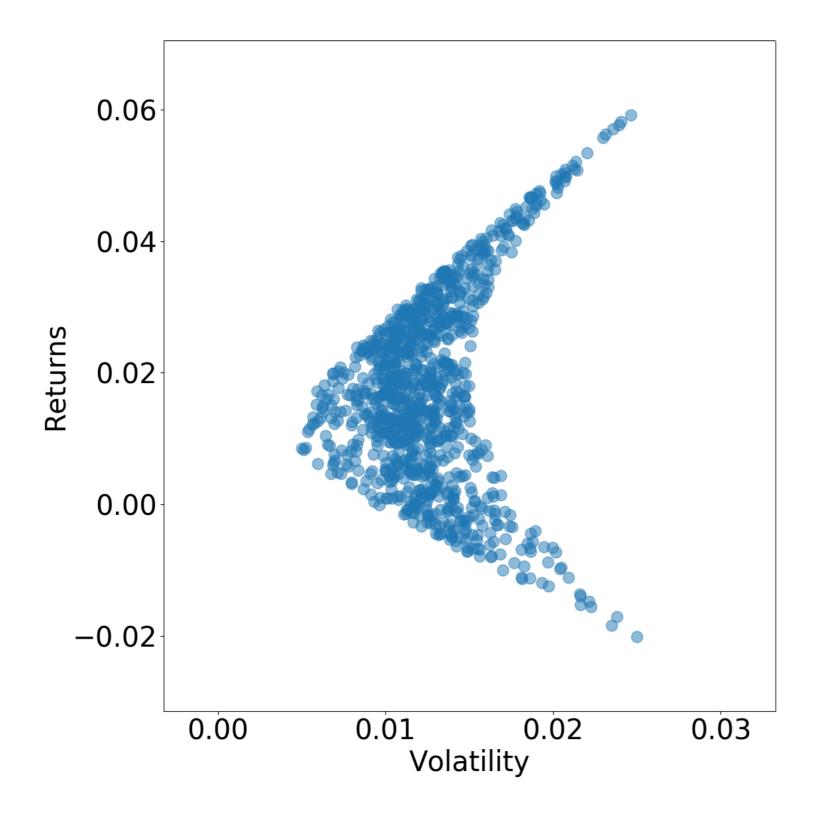




Modern portfolio theory (MPT); efficient frontiers

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Data Science Professor





Joining data

```
stocks = ['AMD', 'CHK', 'QQQ']
full_df = pd.concat([amd_df, chk_df, qqq_df], axis=1).dropna()
full_df.head()
```

```
AMD
                       CHK
                                  QQQ
Date
           8.690
1999 - 03 - 10
                  0.904417
                            45.479603
1999-03-11
           8.500
                 0.951617 45.702324
1999-03-12 8.250 0.951617 44.588720
1999 - 03 - 15
           8.155
                 0.951617 45.880501
1999-03-16
                 0.951617 46.281398
           8.500
```



Calculating returns

```
# calculate daily returns of stocks
returns_daily = full_df.pct_change()

# resample the full dataframe to monthly timeframe
monthly_df = full_df.resample('BMS').first()

# calculate monthly returns of the stocks
returns_monthly = monthly_df.pct_change().dropna()

print(returns_monthly.tail())
```

```
AMD CHK QQQ
Date
2018-01-01 0.023299 0.002445 0.028022
2018-02-01 0.206740 -0.156098 0.059751
2018-03-01 -0.101887 -0.190751 -0.020719
2018-04-02 -0.199160 0.060714 -0.052971
2018-05-01 0.167891 0.003367 0.046749
```



Covariances

```
# daily covariance of stocks (for each monthly period)
covariances = {}
for i in returns_monthly.index:
    rtd_idx = returns_daily.index
    # mask daily returns for each month (and year) and calculate covariance
    mask = (rtd_idx.month == i.month) & (rtd_idx.year == i.year)
    covariances[i] = returns_daily[mask].cov()
print(covariances[i])
```

```
AMD CHK QQQ
AMD 0.000257 0.000177 0.000068
CHK 0.000177 0.002057 0.000108
QQQ 0.000068 0.000108 0.000051
```



Generating portfolio weights

```
for date in covariances.keys():
    cov = covariances[date]
    for single_portfolio in range(5000):
        weights = np.random.random(3)
        weights /= np.sum(weights)
```



Calculating returns and volatility

```
portfolio_returns, portfolio_volatility, portfolio_weights = {}, {}, {}
# get portfolio performances at each month
for date in covariances.keys():
    cov = covariances[date]
    for single_portfolio in range(5000):
        weights = np.random.random(3)
        weights /= np.sum(weights)
        returns = np.dot(weights, returns_monthly.loc[date])
        volatility = np.sqrt(np.dot(weights.T, np.dot(cov, weights)))
        portfolio_returns.setdefault(date, []).append(returns)
        portfolio volatility.setdefault(date, []).append(volatility)
        portfolio_weights.setdefault(date, []).append(weights)
```



Plotting the efficient frontier





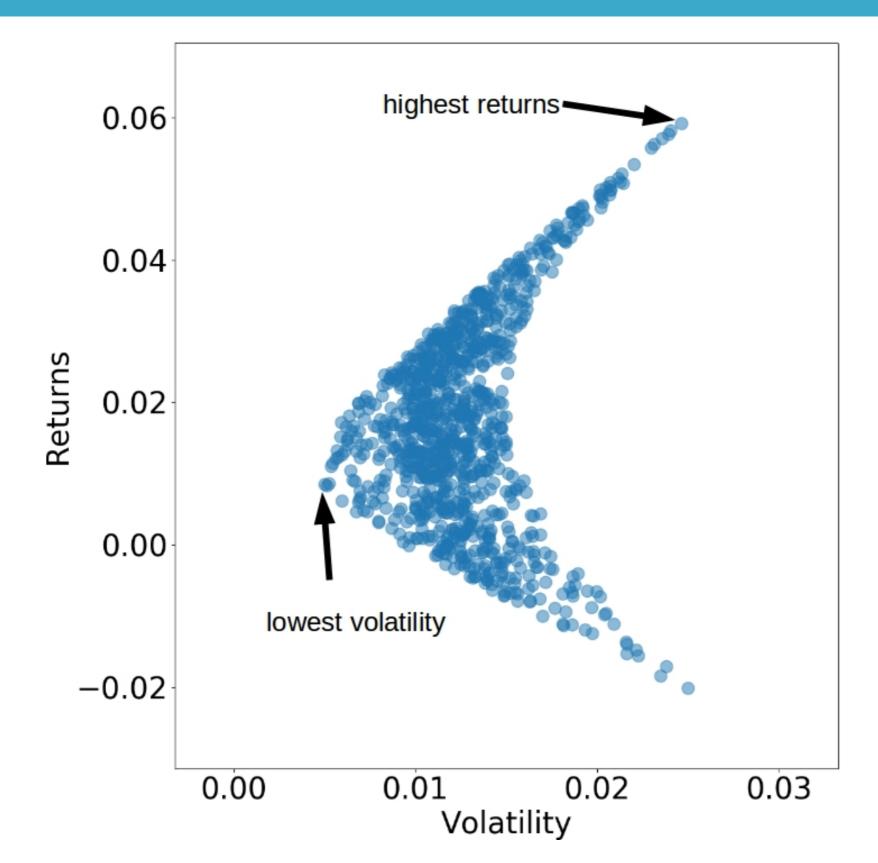
Calculate MPT portfolios!

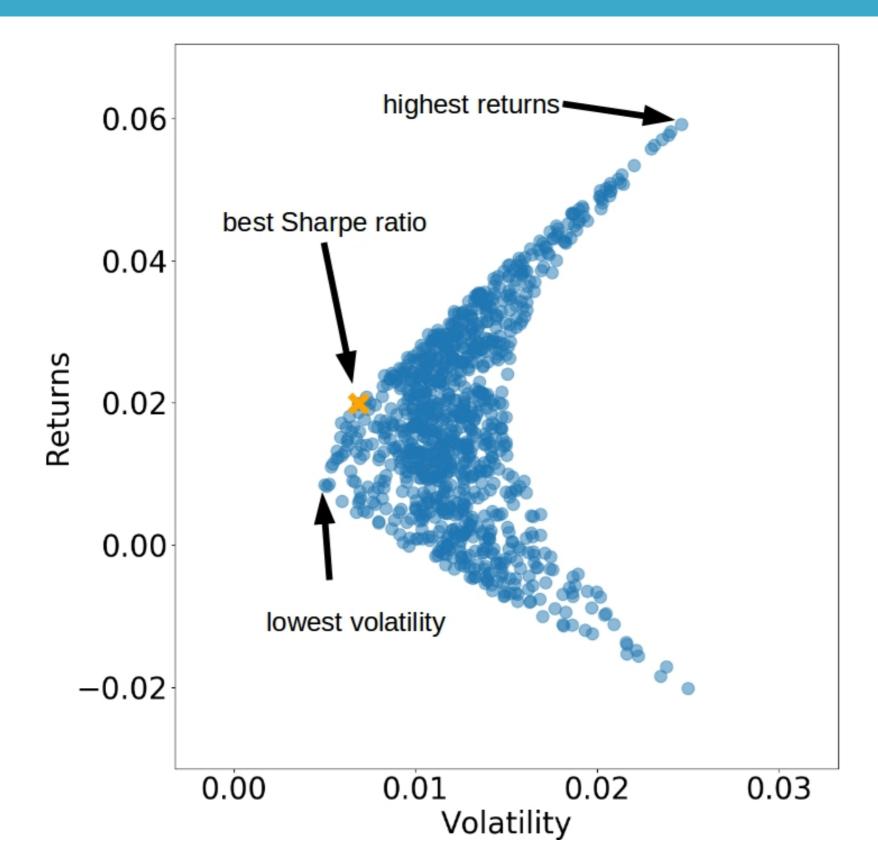




Sharpe ratios; features and targets

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Data Science Professor





Sharpe ratio = $\frac{\text{portfolio return} - \text{risk free return}}{\text{portfolio standard deviation}}$



Getting our Sharpe ratios

```
# empty dictionaries for sharpe ratios and best sharpe indexes by date
sharpe_ratio, max_sharpe_idxs = {}, {}

# loop through dates and get sharpe ratio for each portfolio
for date in portfolio_returns.keys():
    for i, ret in enumerate(portfolio_returns[date]):
        volatility = portfolio_volatility[date][i]
        sharpe_ratio.setdefault(date, []).append(ret / volatility)

# get the index of the best sharpe ratio for each date
    max_sharpe_idxs[date] = np.argmax(sharpe_ratio[date])
```



Create features

```
# calculate exponentially-weighted moving average of daily returns
ewma_daily = returns_daily.ewm(span=30).mean()

# resample daily returns to first business day of the month
ewma_monthly = ewma_daily.resample('BMS').first()

# shift ewma 1 month forward
ewma_monthly = ewma_monthly.shift(1).dropna()
```



Calculate features and targets

```
targets, features = [], []

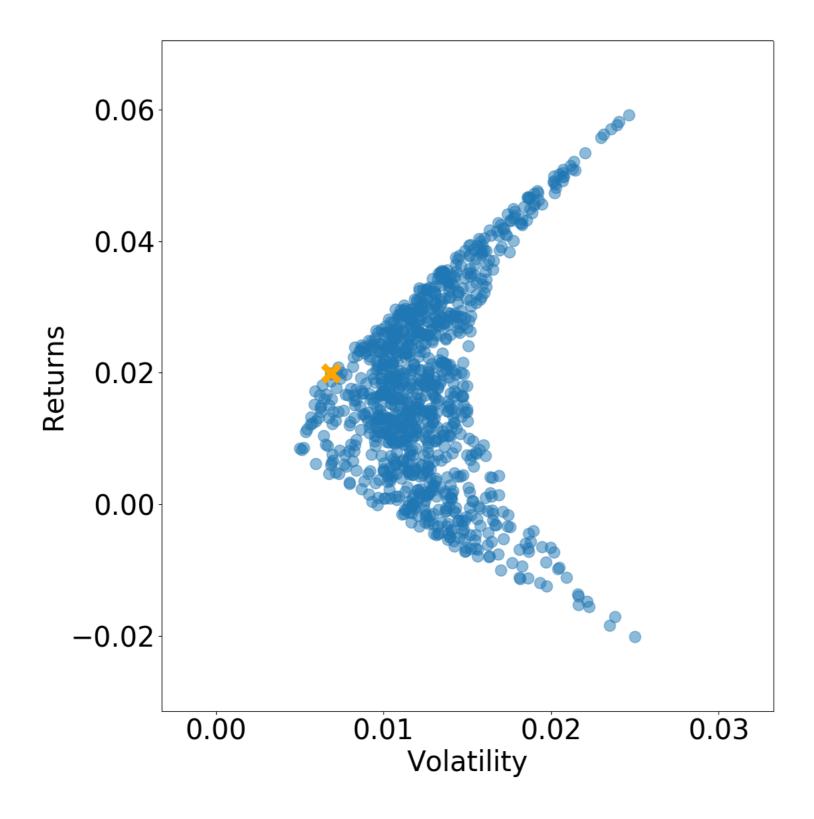
# create features from price history and targets as ideal portfolio
for date, ewma in ewma_monthly.iterrows():
    # get the index of the best sharpe ratio
    best_idx = max_sharpe_idxs[date]
    targets.append(portfolio_weights[date][best_idx])
    features.append(ewma)

targets = np.array(targets)
features = np.array(features)
```



Re-plot efficient frontier

```
# latest date
date = sorted(covariances.keys())[-1]
cur_returns = portfolio_returns[date]
cur_volatility = portfolio_volatility[date]
plt.scatter(x=cur_volatility,
            y=cur_returns,
            alpha=0.1,
            color='blue')
best_idx = max_sharpe_idxs[date]
plt.scatter(cur_volatility[best_idx],
            cur_returns[best_idx],
            marker='x',
            color='orange')
plt.xlabel('Volatility')
plt.ylabel('Returns')
plt.show()
```







Get Sharpe!





Machine learning for MPT

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Make train and test sets

```
# make train and test features
train_size = int(0.8 * features.shape[0])
train_features = features[:train_size]
train_targets = targets[:train_size]

test_features = features[train_size:]
test_targets = targets[train_size:]

print(features.shape)

(230, 3)
```



Fit the model

```
from sklearn.ensemble import RandomForestRegressor

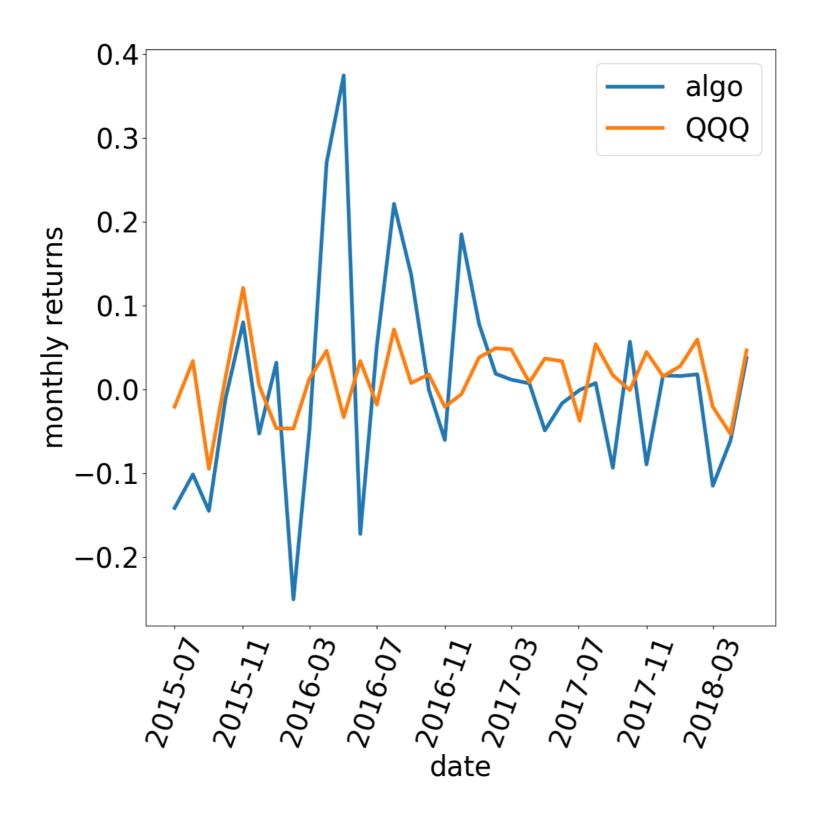
# fit the model and check scores on train and test
rfr = RandomForestRegressor(n_estimators=300, random_state=42)
rfr.fit(train_features, train_targets)

print(rfr.score(train_features, train_targets))
print(rfr.score(test_features, test_targets))
```

```
0.8382262317599827
0.09504859048985377
```



Evaluate the model's performance





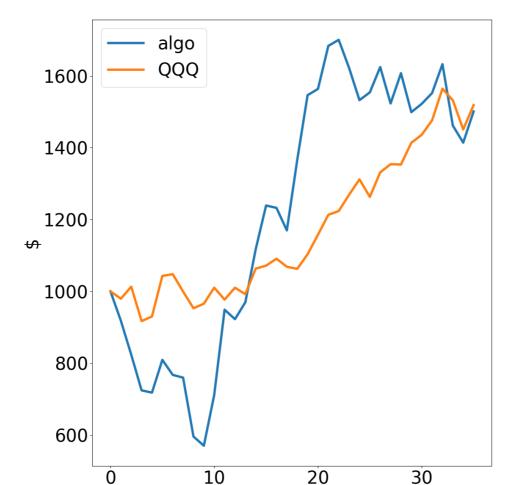
Calculate hypothetical portfolio

```
cash = 1000
algo_cash = [cash]
for r in test returns:
    cash *= 1 + r
    algo_cash.append(cash)
# calculate performance for QQQ
cash = 1000 # reset cash amount
qqq_{cash} = [cash]
for r in returns_monthly['QQQ'].iloc[train_size:]:
    cash *= 1 + r
    qqq_cash.append(cash)
print('algo returns:', (algo_cash[-1] - algo_cash[0]) / algo_cash[0])
print('QQQ returns:', (qqq_cash[-1] - qqq_cash[0]) / qqq_cash[0])
```

```
algo returns: 0.5009443507049591
QQQ returns: 0.5186775933696601
```

Plot the results

```
plt.plot(algo_cash, label='algo')
plt.plot(qqq_cash, label='QQQ')
plt.ylabel('$')
plt.legend() # show the legend
plt.show()
```







Train your model!





Final thoughts

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Toy examples

Tools for bigger data:

- Python 3 multiprocessing
- Dask
- Spark
- AWS or other cloud solutions



Get more and better data

Data in this course:

From Quandl.com/EOD (free subset available)

Alternative and other data:

- satellite images
- sentiment analysis (e.g. PsychSignal)
- analyst predictions
- fundamentals data





Be careful, and Godspeed!