

# Nested Cross-Validation

# Uses of Cross-Validation

- Estimate the generalization error of a given model
- Select best performing model from a group of models
  - Different algorithms
  - Different feature subsets
- Select hyperparameters

# Uses of Cross-Validation

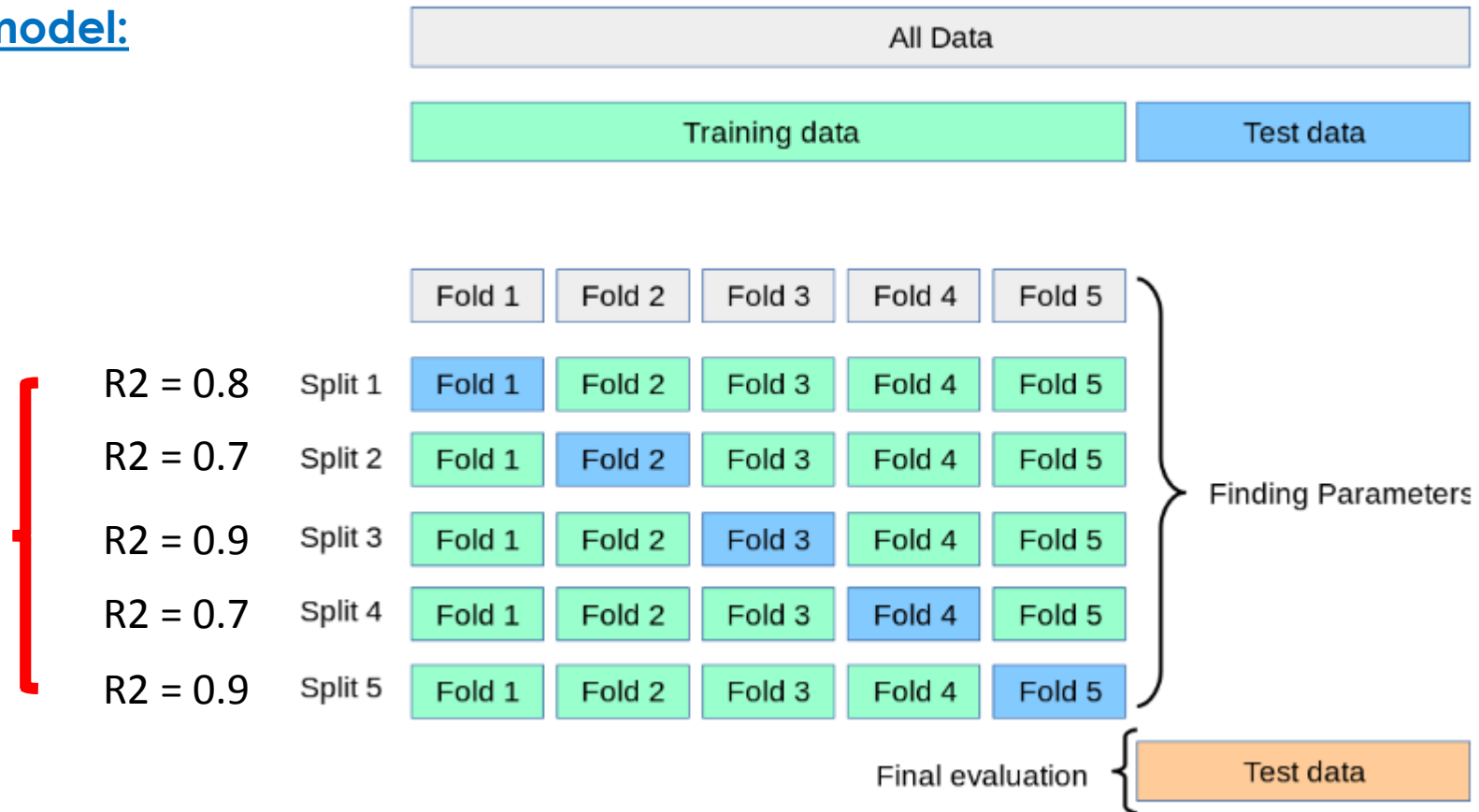
- Estimate the generalization error of a given model
- Select best performing model from a group of models
  - Different algorithms
  - Different feature subsets
- Select hyperparameters

# Cross-Validation & Generalization Error

When we have 1 model:

Generalization  
Error:

$R^2 = 0.8 \pm 0.1$



[https://scikit-learn.org/stable/modules/cross\\_validation.html](https://scikit-learn.org/stable/modules/cross_validation.html)

# Model selection, CV & Generalization Error

Generalization Error:

$R^2 = 0.8 \pm 0.1$

$R^2 = 0.8$   
 $R^2 = 0.7$   
 $R^2 = 0.9$   
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Fold 1	Fold 2	Fold 3	Fold 4	Fold 5
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Hyperparams 1

Generalization Error:

$R^2 = 0.84 \pm 0.06$

$R^2 = 0.8$   
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Hyperparams 2

Generalization Error:

$R^2 = 0.78 \pm 0.11$

$R^2 = 0.7$   
 $R^2 = 0.7$   
 $R^2 = 0.9$   
 $R^2 = 0.7$   
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Hyperparams 3

# Model selection, CV & Generalization Error

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Generalization Error:

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Hyperparams 2

Generalization Error:

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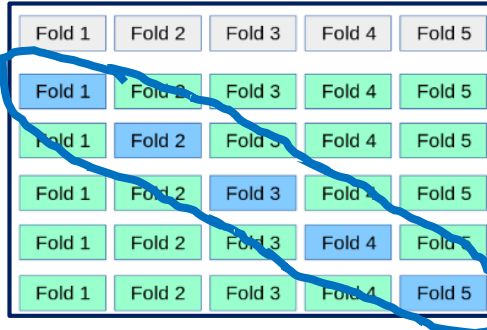
Hyperparams 3

# Model selection, CV & Generalization Error

Generalization Error:

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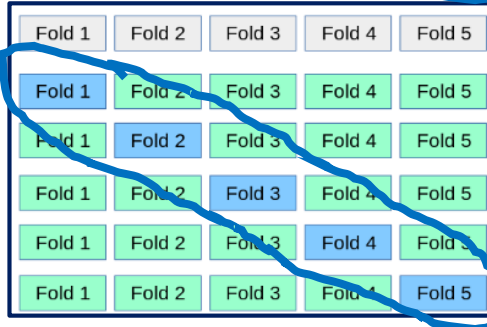


Hyperparameters 1

Generalization Error:

$R^2 = 0.84 \pm 0.06$

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 $R^2 = 0.8$   
 $R^2 = 0.9$   
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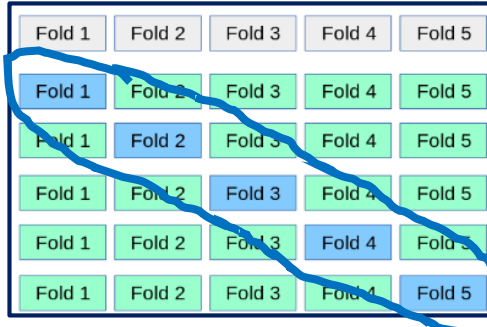


Hyperparameters 2

Generalization Error:

$R^2 = 0.78 \pm 0.11$

$R^2 = 0.7$   
 $R^2 = 0.7$   
 $R^2 = 0.9$   
 $R^2 = 0.7$   
 $R^2 = 0.9$



Hyperparameters 3

- Validation tests are the **same** for all models
- Validation set “leaks” information to model “selection” procedure
- Generalization error is optimistically biased

# Model selection, CV & Generalization Error

We need a *different* test set to get an **unbiased** evaluation of the generalization error of selected model (or selected hyperparameters for the purpose of this course)

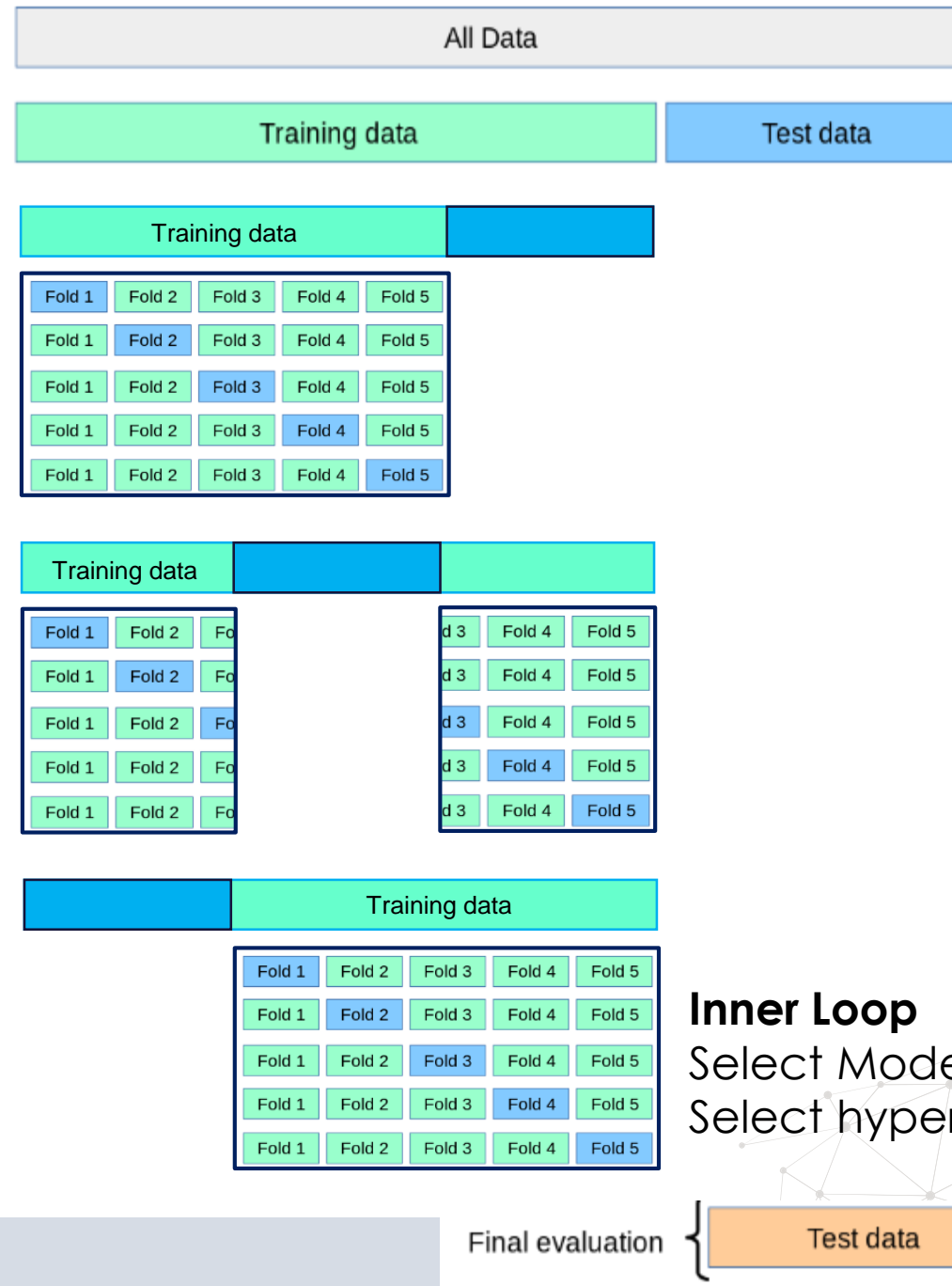
Particularly important for data science competitions.



# Nested CV

## Outer Loop

Estimate  
Generalization Error



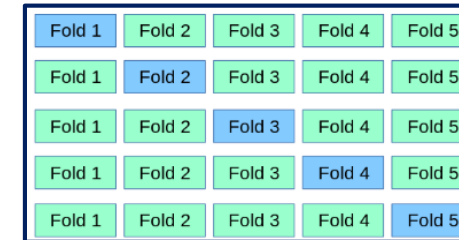
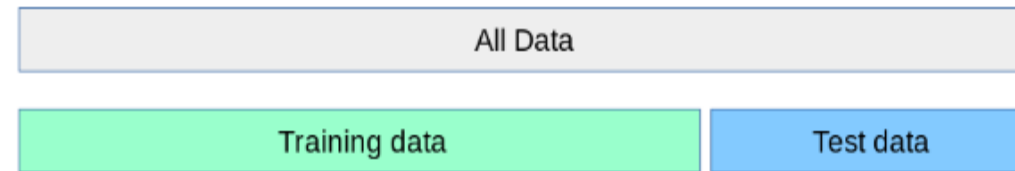
## Inner Loop

Select Model –  
Select hyperparameters

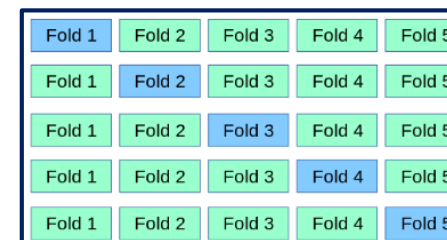
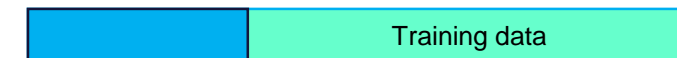
# Nested CV

## Outer Loop

Estimate  
Generalization Error

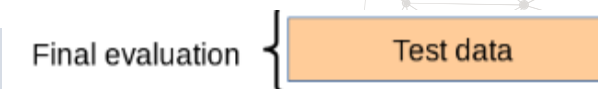


- Train all models
- Select Hyperparams
  - Asses error on outer loop



## Inner Loop

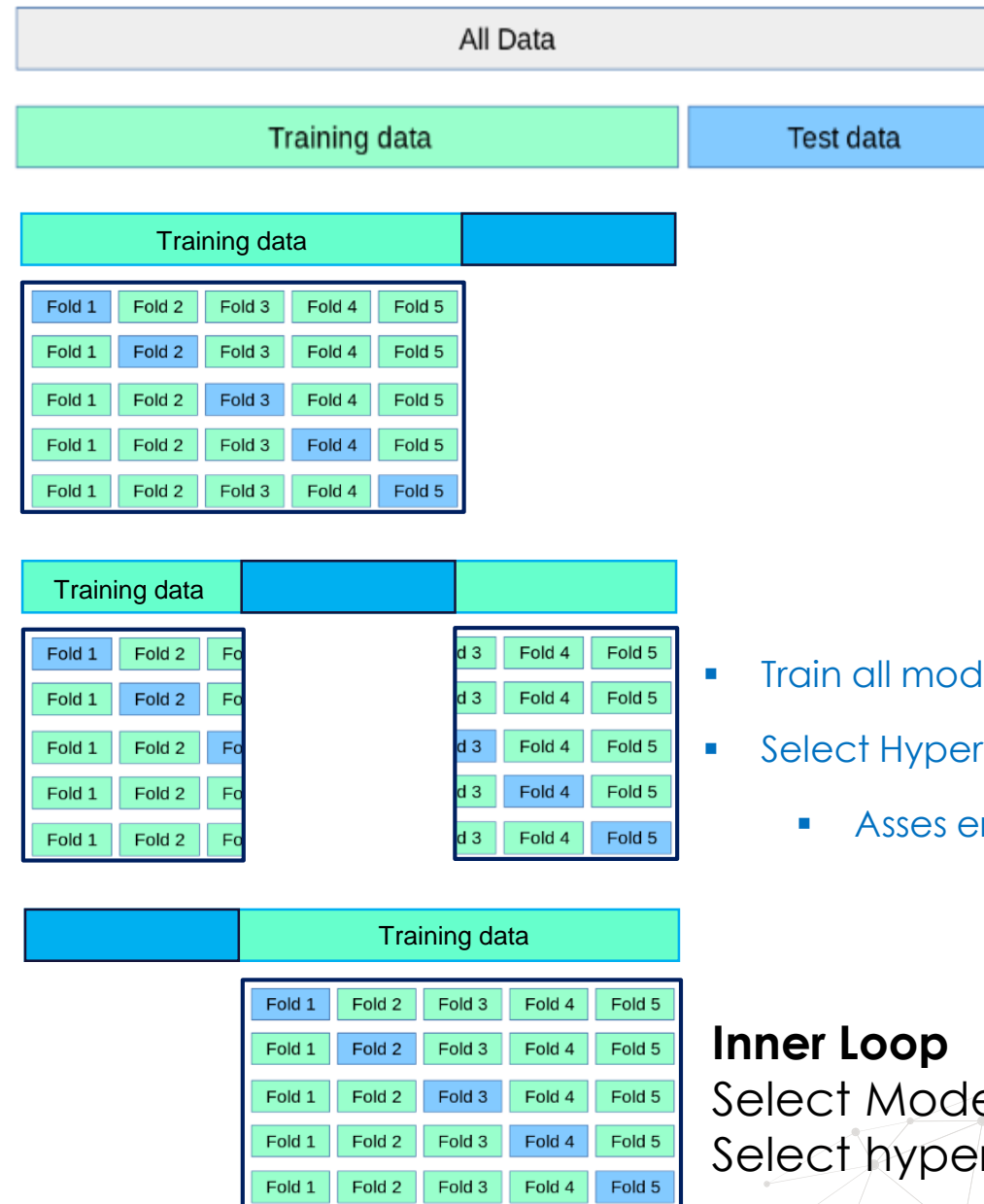
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Select hyperparameters



# Nested CV

## Outer Loop

Estimate  
Generalization Error



- Train all models
- Select Hyperparams
  - Asses error on outer loop

## Inner Loop

Select Model –  
Select hyperparameters

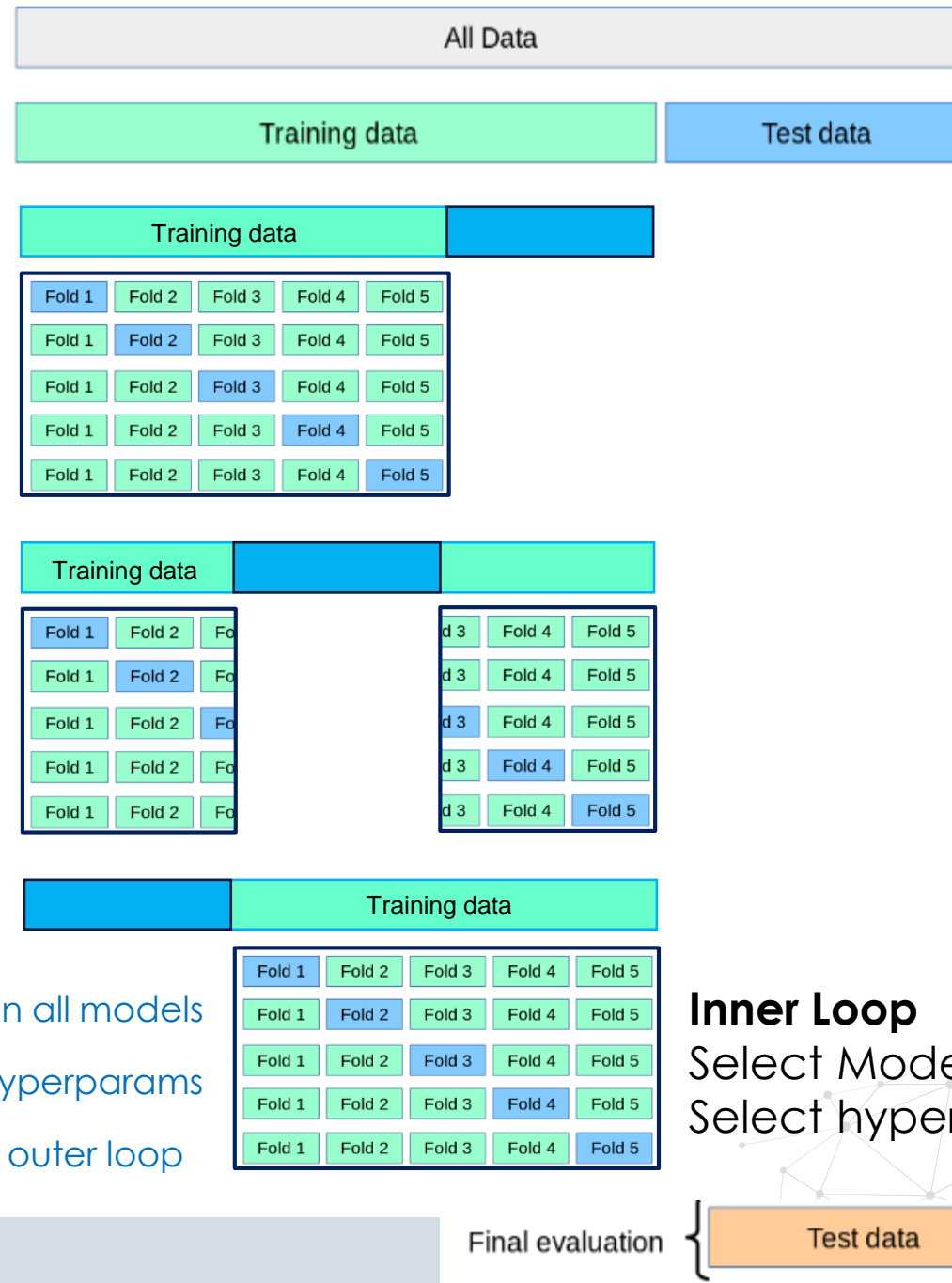


# Nested CV

## Outer Loop

Estimate  
Generalization Error

- Train all models
- Select Hyperparams
- Asses error on outer loop



# Nested CV, considerations

- Computationally expensive
- Useful when we need a good estimation of the generalization error
- Different inner models may have different hyperparameters, although I would expect to be among the top performing hyperparameters.

# THANK YOU

[www.trainindata.com](http://www.trainindata.com)