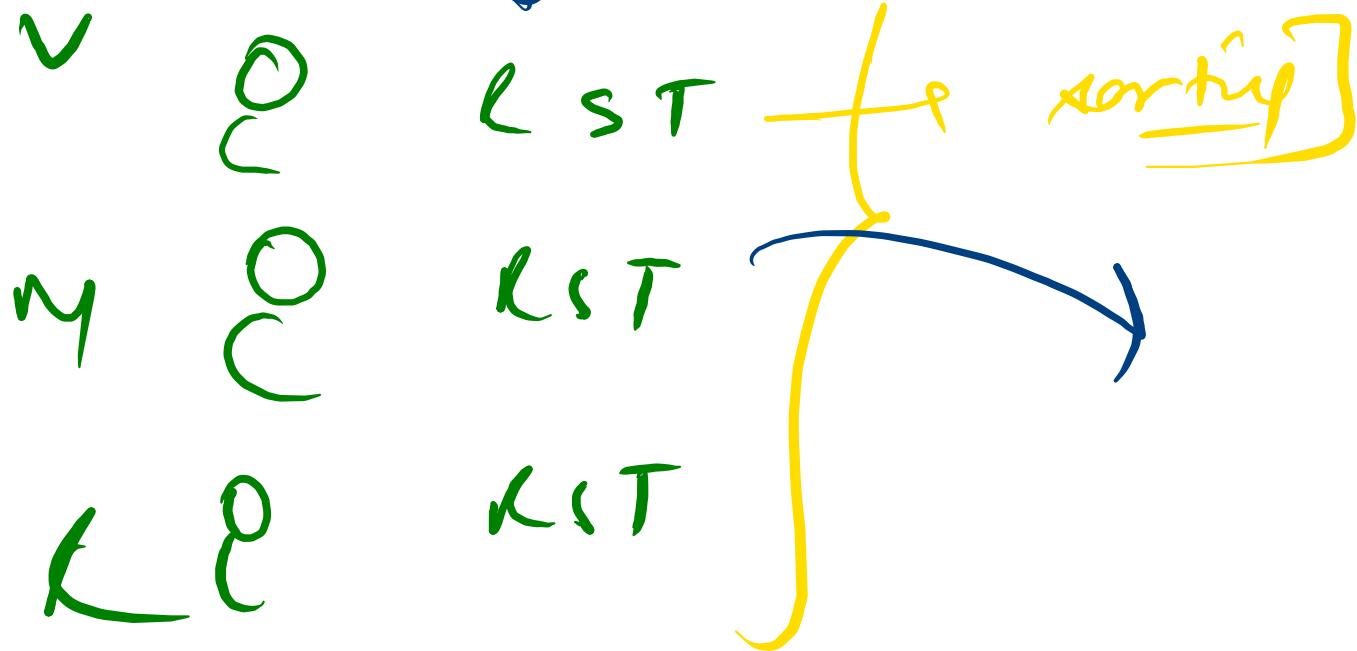


Fear Measles

Watts App

[Unit names retired]

↓ sort the Measles



Unstable  
entry

## → Stable sort

```
def bubbleSort(arr):  
    for i in range(len(arr)-1, 0 , -1):  
        for j in range(i):  
            if(arr[j]>arr[j+1]):  
                arr[j],arr[j+1] = arr[j+1],arr[j]
```

{ 1, 2, 1, 3, 4 }

{ 1, 2, 3, 1, 4 }

{ 1, 2, 1, 3, 4 }

{ 1, 2, 3, 1, 4 }

{ 1, 2, 1, 3, 4 }

{ 1, 2, 3, 1, 4 }

{ 1, 2, 1, 3, 4 }

{ 3, 1, 2, 4, 1 }

{ 1, 3, 2, 4, 1 }

{ 1, 2, 3, 4, 1 }

{ 1, 2, 3, 4, 1 }

{ 1, 2, 3, 1, 4 }

```
def bubbleSort(arr):  
    for i in range(len(arr)-1, 0 , -1):  
        for j in range(i):  
            if(arr[j]>arr[j+1]):  
                arr[j],arr[j+1] = arr[j+1],arr[j]
```

→  $O(n^2)$

bubble sort

[1, 2, 3, 4, 5]

→  $\cup O(n^2)$

$n^2 \times$

visit

```
def bubbleSort(arr):
```

```
    for i in range(len(arr)-1, 0, -1):
```

```
        for j in range(i):
```

```
            if(arr[j]>arr[j+1]):
```

```
                arr[j],arr[j+1] = arr[j+1],arr[j]
```

left element is being compared  
current

{ 3, 5, 4, 2 }

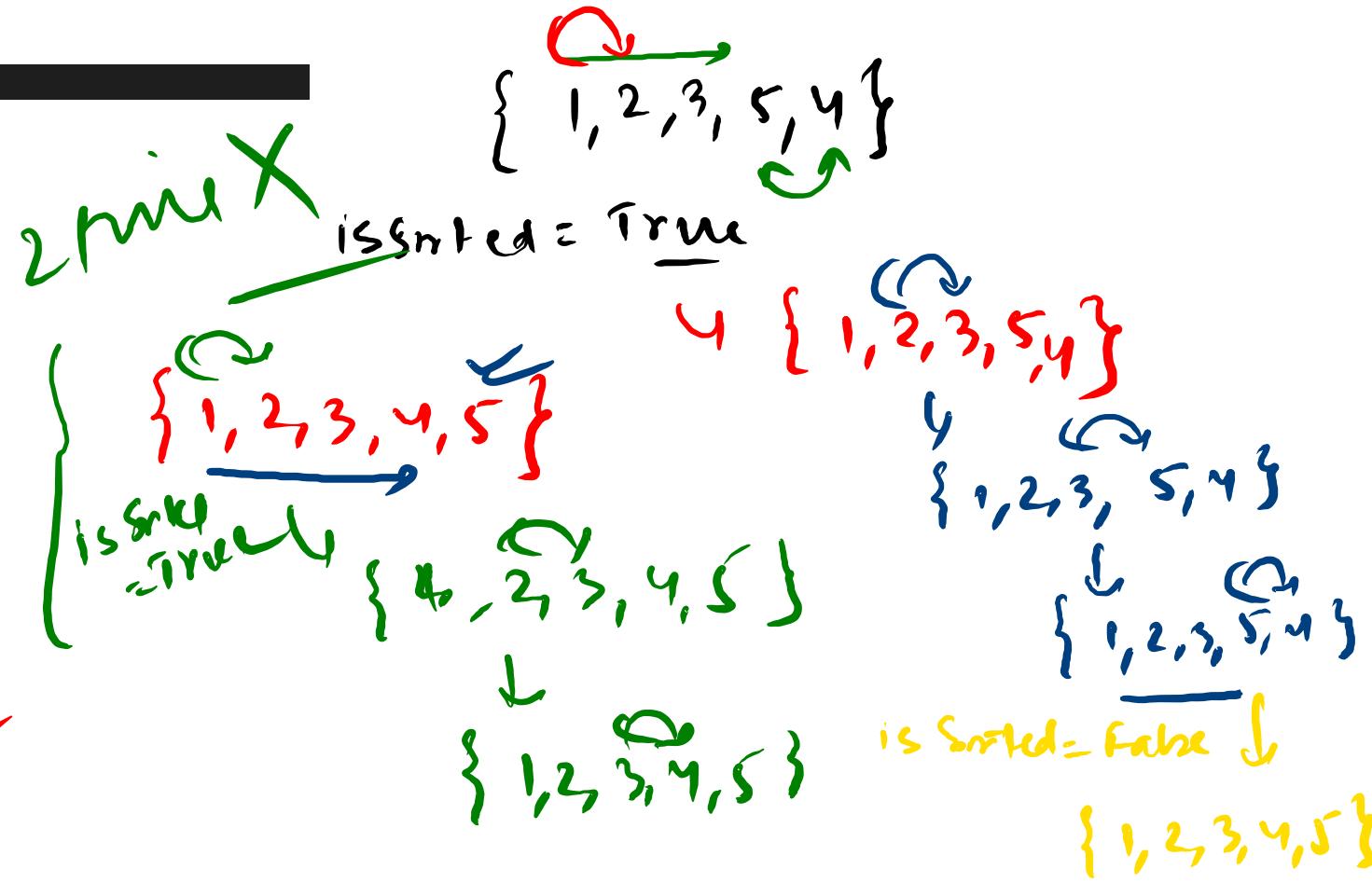
{ 2, 3, 4, 5 } → sorted

```

def bubbleSortOptimized(arr):
    for i in range(len(arr)-1, 0, -1):
        isSorted = True
        for j in range(i):
            if arr[j] > arr[j+1]:
                isSorted = False
                arr[j], arr[j+1] = arr[j+1], arr[j]
        if isSorted:
            print("Array is already sorted")
            break

```

fewer swaps  
 worst case  $O(n^2)$   
~~better  $O(n)$~~



```
def bubbleSort(arr):
    for i in range(len(arr)-1, 0 , -1):
        for j in range(i):
            if(arr[j]>arr[j+1]):
                arr[j],arr[j+1] = arr[j+1],arr[j]
```

sorted

$n$

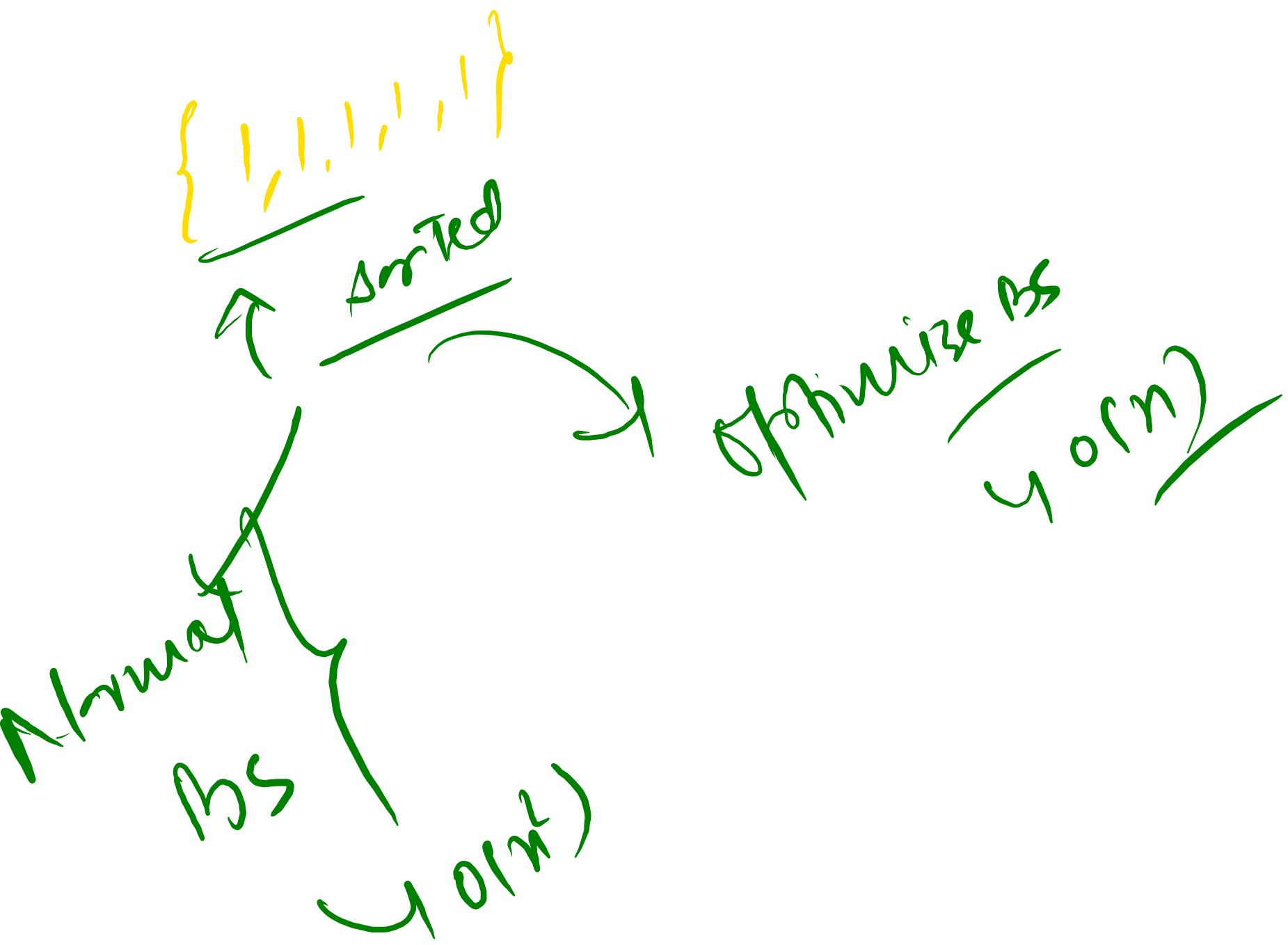
$n^2$

{ 1, 2, 3, 4, 5 }

$O(n)$

```
def bubbleSortOptimized(arr):
    for i in range(len(arr)-1, 0 , -1):
        isSorted = True
        for j in range(i): → n time (n-1)
            if(arr[j]>arr[j+1]):
                isSorted = False
                arr[j],arr[j+1] = arr[j+1],arr[j]
        if isSorted : → True
            print("Array is already sorted")
            break
```

$\rightarrow TC = O(n)$



```
for i in range (10)  
    print (sift)
```

(  
+  
for i in range (10)  
 for i in range (10)  
 print sift'

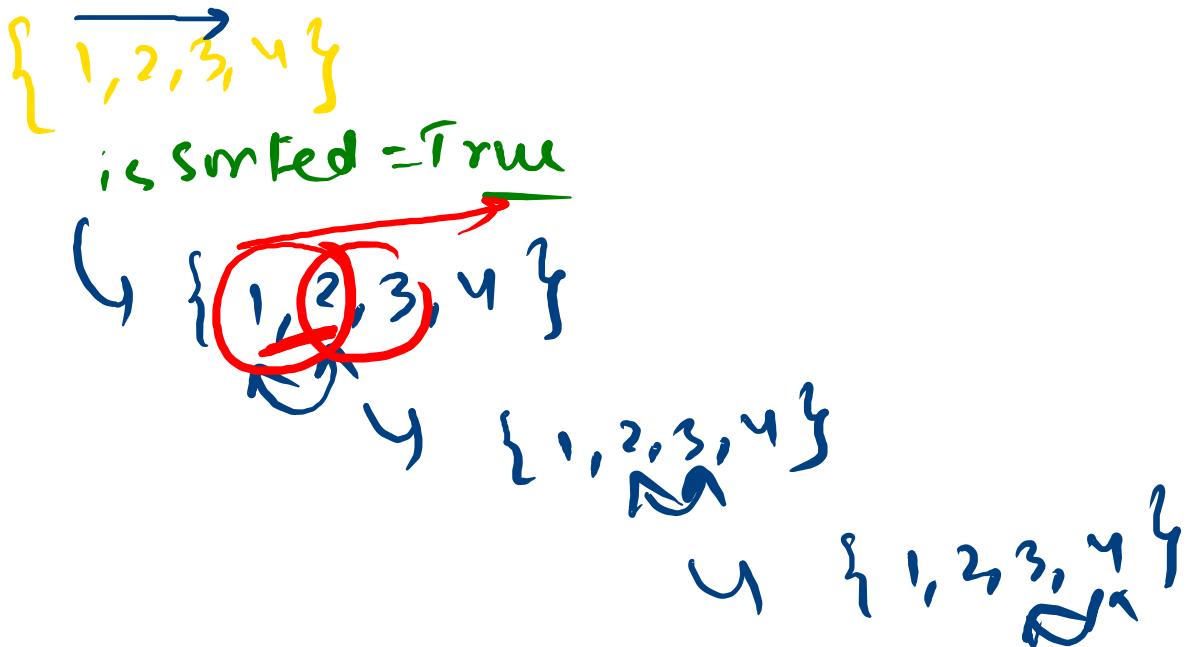
n  
 ↗ for i in range(n)  
 ↗ for j in range(i)  
 ↘ (n-1)  
 ↗ print("Hello")  
 TotalNr of operations  
 =  $\frac{n(n-1)}{2}$   
 =  $\frac{n^2 - n}{2}$

No of Operations  
 = No of Hello printed  
 $= (n-1) + (n-2) + (n-3)$   
 + ... (1)

$Tc \in O(n^2)$

Time complexity  
No of execution is  
proportional to the input size

```
def isSorted(arr):  
    isSorted = True  
    for i in range(len(arr)-1):  
        if arr[i]>arr[i+1]:  
            isSorted = False  
            break  
    if isSorted:  
        print("Array is sorted")  
    else:  
        print("Array is not sorted")
```



$$\{3, 1, 2, 4, 6, 5\}$$

9  
4     $\{1, 3, 2, 4, 6, 5\}$

selection sort

selection

The diagram illustrates the selection sort algorithm. It features a blue oval containing the word "selection". Two black lines extend from the top of this oval to a bracket located below it. This bracket groups the words "selection" and "sort", indicating that both terms refer to the same process.

$\{3, 2, 1, 4, 5\}$ 

see the smallest ①

x ↓  
 $\{1, 2, 3, 4, 5\}$

② → see the smallest

4 {1, 2, 3, 4, 5} ③

← {1, 2, 3, 4, 5}

$\{5, 4, 3, 2, 1\}$

①

smallest

①

$\{1, 4, 3, 2, 5\}$

②

next smallest ↗ ②

$\{1, 2, 3, 4, 5\}$

smallest

$\{1, 2, 3, 4, 5\}$

posted

$\{5, 4, 8, 9, 2, 1\}$

select the smallest  $\rightarrow$  !

$\{1, 4, 8, 9, 2, 5\}$

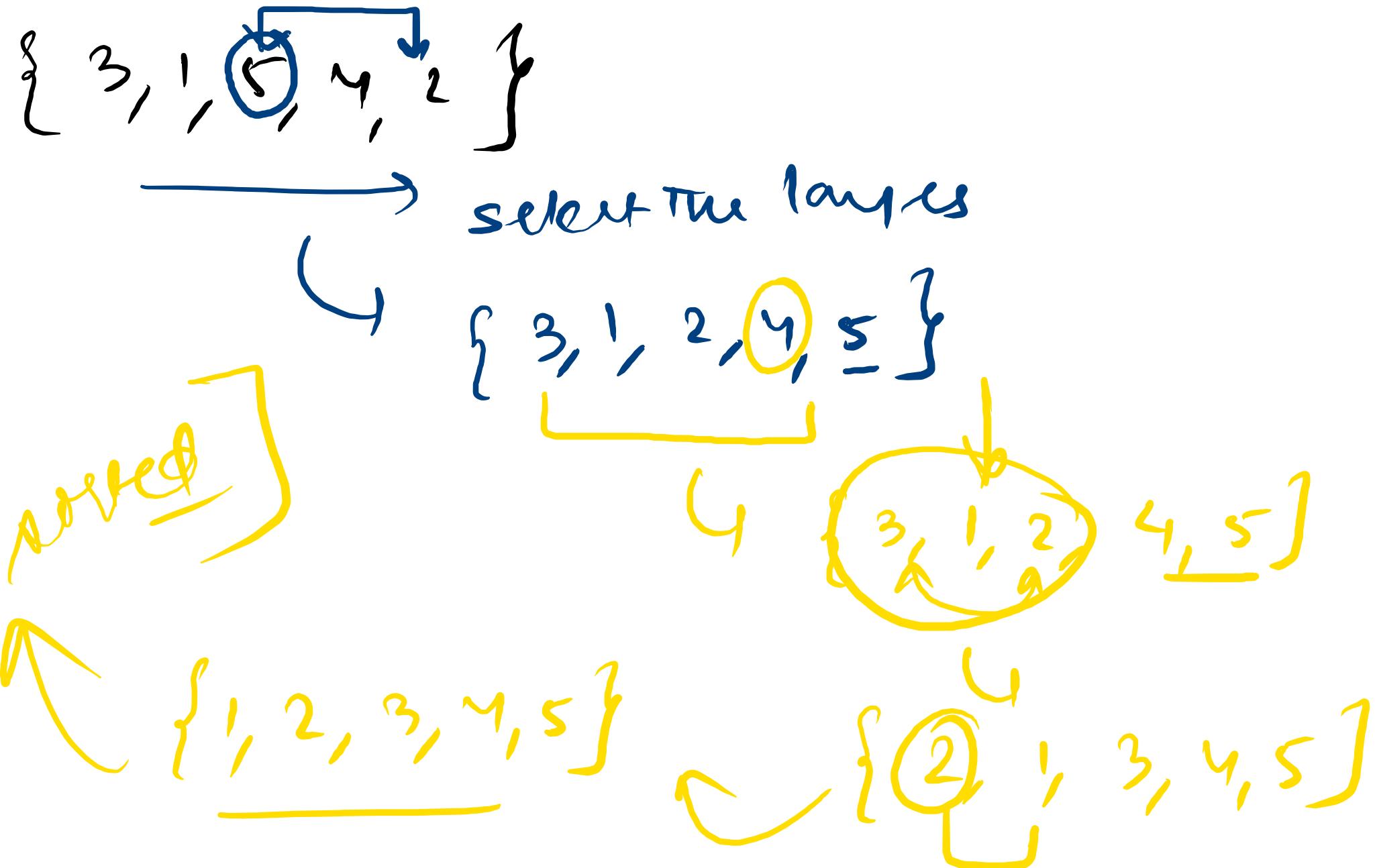
smallest  $\rightarrow$  ?

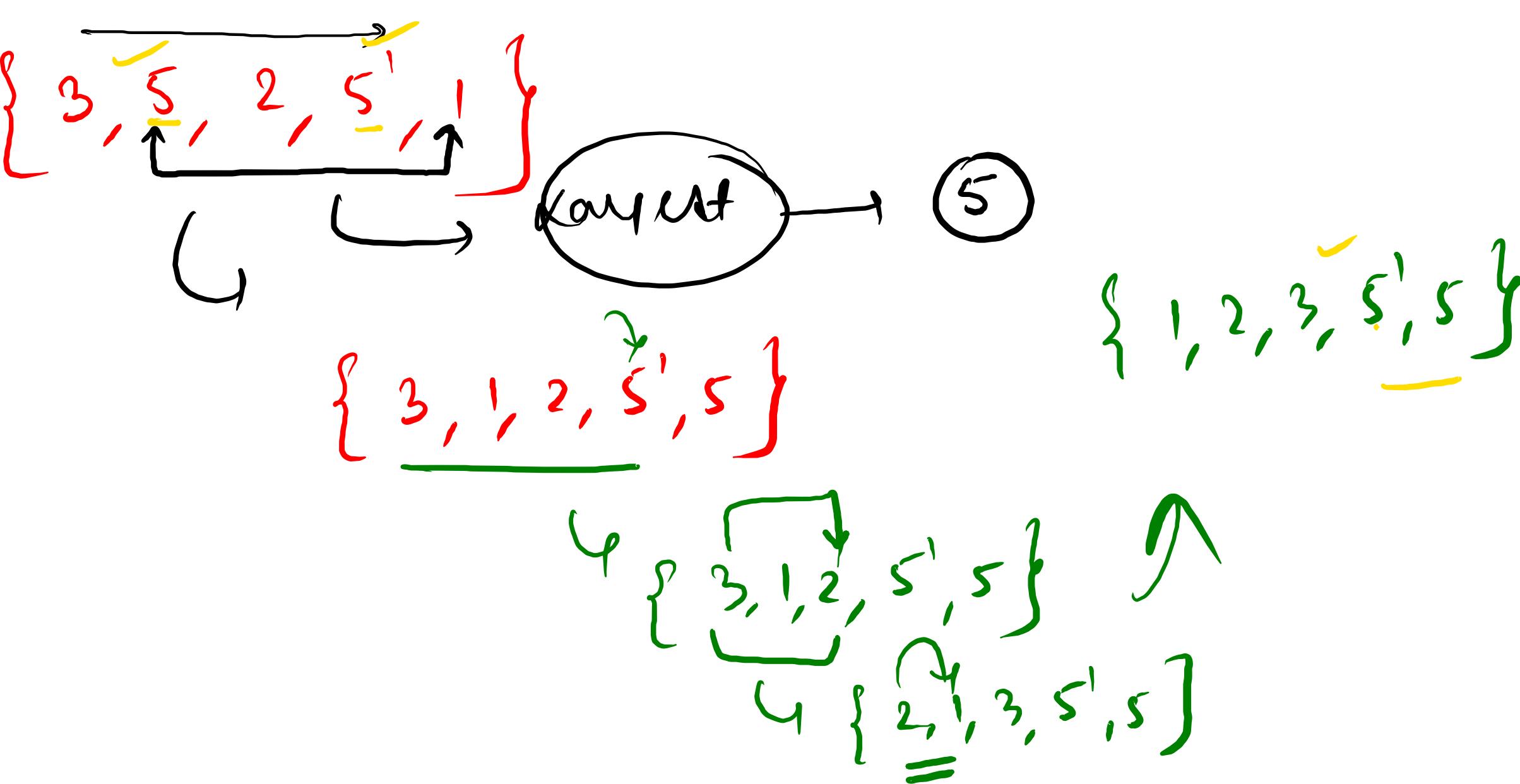
$\{1, 2, 5, 4, 9, 8\}$

$\{1, 2, 8, 9, 4, 5\}$

$\{1, 2, 5, 4, 8, 1\}$

$\{1, 2, 5, 4, 9, 8\}$





$\{1, 2, 6, 5, 1, 6\}$

start num

$\downarrow \{1, 2, 6, 5, 1, 6, 1\}$

$\{1, 1, 1, 2, 5, 1, 1\}$

$\downarrow \{1, 1, 1, 5, 2, 1, 1\}$

$\downarrow \{1, 1, 1, 2, 5, 1, 1\}$

start num

$\downarrow \{1, 1, 1, 5, 2, 1, 1\}$

```
#Selection Sorting
def selectionSort(arr):
    for i in range(len(arr)):
        min = i
        for j in range(i+1, len(arr)):
            if arr[j] < arr[min]:
                min = j
        #Find the smallest values
        arr[i], arr[min] = arr[min], arr[i]
```



Unstable

```
#Selection Sorting
def selectionSort(arr):
    for i in range(len(arr)):
        min = i
        for j in range(i+1, len(arr)):
            if arr[j] < arr[min]:
                min = j
        #Find the smallest values
        arr[i], arr[min] = arr[min], arr[i]
```

Comparisons

$O(n^2)$

Swaps

$\rightarrow \propto n^2$

n

Better performance

$O(n^2)$

$\propto n^2$

$\propto n^2$

def bubbleSort(arr):

```
for i in range(len(arr)-1, 0, -1):
    for j in range(i):
        if(arr[j]>arr[j+1]):
            arr[j], arr[j+1] = arr[j+1], arr[j]
```

Stable

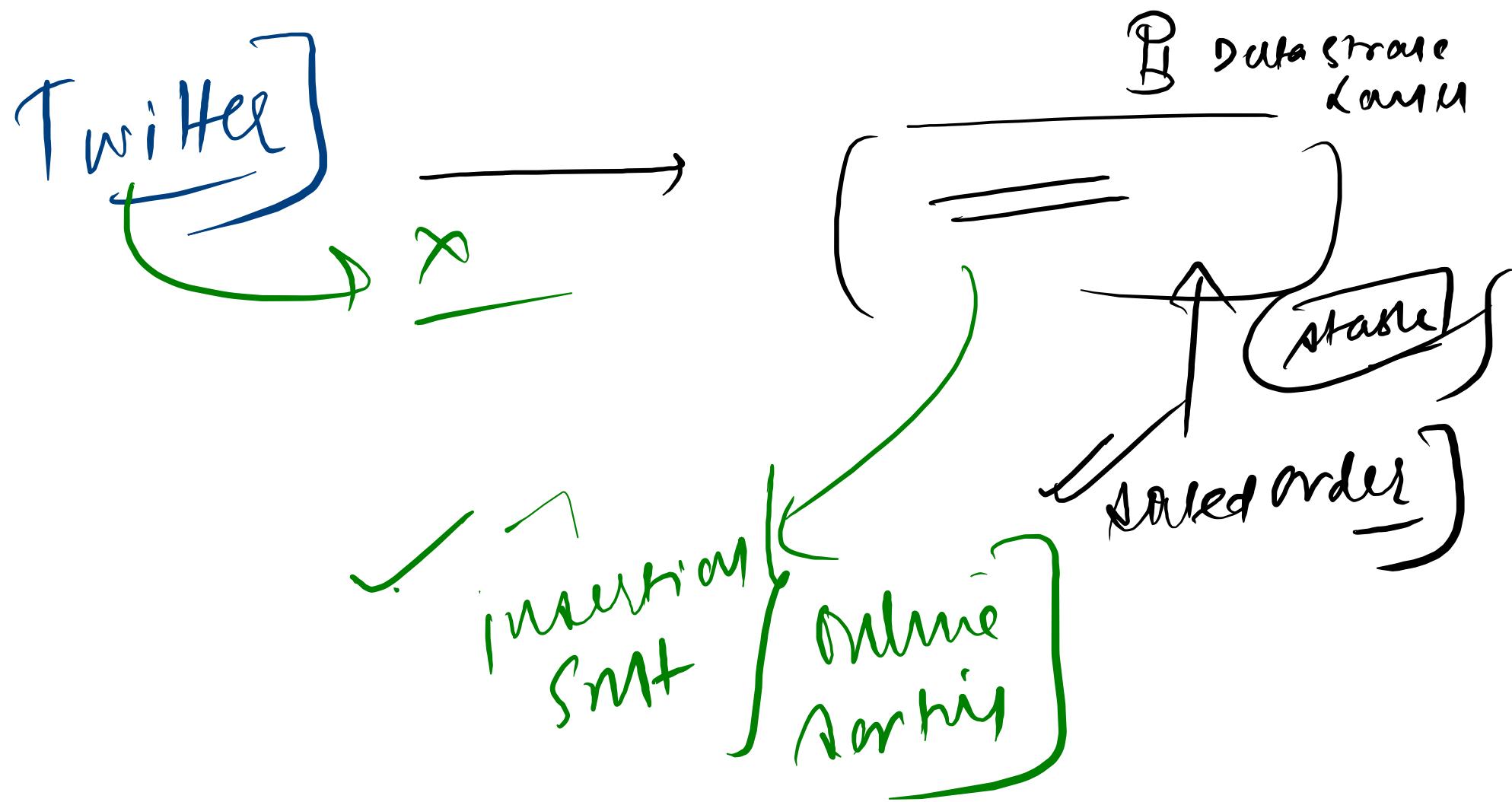
```
#Selection Sorting
def selectionSort(arr):
    for i in range(len(arr)):
        min = i
        for j in range(i+1, len(arr)):
            if arr[j] < arr[min]:
                min = j
        #Find the smallest values
        arr[i], arr[min] = arr[min], arr[i]
```

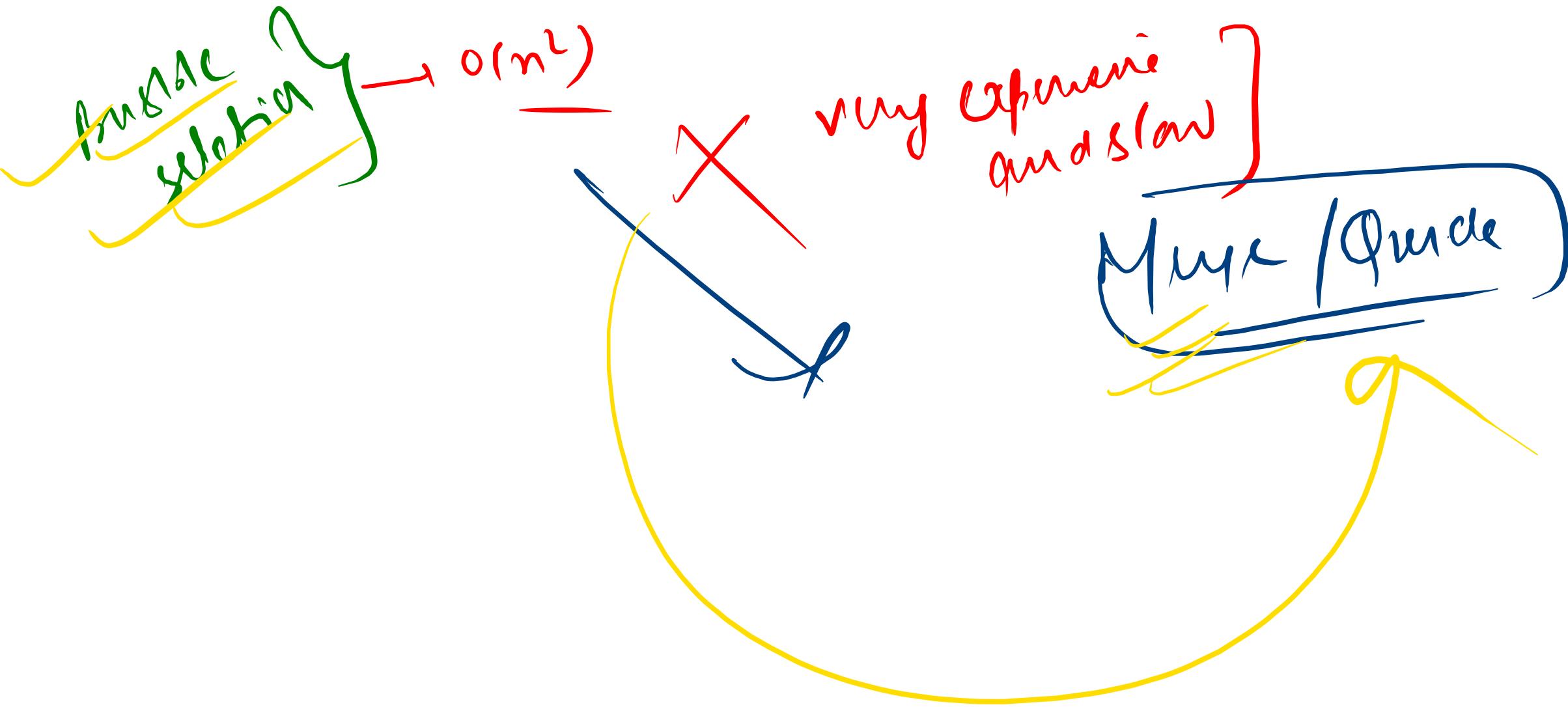
unsorted array

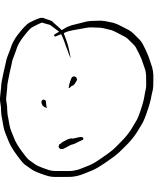
{ 5, 3, 5, 2, 1 }



real case)

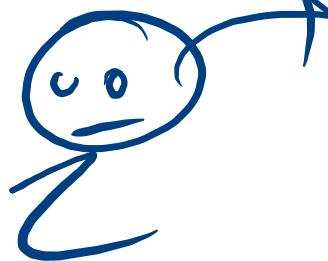






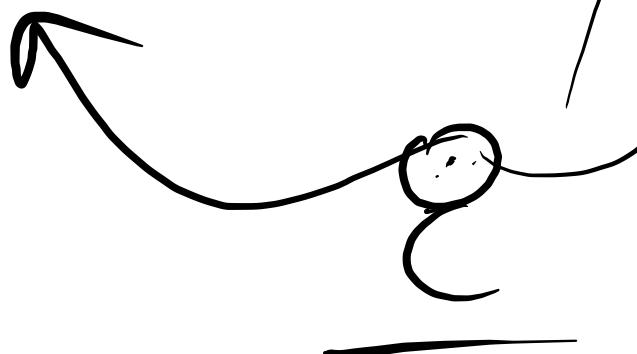
{

wants to learn  
tree?

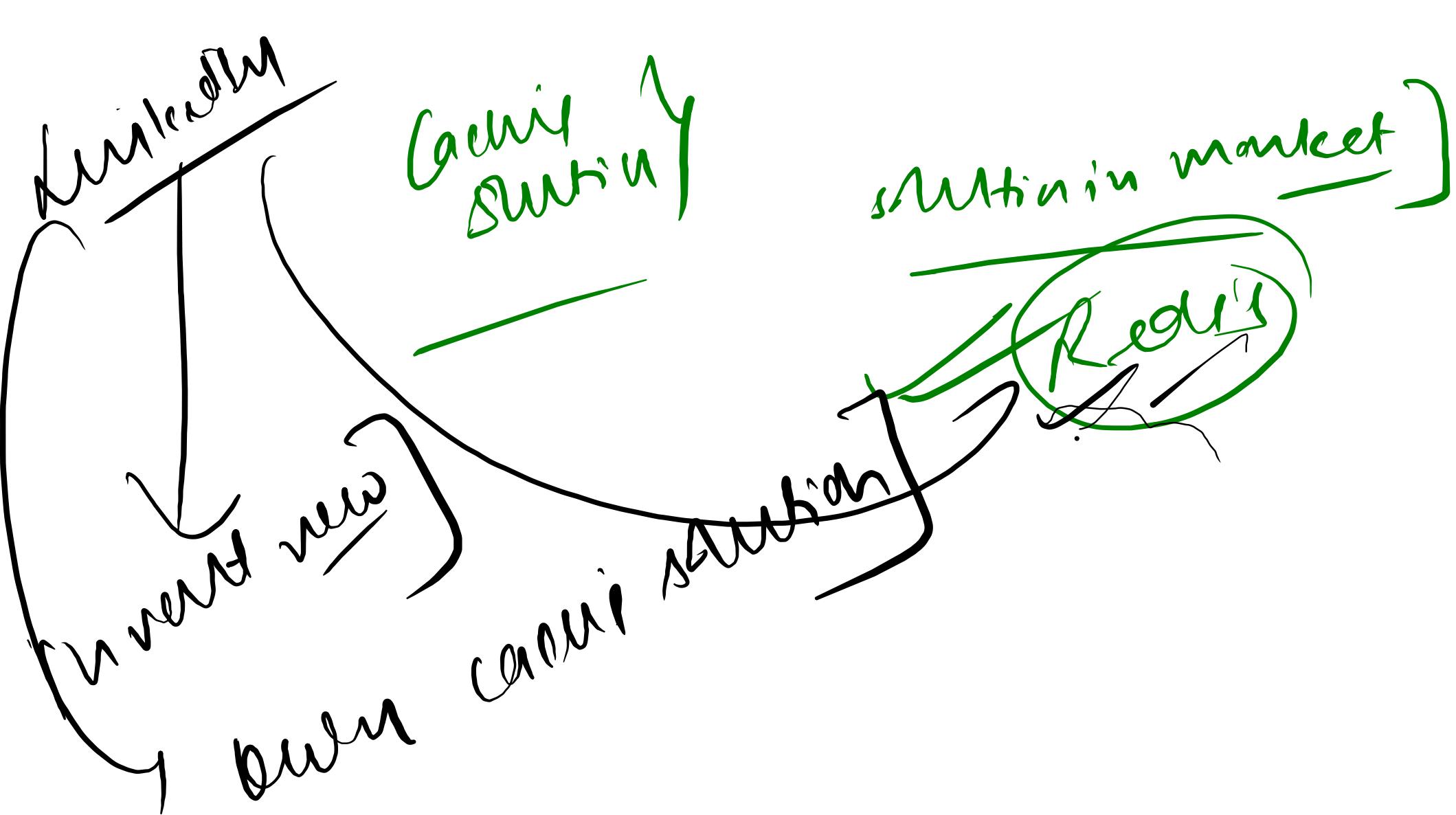


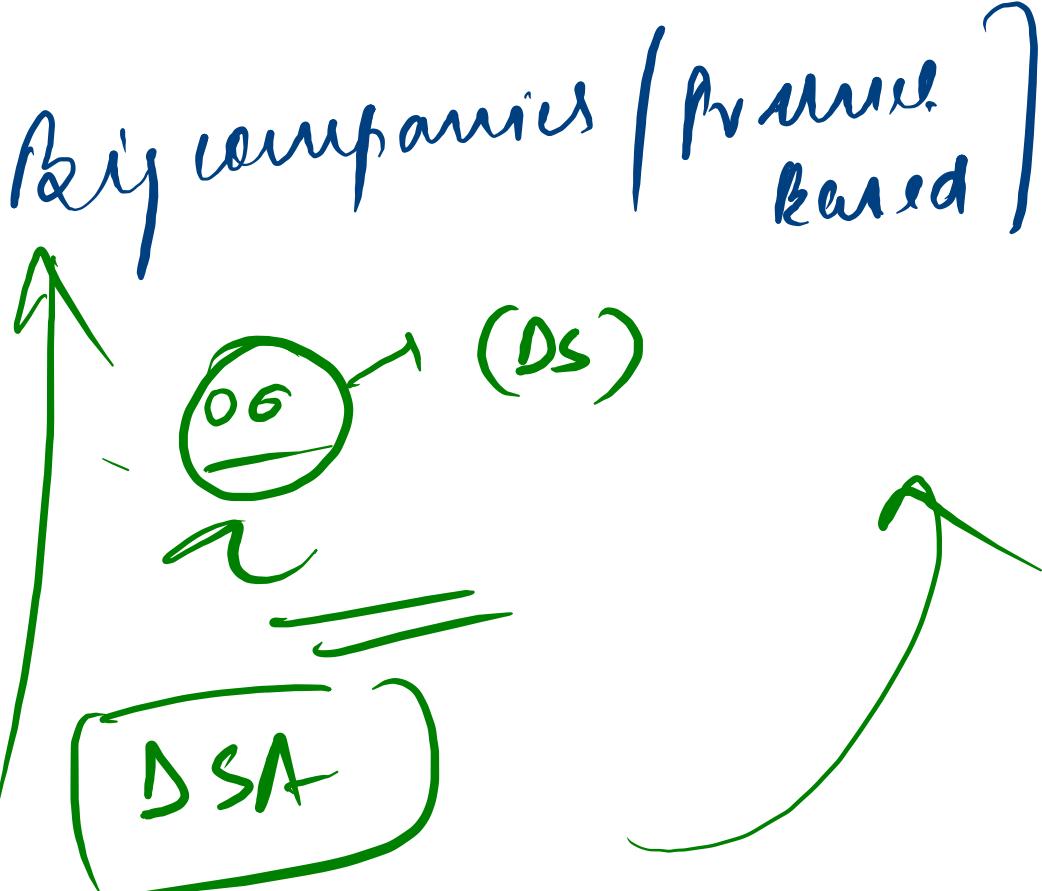
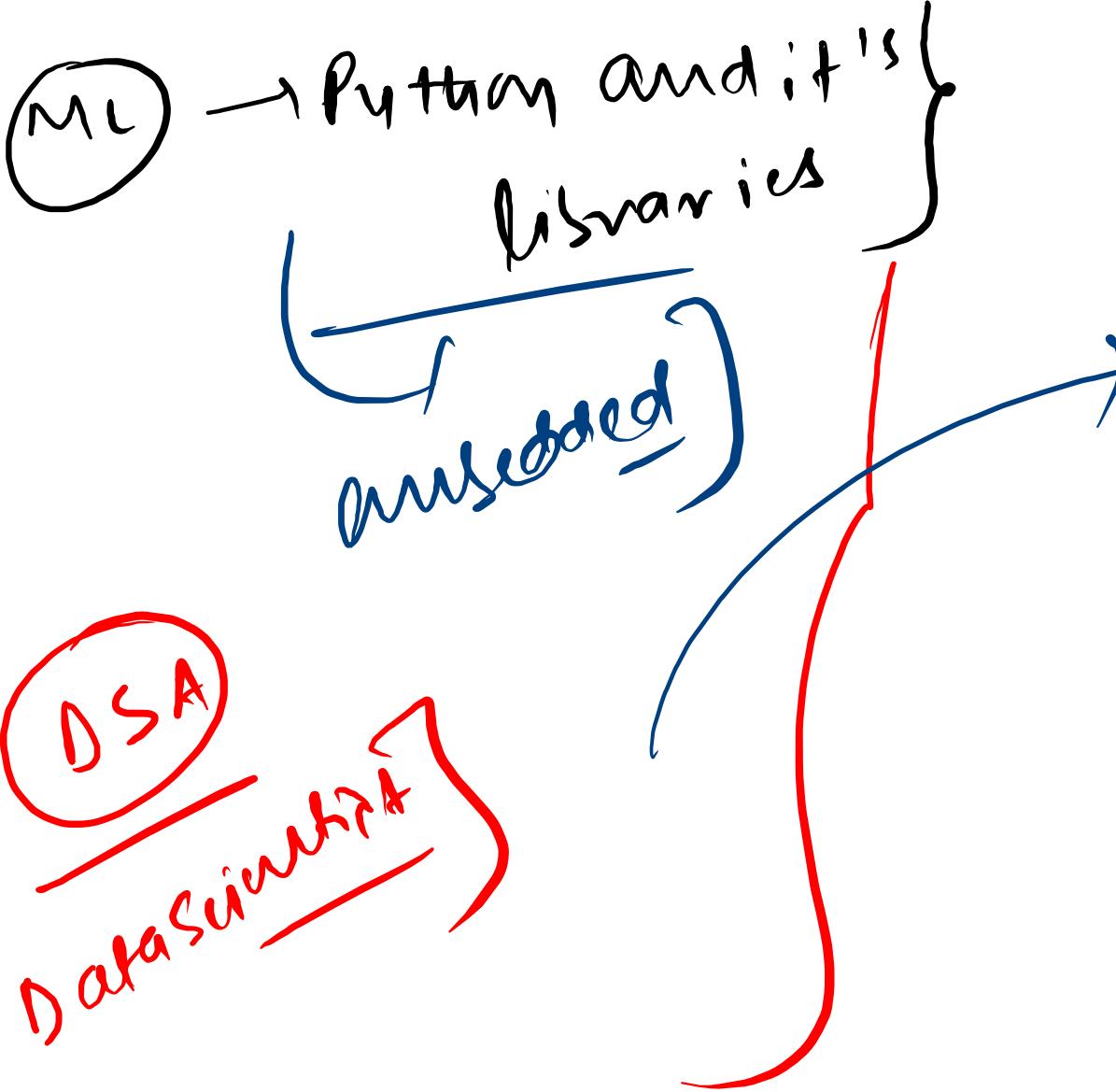
imay) use

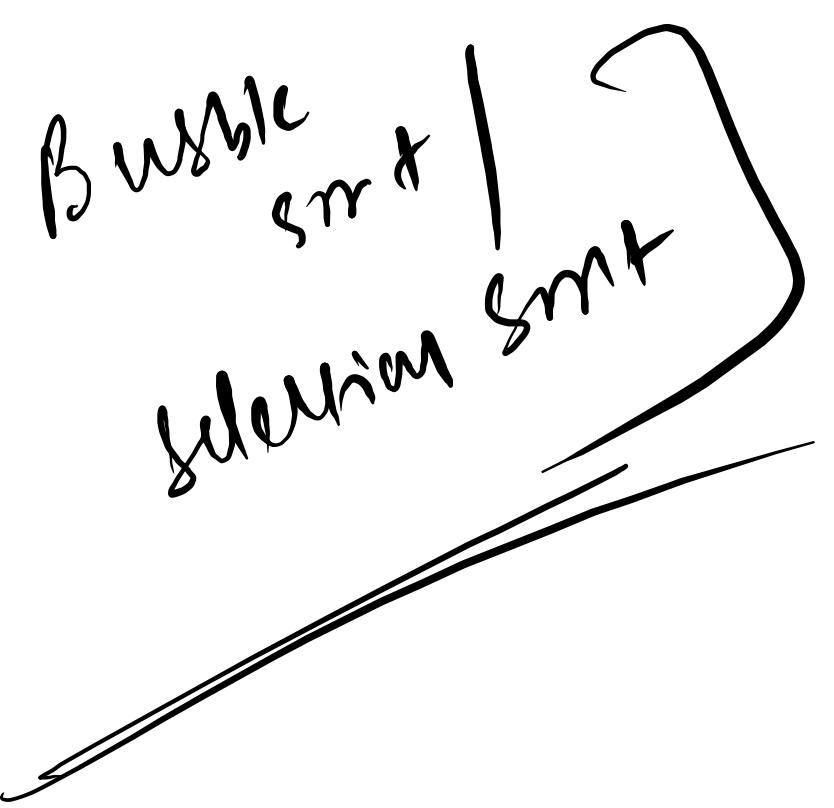
use



(create his own)





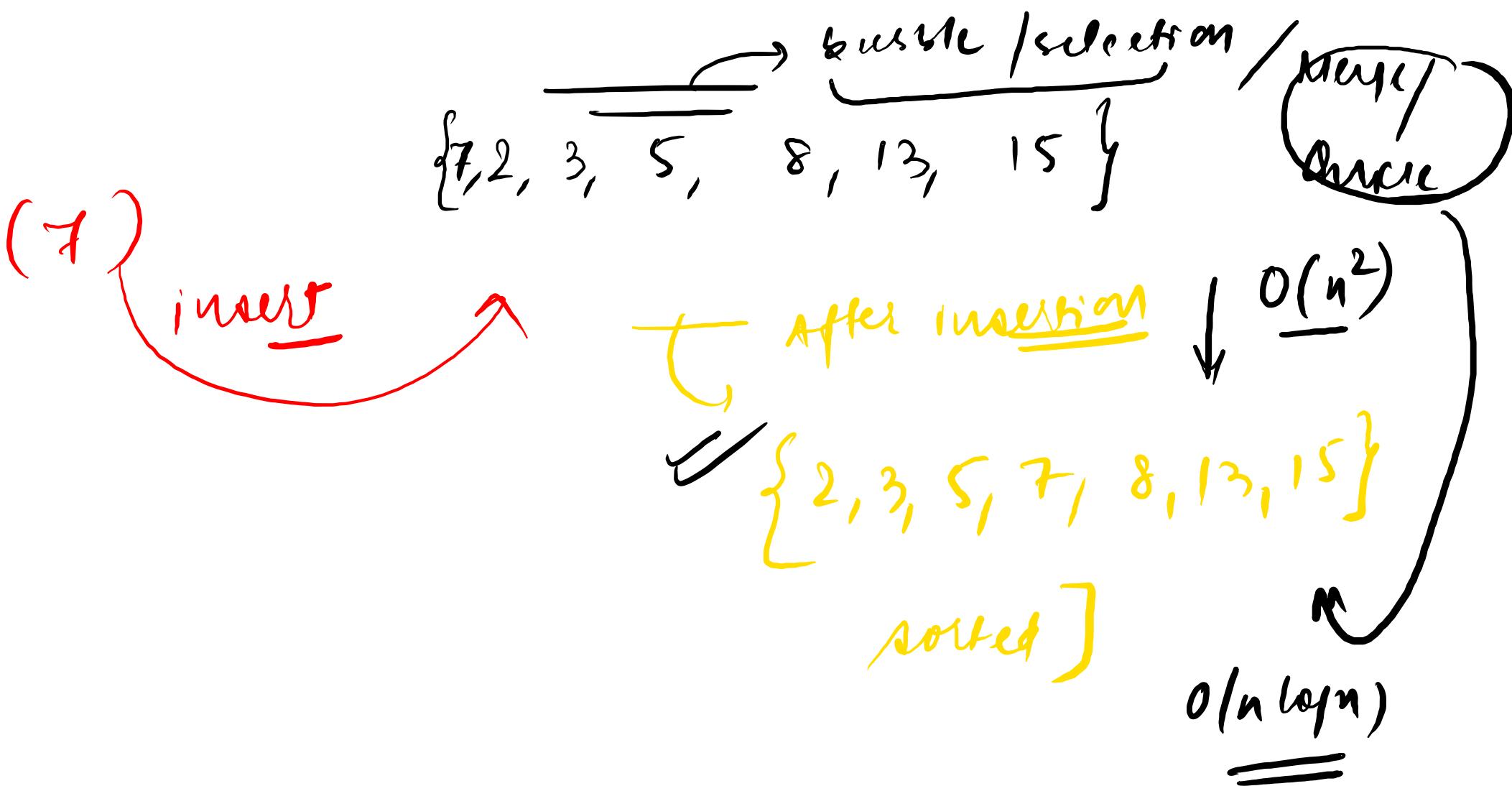


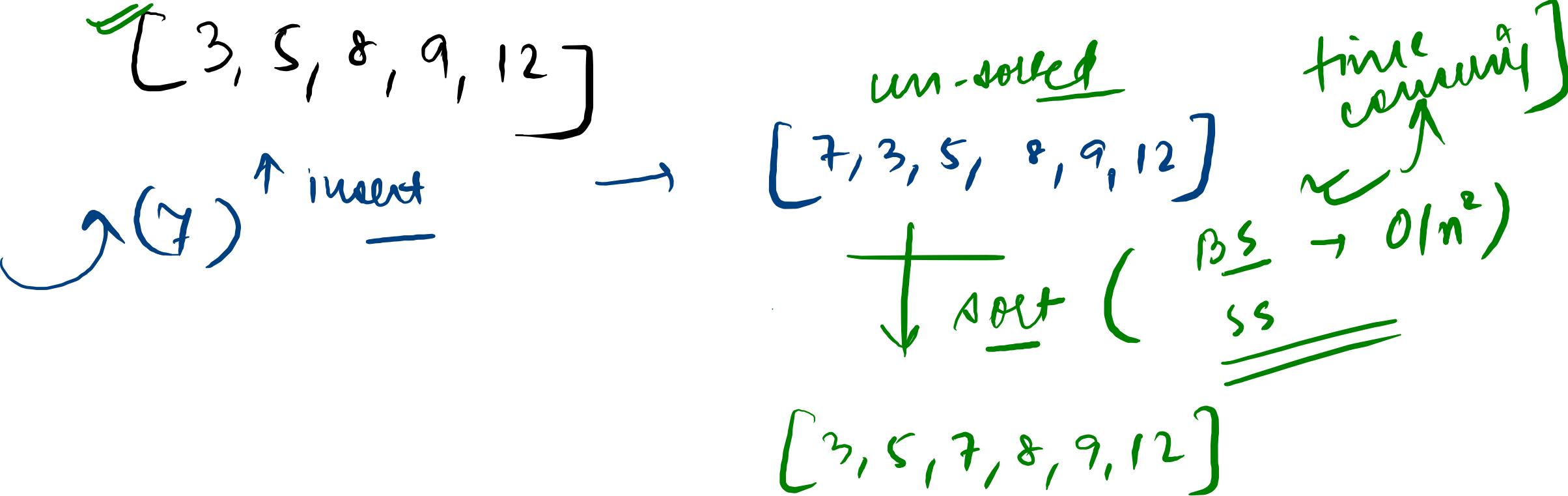
~~DSA~~ ↗ Gangto sym

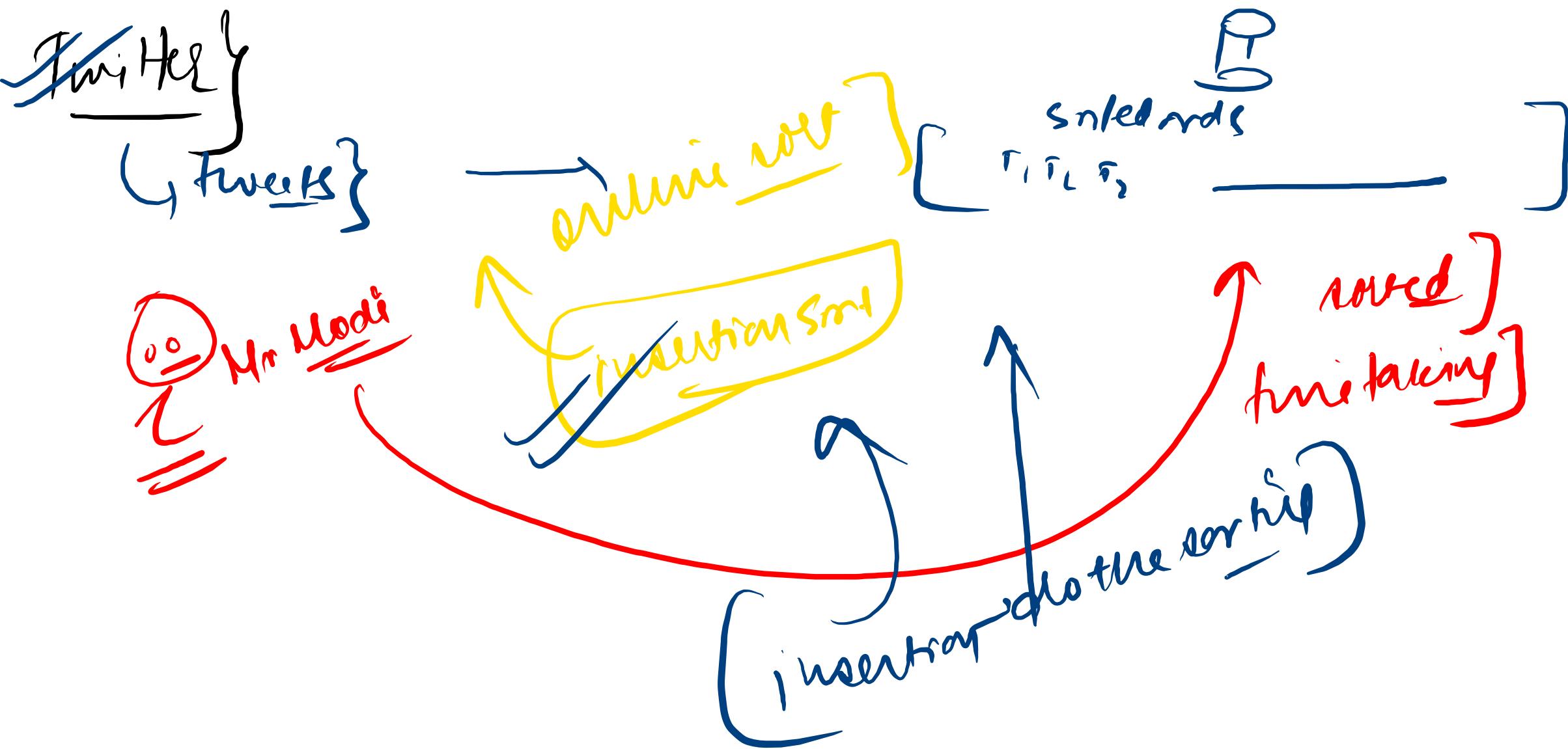
Q ↗

Tournament Sort } online sorting Algorithm

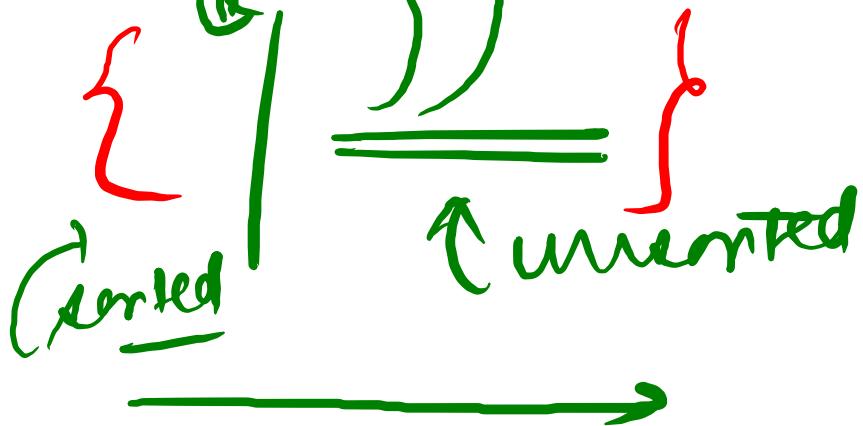
{ complex  
Alert

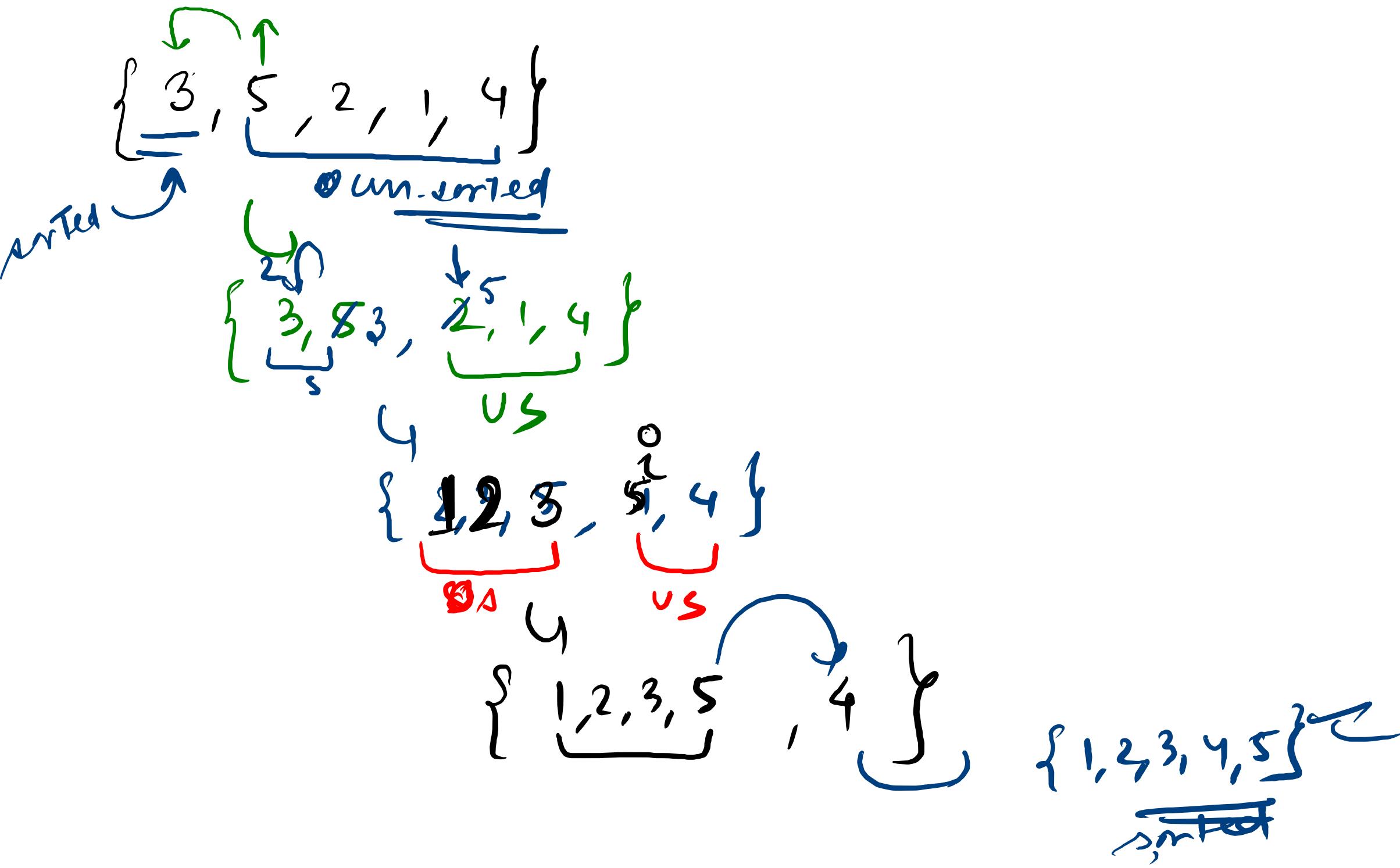


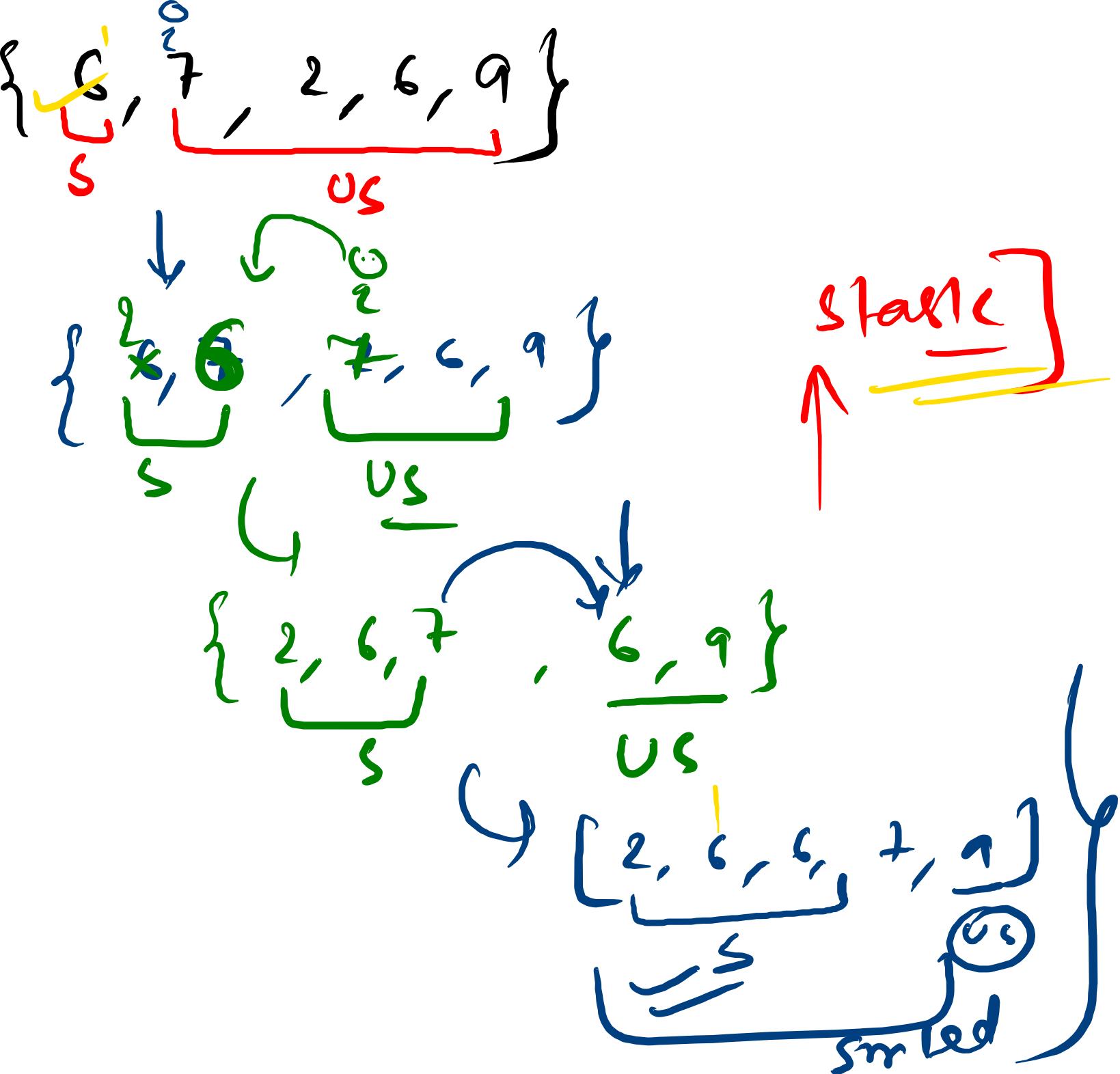




mention} assumption





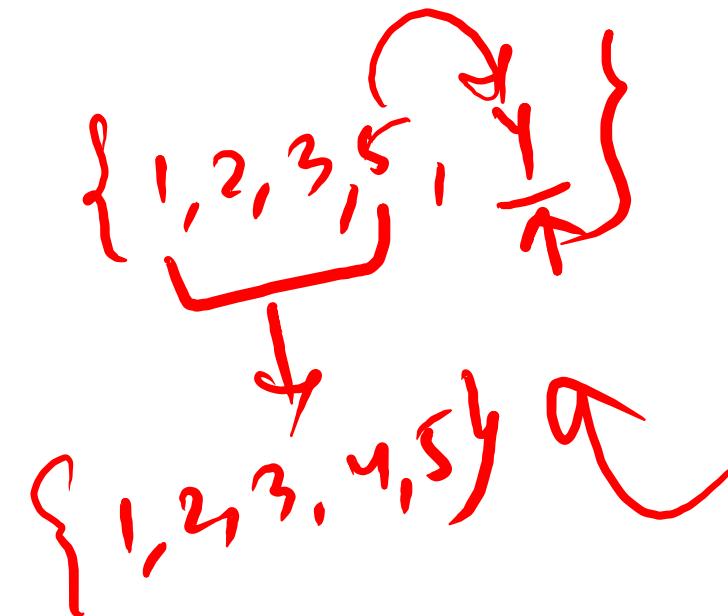


```

def insertion_sort(arr):
    for i in range(1, len(arr)):
        v = arr[i]
        j = i - 1
        while(j >= 1 and arr[j-1] > v):
            arr[j] = arr[j-1]
            j -= 1
        arr[j] = v

```

using pattern }



```
def insertion_sort(arr):
```

```
    for i in range(1, len(arr)):
```

v = arr[i] = 4  
j = i = 4 // 3 2 ←  
while(j >= 1 and arr[j-1] > v):  
 arr[j] = arr[j-1]  
 j -= 1 = 2 ←  
arr[j] = v  
  
 2 ↑ 4

0 1 2 3 4  
{ 2, 5, 3, 8, 4 }  
↓ ↓ ↓ ↓ ↓

→ { 2, 3, 5, 8, 4 }  
0 1 2 3 4  
↓ ↓ ↓ ↓ ↓

→ { 2, 3, 5, 8, 4 }  
0 1 2 3 4  
↓ ↓ ↓ ↓ ↓

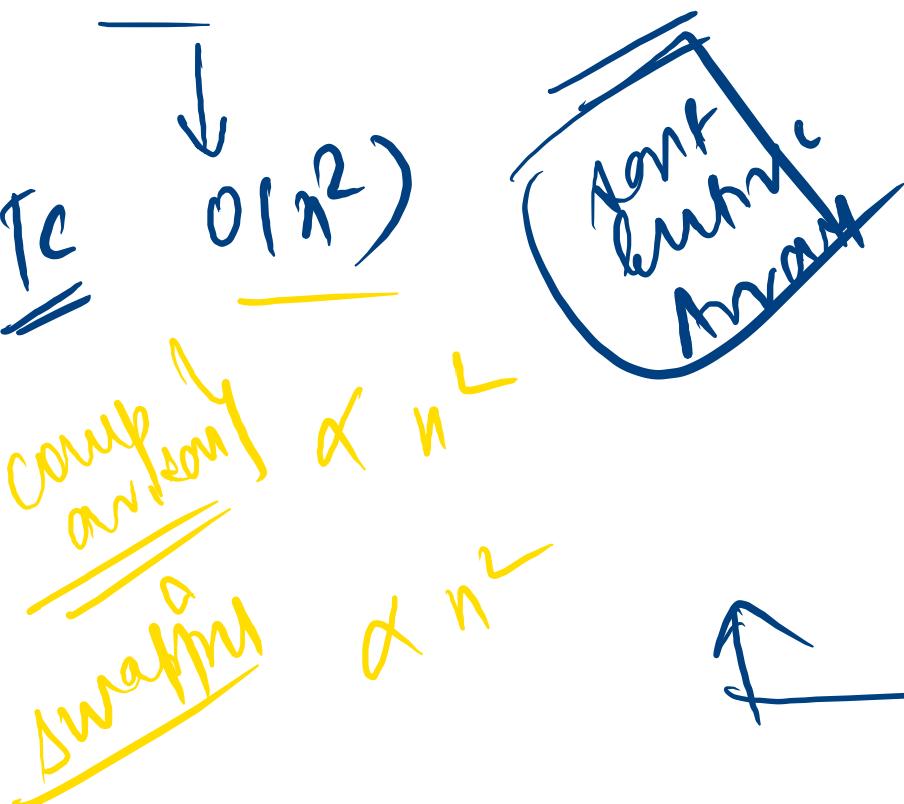
→ { 2, 3, 4, 8, 5 }  
0 1 2 3 4  
↓ ↓ ↓ ↓ ↓

→ [2, 3, 4, 5, 8]      worked

```

def insertion_sort(arr):
    for i in range(1, len(arr)):
        v = arr[i]
        j=i
        while(j>=1 and arr[j-1]>v):
            arr[j]=arr[j-1]
            j-=1
        arr[j]=v

```



```

#Selection Sorting
def selectionSort(arr):
    for i in range(len(arr)):
        min = i
        for j in range(i+1, len(arr)):
            if arr[j] < arr[min]:
                min = j
        #Find the smallest values
        arr[i], arr[min] = arr[min], arr[i]

```

$O(n^2)$

$n^2$

$n$

```

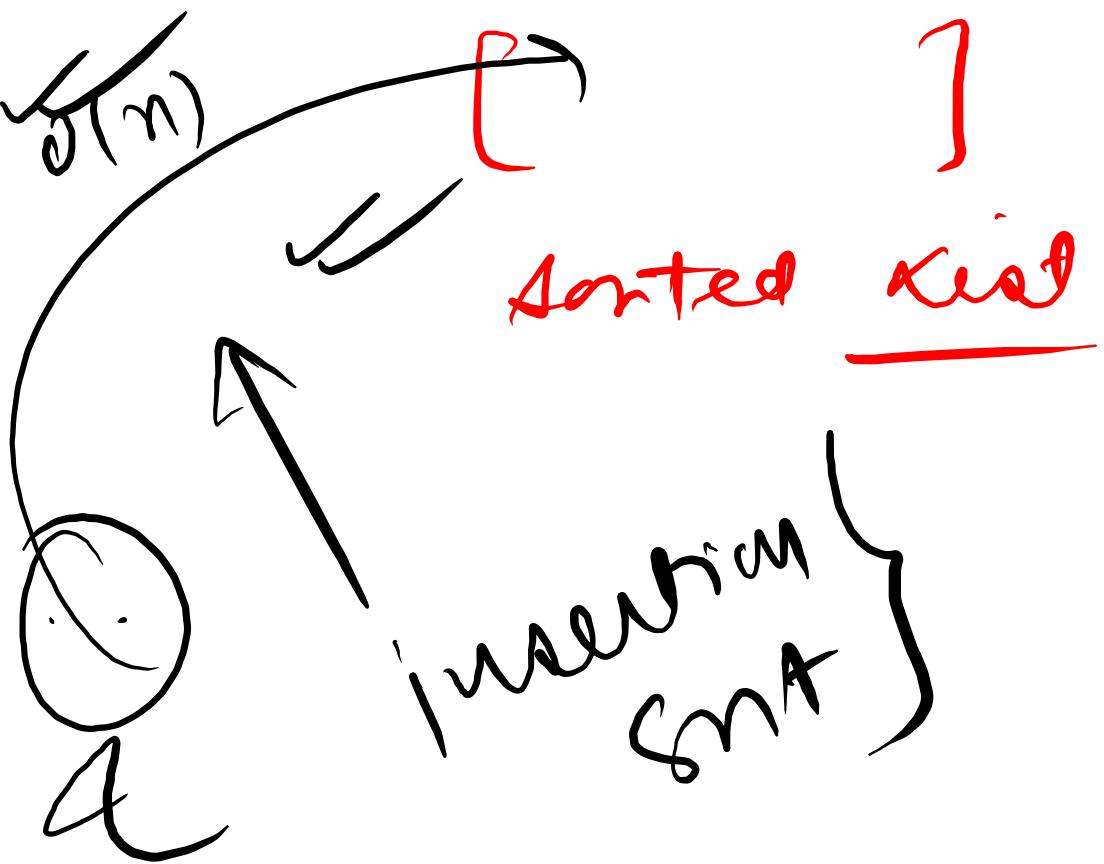
def bubbleSort(arr):
    for i in range(len(arr)-1, 0, -1):
        for j in range(i):
            if(arr[j]>arr[j+1]):
                arr[j], arr[j+1] = arr[j+1], arr[j]

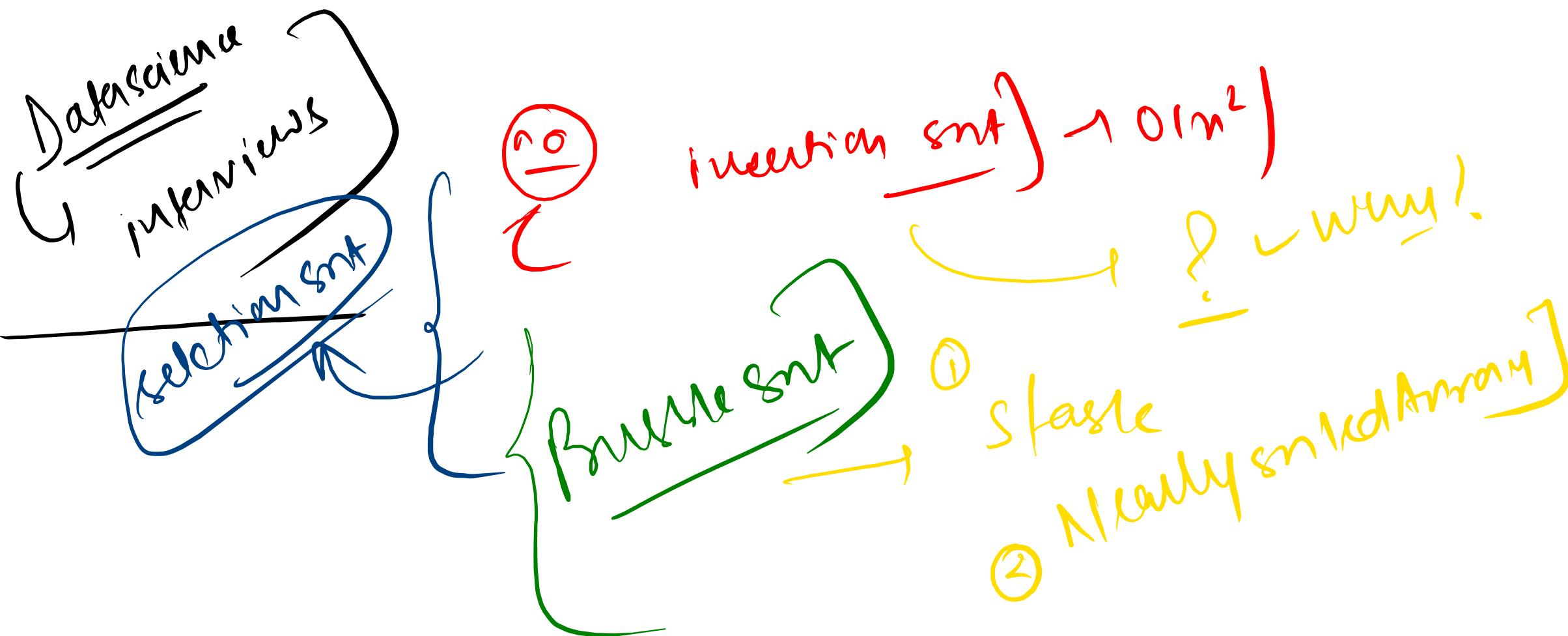
```

$O(n^2)$

$n^2$

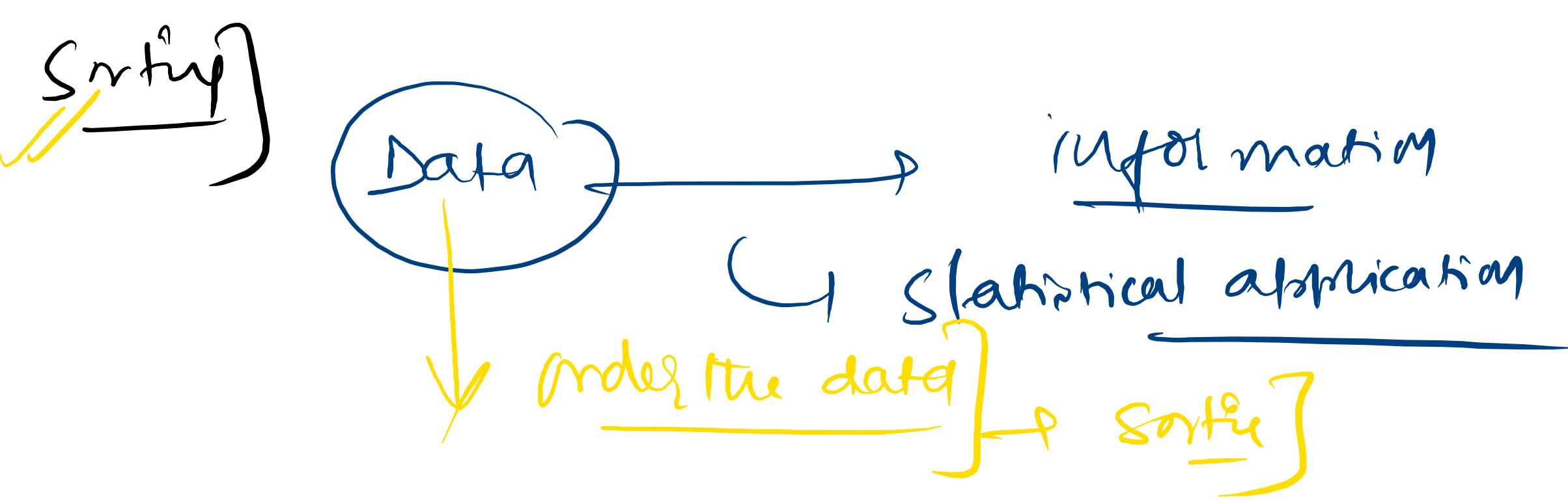
$n$



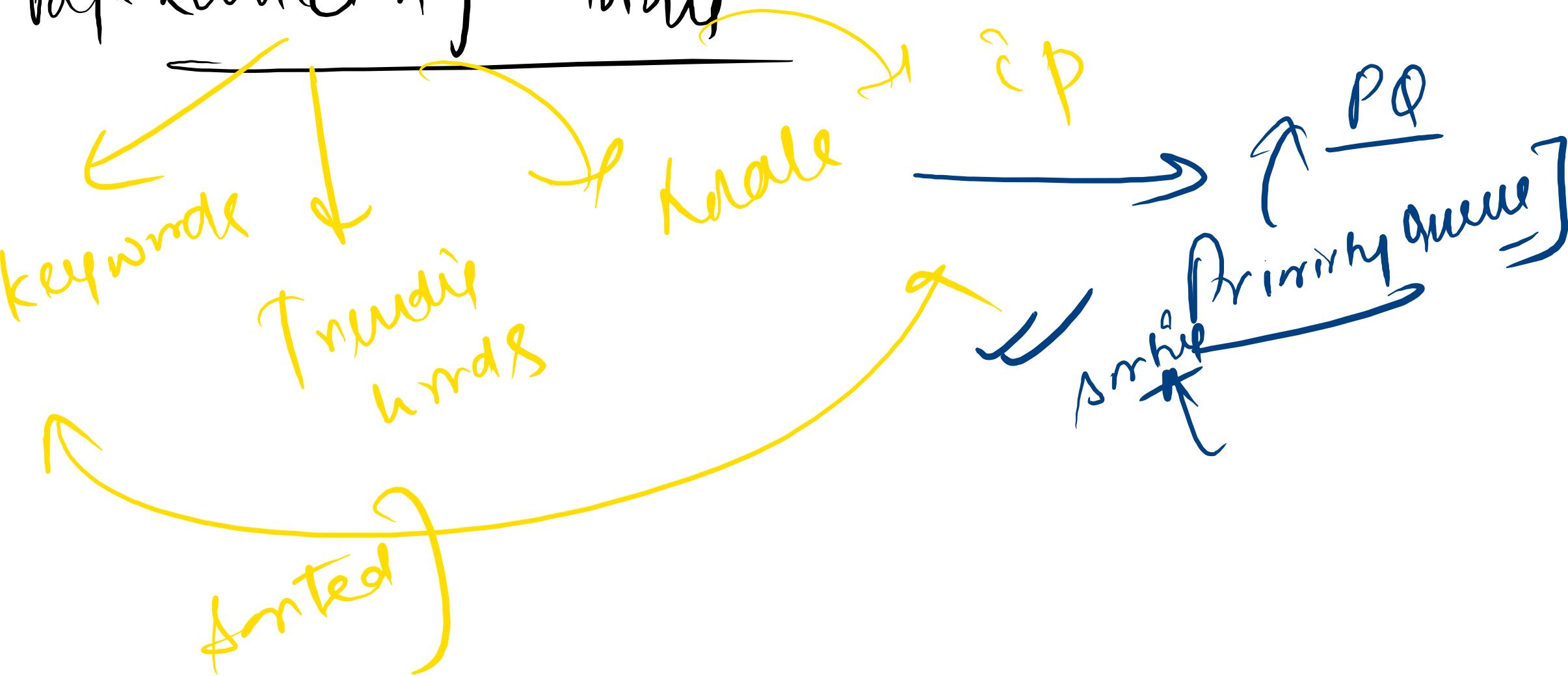


Shake smt

wuy?



# Page Rank Algorithm



30 min

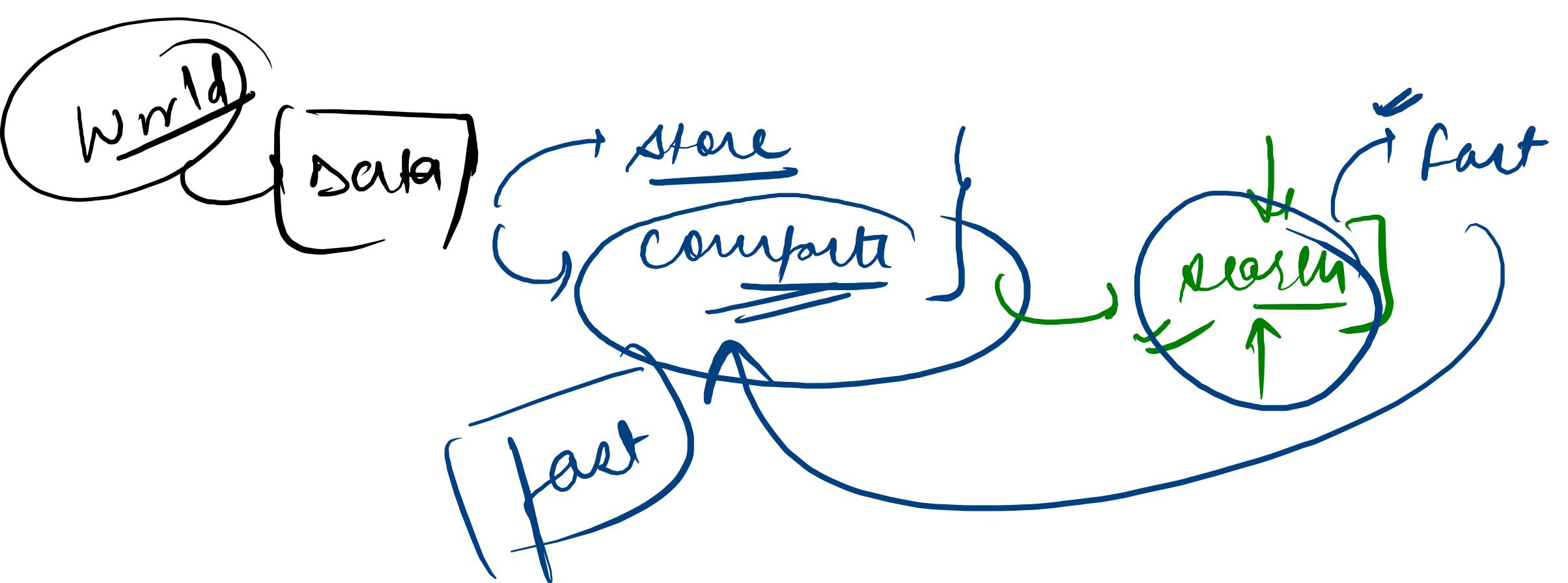
(P)

100X

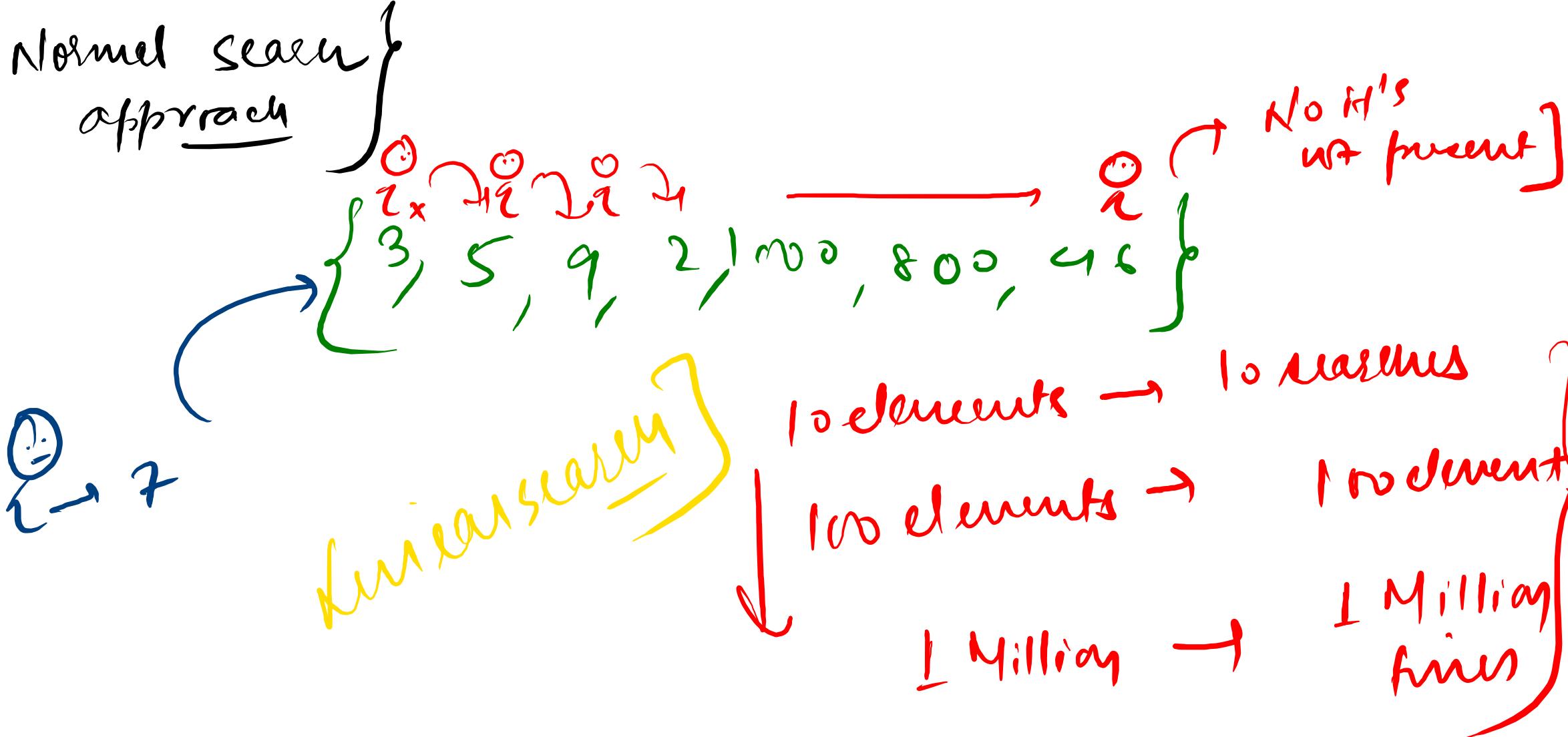
~~Sorting Algorithms~~



search



~~soaring~~ learn → super fast]

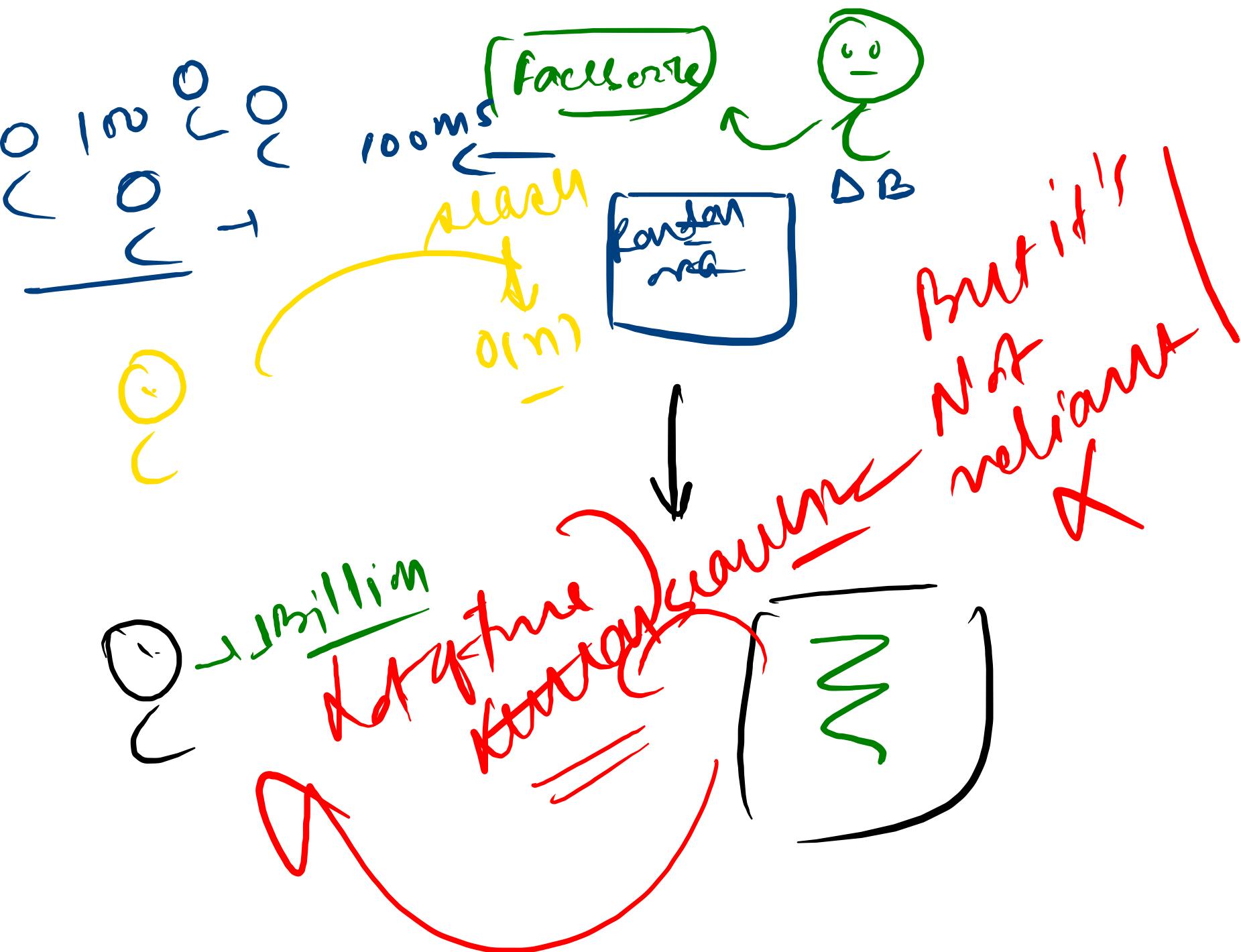


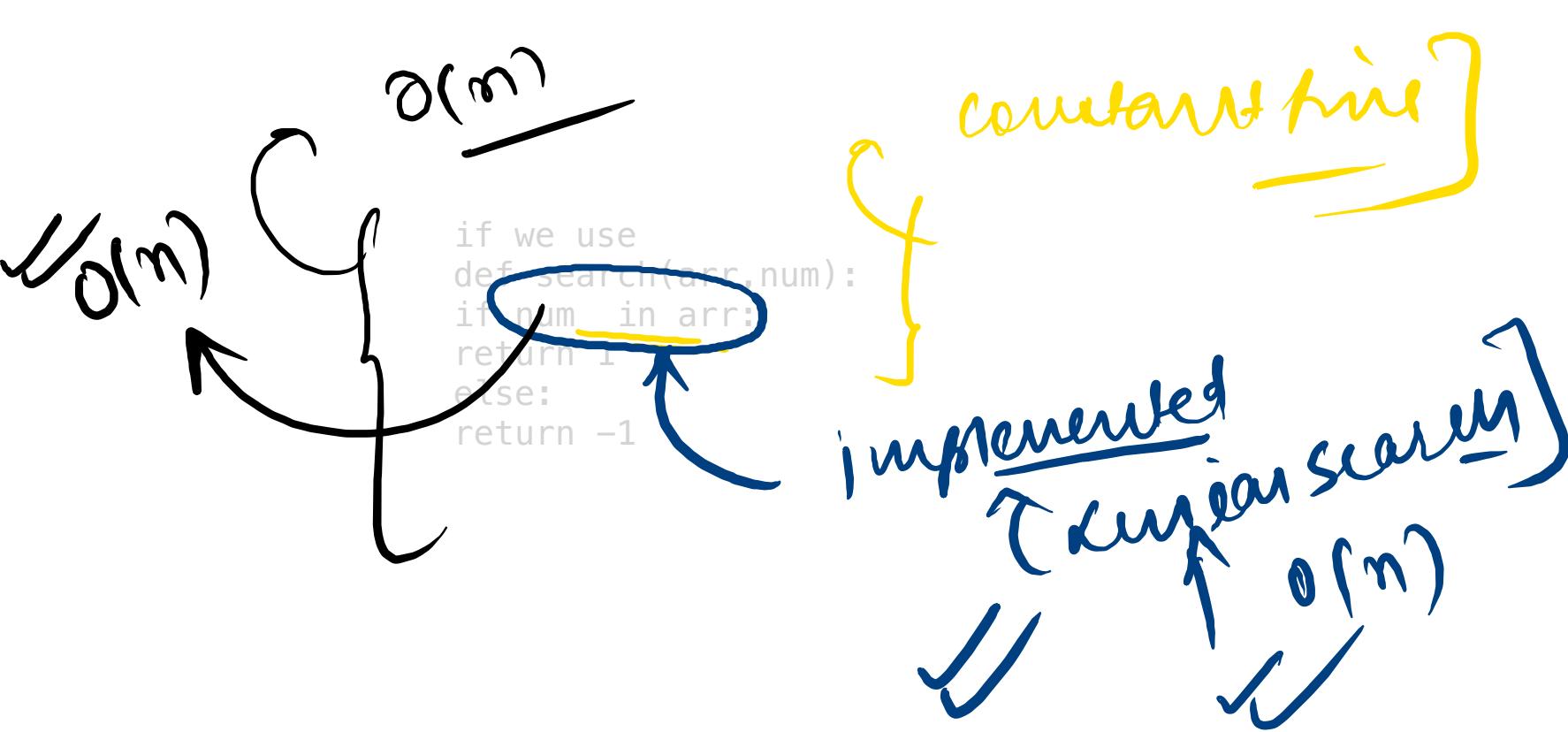
```
def search(arr, num):  
    for i in range(len(arr)):  
        if arr[i]==num:  
            return i  
    return -1
```

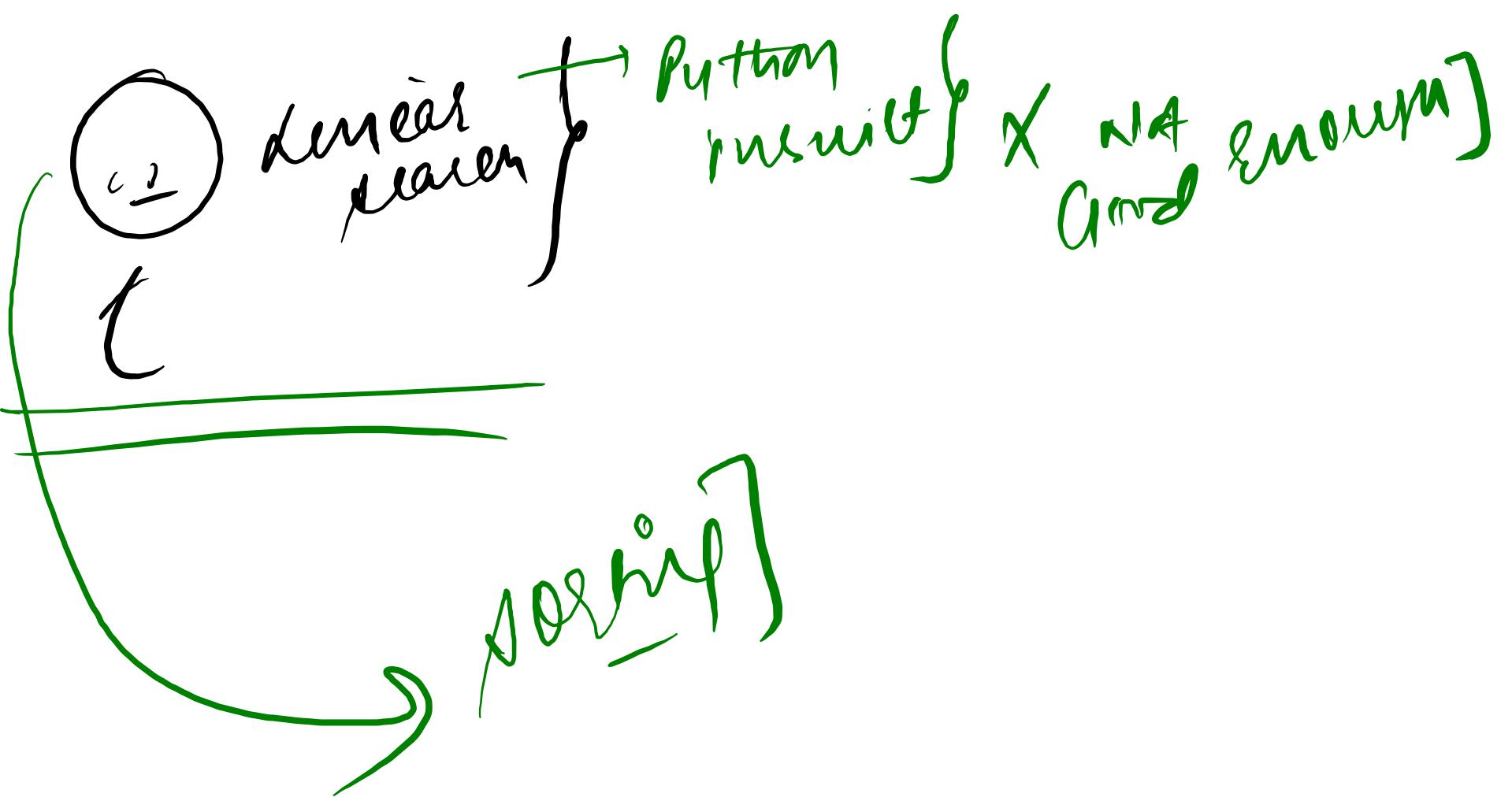
$\uparrow n$

$$TC = \underline{\underline{O(n)}}$$

More the number of items  
search time will be







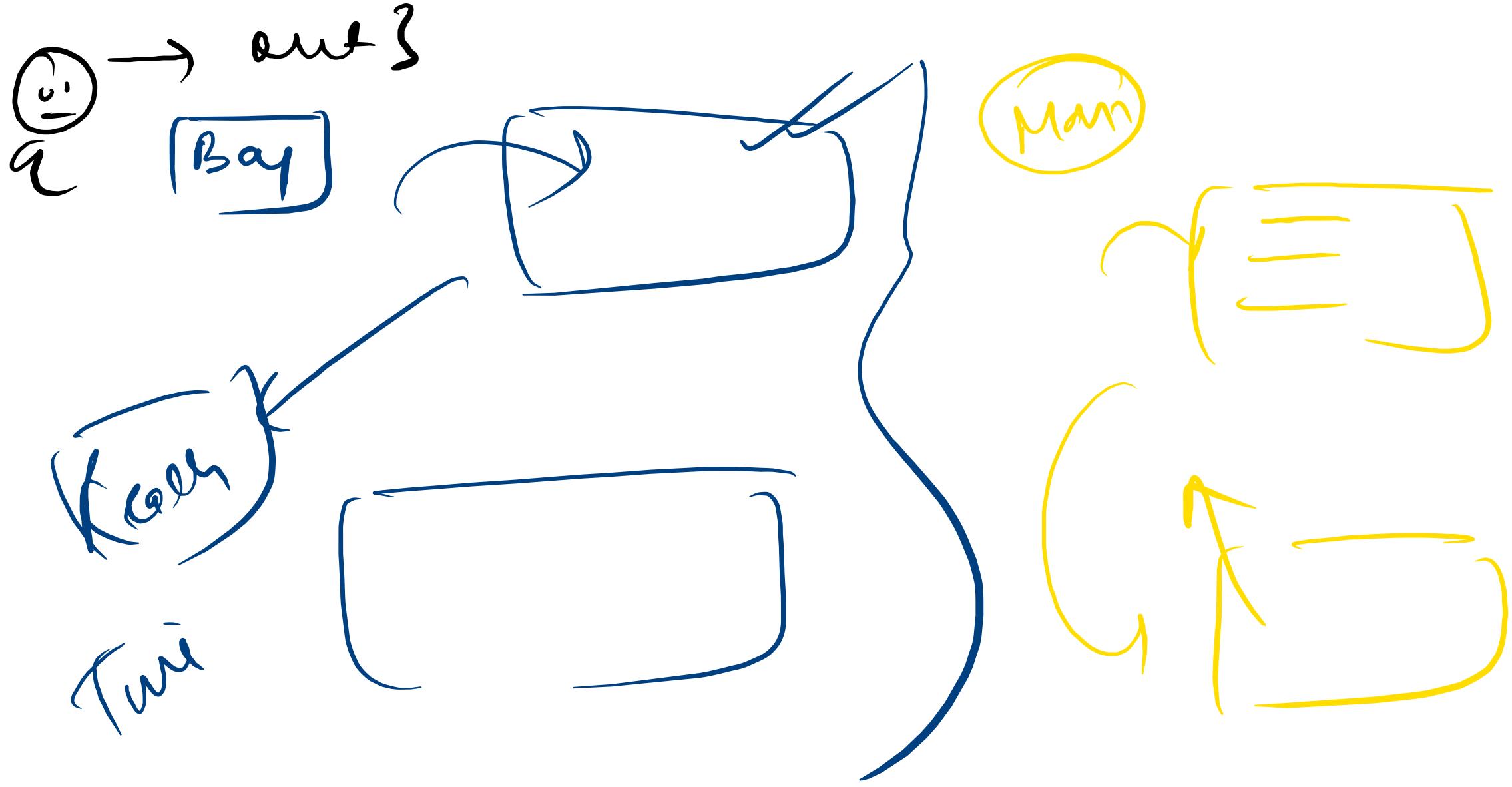
Monopoly  
sup

Room } Medicines ]  
↓ Alphabatically Arranged ]

Dictionary → Meaning of wrds

→ Arranged alphabetically

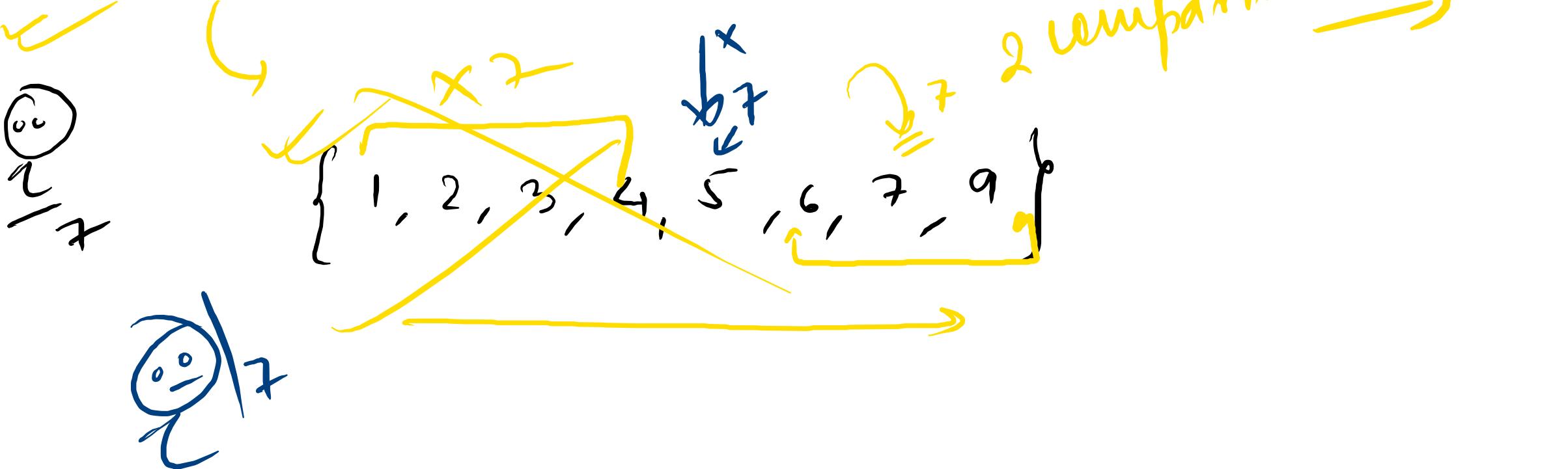
Real word



search  
→ sorted ]

↑  $O(1)$   
maps

$\{3, 1, 2, 5, 4, 6, 9, 7\} \leftarrow O(n)$



sorted] ~~X < mid~~  $\leq$  X

$\{2, 9, 18, 63, 54, 136, 259, 999, 1226\}$

Linear  
1226

9 comparisons

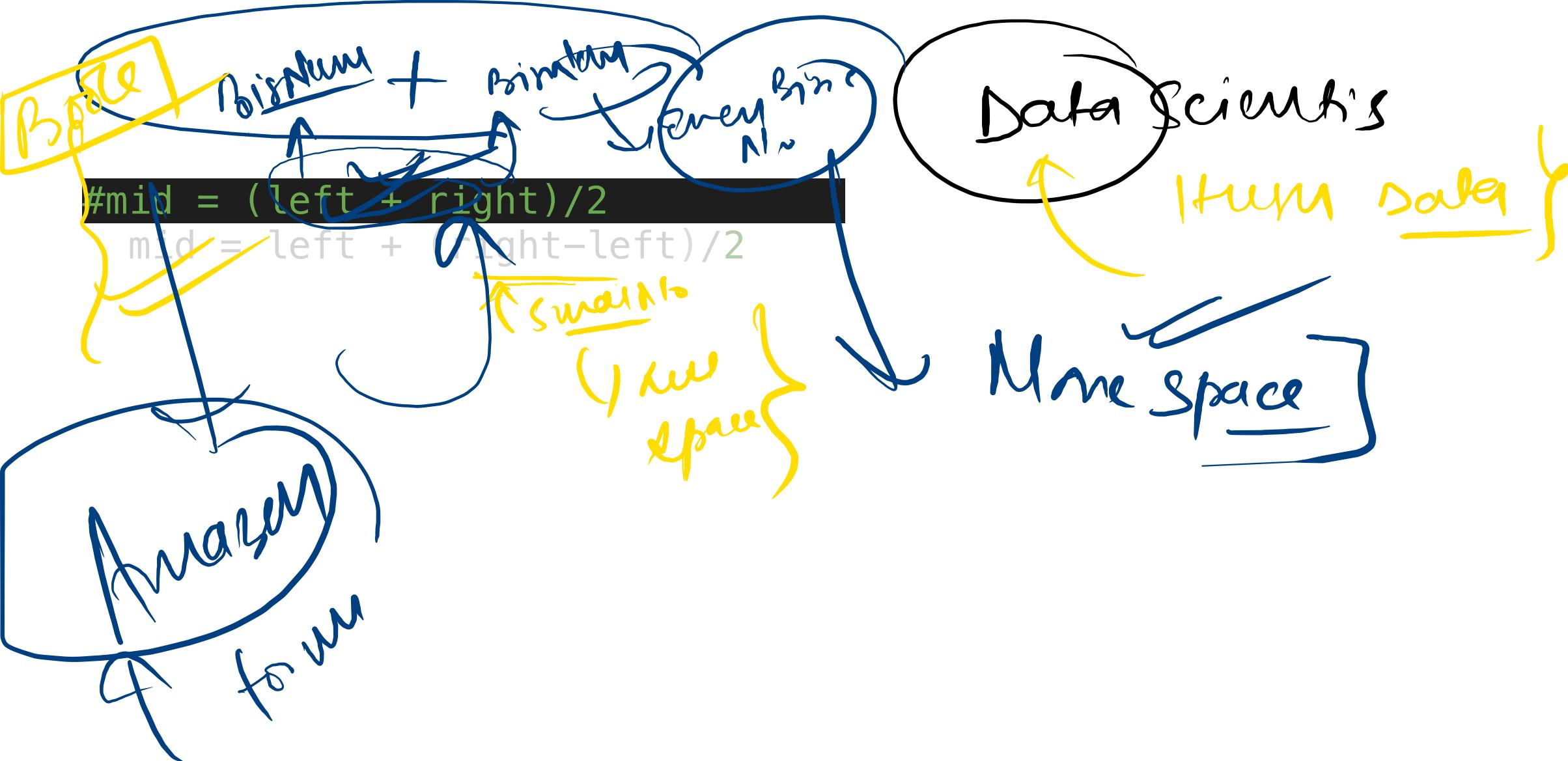
$\{2, 9, 18, \cancel{63}, 54, 136, \cancel{1226}\}$

1286  
1226  
 $\{259, 999, \cancel{1226}\}$

3 comparisons

Binary Search

Binary search ✓  
Data should be sorted Already ✗



$\{10, 15, 9, 8, \text{c}\}$

$\{9, \underline{10}, 15, 8, \text{c}\}$

$\{8, \underline{9, 10}, 15, \text{c}\}$

$\{8, 9, \underline{10, 15, \text{c}}\}$

$\{6, 8, 9, 10, 15\}$

no seq

```

def binarySearch(arr, num):
    left = 0
    right = len(arr) - 1 = 5
    while(left <=right):
        mid = int(left + (right-left)/2) = 2
        if arr[mid] == num: 10
            return mid = 9 10
        elif arr[mid] > num :
            right = mid-1
        else :
            left = mid+1 = 3
    return -1

```

$$\{ \frac{2, 4, 6, 8, 10, 12}{X}, 10 \}$$

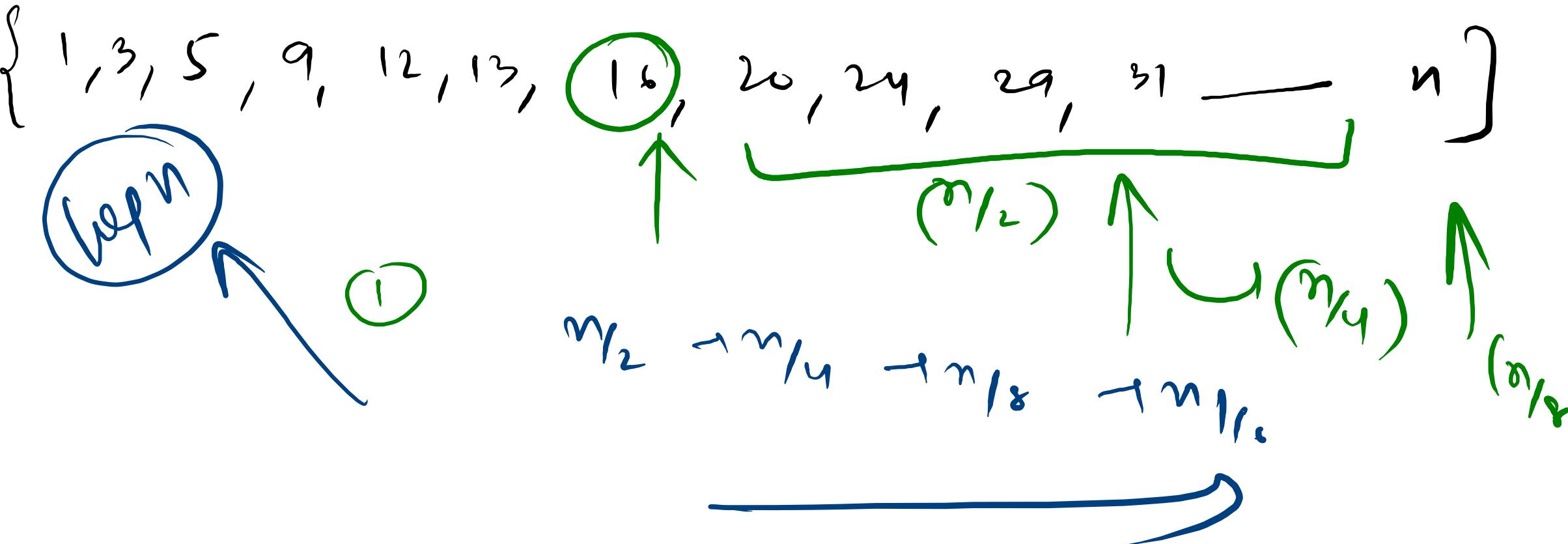
$$0 + (5-0)_2 = (2 \cdot 5) = 2$$

$$3 + (5-3)_2 = 3 + 2_2 = 4$$

```
def binarySearch(arr, num):  
    left = 0  
    right = len(arr) -1  
  
    while(left <=right):  
        mid = int(left + (right-left)/2)  
        if arr[mid] == num:  
            return mid  
        elif arr[mid] > num :  
            right = mid-1  
        else :  
            left = mid+1  
    return -1
```

Time comparisons {

1 , 3 ,  
O(log n)



`range(5)` → 0, 1, 2, 3, 4

`range(1, 5)` → 1, 2, 3, 4

`range(5, 0, -1)` → 5, 4, 3, 2, 1