Differential Evolution Illustration : Cross over Operations

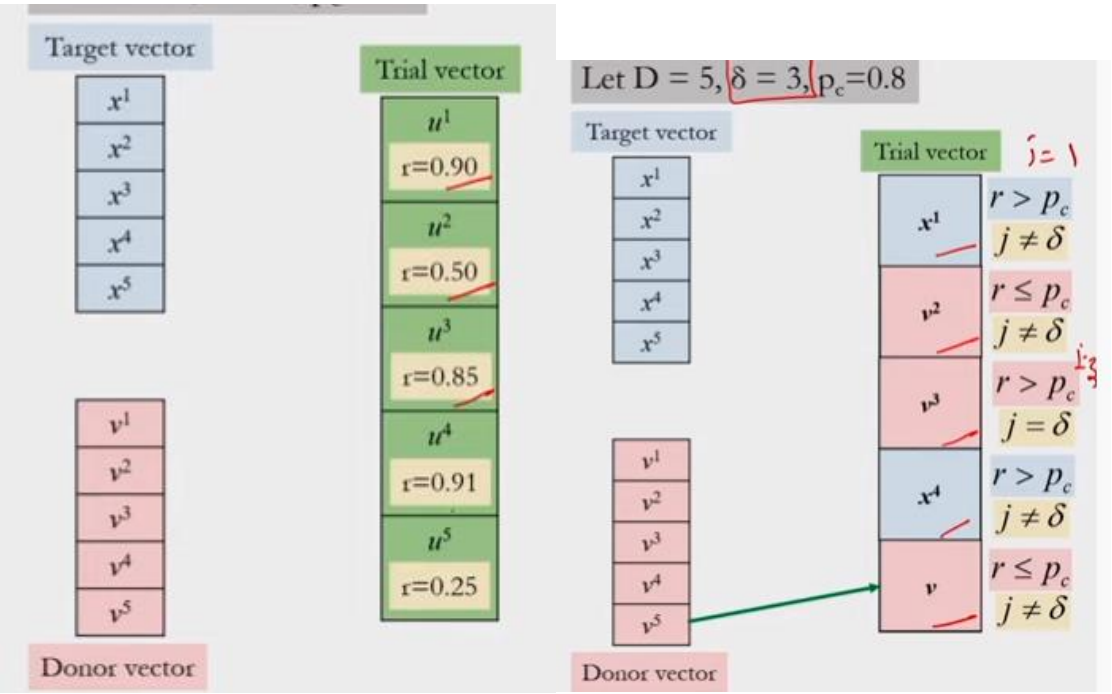
Bionomial Crossover Operation

Question 1: Consider Control parameters as D = 5, delta (or beta) = 3 and four elements as Target vector: $x^1x^2x^3x^4$.

The parameter setting of a random number and delta is as follows:

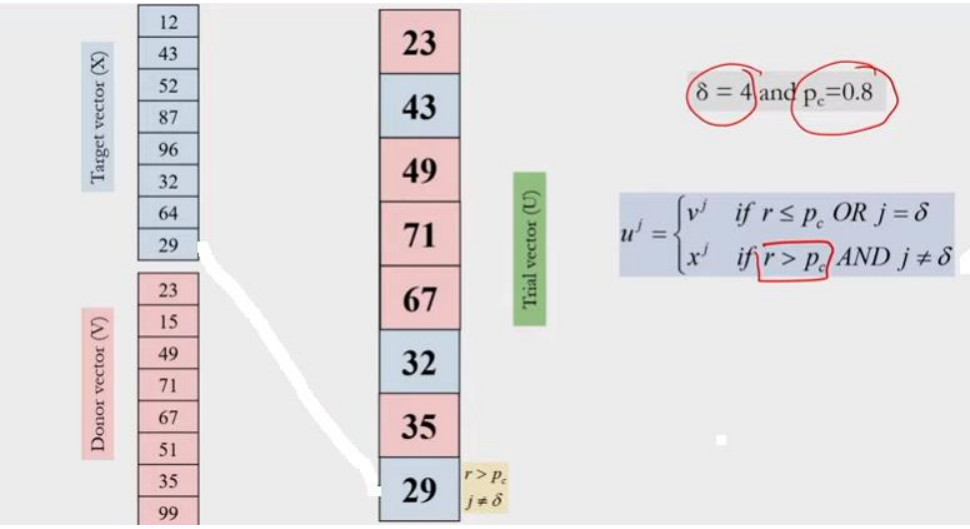
$$u^j = \begin{cases} v^j & \text{if } r \le p_c \text{ OR } j = \delta \\ x^j & \text{if } r > p_c \text{ AND } j \ne \delta \end{cases}$$

The bionomial crossover can be shown as follows:



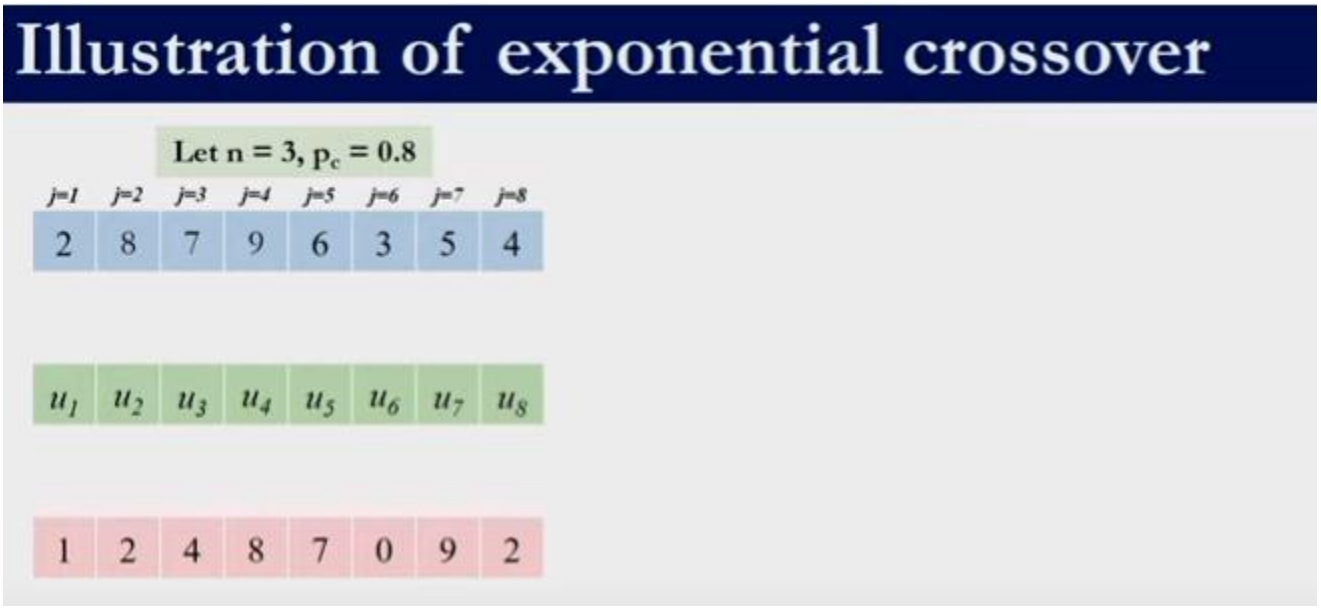
Question 2 : Consider another example where delta (beta) = 4 and Probabilty= 0.8

Perform the bionomial cross over



Exponiential Cross over:

Question 1



Given :Target vector and donor vector. Random number n and Pc is given. Determine the trial b=vector U1, u2….

Generate a random number between 1 and 8 as n = 3 and let Pc= 0.8

So direct copy third variable directly copy third variable from the donor vector

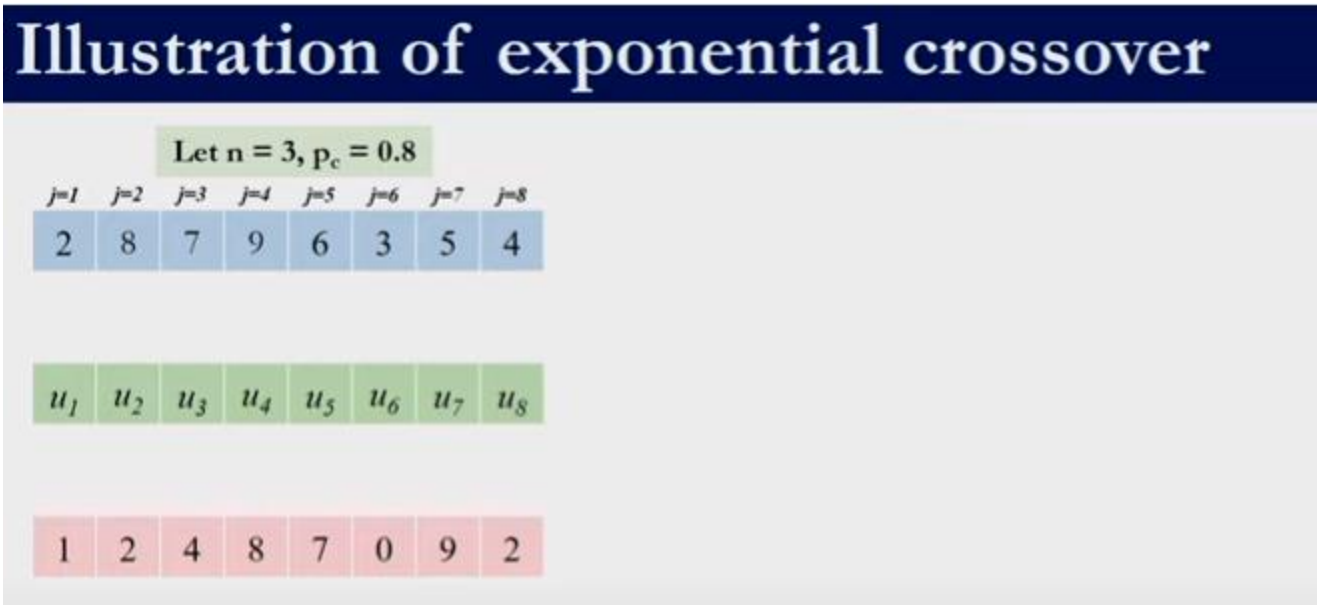


Illustration of exponential crossover
Let n = 3, p_c = 0.8
j=1 j=2 j=3 j=4 j=5 j=6 j=7 j=8
2 8 7 9 6 3 5 4
u_1 u_2 u_3 u_4 u_5 u_6 u_7 u_8
1 2 4 8 7 0 9 2

Case 1:

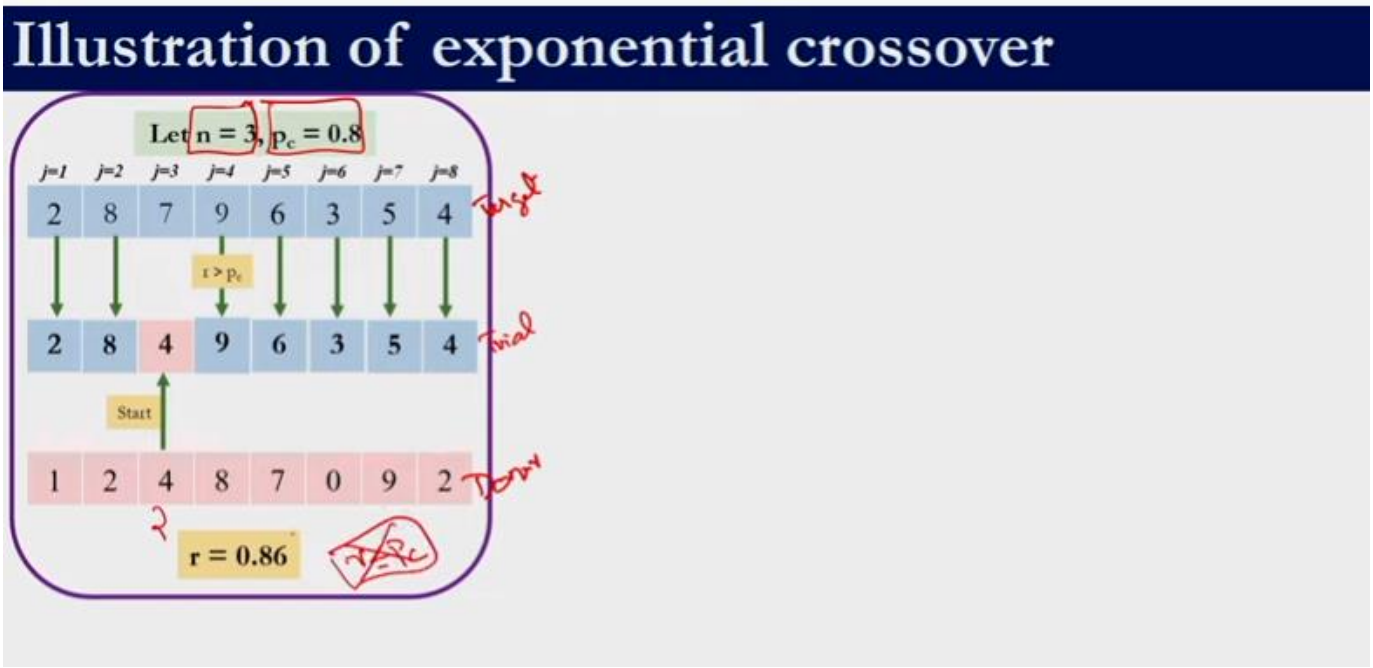
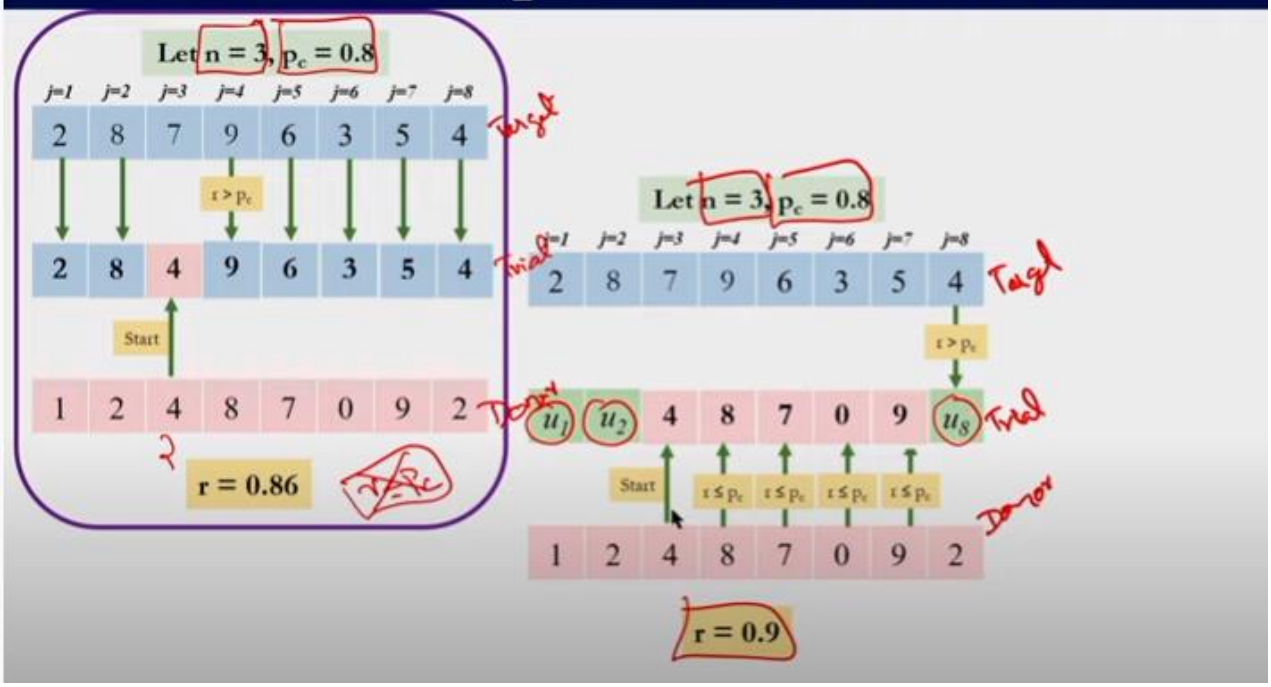
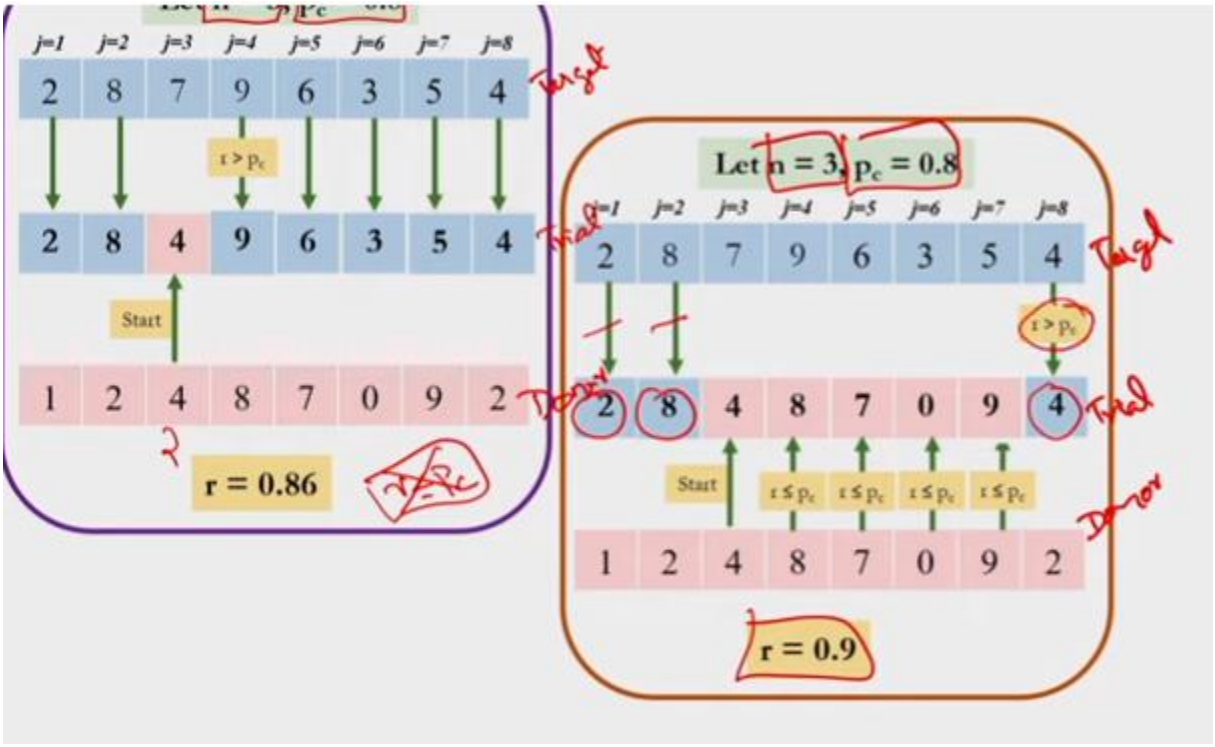


Illustration of exponential crossover
Let n = 3, p_c = 0.8
j=1 j=2 j=3 j=4 j=5 j=6 j=7 j=8
2 8 7 9 6 3 5 4
r > p_c
2 8 4 9 6 3 5 4
Start
1 2 4 8 7 0 9 2
r = 0.86

Case 2:

Illustration of exponential crossover




j=1 j=2 j=3 j=4 j=5 j=6 j=7 j=8
2 8 7 9 6 3 5 4
Target
r > pc
2 8 4 9 6 3 5 4
Start
1 2 4 8 7 0 9 2
Donor
r = 0.86
Let n = 3, pc = 0.8
Trial
2 8 7 9 6 3 5 4
r > pc
2 8 4 8 7 0 9 4
r ≤ pc
r = 0.9

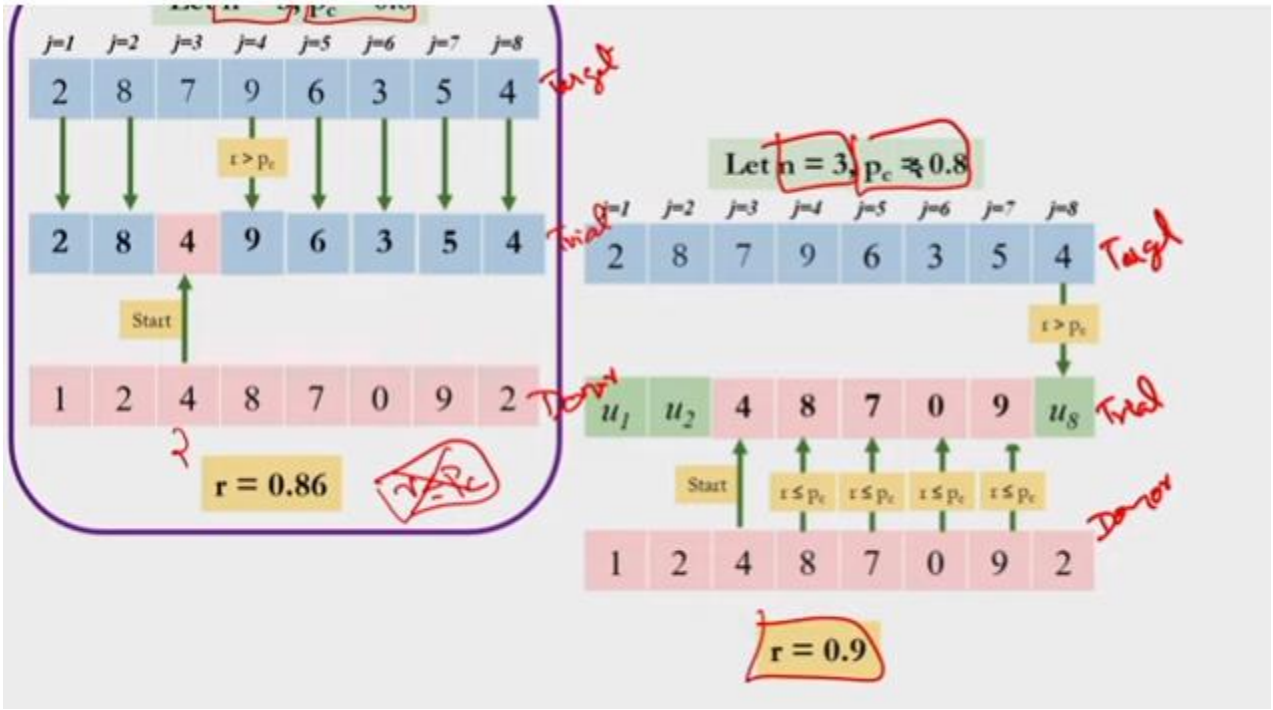

j=1 j=2 j=3 j=4 j=5 j=6 j=7 j=8
2 8 7 9 6 3 5 4
Target
r > pc
2 8 4 9 6 3 5 4
Start
1 2 4 8 7 0 9 2
Donor
r = 0.86
Let n = 3, pc = 0.8
Trial
2 8 7 9 6 3 5 4
r > pc
u1 u2 4 8 7 0 9 u8
r ≤ pc
1 2 4 8 7 0 9 2
r = 0.9

Illustration of exponential crossover