

Tree-structured Parzen Estimators TPE

Bayes' Rule

$$P(y | x) = \frac{P(x | y) \times P(y)}{P(x)}$$

y is the score → f(x)

x is the hyperparameters

Gaussian Process Optimization

Approximate $P(y | x)$
with surrogate
function

- Gaussian Process

$$\left\{ \begin{array}{l} P(y | x) = \frac{P(x | y) \times P(y)}{P(x)} \end{array} \right.$$

y is the score $\rightarrow f(x)$

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Approximate $P(x | y)$
with surrogate
function

$$P(y | x) = \frac{P(x | y) \times P(y)}{P(x)}$$

y is the score $\rightarrow f(x)$

x is the hyperparameters

$$p(x|y) = \begin{cases} \ell(x) & \text{if } y < y^* \\ g(x) & \text{if } y \geq y^* \end{cases}$$

TPE

Approximate $P(x | y)$
with surrogate
function

$$P(y | x) = \frac{\overbrace{P(x | y) \times P(y)}^{P(x)}}{P(x)}$$

y is the score $\rightarrow f(x)$

x is the hyperparameters

$$p(x|y) = \begin{cases} \ell(x) & \text{if } y < y^* \\ g(x) & \text{if } y \geq y^* \end{cases}$$



$$EI_{y^*}(x) \propto \left(\gamma + \frac{g(x)}{\ell(x)}(1 - \gamma) \right)^{-1}$$

Approximate $P(x | y)$
with surrogate
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y is the score $\rightarrow f(x)$

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Guides where to sample next
for hyperparameters

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$$EI_{y^*}(x) \propto \left(\gamma + \frac{g(x)}{\ell(x)}(1 - \gamma) \right)^{-1}$$

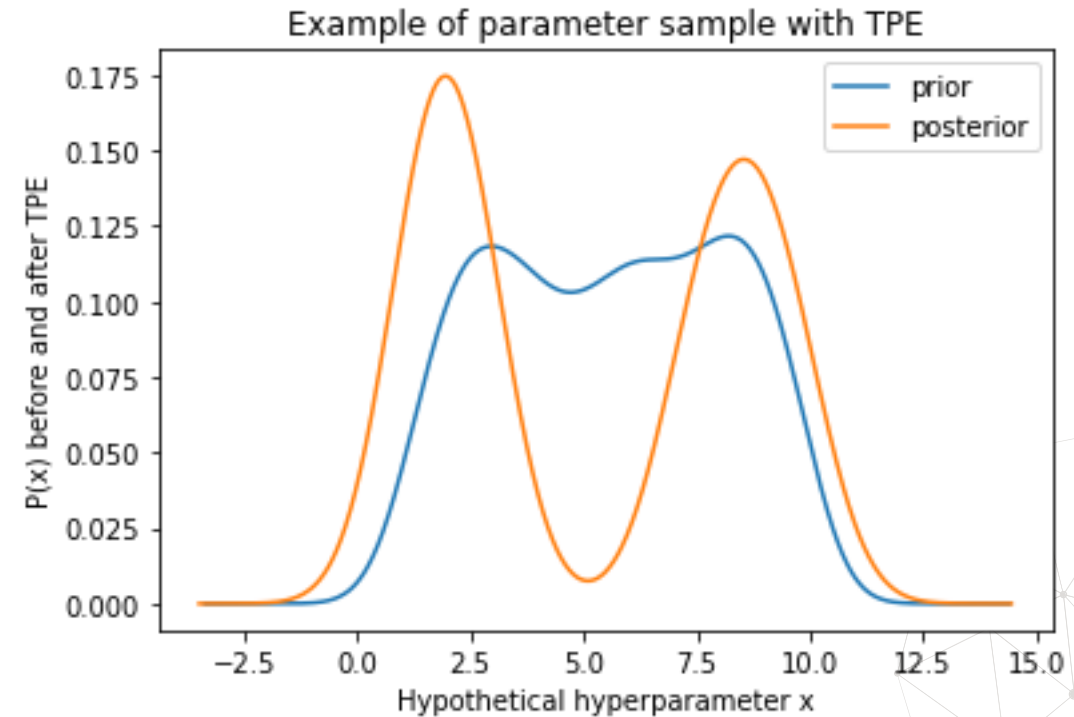
TPE - intuition

Approximate $P(x | y)$
with surrogate
function

$$P(y | x) = \frac{\overbrace{P(x | y) \times P(y)}^{P(x)}}{P(x)}$$

y is the score $\rightarrow f(x)$

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THANK YOU

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