

# Region and Shape Representation and Description

Presented by  
Dr. Subarna Chatterjee  
[subarna.cs.et@msruas.ac.in](mailto:subarna.cs.et@msruas.ac.in)



# CONTENTS

- After performing image segmentation, a region may be represented in terms of
  - external characteristics (boundaries).
  - internal characteristics (texture).
- A shape may be considered as a filled region with a unique value,
  - e.g.  $f(x,y)=1$



# Boundary Processing

- The segmentation techniques discussed earlier, yield raw data in the form of pixels along a boundary or pixels contained in a region.
- It is standard practice to use schemes that compact the segmented data into representations that facilitate the computation of descriptors.
- In this section, we discuss various boundary pre-processing approaches suitable for this purpose.



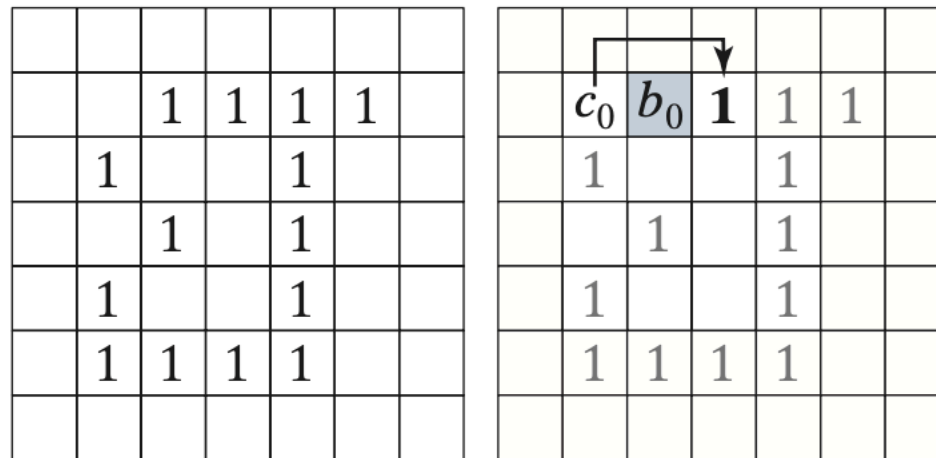
# Boundary Following (Tracing)

- The points in the boundary of a region be ordered in a **clockwise** or **counter-clockwise** direction.
- Consequently, we will discuss **boundary-following** algorithm whose output is an *ordered* sequence of points.
- We assume
  1. Binary Images (object and background points are labelled 1 and 0);
  2. Images are padded with a border of 0's to eliminate the possibility of an object merging with the image borders.
  3. We limit the discussion to single regions. This extends to multiple, disjoint regions by processing the regions individually.



# Cont..

- Given a binary region  $R$  or its boundary, the algorithm for following the border of  $R$ :
  - Let the starting point  $b_0$ , be the uppermost, leftmost point in the image labelled 1.
  - Denote by  $c_0$  the west neighbour of  $b_0$ .  $c_0$  is always a background point.



## Cont..

3. Examine the 8-neighbors of  $b_0$ , starting at  $c_0$  and proceeding in a clockwise direction.
4. Let  $b_1$  denote the first neighbour encountered whose value is 1.
5. Let  $c_1$  denote the background point immediately preceding  $b_1$  in the sequence.

|  |   |   |   |   |   |  |  |  |  |
|--|---|---|---|---|---|--|--|--|--|
|  |   |   |   |   |   |  |  |  |  |
|  |   | 1 | 1 | 1 | 1 |  |  |  |  |
|  | 1 |   |   | 1 |   |  |  |  |  |
|  |   | 1 |   | 1 |   |  |  |  |  |
|  | 1 |   |   | 1 |   |  |  |  |  |
|  | 1 | 1 | 1 | 1 |   |  |  |  |  |
|  |   |   |   |   |   |  |  |  |  |

|  |       |       |   |   |   |  |  |  |  |
|--|-------|-------|---|---|---|--|--|--|--|
|  |       |       |   |   |   |  |  |  |  |
|  | $c_0$ | $b_0$ | 1 | 1 | 1 |  |  |  |  |
|  | 1     |       |   | 1 |   |  |  |  |  |
|  |       | 1     |   | 1 |   |  |  |  |  |
|  | 1     |       |   | 1 |   |  |  |  |  |
|  | 1     | 1     | 1 | 1 |   |  |  |  |  |
|  |       |       |   |   |   |  |  |  |  |



# Cont..

6. Store the locations of  $b_0$  and  $b_1$  for use in Step 10.
7. Let  $b=b_1$  and  $c=c_1$ .
8. Let the 8-neighbors of  $b$ , starting at  $c$  and proceeding in a clockwise direction, be denoted by  $n_1, n_2, \dots, n_8$ . Find the first  $n_k$  labeled 1.

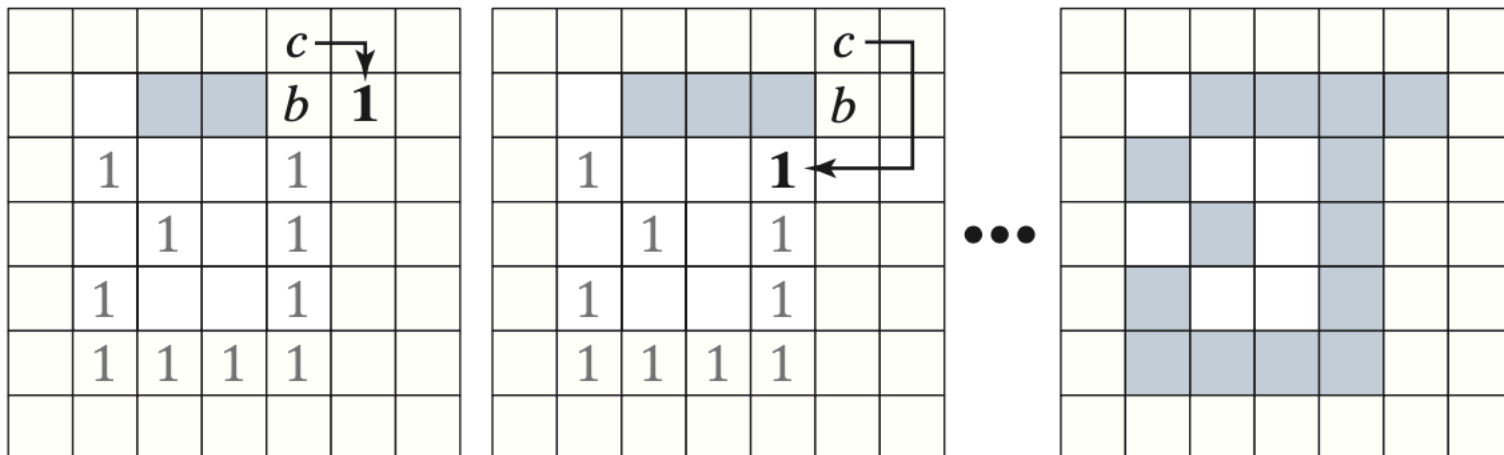
|  |   |   |   |   |   |  |
|--|---|---|---|---|---|--|
|  |   |   |   |   |   |  |
|  |   | 1 | 1 | 1 | 1 |  |
|  | 1 |   |   | 1 |   |  |
|  |   | 1 |   | 1 |   |  |
|  | 1 |   |   | 1 |   |  |
|  | 1 | 1 | 1 | 1 |   |  |
|  |   |   |   |   |   |  |

|  |       |       |   |   |   |  |
|--|-------|-------|---|---|---|--|
|  |       |       |   |   |   |  |
|  | $c_0$ | $b_0$ | 1 | 1 | 1 |  |
|  | 1     |       |   | 1 |   |  |
|  |       | 1     |   | 1 |   |  |
|  | 1     |       |   | 1 |   |  |
|  | 1     | 1     | 1 | 1 |   |  |
|  |       |       |   |   |   |  |

|  |   |   |     |   |   |  |
|--|---|---|-----|---|---|--|
|  |   |   | $c$ |   |   |  |
|  |   |   | $b$ | 1 | 1 |  |
|  | 1 |   |     | 1 |   |  |
|  |   | 1 |     | 1 |   |  |
|  | 1 |   |     | 1 |   |  |
|  | 1 | 1 | 1   | 1 |   |  |
|  |   |   |     |   |   |  |

# Cont..

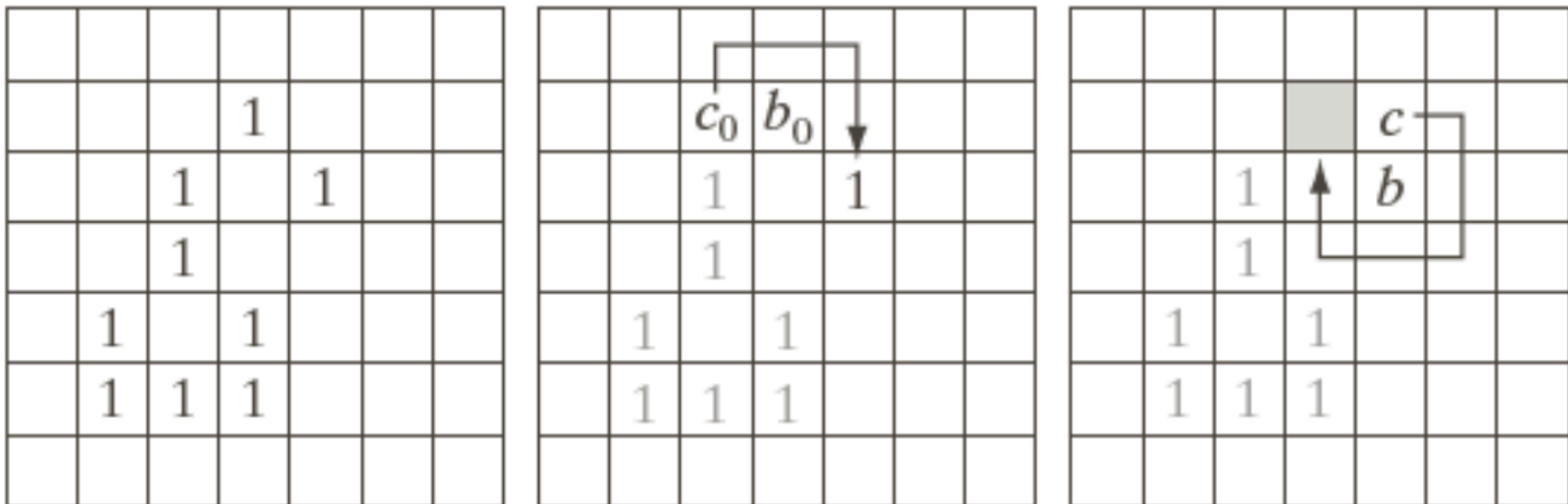
9. Let  $b=n_k$  and  $c=n_{k-1}$ .
  10. Repeat steps 8 and 9 until  $b=b_0$ , that is, we have reached the first point and the next boundary point found is  $b_1$ .
- The algorithm is due to G. Moore [1968]



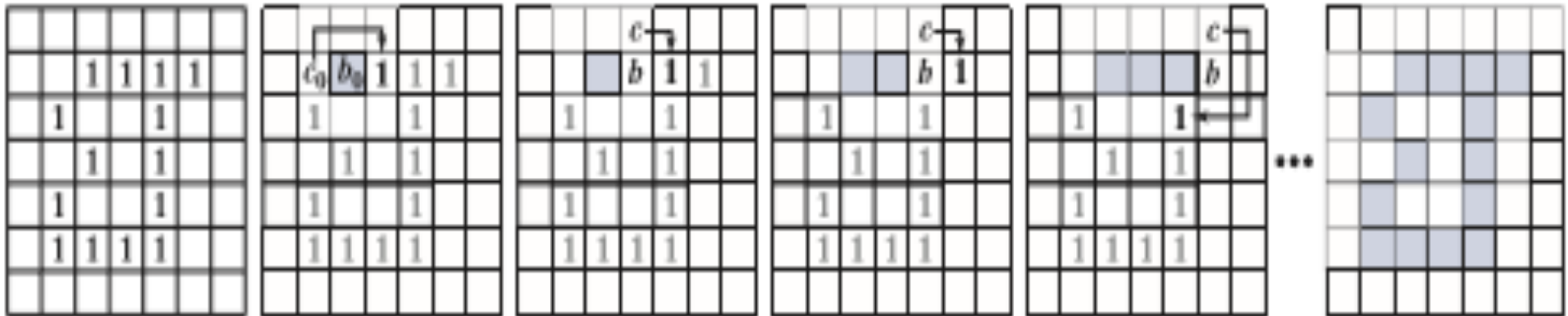


# Cont..

- The need for the stopping rule “... and the next boundary point found is  $b_1$ ” is shown below.
- We would only include the spur at the right if we stop when we reach the initial point without checking the next point.



# Cont..



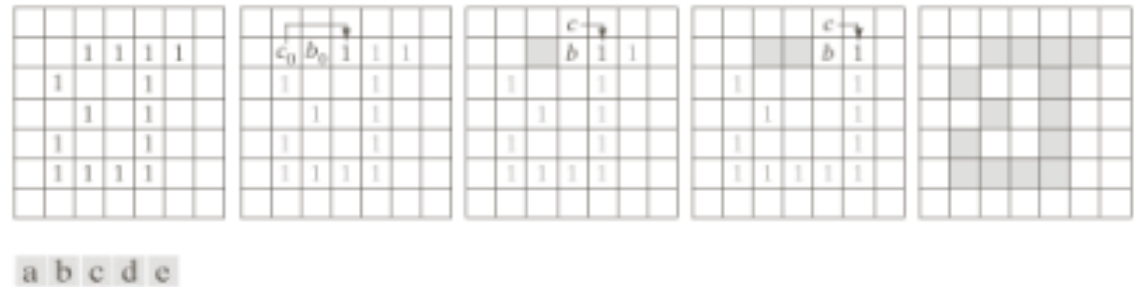
a b c d e f

**FIGURE 11.1** Illustration of the first few steps in the boundary-following algorithm. The point to be processed next is labeled in bold, black; the points yet to be processed are gray; and the points found by the algorithm are shaded. Squares without labels are considered background (0) values.

# Cont..

## Assumptions:

1. The image is binary where 1=foreground and 0=background
2. The image is padded with a border of 0's so an object cannot merge with the border.
3. There is only one object in this example.

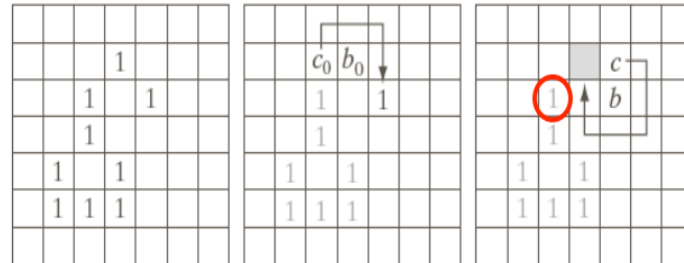


**FIGURE 11.1** Illustration of the first few steps in the boundary-following algorithm. The point to be processed next is labeled in black, the points yet to be processed are gray, and the points found by the algorithm are labeled as gray squares.

## Moore Boundary Tracking Algorithm [1968]:

1. Start with the uppermost, leftmost foreground point  $b_0$  in the image. Let  $c_0$  be the west neighbor of  $b_0$ . Going clockwise from  $c_0$  identify the first non-zero neighbor  $b_1$  of  $b_0$ . Let  $c_1$  be the background point immediately preceding  $b_1$  in the sequence.
  2. Let  $b=b_1$  and  $c=c_1$ .
  3. Let the 8-neighbors of  $b$  starting at  $c$  and proceeding clockwise be denoted as  $n_1, n_2, \dots, n_8$ . Find the first  $n_k$  which is foreground (i.e., a "1").
  4. Let  $b=n_k$  and  $c=n_{k-1}$ .
  5. Repeat steps 3 and 4 until  $b=b_0$  and the next boundary point found is  $b_1$ .
- The sequence of  $b$  points found when the algorithm stops is the set of ordered boundary points.

# Boundary Tracking



a b c

**FIGURE 11.2** Illustration of an erroneous result when the stopping rule is such that boundary-following stops when the starting point,  $b_0$ , is encountered again.

The Moore boundary following algorithm repeats until  $b=b_0$  and the next boundary point found is  $b_1$ .

This prevents errors encountered in spurs. Simply finding  $b_0$  again is not enough. For example, in this figure the algorithm would start at  $b_0$ , find  $b$ , and then come back to  $b_0$  stopping prematurely with only  $b=b_0$ . However, the next boundary point found should be the circled point which is NOT  $b_1$ . Adding "and the next boundary point found is  $b_1$ " will cause the algorithm to traverse the lower part of the object.

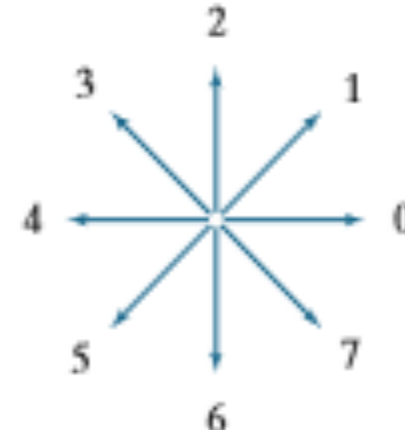
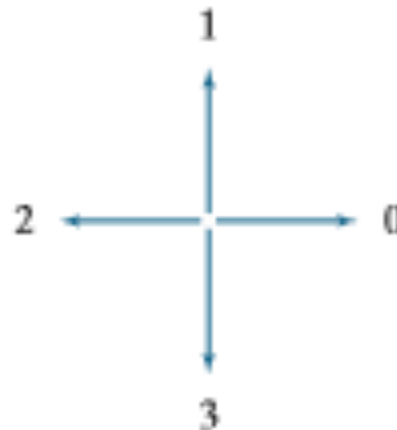
# Boundary Representation: Chain code

- We describe the shape of the boundary of an object in an image, known as *chain code* although name is *Freeman chain code*.
- The idea is to traverse the boundary of the object, and for every new pixel, transcript the direction we travelled to reach this object. i.e. describe the sequence of steps generated when walking around the boundary
- The direction is coded by a numbering scheme (4 or 8-connectivity)

a b

**FIGURE 11.3**

Direction numbers for (a) 4-directional chain code, and (b) 8-directional chain code.



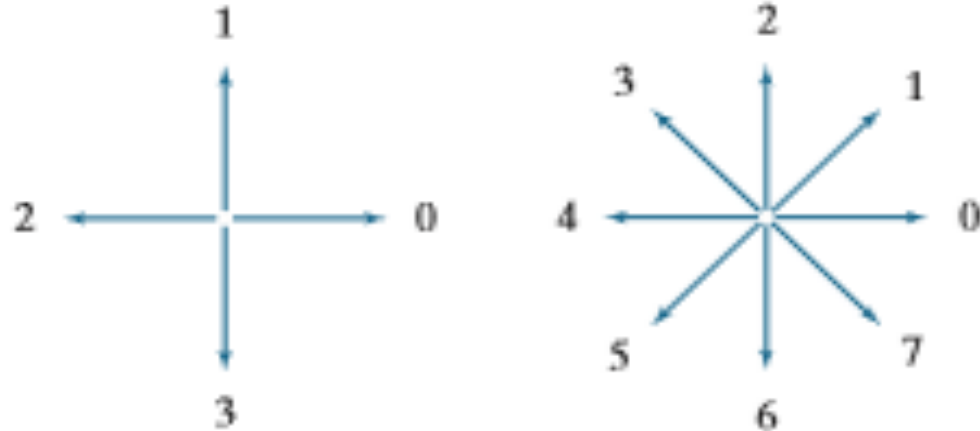
# Chain code

- Freeman codes [1961] represent a boundary by the sequence of straight line segments of specified length and direction.
- It is common to denote the code relative to either a  $N_4$  or a  $N_8$ , and we have two major classes: *absolute chain code* and *relative chain code*. In both cases, the code consists of directions (referring to the enumerated directions in Figure that you need to follow in order to traverse the boundary

a b

**FIGURE 11.3**

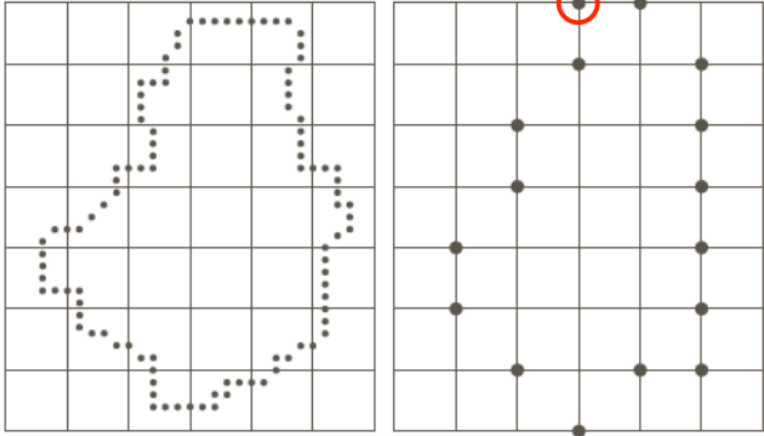
Direction numbers for (a) 4-directional chain code, and (b) 8-directional chain code.



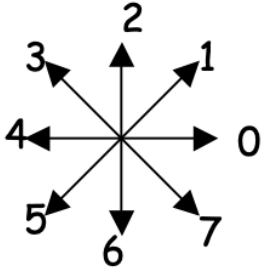
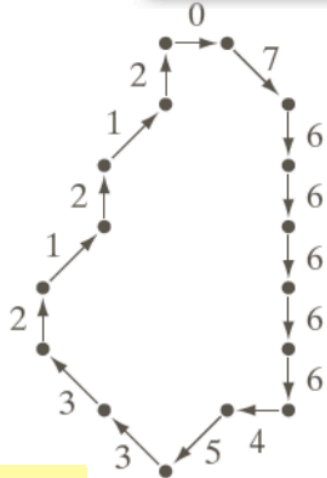
Using original pixels usually results in a code which is too long and subject to noise.

Arbitrarily start  
chain code here

## 8-direction chain coded boundary



Resample original image on a larger grid to reduce code size.



a b c

**FIGURE 11.4**  
(a) Digital boundary with resampling grid superimposed.  
(b) Result of resampling.  
(c) 8-directional chain-coded boundary.

8-connected code:  
0766666453321212



# Cont..

- Chain codes can be based on either 4-connectedness or 8-connectedness.
- **The first difference of the chain code:**
  - This difference is obtained by counting the number of direction changes (in a counterclockwise direction)
  - For example, the 1<sup>st</sup> difference of the 4-direction chain code 10103322 is 3133030.
- Assuming the first difference code represent a closed path, **rotation normalization** can be achieved by circularly shifting the number of the code so that the list of numbers forms the smallest possible integer.
- **Size normalization** can be achieved by adjusting the size of the resampling grid.





# Cont..

- To avoid noise degradation and long chains a resampling of the image grid is commonly used to describe the boundary at a coarser level.
- The chain code depends on the **starting point**.
- To **normalize** it, we treat the code as a circular sequence of direction numbers and redefine the starting point so that the resulting sequence forms an integer of minimum magnitude.
- To account for **rotation**, we use the first differences of the chain code instead of the code itself.
- The 1<sup>st</sup> difference is obtained by counting the number of direction changes that separate two adjacent elements of the code.

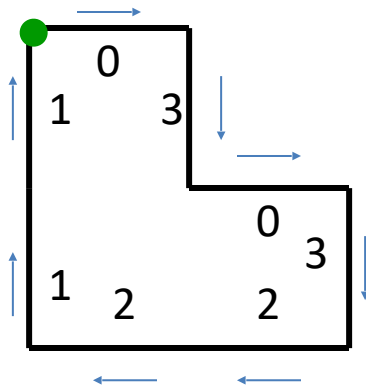


# Cont..

- Given an image WD the 4 chain and 8 chain and found the shape number.
- Ans:-
- Steps to find **Normalized Chain Code** :-
  1. Calculate the **Chain Code**.
  2. Calculate **Circulate 1<sup>st</sup> Difference** (CFD)
  3. Calculate **Normalize Chain Code** or **shape number**  
[**Normalized Circular 1<sup>st</sup> Difference** (NCFD)]



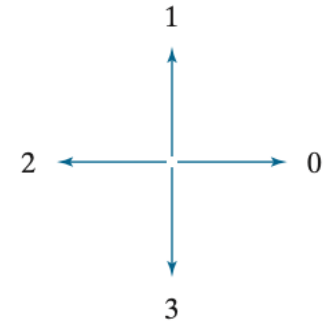
# Calculate Normalize Chain Code or Shape Number



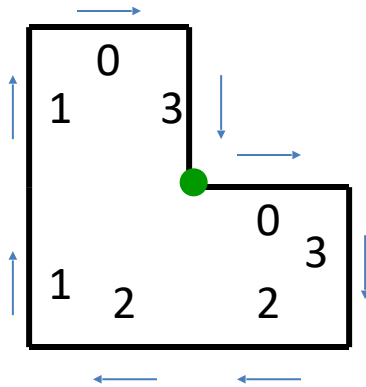
Chain Code: 03032211

CFD : 31330303

NCFD: 03033133



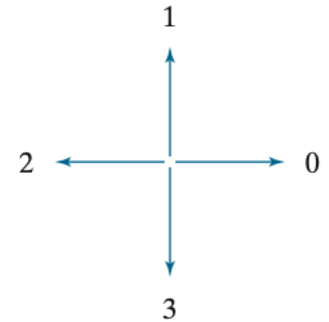
# Change Starting Point



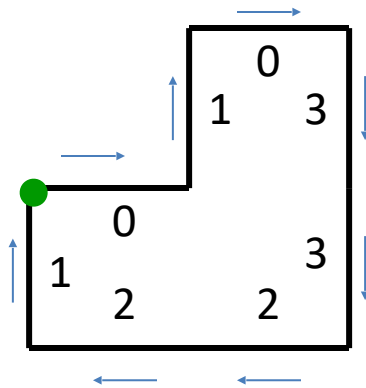
Chain Code: 03221103

CFD : 33030331

NCFD: 03033133



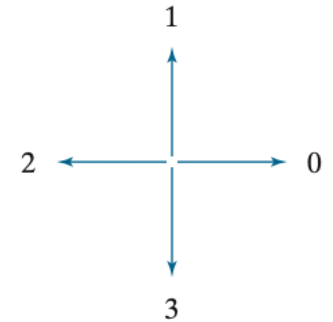
# Reflex



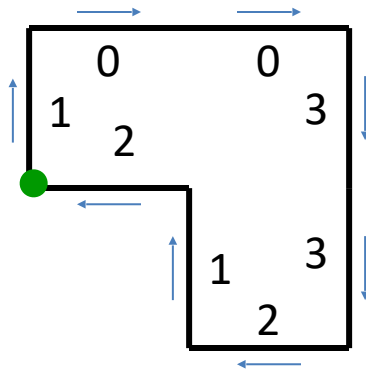
Chain Code: 01033221

CFD : 13303033

NCFD: 03033133



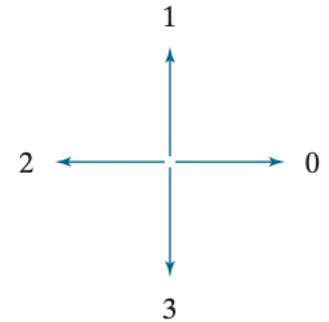
# Rotation



Chain Code: 10033212

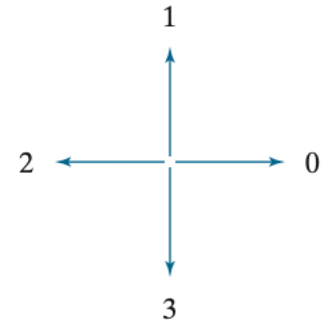
CFD : 30303313

NCFD: 03033133



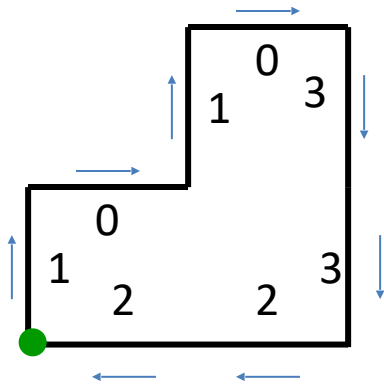
# Cont..

- **Example:-** Chain Code 10103322 (in a counter-clockwise direction)



# Cont..

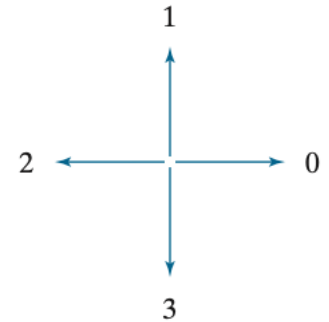
- Example:-** Chain Code 10103322 (in a counter-clockwise direction)



Chain Code: 10103322

CFD : 3133030

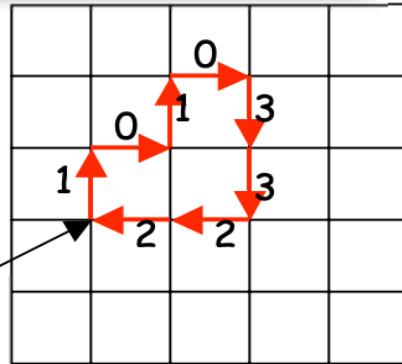
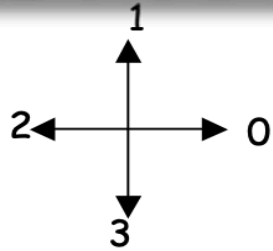
NCFD: 2201313





# Cont..

## 4-direction chain coded boundary



Arbitrarily start  
chain code here

4-connected code:  
10103322

One practice is to rotate (pick start)  
to get smallest integer code.

(START CODE HERE) —————→  
Between end and start of boundary

Chain codes can be normalized for  
rotation by using first  
differences.

To compute the first difference  
go in counter-clockwise direction  
and find number of  $90^\circ$  rotations  
of direction.

|     |                             |
|-----|-----------------------------|
| 1→0 | <u>3</u> -90° rotations ccw |
| 0→1 | <u>1</u> -90° rotation ccw  |
| 1→0 | <u>3</u> -90° rotations ccw |
| 0→3 | <u>3</u> -90° rotations ccw |
| 3→3 | <u>0</u> -90° rotations ccw |
| 3→2 | <u>3</u> -90° rotations ccw |
| 2→2 | <u>0</u> -90° rotations ccw |
| 2→1 | <u>3</u> -90° rotations ccw |

4-connected difference code:  
33133030

# Cont..

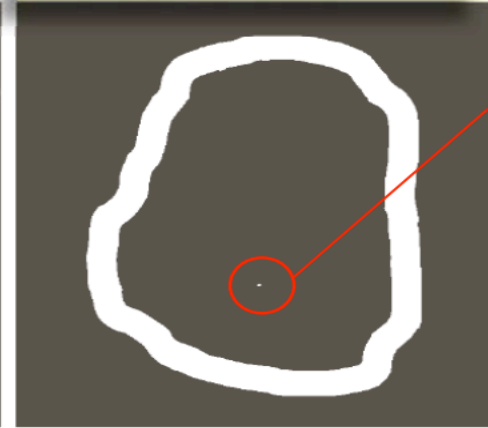
Noisy 570x570 image



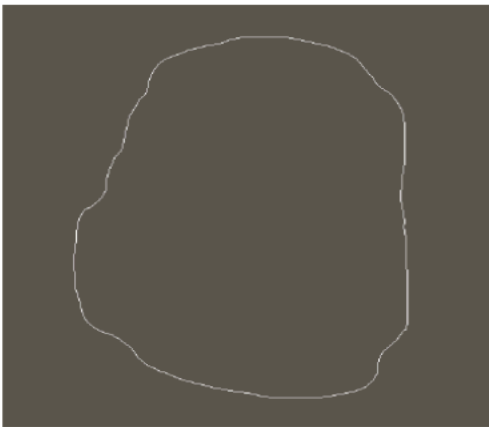
9x9 averaging mask



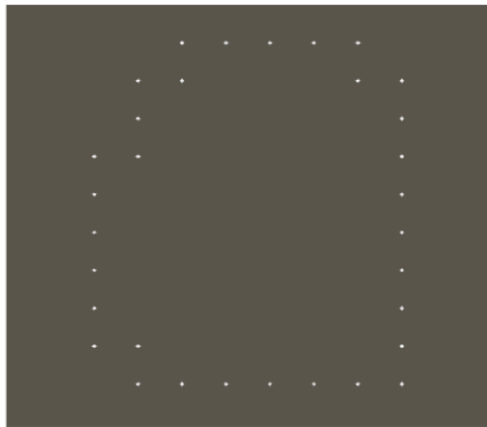
Otsu thresholded



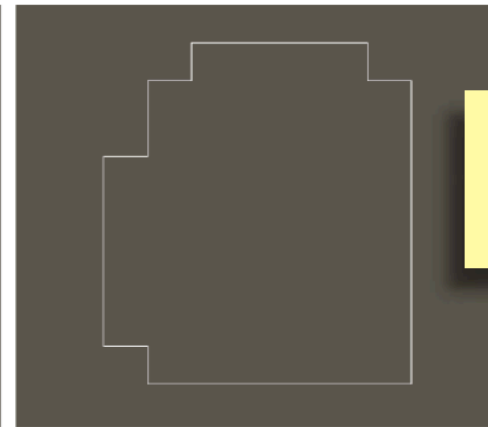
Single-point from Otsu thresholding (ignored)



Longest outer boundary



Resampled on a 50x50 pixel grid



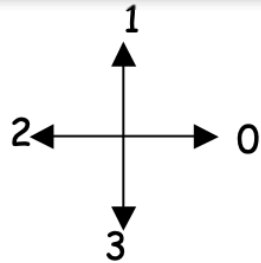
Joining resampled pixels by straight lines

8-directed chain code:  
000060666666666644444424222202202  
Minimum magnitude integer:  
000060666666666644444424222202202  
First difference:  
00062600000006000006260000620626

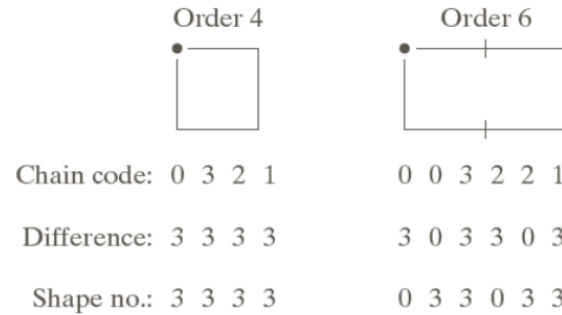


# Shape Number – A boundary descriptor

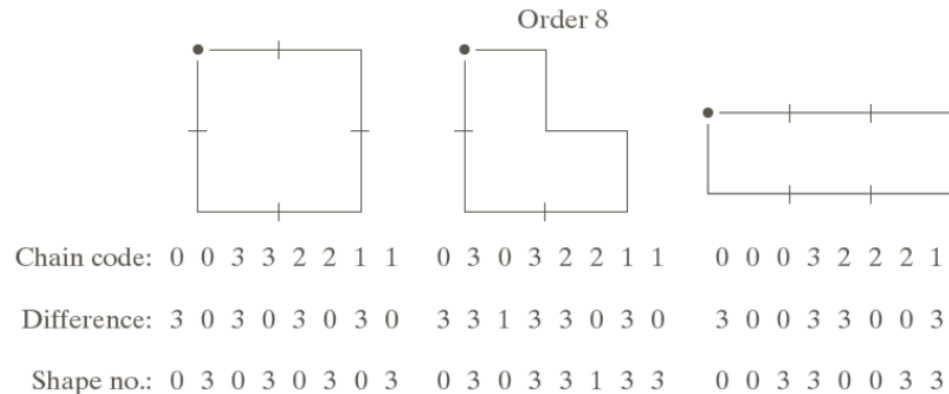
## 4-direction chain code



To compute the first difference go in counter-clockwise direction and find number of  $90^\circ$  rotations of direction.



**FIGURE 11.17**  
All shapes of order 4, 6, and 8. The directions are from Fig. 11.3(a), and the dot indicates the starting point.



The shape number  $n$  is the smallest magnitude first difference chain code.  
 $n$  is even for closed boundaries

# Cont..

## Definitions:

Diameter =  $\max[D(p_i), D(p_j)]$  where  $p_i$  and  $p_j$  are points on the boundary.

Major axis is the line segment of length equal to the diameter and connecting two points on the boundary.

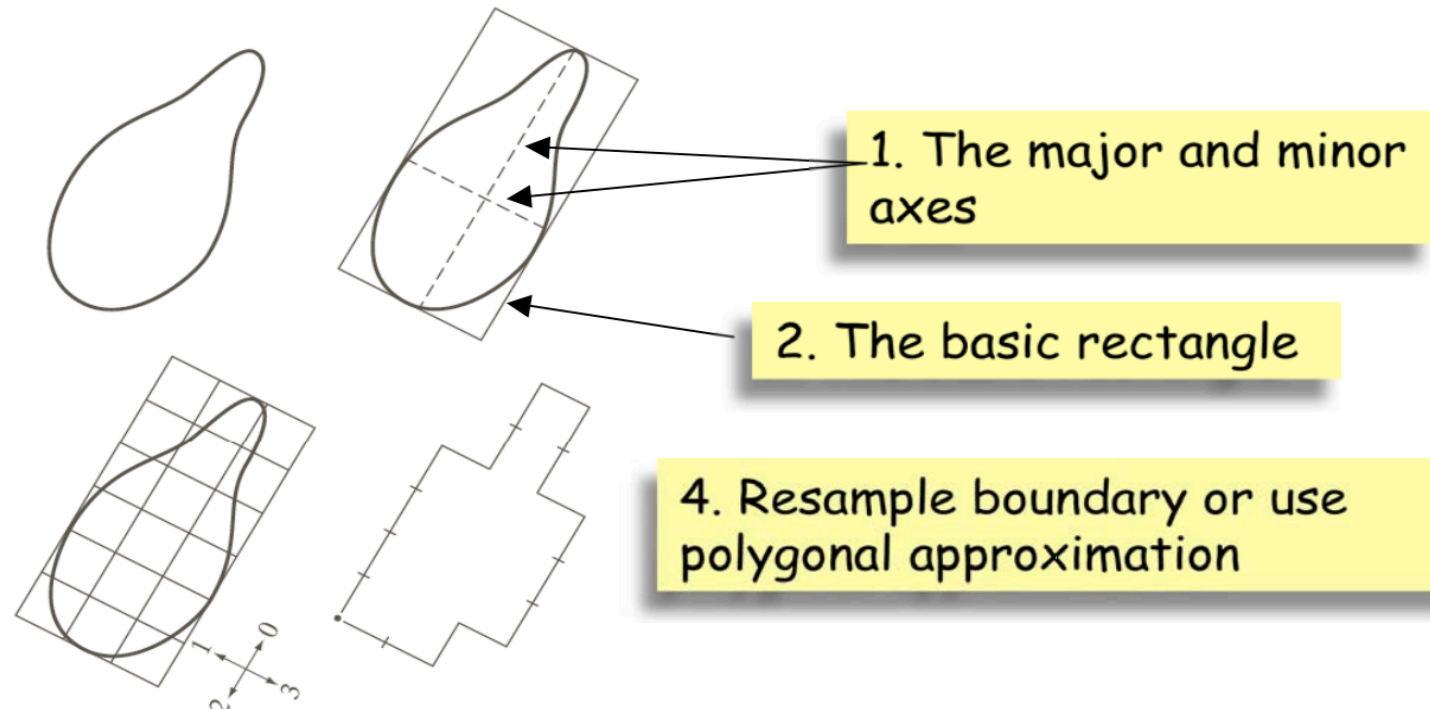
Minor axis is the line perpendicular to the major axis and of such length that a box passing through the outer four points of intersection of the boundary and the major/minor axes completely enclose the boundary

This box enclosing the boundary is called the basic rectangle.

Eccentricity is the ratio of major to minor axis.



# Cont..



3. Use the rectangle with  $n=18$  (given) which best approximates the shape of basic rectangle, i.e.,  $6 \times 3 = 18$ .

Chain code: 0 0 0 0 3 0 0 3 2 2 3 2 2 2 1 2 1 1

Difference: 3 0 0 0 3 1 0 3 3 0 1 3 0 0 3 1 3 0

Shape no.: 0 0 0 3 1 0 3 3 0 1 3 0 0 3 1 3 0 3

5. Computer chain code, its first difference, and the corresponding shape number.

|   |   |
|---|---|
| a | b |
| c | d |

**FIGURE 11.18**  
Steps in the generation of a shape number.

# Chain Coding issues/drawbacks

- Code becomes very long and noise sensitive
  - Use larger grid spacing, smooth/edit the code
- Scale dependent
  - Choose appropriate grid spacing
- Start point determines result
  - Treat code as circular (minimum magnitude integer) 754310 -> 075431
- Depends on rotation
  - Calculate difference code (counter-clockwise) 075431 -> 767767





# Cont..

- Chain codes are generated by following a boundary in a clockwise or counter-clockwise direction and assigning a direction to the segments connecting every pair of pixels.
- Disadvantage: Can be unacceptably long.
  - Solution: Re-sampling (down sample) the boundary
- Disadvantage: Is starting point dependent
  - Solution: Normalize the representation string to the smallest integer.



*Thank You*

