# Bce vs Bce with logit

**BCE** (**Binary Cross Entropy**) **Loss:** BCE Loss is short for Binary Cross Entropy Loss. It is a common loss function used in binary classification problems, where the target variable has only two possible classes (0 or 1). The BCE Loss measures the dissimilarity between the predicted probability distribution and the true binary labels.

### **Advantages of BCE Loss:**

- Simplicity: BCE Loss is straightforward and easy to implement.
- Stable Training: It often provides stable training and convergence, especially when combined with the sigmoid activation function at the output layer.
- Interpretability: The loss value can be interpreted as a measure of dissimilarity between the predicted probabilities and the ground-truth binary labels.

When to use BCE Loss: BCE Loss is commonly used in binary classification problems when you have a single binary outcome (e.g., spam vs. non-spam, positive vs. negative sentiment).

**BCELogitLoss (Binary Cross Entropy with Logits Loss):** BCELogitLoss is short for Binary Cross Entropy with Logits Loss. It is also used in binary classification problems but operates on the logits (i.e., the raw model outputs before applying the sigmoid function) rather than the probabilities.

### Advantages of BCELogitLoss:

- Numerical Stability: Working with logits can sometimes be more numerically stable than probabilities, especially when the probabilities are close to 0 or 1.
- Efficient Gradient Computation: The BCELogitLoss can be advantageous in deep learning frameworks since the computation of gradients with respect to logits can be more efficient.

When to use BCELogitLoss: BCELogitLoss can be useful in situations where the model outputs are already in the logit form or when you want to avoid potential numerical instability that may arise from working directly with probabilities.

In summary, both BCE Loss and BCELogitLoss are used for binary classification tasks. BCE Loss is more commonly used and is suitable in most cases, while BCELogitLoss can be advantageous in specific situations where logits are more appropriate or for better numerical stability. The choice between the two depends on the specific requirements of your model and the characteristics of your dataset. In many practical scenarios, you can start with BCE Loss and then explore using BCELogitLoss if you encounter any numerical stability issues.

## Formulas --

#### **Binary Cross Entropy (BCE) Loss:**

Given the true binary label y (0 or 1) and the predicted probability of the positive class  $\hat{y}$  (between 0 and 1), the BCE Loss is calculated as:

BCE Loss = -[ 
$$y * log(\hat{y}) + (1 - y) * log(1 - \hat{y})$$
 ]

where:

- y is the true binary label (0 or 1).
- $\hat{y}$  is the predicted probability of the positive class (between 0 and 1).
- log() denotes the natural logarithm.

The BCE Loss function penalizes the model more when the predicted probability  $\hat{y}$  diverges from the true label y.

### Binary Cross Entropy with Logits (BCELogitLoss):

Given the true binary label y (0 or 1) and the logits z (the raw model output before applying the sigmoid function), the BCELogitLoss is calculated as:

$$BCELogitLoss = max(z, 0) - z * y + log(1 + exp(-abs(z)))$$

where:

- y is the true binary label (0 or 1).
- z is the logit, which is the raw model output before applying the sigmoid function.
- log() denotes the natural logarithm.
- exp() is the exponential function.

The BCELogitLoss function is used when working with logits directly, and it can provide numerical stability benefits, especially when z is large or small. The function penalizes the model based on the deviation of the logits from the true label y.

It's important to note that in practice, many deep learning libraries and frameworks, such as PyTorch and TensorFlow, have built-in functions for computing these loss functions. So, you don't need to calculate the loss manually. Instead, you can leverage the library-provided functions to compute the loss during the training process.