

Divide & Conquer

Sorted array

Rotated

{ 1, 2, 3, 5, 6, 7, 8, 9, 10 }

{ 5, 6, 7, 8, 9, 10, 1, 2, 3 }

Rotated sorted array

{⁰5, ¹6, ²7, ³8, ⁴9, ⁵10, ⁶1, ⁷2, ⁸3}

↑

Key = 10

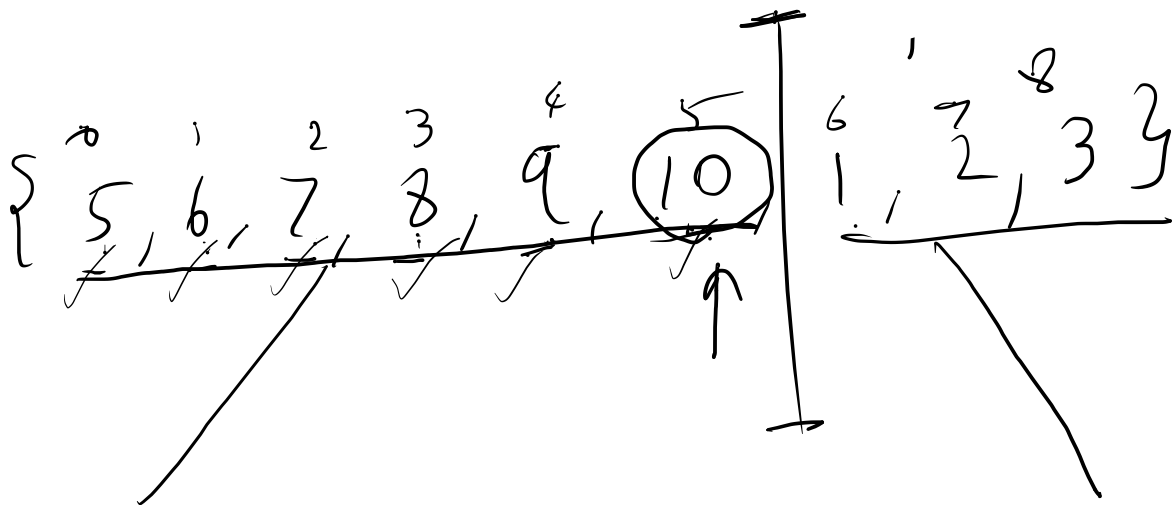
Linear search $\rightarrow O(N)$

Rotated sorted array

$\{ \overset{0}{5}, \overset{1}{6}, \overset{2}{7}, \overset{3}{8}, \overset{4}{9}, \overset{5}{10}, \overset{6}{1}, \overset{7}{2}, \overset{8}{3} \}$

Key = 10

binary search $(0, n-1)$



$$\{5, 6, 7, 8, 9, 10\}$$

bs

$$\{1, 2, 3\}$$

bs

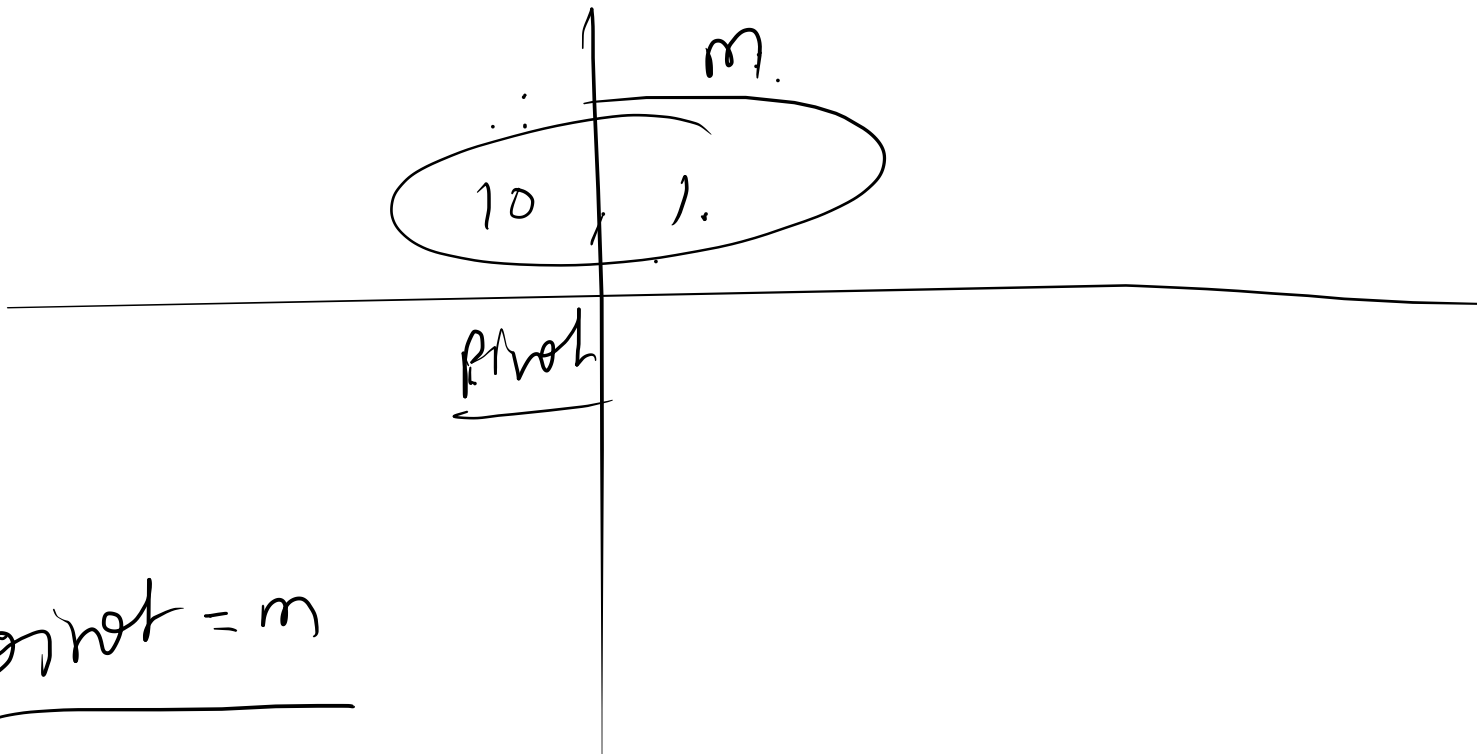
$$\{ \overset{l}{5}, \overset{l}{6}, \overset{l}{7}, \overset{l}{8}, \overset{l}{9}, \overset{m-1}{10}, \overset{m}{1}, \overset{h}{2}, \overset{h}{3} \}$$

$$\text{if } (\text{arr}[m] > \text{arr}[m+1])$$

$$\text{return } \underline{m}$$

$$\text{if } (\text{arr}[m-1] > \text{arr}[m])$$

$$\text{return } \underline{m-1}$$



$$\underline{\text{pivot} = m}$$

$$\text{pivot} = m - 1$$

$\{ 5, 6, \underline{7}, 8, 9, 10, 1, 2, 3 \}$

$$\underline{L = m + 1}$$

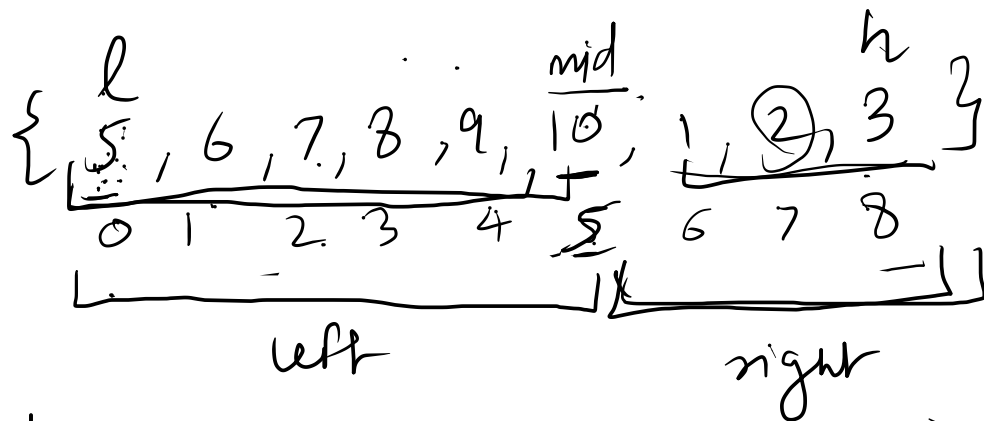
$$\underline{R = m - 1}$$

1	2	3	4	5	6	7	8
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return -1

Linear search $\rightarrow O(n)$

✓ Binary search $\rightarrow O(\log n)$



key = 2

key = 7

if (key > arr[l])

$l = m + 1$

else

$l = m + 1$

Key = 6

					^l	^m		^h	
{	5	,	6	,	7	,	8	,	9
					<u>10</u>	,	<u>1</u>	,	2
									3 }
	0		1		2		3		4
					5		6		7
									8

$$\frac{arr[m] > arr[m+1]}{1 > 2 \quad ? \quad X}$$

$$\underline{10} > 1 \quad ?$$

$$\underline{arr[m-1] > arr[m]}$$

return m-1

✓

(10, ^X1)

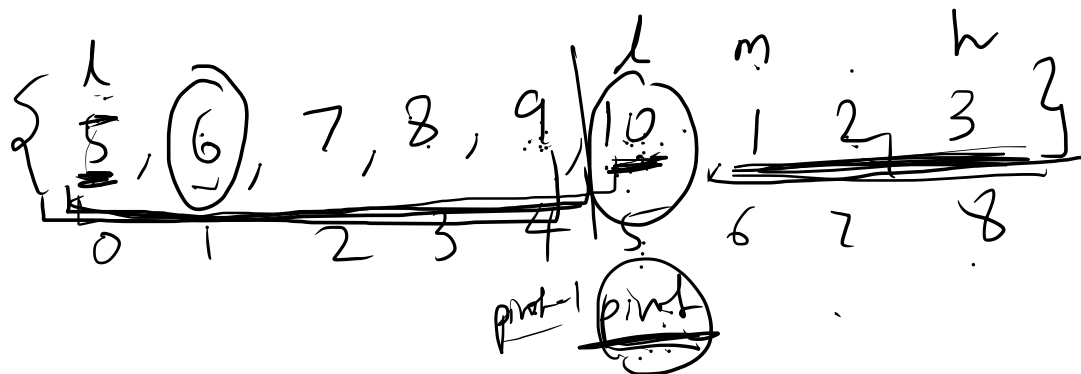
m-1 m

6

—

Key = 6

pivot = 5



$6 > 5$
if (Key \geq arr[pivot])

$h = pivot - 1$

else

$l = pivot + 1$

① find pivot

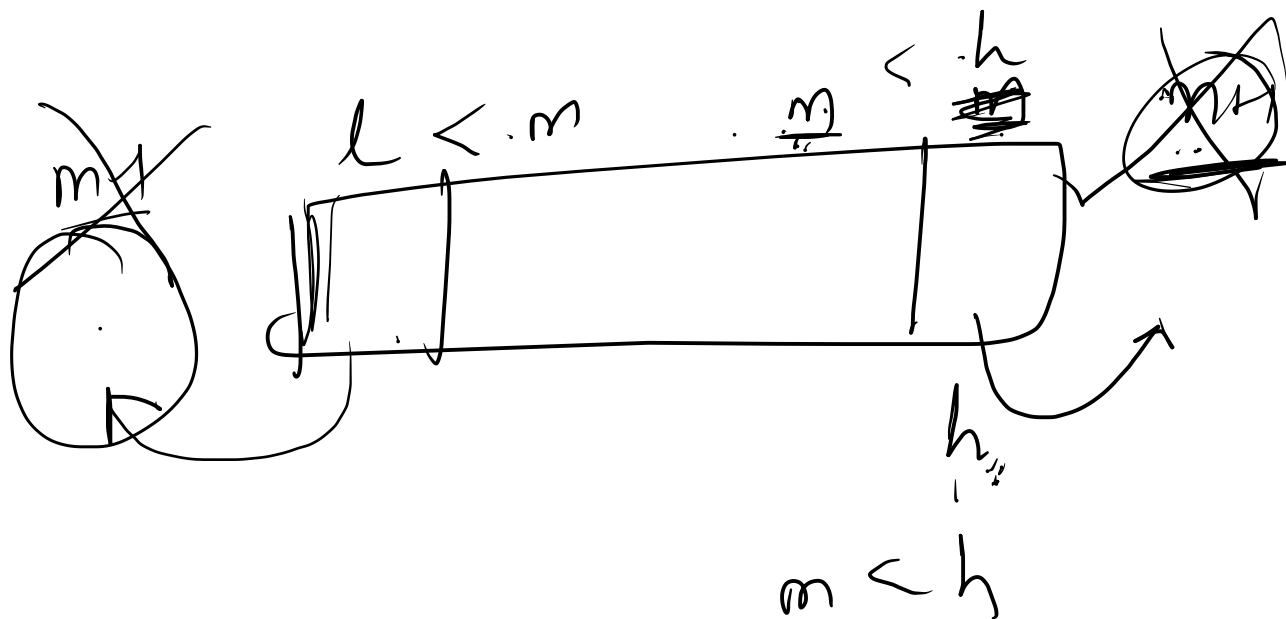
$$10 > 1$$



if $(arr[m] > arr[m+1])$

$$\left(\overset{m-1}{\cancel{\quad}}, \overset{m}{1} \right)$$

$$\underline{A[m-1]} > \underline{A[m]}$$



left	m
<u>5</u> 6, 7, 8, 9, 10, 11	<u>2</u> , 3

✓ Time complexity : $O(\log n)$

$$S.C = \underline{O(1)}$$

not smaller \neq greater

not smaller = greater or equal

peak element

X	X	X	✓	X	X
1	2	3	8	4	3

peak element

x	x	x	✓	x	✓
1	2	3	8	4	6

Peak element

✓	x	x	x	✓	x
6	1	2	3	4	2

Peak element

✓	x	x	x	✓	x
6	1	2	3	4	2

if (arr[m] >= arr[m-1] $\&\&$
arr[m] >= arr[m+1])

return m

			l			
1	2	3	8 ^m	4	3	
0	1	2	3	4	5	
			h			

$$m = \frac{l+h}{2} = \frac{3+5}{2} = 3$$

if (arr[m] > left 8 > 3 ✓
 && arr[m] > right) 8 > 4 ✓
 return m

① find pivot

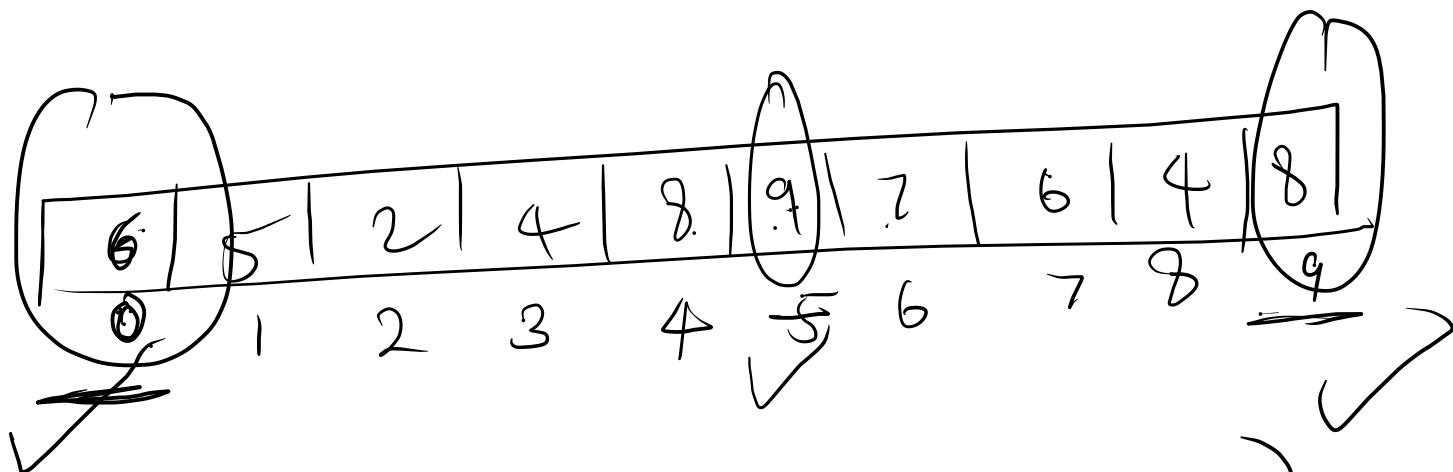
if (arr[m-1] > arr[m])

h = m-1

if (arr[m+1] > arr[m])

l = m+1

if (arr[m] > arr[m+1] && arr[m] > arr[m-1])
return m



- ① $(arr[m] > left \quad || \quad m == 0)$
- ② $(arr[m] > right \quad || \quad m == n-1)$

Time complexity = $O(\log n)$