



# Joint Distribution and Conditional Probability

# Data – Counts

	German Sheppard	Dobermann	Labrador	Marginal (Dysplasia)
None	10	30	60	100
Mild	30	40	210	280
Severe	170	30	30	230
Marginal (Breed)	200	100	300	600

- Dog breeds as columns
- The degree of hip dysplasia as rows

# Data – Frequency, Probability

	German Sheppard	Dobermann	Labrador	Marginal (Dysplasia)
None	0.017	0.050	0.100	0.167
Mild	0.050	0.067	0.350	0.467
Severe	0.283	0.050	0.050	0.383
Marginal (Breed)	0.333	0.167	0.500	1.000

- Dog breeds as columns
- The degree of hip dysplasia as rows

# Marginal Probability

	German Sheppard	Dobermann	Labrador	Marginal (Dysplasia)
None	0.017	0.050	0.100	0.167
Mild	0.050	0.067	0.350	0.467
Severe	0.283	0.050	0.050	0.383
Marginal (Breed)	0.333	0.167	0.500	1.000

- Probability that we select a dog of our population and it is a German Sheppard.
- $P(\text{breed}) \rightarrow$  marginal probability

# Marginal Probability

	German Sheppard	Dobermann	Labrador	Marginal (Dysplasia)
None	0.017	0.050	0.100	0.167
Mild	0.050	0.067	0.350	0.467
Severe	0.283	0.050	0.050	0.383
Marginal (Breed)	0.333	0.167	0.500	1.000

- Probability that we select a dog of our population and it shows mild dysplasia.
- $P(\text{dysplasia}) \rightarrow$  marginal probability

# Joint Probability

	German Sheppard	Dobermann	Labrador	Marginal (Dysplasia)
None	0.017	0.050	0.100	0.167
Mild	0.050	0.067	0.350	0.467
Severe	0.283	0.050	0.050	0.383
Marginal (Breed)	0.333	0.167	0.500	1.000

- Probability that we select a dog of our population and it is a Dobermann with mild dysplasia.
- $P(\text{breed, dysplasia}) \rightarrow$  joint probability

# Joint Probability

- The probability of particular combinations of 2 events taking place.
- The joint probability is symmetric  $\rightarrow P(A, B) = P(B, A)$
- In our example,  $P(\text{breed, dysplasia}) = P(\text{dysplasia, breed})$

# Marginal Probability

- The marginal probability is the probability of particular event, collapsed across the values of the other event.
- The marginal probability is the sum of the joint probabilities.
- $P(A) = \sum P(A, B)$
- In our example,  $P(\text{breed}) = \sum P(\text{dysplasia}, \text{breed})$



# Conditional Probability

	German Sheppard
None	0.017
Mild	0.050
Severe	0.283
Marginal (Breed)	0.333

Divide by 0.333



	German Sheppard
None	0.050
Mild	0.150
Severe	0.851
Marginal (Breed)	1

- A German Sheppard comes to the vet.
- We wonder: what is the probability of dysplasia given that it is a German Sheppard?

# Conditional Probability

- Probability of 1 outcome, given that the other is true.
- $P(A | B) \rightarrow$  probability of A given B
- $P(A | B) = P(A, B) / P(B)$
- Conditional probability is not symmetric  $\rightarrow P(A | B) \neq P(B | A)$
- In our example,  $P(\text{dysplasia} | \text{breed}) = \frac{P(\text{dysplasia, breed})}{P(\text{breed})}$

# Prior and Posterior Probability

- Prior probability is the unconditional probability assigned to an event before any relevant information is taken into account.
  - In our example,  $P(\text{dysplasia})$
- The posterior probability of an event, is the **conditional probability** that is assigned after taking into account the new evidence.
  - In our example,  $P(\text{dysplasia} \mid \text{breed} = \text{German Sheppard})$
- Prior and posterior are mathematically related by Bayes' Rule

# THANK YOU

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