

# PBblas

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[Go Up](#)

Name	PBblas
Version	3.0.1
Description	Parallel Block Basic Linear Algebra Subsystem
License	<a href="http://www.apache.org/licenses/LICENSE-2.0">http://www.apache.org/licenses/LICENSE-2.0</a>
Copyright	Copyright (C) 2016, 2017 HPCC Systems
Authors	HPCCSystems
DependsOn	ML_Core
Platform	6.2.0

## Table of Contents

<a href="#">Apply2Elements.ecl</a>
Apply a function to each element of the matrix Use PBblas.IElementFunc as the prototype function
<a href="#">asum.ecl</a>
Absolute sum – the "Entrywise" 1-norm
<a href="#">axpy.ecl</a>
Implements $\alpha * X + Y$
<a href="#">Constants.ecl</a>
<a href="#">Converted.ecl</a>
Module to convert between ML_Core/Types Field layouts (i.e
<a href="#">ExtractTri.ecl</a>
Extract the upper or lower triangle from the composite output from getrf (LU Factorization)
<a href="#">gemm.ecl</a>
Extended Parallel Block Matrix Multiplication Module Implements: $Result = \alpha * op(A)op(B) + \beta * C$
<a href="#">getrf.ecl</a>
LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks
<a href="#">HadamardProduct.ecl</a>

Element-wise multiplication of $X * Y$
<a href="#">IElementFunc.ecl</a> Function prototype for a function to apply to each element of the
<a href="#">MatUtils.ecl</a> Provides various utility attributes for manipulating cell-based matrixes
<a href="#">potrf.ecl</a> Implements Cholesky factorization of $A = U^{**T} * U$ if Triangular.Upper requested or $A = L * L^{**T}$ if Triangualr.Lower is requested
<a href="#">scal.ecl</a> Scale a matrix by a constant Result is $\alpha * X$ This supports a "myriad" style interface in that X may be a set of independent matrices separated by different work-item ids
<a href="#">tran.ecl</a> Transpose a matrix and sum into base matrix
<a href="#">trsm.ecl</a> Partitioned block parallel triangular matrix solver
<a href="#">Types.ecl</a> Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes
<a href="#">Vector2Diag.ecl</a> Convert a vector into a diagonal matrix

# PBblas/ Apply2Elements

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | std.blas |

## DESCRIPTIONS

### **FUNCTION** Apply2Elements

<b>DATASET</b> (Layout_Cell)	Apply2Elements
(DATASET(Layout_Cell) X, IElementFunc f)	

Apply a function to each element of the matrix Use PBblas.IElementFunc as the prototype function. Input and output may be a single matrix, or myriad matrixes with different work item ids.

**PARAMETER** f ||| FUNCTION [ REAL8 , UNSIGNED4 , UNSIGNED4 ] ( REAL8 ) — A function based on the IElementFunc prototype

**PARAMETER** X ||| TABLE ( Layout\_Cell ) — A matrix (or multiple matrices) in Layout\_Cell form

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — A matrix (or multiple matrices) in Layout\_Cell form

**SEE** PBblas/IElementFunc

**SEE** PBblas/Types.Layout\_Cell

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# PBblas/ asum

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims | PBblas.internal.Converted | std.blas |

## DESCRIPTIONS

### **FUNCTION** asum

<b>DATASET(Layout_Norm)</b>	<b>asum</b>
<b>(DATASET(Layout_Cell) X)</b>	

Absolute sum – the "Entrywise" 1-norm Compute  $\text{SUM}(\text{ABS}(X))$

**PARAMETER** **X** ||| **TABLE** ( **Layout\_Cell** ) — Matrix or set of matrices in **Layout\_Cell** format

**RETURN** **TABLE** ( { **UNSIGNED2** **wi\_id** , **REAL8** **v** } ) — **DATASET(Layout\_Norm)** with one record per work item

**SEE** PBblas/Types.Layout\_Cell

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[Go Up](#)

## **IMPORTS**

PBblas | PBblas.Types |

## **DESCRIPTIONS**

### **FUNCTION** **axpy**

<code>DATASET(Layout_Cell)</code>	<b>axpy</b>
<code>(value_t alpha, DATASET(Layout_Cell) X, DATASET(Layout_Cell) Y)</code>	

Implements  $\alpha * X + Y$  X and Y must have same shape

**PARAMETER** alpha ||| REAL8 — Scalar multiplier for the X matrix

**PARAMETER** Y ||| TABLE ( Layout\_Cell ) — Y matrix in DATASET(Layout\_Cell) form

**PARAMETER** X ||| TABLE ( Layout\_Cell ) — X matrix in DATASET(Layout\_Cell) form

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — Matrix in DATASET(Layout\_Cell) form

**SEE** PBblas/Types.layout\_cell

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# PBblas/ Constants

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[Go Up](#)

## DESCRIPTIONS

### **MODULE** Constants

Constants
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No Documentation Found

### Children

1. [Block\\_Minimum](#) : No Documentation Found
2. [Block\\_NoSplit](#) : No Documentation Found
3. [Block\\_Maximum](#) : No Documentation Found
4. [Block\\_Vec\\_Rows](#) : No Documentation Found
5. [Dimension\\_Incompat](#) : No Documentation Found
6. [Dimension\\_IncompatZ](#) : No Documentation Found
7. [Distribution\\_Error](#) : No Documentation Found
8. [Distribution\\_ErrorZ](#) : No Documentation Found
9. [Not\\_Square](#) : No Documentation Found
10. [Not\\_SquareZ](#) : No Documentation Found
11. [Not\\_PositiveDef](#) : No Documentation Found
12. [Not\\_PositiveDefZ](#) : No Documentation Found
13. [Not\\_Single\\_Block](#) : No Documentation Found
14. [Not\\_Single\\_BlockZ](#) : No Documentation Found

- 15. [Not\\_Block\\_Vector](#) : No Documentation Found
- 16. [Not\\_Block\\_VectorZ](#) : No Documentation Found

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## ATTRIBUTE Block\_Minimum

[Constants](#) \

	Block_Minimum
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No Documentation Found

**RETURN** INTEGER8 —

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## ATTRIBUTE Block\_NoSplit

[Constants](#) \

	Block_NoSplit
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No Documentation Found

**RETURN** INTEGER8 —

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## ATTRIBUTE Block\_Maximum

[Constants](#) \

	Block_Maximum
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No Documentation Found

**RETURN** INTEGER8 —

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## **ATTRIBUTE** Block\_Vec\_Rows

[Constants](#) \

	Block_Vec_Rows
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No Documentation Found

**RETURN** INTEGER8 —

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## **ATTRIBUTE** Dimension\_Incompat

[Constants](#) \

	Dimension_Incompat
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No Documentation Found

**RETURN** STRING34 —

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## **ATTRIBUTE** Dimension\_IncompatZ

[Constants](#) \

	Dimension_IncompatZ
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No Documentation Found



**RETURN** INTEGER8 —

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## **ATTRIBUTE** Distribution\_Error

[Constants](#) \

	Distribution_Error
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No Documentation Found

**RETURN** STRING32 —

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## **ATTRIBUTE** Distribution\_ErrorZ

[Constants](#) \

	Distribution_ErrorZ
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No Documentation Found

**RETURN** INTEGER8 —

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## **ATTRIBUTE** Not\_Square

[Constants](#) \

	Not_Square
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No Documentation Found

**RETURN** STRING20 —

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**ATTRIBUTE** Not\_SquareZ

[Constants](#) \

	Not_SquareZ
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No Documentation Found

**RETURN** INTEGER8 —

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**ATTRIBUTE** Not\_PositiveDef

[Constants](#) \

	Not_PositiveDef
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No Documentation Found

**RETURN** STRING40 —

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**ATTRIBUTE** Not\_PositiveDefZ

[Constants](#) \

	Not_PositiveDefZ
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No Documentation Found

**RETURN** INTEGER8 —

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## **ATTRIBUTE** Not\_Single\_Block

[Constants](#) \

	Not_Single_Block
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No Documentation Found

**RETURN** STRING28 —

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## **ATTRIBUTE** Not\_Single\_BlockZ

[Constants](#) \

	Not_Single_BlockZ
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No Documentation Found

**RETURN** INTEGER8 —

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## **ATTRIBUTE** Not\_Block\_Vector

[Constants](#) \

	Not_Block_Vector
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No Documentation Found

**RETURN** STRING25 —

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**ATTRIBUTE** Not\_Block\_VectorZ

[Constants](#) \

	Not_Block_VectorZ
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No Documentation Found

**RETURN** INTEGER8 —

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# PBblas/ Converted

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | ML\_Core.Types |

## DESCRIPTIONS

### **MODULE** Converted

	Converted
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Module to convert between ML\_Core/Types Field layouts (i.e. NumericField and DiscreteField) and PBblas matrix layout (i.e. Layout\_Cell)

### Children

1. [NFToMatrix](#) : Convert NumericField dataset to Matrix
2. [DFToMatrix](#) : Convert DiscreteField dataset to Matrix
3. [MatrixToNF](#) : Convert Matrix to NumericField dataset
4. [MatrixToDF](#) : Convert Matrix to DiscreteField dataset

## FUNCTION NFToMatrix

Converted \

<b>DATASET(Layout_Cell)</b>	<b>NFToMatrix</b>
(DATASET(NumericField) recs)	

Convert NumericField dataset to Matrix

**PARAMETER** **recs** ||| TABLE ( NumericField ) — Record Dataset in DATASET(NumericField) format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — Matrix in DATASET(Layout\_Cell) format

**SEE** PBblas/Types.Layout\_Cell

**SEE** ML\_Core/Types.NumericField

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## FUNCTION DFToMatrix

Converted \

<b>DATASET(Layout_Cell)</b>	<b>DFToMatrix</b>
(DATASET(DiscreteField) recs)	

Convert DiscreteField dataset to Matrix

**PARAMETER** **recs** ||| TABLE ( DiscreteField ) — Record Dataset in DATASET(DiscreteField) format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — Matrix in DATASET(Layout\_Cell) format

**SEE** PBblas/Types.Layout\_Cell

**SEE** ML\_Core/Types.DiscreteField

## FUNCTION MatrixToNF

Converted \

DATASET(NumericField)	MatrixToNF
(DATASET(Layout_Cell) mat)	

Convert Matrix to NumericField dataset

**PARAMETER** mat ||| TABLE ( Layout\_Cell ) — Matrix in DATASET(Layout\_Cell) format

**RETURN** TABLE ( { UNSIGNED2 wi , UNSIGNED8 id , UNSIGNED4 number , REAL8 value } ) — NumericField Dataset

**SEE** PBblas/Types.Layout\_Cell

**SEE** ML\_Core/Types.NumericField

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## FUNCTION MatrixToDF

Converted \

DATASET(DiscreteField)	MatrixToDF
(DATASET(Layout_Cell) mat)	

Convert Matrix to DiscreteField dataset

**PARAMETER** mat ||| TABLE ( Layout\_Cell ) — Matrix in DATASET(Layout\_Cell) format

**RETURN** TABLE ( { UNSIGNED2 wi , UNSIGNED8 id , UNSIGNED4 number , INTEGER4 value } ) — DiscreteField Dataset

**SEE** PBblas/Types.Layout\_Cell

**SEE** ML\_Core/Types.DiscreteField

# PBblas/ ExtractTri

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[Go Up](#)

## IMPORTS

PBblas | std.blas | PBblas.Types | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims | PBblas.internal.Converted |

## DESCRIPTIONS

### **FUNCTION** ExtractTri

<code>DATASET(Layout_Cell)</code>	<code>ExtractTri</code>
<code>(Triangle tri, Diagonal dt, DATASET(Layout_Cell) A)</code>	

Extract the upper or lower triangle from the composite output from getrf (LU Factorization).

**PARAMETER** `tri` ||| UNSIGNED1 — Triangle type: Upper or Lower (see Types.Triangle)

**PARAMETER** `dt` ||| UNSIGNED1 — Diagonal type: Unit or non unit (see Types.Diagonal)

**PARAMETER** `A` ||| TABLE ( Layout\_Cell ) — Matrix of cells. See Types.Layout\_Cell

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — Matrix of cells in Layout\_Cell format representing a triangular matrix (upper or lower)

**SEE** Std.PBblas.Types

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# PBblas/ gemm

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | PBblas.internal | PBblas.internal.Types | std.blas |  
PBblas.internal.MatDims | std.system.Thorlib |

## DESCRIPTIONS

### **FUNCTION** `gemm`

<code>DATASET(Layout_Cell)</code>	<code>gemm</code>
<code>(BOOLEAN transposeA, BOOLEAN transposeB, value_t alpha, DATASET(Layout_Cell) A_in, DATASET(Layout_Cell) B_in, DATASET(Layout_Cell) C_in=emptyC, value_t beta=0.0)</code>	

Extended Parallel Block Matrix Multiplication Module Implements:  $\text{Result} = \alpha * \text{op}(\text{A})\text{op}(\text{B}) + \beta * \text{C}$ . op is No Transpose or Transpose. Multiplies two matrixes A and B, with an optional pre-multiply transpose for each Optionally scales the product by the scalar "alpha". Then adds an optional C matrix to the product after scaling C by the scalar "beta". A, B, and C are specified as DATASET(Layout\_Cell), as is the Resulting matrix. Layout\_Cell describes a sparse matrix stored as a list of x, y, and value. This interface also provides a "Myriad" capability allowing multiple similar operations to be performed on independent sets of matrixes in parallel. This is done by use of the work-item id (wi\_id) in each cell of the matrixes. Cells with the same wi\_id are considered part of the same matrix. In the myriad form, each input matrix A, B, and (optionally) C can contain many independent matrixes. The wi\_ids are matched up such that each operation involves the A, B, and C with the same wi\_id. A and B must therefore contain the same set of wi\_ids, while C is optional for any wi\_id. The same parameters: alpha, beta, transposeA, and transposeB are used for all work-items. The result will contain cells from all provided work-items. Result has same shape as C if provided. Note that matrixes are not explicitly

dimensioned. The shape is determined by the highest value of x and y for each work-item.

**PARAMETER** alpha ||| REAL8 — Scalar multiplier for  $\alpha * A * B$

**PARAMETER** transposeA ||| BOOLEAN — Boolean indicating whether matrix A should be transposed before multiplying

**PARAMETER** C\_in ||| TABLE ( Layout\_Cell ) — Same as above for the 'C' matrix (addend). May be omitted.

**PARAMETER** beta ||| REAL8 — A scalar multiplier for  $\beta * C$ , scales the C matrix before addition. May be omitted.

**PARAMETER** B\_in ||| TABLE ( Layout\_Cell ) — Same as above for the 'B' matrix (multiplicand)

**PARAMETER** transposeB ||| BOOLEAN — Same as above but for matrix B

**PARAMETER** A\_in ||| TABLE ( Layout\_Cell ) — 'A' matrix (multiplier) in Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — Result matrix in Layout\_Cell format.

**SEE** PBblas/Types.Layout\_Cell

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# PBblas/ getrf

[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | PBblas.internal | PBblas.internal.Types | std.blas |  
PBblas.internal.MatDims | std.system.Thorlib |

## DESCRIPTIONS

### FUNCTION `getrf`

<code>DATASET(Layout_Cell)</code>	<code>getrf</code>
<code>(DATASET(Layout_Cell) A)</code>	

LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks. Iterates through the matrix a row of blocks and column of blocks at a time. Partition A into M block rows and N block columns. The A11 cell is a single block. A12 is a single row of blocks with N-1 columns. A21 is a single column of blocks with M-1 rows. A22 is a sub-matrix of M-1 x N-1 blocks. | A11 A12 | | L11 0 | | U11 U12 | | A21 A22 | == | L21 L22 | \* | 0 U22 | | L11\*U11 L11\*U12 | == | L21\*U11 L21\*U12 + L22\*U22 | Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi\_id). Note: The returned matrix includes both the upper and lower factors. This matrix can be used directly by trsm which will only use the part indicated by trsm's 'triangle' parameter (i.e. upper or lower). To extract the upper or lower triangle explicitly for other purposes, use the ExtractTri function. When passing the Lower matrix to the triangle solver (trsm), set the "Diagonal" parameter to "UnitTri". This is necessary because both triangular matrixes returned from this function are packed into a square matrix with only one diagonal. By convention, The Lower triangle is assumed to be a Unit Triangle (diagonal all ones), so the diagonal

contained in the returned matrix is for the Upper factor and must be ignored (i.e. assumed to be all ones) when referencing the Lower triangle.

**PARAMETER** **A** ||| TABLE ( Layout\_Cell ) — The input matrix in Types.Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — Resulting factored matrix in Layout\_Cell format

**SEE** Types.Layout\_Cell

**SEE** ExtractTri

# PBblas/ HadamardProduct

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[Go Up](#)

## IMPORTS

PBblas | PBblas.internal | PBblas.internal.MatDims | PBblas.Types |  
PBblas.internal.Types | PBblas.internal.Converted | std.blas | std.system.Thorlib |

## DESCRIPTIONS

### **FUNCTION** HadamardProduct

<b>DATASET</b> (Layout_Cell)	<b>HadamardProduct</b>
(DATASET(Layout_Cell) X, DATASET(Layout_Cell) Y)	

Element-wise multiplication of  $X * Y$ . Supports the "myriad" style interface – X and Y may contain multiple separate matrixes. Each X will be multiplied by the Y with the same work-item id. Note: This performs element-wise multiplication. For dot-product matrix multiplication, use PBblas.gemm.

**PARAMETER** Y ||| TABLE ( Layout\_Cell ) — A matrix (or multiple matrices) in Layout\_Cell form

**PARAMETER** X ||| TABLE ( Layout\_Cell ) — A matrix (or multiple matrices) in Layout\_Cell form

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — A matrix (or multiple matrices) in Layout\_Cell form

**SEE** PBblas/Types.Layout\_Cell

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# PBblas/ IElementFunc

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[Go Up](#)

## IMPORTS

PBblas |

## DESCRIPTIONS

### **FUNCTION** IElementFunc

<code>value_t</code>	<b>IElementFunc</b>
<code>(value_t v, dimension_t r, dimension_t c)</code>	

Function prototype for a function to apply to each element of the distributed matrix Base your function on this prototype:

**PARAMETER** `r` ||| UNSIGNED4 — Row number (1 based)

**PARAMETER** `v` ||| REAL8 — Input value

**PARAMETER** `c` ||| UNSIGNED4 — Column number (1 based)

**RETURN** REAL8 — Output value

**SEE** PBblas/Apply2Elements

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# PBblas/ MatUtils

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims |

## DESCRIPTIONS

### **MODULE** MatUtils

MatUtils
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Provides various utility attributes for manipulating cell-based matrixes

**SEE** Std/PBblas/Types.Layout\_Cell

### Children

1. [GetWorkItems](#) : Get a list of work-item ids from a matrix containing one or more work items
  2. [InsertCols](#) : Insert one or more columns of a fixed value into a matrix
  3. [Transpose](#) : Transpose a matrix This attribute supports the myriad interface
-



## FUNCTION GetWorkItems

MatUtils \

<b>DATASET(Layout_WI_ID)</b>	<b>GetWorkItems</b>
(DATASET(Layout_Cell) cells)	

Get a list of work-item ids from a matrix containing one or more work items

**PARAMETER** cells ||| TABLE ( Layout\_Cell ) — A matrix in Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id } ) — DATASET(Layout\_WI\_ID), one record per work-item

**SEE** PBblas/Types.Layout\_Cell

**SEE** PBblas/Types.Layout\_WI\_ID

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## FUNCTION InsertCols

MatUtils \

<b>DATASET(Layout_Cell)</b>	<b>InsertCols</b>
(DATASET(Layout_Cell) M, UNSIGNED cols_to_insert=1, value_t insert_val=1)	

Insert one or more columns of a fixed value into a matrix. Columns are inserted before the first original column. This attribute supports the myriad interface. Multiple independent matrixes can be represented by M.

**PARAMETER** insert\_val ||| REAL8 — the value for each cell of the new column(s), default 0

**PARAMETER** cols\_to\_insert ||| UNSIGNED8 — the number of columns to insert, default 1

**PARAMETER** M ||| TABLE ( Layout\_Cell ) — the input matrix

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — matrix in Layout\_Cell format with additional column(s)

## FUNCTION Transpose

MatUtils \

<code>DATASET(Layout_Cell)</code>	<b>Transpose</b>
<code>(DATASET(Layout_Cell) M)</code>	

Transpose a matrix This attribute supports the myriad interface. Multiple independent matrixes can be represented by M.

**PARAMETER** M ||| TABLE ( Layout\_Cell ) — A matrix represented as DATASET(Layout\_Cell)

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
) — Transposed matrix in Layout\_Cell format

**SEE** PBblas/Types.Layout\_Cell

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# PBblas/ potrf

[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | std.blas | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims | PBblas.internal.Converted | std.system.Thorlib |

## DESCRIPTIONS

### **FUNCTION** potrf

<code>DATASET(Layout_Cell)</code>	<code>potrf</code>
<code>(Triangle tri, DATASET(Layout_Cell) A_in)</code>	

Implements Cholesky factorization of  $A = U^{**T} * U$  if Triangulr.Upper requested or  $A = L * L^{**T}$  if Triangulr.Lower is requested. The matrix A must be symmetric positive definite.

$$\begin{array}{|cc|} \hline A11 & A12 \\ \hline A21 & A22 \\ \hline \end{array} == \begin{array}{|cc|} \hline L11 & 0 \\ \hline L21 & L22 \\ \hline \end{array} * \begin{array}{|cc|} \hline L11^{**T} & L21^{**T} \\ \hline 0 & L22 \\ \hline \end{array}$$
$$== \begin{array}{|cc|} \hline L11 * L11^{**T} & L11 * L21^{**T} \\ \hline L21 * L11^{**T} & L21 * L21^{**T} + L22 * L22^{**T} \\ \hline \end{array}$$

So, use Cholesky on the first block to get L11.  $L21 = A21 * L11^{**T} ** -1$  which can be found by dtrsm on each column block A22' is  $A22 - L21 * L21^{**T}$

Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra

This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi\_id).

**PARAMETER** tri ||| UNSIGNED1 — Types.Triangle enumeration indicating whether we are looking for the Upper or the Lower factor

**PARAMETER** A\_in ||| TABLE ( Layout\_Cell ) — The matrix or matrixes to be factored in Types.Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — Triangular matrix in Layout\_Cell format

**SEE** Std.PBblas.Types.Layout\_Cell

**SEE** Std.PBblas.Types.Triangle

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[Go Up](#)

## IMPORTS

PBblas | PBblas.Types |

## DESCRIPTIONS

### **FUNCTION** scal

<code>DATASET(Layout_Cell)</code>	<code>scal</code>
<code>(value_t alpha, DATASET(Layout_Cell) X)</code>	

Scale a matrix by a constant Result is  $\alpha * X$  This supports a "myriad" style interface in that X may be a set of independent matrices separated by different work-item ids.

**PARAMETER** alpha ||| REAL8 — A scalar multiplier

**PARAMETER** X ||| TABLE ( Layout\_Cell ) — The matrix(es) to be scaled in Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — Matrix in Layout\_Cell form, of the same shape as X

**SEE** PBblas/Types.Layout\_Cell

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# PBblas/ tran

[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims | PBblas.internal.Converted | std.blas | std.system.Thorlib |

## DESCRIPTIONS

### FUNCTION tran

<code>DATASET(Layout_Cell)</code>	tran
<code>(value_t alpha, DATASET(Layout_Cell) A, value_t beta=0, DATASET(Layout_Cell) C=empty_c)</code>	

Transpose a matrix and sum into base matrix result  $\leq \alpha * A^{**t} + \beta * C$ , A is n by m, C is m by n  $A^{**T}$  (A Transpose) and C must have same shape

**PARAMETER** C ||| TABLE ( Layout\_Cell ) — C matrix in DATASET(Layout\_Cell) form

**PARAMETER** alpha ||| REAL8 — Scalar multiplier for the  $A^{**T}$  matrix

**PARAMETER** A ||| TABLE ( Layout\_Cell ) — A matrix in DATASET(Layout\_Cell) form

**PARAMETER** beta ||| REAL8 — Scalar multiplier for the C matrix

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v }  
 ) — Matrix in DATASET(Layout\_Cell) form  $\alpha * A^{**T} + \beta * C$

**SEE** PBblas/Types.layout\_cell

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# PBblas/ trsm

[Go Up](#)

## IMPORTS

PBblas | PBblas.Types | std.blas | PBblas.internal | PBblas.internal.Types |  
PBblas.internal.MatDims | PBblas.internal.Converted | std.system.Thorlib |

## DESCRIPTIONS

### FUNCTION trsm

<code>DATASET(Layout_Cell)</code>	<code>trsm</code>
<pre>(Side s, Triangle tri, BOOLEAN transposeA, Diagonal diag, value_t alpha, DATASET(Layout_Cell) A_in, DATASET(Layout_Cell) B_in)</pre>	

Partitioned block parallel triangular matrix solver. Solves for X using:  $AX = B$  or  $XA = B$  A is a square triangular matrix, X and B have the same dimensions. A may be an upper triangular matrix ( $UX = B$  or  $XU = B$ ), or a lower triangular matrix ( $LX = B$  or  $XL = B$ ). Allows optional transposing and scaling of A. Partially based upon an approach discussed by MJ DAYDE, IS DUFF, AP CERFACS. A Parallel Block implementation of Level-3 BLAS for MIMD Vector Processors ACM Tran. Mathematical Software, Vol 20, No 2, June 1994 pp 178-193 and other papers about PB-BLAS by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. Corresponding A and B matrixes are related by a common work-item identifier (wi\_id) within each cell of the matrix. The returned X matrix will contain cells for the same set of work-items as specified for the A and B matrices.

**PARAMETER** `transposeA` ||| BOOLEAN — Boolean indicating whether or not to transpose the A matrix before solving



**PARAMETER** diag ||| UNSIGNED1 — Types.Diagonal enumeration indicating whether A is a unit matrix or not. This is primarily used after factoring matrixes using getrf (LU factorization). That module produces a factored matrix stored within the same space as the original matrix. Since the diagonal is used by both factors, by convention, the Lower triangle has a unit matrix (diagonal all 1's) while the Upper triangle uses the diagonal cells. Setting this to UnitTri, causes the contents of the diagonal to be ignored, and assumed to be 1. NotUnitTri should be used for most other cases.

**PARAMETER** tri ||| UNSIGNED1 — Types.Triangle enumeration indicating whether we are solving an Upper or Lower triangle.

**PARAMETER** alpha ||| REAL8 — Multiplier to scale A

**PARAMETER** B\_in ||| TABLE ( Layout\_Cell ) — The B matrix in Layout\_Cell format

**PARAMETER** A\_in ||| TABLE ( Layout\_Cell ) — The A matrix in Layout\_Cell format

**PARAMETER** s ||| UNSIGNED1 — Types.Side enumeration indicating whether we are solving  $AX = B$  or  $XA = B$

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — X solution matrix in Layout\_Cell format

**SEE** Types.Layout\_Cell

**SEE** Types.Triangle

**SEE** Types.Side

# PBblas/ Types

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[Go Up](#)

## IMPORTS

ML\_Core | ML\_Core.Types |

## DESCRIPTIONS

### **MODULE** Types

Types
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Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes.

### Children

1. [dimension\\_t](#) : Type for matrix dimensions
2. [partition\\_t](#) : Type for partition id – only supports up to 64K partitions
3. [work\\_item\\_t](#) : Type for work-item id – only supports up to 64K work items
4. [value\\_t](#) : Type for matrix cell values
5. [m\\_label\\_t](#) : Type for matrix label
6. [Triangle](#) : Enumeration for Triangle type
7. [Diagonal](#) : Enumeration for Diagonal type
8. [Side](#) : Enumeration for Side type

9. `t_mu_no` : Type for matrix universe number
  10. `Layout_Cell` : Layout for Matrix Cell Main representation of Matrix cell at interface to all PBBlas functions
  11. `Layout_Norm` : Layout for Norm results
- 

## **ATTRIBUTE** `dimension_t`

Types \

<code>dimension_t</code>
--------------------------

Type for matrix dimensions. Uses UNSIGNED four as matrixes are not designed to support more than 4 B rows or columns.

**RETURN** UNSIGNED4 —

---

## **ATTRIBUTE** `partition_t`

Types \

<code>partition_t</code>
--------------------------

Type for partition id – only supports up to 64K partitions

**RETURN** UNSIGNED2 —

---

## **ATTRIBUTE** `work_item_t`

Types \

	<code>work_item_t</code>
--	--------------------------

Type for work-item id – only supports up to 64K work items

**RETURN** UNSIGNED2 —

---

**ATTRIBUTE** `value_t`

[Types \](#)

	<code>value_t</code>
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Type for matrix cell values WARNING: type used in C++ attribute

**RETURN** REAL8 —

---

**ATTRIBUTE** `m_label_t`

[Types \](#)

	<code>m_label_t</code>
--	------------------------

Type for matrix label. Used for Matrix dimensions (see `Layout_Dims`) and for partitions (see `Layout_Part`)

**RETURN** STRING3 —

---

**ATTRIBUTE** `Triangle`

[Types \](#)

<b>Triangle</b>
-----------------

Enumeration for Triangle type WARNING: type used in C++ attribute

**RETURN** UNSIGNED1 —

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**ATTRIBUTE** Diagonal

[Types \](#)

<b>Diagonal</b>
-----------------

Enumeration for Diagonal type WARNING: type used in C++ attribute

**RETURN** UNSIGNED1 —

---

**ATTRIBUTE** Side

[Types \](#)

<b>Side</b>
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Enumeration for Side type WARNING: type used in C++ attribute

**RETURN** UNSIGNED1 —

---

**ATTRIBUTE** t\_mu\_no

[Types \](#)

<b>t_mu_no</b>
----------------

Type for matrix universe number Allow up to 64k matrices in one universe

**RETURN** UNSIGNED2 —

## **RECORD** Layout\_Cell

Types \

<b>Layout_Cell</b>
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Layout for Matrix Cell Main representation of Matrix cell at interface to all PBBlas functions. Matrixes are represented as DATASET(Layout\_Cell), where each cell describes the row and column position of the cell as well as its value. Only the non-zero cells need to be contained in the dataset in order to describe the matrix since all unspecified cells are considered to have a value of zero. The cell also contains a work-item number that allows multiple separate matrixes to be carried in the same dataset. This supports the "myriad" style interface that allows the same operations to be performed on many different sets of data at once. Note that these matrixes do not have an explicit size. They are sized implicitly, based on the maximum row and column presented in the data. A matrix can be converted to an explicit dense form (see matrix\_t) by using the utility module MakeR8Set. This module should only be used for known small matrixes (< 1M cells) or for partitions of a larger matrix. The Converted module provides utility functions to convert to and from a set of partitions (See Layout\_parts).

**FIELD** v ||| REAL8 — Real value for the cell

**FIELD** x ||| UNSIGNED4 — 1-based row position within the matrix

**FIELD** y ||| UNSIGNED4 — 1-based column position within the matrix

**FIELD** wi\_id ||| UNSIGNED2 — Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

**SEE** matrix\_t

**SEE** Std/PBblas/MakeR8Set.ecl

**SEE** Std/PBblas/Converted.ecl WARNING: Used as C++ attribute. Do not change without corresponding changes to MakeR8Set.

## RECORD Layout\_Norm

Types \

	Layout_Norm
--	-------------

Layout for Norm results.

**FIELD** v ||| REAL8 — Real value for the norm

**FIELD** wi\_id ||| UNSIGNED2 — Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

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# PBblas/ Vector2Diag

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[Go Up](#)

## IMPORTS

PBblas | PBblas.internal | PBblas.internal.MatDims | PBblas.Types |  
PBblas.internal.Types | PBblas.Constants |

## DESCRIPTIONS

### **FUNCTION** Vector2Diag

<b>DATASET</b> (Layout_Cell)	Vector2Diag
(DATASET(Layout_Cell) X)	

Convert a vector into a diagonal matrix. The typical notation is  $D = \text{diag}(V)$ . The input X must be a 1 x N column vector or an N x 1 row vector. The resulting matrix, in either case will be N x N, with zero everywhere except the diagonal.

**PARAMETER** **X** ||| TABLE ( Layout\_Cell ) — A row or column vector (i.e. N x 1 or 1 x N) in Layout\_Cell format

**RETURN** TABLE ( { UNSIGNED2 wi\_id , UNSIGNED4 x , UNSIGNED4 y , REAL8 v } ) — An N x N matrix in Layout\_Cell format

**SEE** PBblas/Types.Layout\_cell

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