

Assignment 2

CSE 422, sec-03

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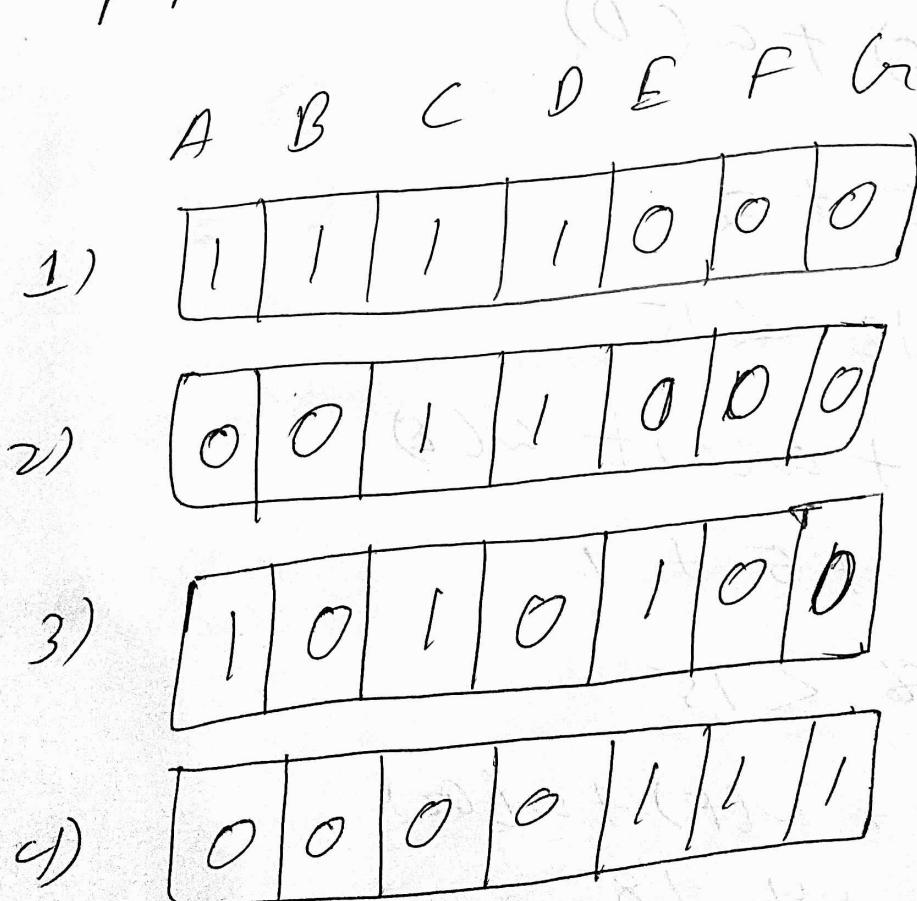
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CSE

Q1) Given,

	w	P
A	2	10
B	3	5
C	5	15
D	2	7
E	1	6
F	4	18
G	8	10

1) Creating 8 different chromosomes for initial population.



Q1) 2) Given -
maximum weight is 15
calculating individual chromosomes
weight

$$1) w(A) + w(B) + w(C) + w(D)$$
$$= 2 + 3 + 5 + 2$$
$$= 12 < 15$$

$$2) w(C) + w(D)$$
$$= 5 + 2$$
$$= 12 < 15$$

$$3) w(A) + w(C) + w(D)$$
$$= 2 + 5 + 1$$
$$= 8 < 15$$

$$4) w(E) + w(F) + w(G)$$
$$= 1 + 4 + 8$$
$$= 13 < 15$$

We will design the fitness function in a way by calculating profits corresponding to selected items.

$$1) F(P_1) = 10 \quad (\text{as it has crossed the maximum weight})$$

$$2) F(P_2) = 15 + 7 \\ = 22$$

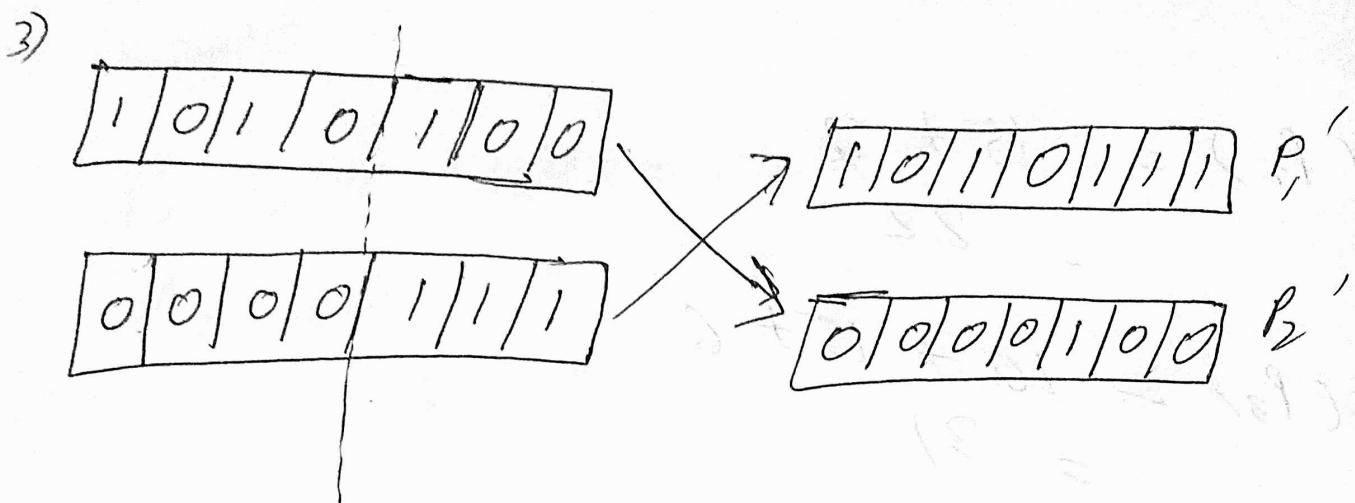
$$3) F(P_3) = 10 + 15 + 6 \\ = 31$$

$$4) F(P_4) = 6 + 18 + 10 \\ = 34$$

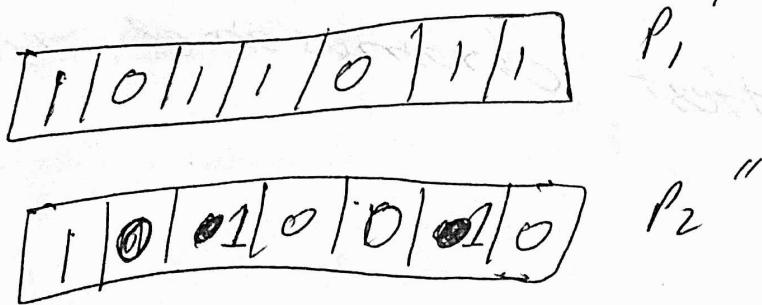
So Here, two fittest chromosomes would be

3 and 4.

Q) 3) Single point crossover



4) Performing mutation



$$\begin{aligned} f(P_1'')_{\text{weights}} &= (2+5+2+4+8) \\ &= 26 \neq 15 \\ \therefore f(P_1'') &= 0 \end{aligned}$$

$F(P_2'')$

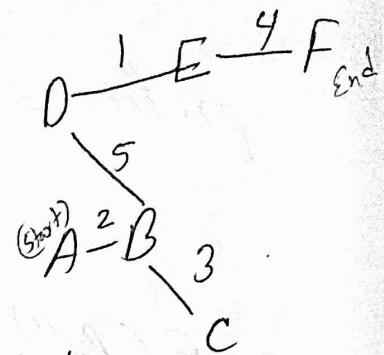
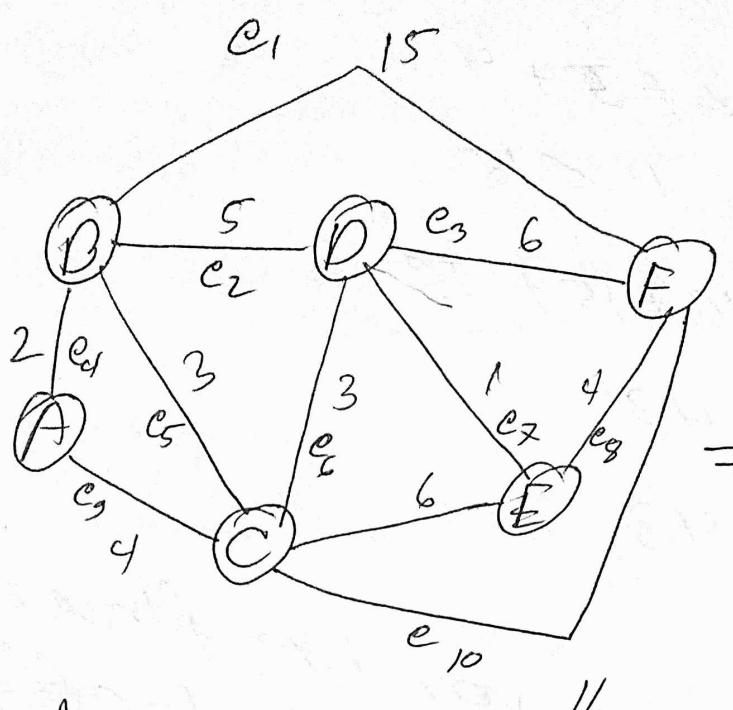
$$\text{weights} = 2 + 5 + 9 \\ = 16 < 15$$

$$\text{profit} = 10 + 15 + 18 \\ = 43$$

$$= F(P_2'') = 43$$

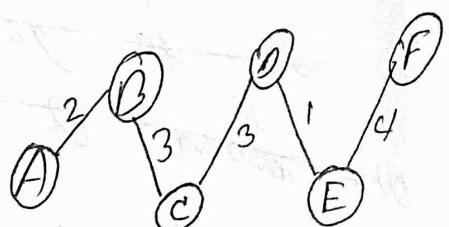
~~so we got one very high fitness and one with 0 fitness in the final offspring~~
We got a higher fitness of the final offspring P_2'' after mutation. while P_1'' has 0 fitness and is discarded.

Q2)



Solved
using Kruskal's
MST Alg = 15

Sorted weight	Src	Dest
1	D	E
2	A	B
3	B	C
4	A	C
4	E	F
5	B	D
6	C	E
6	D	F
11	C	F
15	B	F



Greedy approach.

$$2 + 3 + 3 + 1 + 4$$

$$= 13$$

every city visited
only once with ∞ in
shortest path.

As we are free to choose any node ~~any~~ as start node and end node/goal node.

Let's consider A ~~as~~ the start state and F as the goal state.

Now

A B C D E F

a)

1	0	1	0	1	1
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1	1	1	0	1	1
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a) Generating an initial population of 3 chromosomes keeping at mind the start node and goal node, also making sure all gene cities are visited, for this we will be using weight of the edges connecting two cities as the genes for chromosome sets.

1)	<table border="1"> <tr> <td>2</td><td>6</td><td>1</td><td>1</td><td>6</td><td>1</td><td>15</td></tr> </table>	2	6	1	1	6	1	15
2	6	1	1	6	1	15		

2)	<table border="1"> <tr> <td>4</td><td>3</td><td>6</td><td>1</td><td>1</td><td>11</td></tr> </table>	4	3	6	1	1	11
4	3	6	1	1	11		

3)	<table border="1"> <tr> <td>2</td><td>15</td><td>3</td><td>1</td><td>1</td><td>11</td></tr> </table>	2	15	3	1	1	11
2	15	3	1	1	11		

b) Now as we have used weights of edges between two cities, calculating total weight/costs of each chromosome will give us the ~~fit~~ fitness function. We have already solved the spanning tree using ~~Kruskal's MST algo~~ greedy approach which gave the minimum cost of ₹ 13. So the cost of the chromosome nearer to the ₹ 13 will be the best fit.

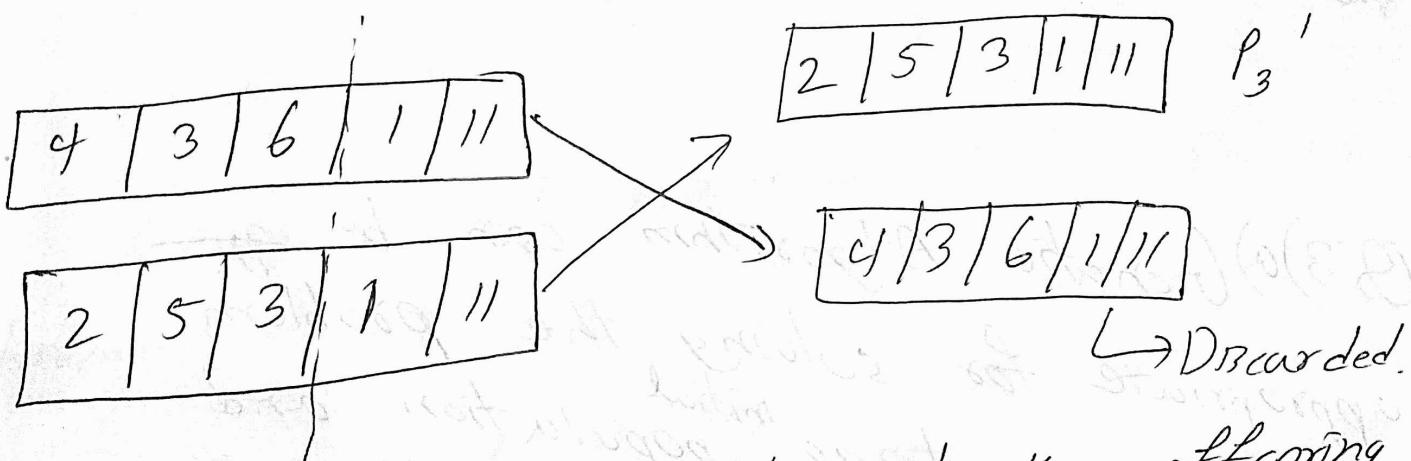
$$1) F(P_1) = 2 + 6 + 1 + 6 + 15 \\ = 30$$

$$F(P_2) = 4 + 3 + 6 + 1 + 11 \\ = 25$$

$$F(P_3) = 2+5+3+1+11 \\ = 22$$

\therefore Two fittest chromosomes are P_2 and P_3 .

c) Performing cross-over between P_2 and P_3 ,



If we consider the parents and the offspring they are not eligible as an optimal solution. Because the cities are visited more than once in the chromosome model and also it doesn't give the optimal minimum distance possible. So we have to perform mutation and repeat the processes until getting the optimal solution.

d)

2	1	5	/	3	/	1	/	1	/	1
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from the above parent each edges weight used of specific edges between two cities are individual genes and the solution is set in the chromosome.

(Q3)a) Genetic Algorithm can be appropriate for solving the problem if have a large initial population and high mutation rate. As this will give us the solution in least number of generations.

b)

Given,

items	weight	Profit
M	3	10
N	5	5
O	2	15
P	10	2
Q	2	6
R	1	3

Creating initial population of 4 different chromosomes.

	M	N	O	P	Q	R
P ₁	0	1	0	0	0	1
P ₂	1	0	0	1	1	1
P ₃	1	0	1	0	1	1
P ₄	0	0	1	1	1	0

$$\text{for } P_1, \text{ weights} \rightarrow (5+2+1) \\ = 13 < 21$$

$$\therefore F(P_1) = (5+15+3) \\ = 23 \quad (\text{profit})$$

$$\text{for } P_2, \text{ weights} \rightarrow (3+10+2+1) \\ = 16 < 21$$

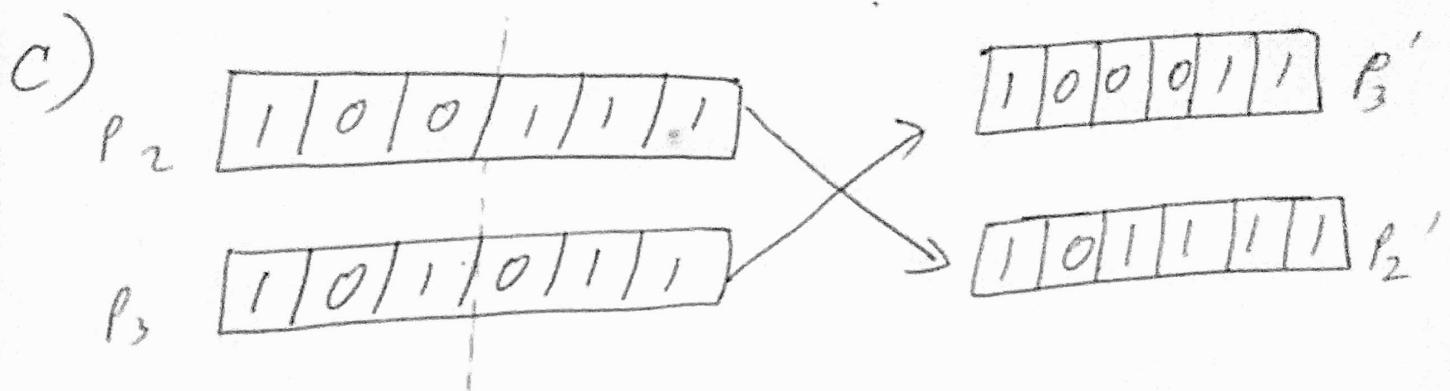
$$\therefore F(P_2) = (10+7+6+3) \\ = 33$$

$$\text{for } P_3, \text{ weights} \rightarrow (3+7+2+1) \\ = 13 < 21$$

$$F(P_3) = 39 \\ (7+10) = 17 < 21$$

$$\text{for } P_4, \text{ weights} \rightarrow (5+7) = 12 \\ F(P_4) = 15+7 = 22$$

Here fitness function B used as to maximize the profit. we found the two fittest chromosomes which are P_2 and P_3



d) performing mutation

P_3'' $[1|1|0|0|1|1]$

P_2'' $[1|0|0|1|1|1]$

$$\text{for } P_3'' \text{ weight} \rightarrow (3+5+2+1) \\ = 11 < 21$$

$$PL(P_3'') = 2^4$$

$$\text{for } P_2'' \text{ weights} \rightarrow (3+10+2+1) \\ = 16 < 21$$

$$PL(P_2'') = 2^6$$