

Name: \_\_\_\_\_

ID: \_\_\_\_\_

## Department of Computer Science and Engineering

## CSE330: Numerical Methods

Summer 2018

## Quiz-1

SET B

Full Marks: 15

Time: 20minutes

Solve  $x = \tan x$  using Newton Raphson's method upto 3 iterations and fill up the table below. Given initial guess,  $x_1 = 4.6$ .

Iteration Count	$x_i$	$ \epsilon_a \%$	$f(x_i)$	$f'(x_i)$
1	4.54573	1.1939%	-1.3989	-35.34
2	4.5061	0.8795%	-0.2725	-22.835
3	4.4942	0.2648%	-0.01602	-20.34

$$f(x) = x - \tan x = 0$$

$$f'(x) = \frac{d}{dx}(x - \tan x) = \frac{d}{dx}(x) - \frac{d}{dx}(\tan x)$$

$$= 1 - \sec^2 x$$

$$= 1 - \frac{1}{\cos^2 x}$$

$$= 1 - \frac{1}{(\cos x)^2}$$

Iteration 1 :-

$$x_0 = 4.6$$

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)} = 4.6 - \frac{f(4.6)}{f'(4.6)}$$

$$= 4.6 - \frac{4.6 - \tan(4.6)}{1 - \left(\frac{1}{\cos 4.6}\right)^2}$$

$$= 4.54573$$

$$f(x_1) = f(4.54573)$$

$$= 4.54573 - \tan(4.54573)$$

$$= -1.3989$$

$$f'(x_1) = f'(4.54573)$$

$$= ~~4.54573~~ 1 - \left( \frac{1}{\cos(4.54573)} \right)^2$$

$$= -35.34$$

$$|e_a| = \left| \frac{x_1 - x_0}{x_1} \right| \times 100\% = \left| \frac{4.54573 - 4.6}{4.54573} \right| \times 100\%$$

$$= 1.1939\%$$

Iteration 2:

$$x_2 = x_1 - \frac{f(x_1)}{f'(x_1)}$$

$$= 4.54573 - \frac{-1.3989}{-35.34}$$

$$= 4.5061$$

$$f(x_2) = f(4.5061) = 4.5061 - \tan(4.5061)$$

$$= -0.2725$$

$$f'(x_2) = f'(4.5061) = 1 - \left( \frac{1}{\cos(4.5061)} \right)^2$$

$$= -22.835$$

$$|e_a| = \left| \frac{x_2 - x_1}{x_2} \right| \times 100\% = \left| \frac{4.5061 - 4.54573}{4.5061} \right| \times 100\%$$

$$= 0.8795\%$$

Iteration 3:

$$x_3 = x_2 - \frac{f(x_2)}{f'(x_2)} = 4.5061 - \frac{-0.2725}{-22.835}$$

$$= 4.4942$$

$$f(x_3) = f(4.4942) = 4.4942 - \tan(4.4942) = -0.01602$$

$$f'(x_3) = f'(4.4942) = 1 - \left( \frac{1}{\cos(4.4942)} \right)^2 = -20.34$$

$$|e_a| = \left| \frac{x_3 - x_2}{x_3} \right| \times 100\% = \left| \frac{4.4942 - 4.5061}{4.4942} \right| \times 100\%$$