1

Assignment 2 SUBHASISH SAIKIA AI20MTECH14001

Abstract—This document explains the properties of a directional vector and how to find out if the given points are the vertices of a parallelogram, using directional vectors

Download all python codes from

https://github.com/subhasishsaikia22/EE5609—Matrix—theory

and latex-tikz codes from

https://github.com/subhasishsaikia22/EE5609—Matrix—theory

1 Problem

Using directional vectors, show that the points

$$\begin{pmatrix} 2 \\ 1 \end{pmatrix}, \quad \begin{pmatrix} 4 \\ 7 \end{pmatrix} \quad \begin{pmatrix} 5 \\ 4 \end{pmatrix} \quad and \quad \begin{pmatrix} 1 \\ 4 \end{pmatrix}$$
 (1.0.1)

are vertices of a parallelogram.

2 EXPLANATION

Two lines are parallel if their respective directional vectors are in the same ratio. Let the points be denoted by:

$$\mathbf{A} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \tag{2.0.1}$$

$$\mathbf{B} = \begin{pmatrix} 5\\4 \end{pmatrix} \tag{2.0.2}$$

$$\mathbf{C} = \begin{pmatrix} 4 \\ 7 \end{pmatrix} \tag{2.0.3}$$

$$\mathbf{D} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} \tag{2.0.4}$$

The directional vector of AB is

$$\begin{pmatrix} 2-5\\1-4 \end{pmatrix} = \begin{pmatrix} -3\\-3 \end{pmatrix}$$
 (2.0.5)

The directional vector of **BC** is

$$\begin{pmatrix} 5 - 4 \\ 4 - 7 \end{pmatrix} = \begin{pmatrix} 1 \\ -3 \end{pmatrix}$$
 (2.0.6)

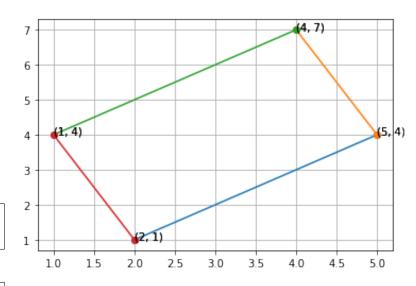


Fig. 1: This is the 2D diagram of the parallelogram with the given vertices

The directional vector of CD is

$$\begin{pmatrix}
4 - 1 \\
7 - 4
\end{pmatrix} = \begin{pmatrix}
3 \\
3
\end{pmatrix}

(2.0.7)$$

The directional vector of **AD** is

$$\begin{pmatrix} 2-1\\1-4 \end{pmatrix} = \begin{pmatrix} 1\\-3 \end{pmatrix}$$
 (2.0.8)

The directional vector of **AC** is

$$\begin{pmatrix}
2-4\\1-7
\end{pmatrix} = \begin{pmatrix}
-2\\-6
\end{pmatrix}

(2.0.9)$$

Since the directional vectors of **AB** and **CD** are in the same ratio, so **AB** and **CD** are parallel and also opposite to each other.

Similarly, the directional vectors of **BC** and **AD** are in the same ratio,hence **BC** and **AD** are parallel and opposite.

Since the two pairs of opposite sides are parallel, the given points are the vertices of the parallelogram.

Moreover the sum of the directional vectors of ${\bf AB}$ and ${\bf BC}$

$$\begin{pmatrix} -3 \\ -3 \end{pmatrix} + \begin{pmatrix} 1 \\ -3 \end{pmatrix} = \begin{pmatrix} -3 + 1 \\ -3 - 3 \end{pmatrix} = \begin{pmatrix} -2 \\ -6 \end{pmatrix}$$

Thus AB + BC = AC, which satisfy parallelogram law of vector addition i.e vector sum of two adjacent side of a parallelogram is the diagonal vector of the parallelogram.