## $\mathbf{root}$

### **Table of Contents**

bundle : ML\_Core

 $\begin{array}{l} \textbf{bundle}: \ \underline{\textbf{LogisticRegression}} \\ \textbf{bundle}: \ \underline{\textbf{LinearRegression}} \end{array}$ 

bundle : PBblas

## ML\_Core

 $Name: ML\_Core\ Version: 3.1.0\ Description: Common\ definitions\ for\ Machine\ Learning\ License: See \ LICENSE.TXT\ Copyright: Copyright\ (C)\ 2017\ HPCC\ Systems\ Authors: HPCCSystems\ Platform: 6.2.0$ 

#### **Table of Contents**

 ${\it file: AppendSeqID.ecl}$ 

file : Config.eclfile : ToField.eclfile : Types.ecl

file: FieldAggregates.ecl

file : Generate.ecl file : Discretize.ecl file : FromField.ecl file : AppendID.ecl

 ${\it file: Constants.ecl\ Useful\ constants}$ 

dir : Tests dir : Interfaces dir : Utils dir : Math

# $ML\_Core.AppendSeqID$

### $\underline{\mathbf{IMPORTS}}$

### **DESCRIPTIONS**

 ${\bf macro: Append Seq ID}$ 

 ${\bf MACRO: AppendSeqID(dIn, idfield, dOut)}$ 

# ML\_Core.Config

### **IMPORTS**

### **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: Config} \\ \mathbf{MODULE: Config} \\ \mathbf{Up} \end{array}$ 

- 1. MaxLookup
- 2. Discrete
- 3. RoundingError

 $\begin{array}{l} \textbf{attribute: MaxLookup} \\ \textbf{ATTRIBUTE: MaxLookup} \\ \textbf{Up} \end{array}$ 

 $\begin{array}{l} \textbf{attribute: Discrete} \\ \textbf{ATTRIBUTE: Discrete} \\ \textbf{Up} \end{array}$ 

 $\begin{tabular}{ll} \bf attribute: Rounding Error \\ ATTRIBUTE: Rounding Error \\ \end{tabular}$ 

# $ML\_Core.ToField$

### $\underline{\mathbf{IMPORTS}}$

### **DESCRIPTIONS**

macro: ToField

 ${\it MACRO: ToField(dIn, dOut, idfield=", wifield=", wivalue=", datafields=")}$ 

## ML\_Core.Types

### **IMPORTS**

### **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: Types} \\ \mathbf{MODULE: Types} \\ \mathbf{Up} \end{array}$ 

- 1. t\_RecordID
- $2. \ t\_FieldNumber$
- $3. \ t\_FieldReal$
- 4. t\_FieldSign
- $5. t_{Discrete}$
- 6. t\_Item
- 7. t\_Count
- $8. \ t\_Work\_Item$
- 9. AnyField
- 10. NumericField
- 11. DiscreteField
- 12. Layout\_Model
- 13. Classify\_Result
- 14. l\_result
- 15. Confusion\_Detail
- 16. ItemElement
- 17. t\_node
- 18.  $t_{level}$
- 19. NodeID

```
attribute: t\_RecordID
```

 $\begin{array}{l} ATTRIBUTE: t\_RecordID \\ Up \end{array}$ 

 $attribute: t\_FieldNumber$ 

 $ATTRIBUTE: t\_FieldNumber$ 

Up

 $attribute: t_FieldReal$ 

 ${\bf ATTRIBUTE: t\_FieldReal}$ 

Up

 $attribute: t\_FieldSign$ 

 $ATTRIBUTE: t\_FieldSign$ 

Up

 $attribute: t\_Discrete$ 

 $ATTRIBUTE: t\_Discrete$ 

Up

 $attribute: t\_Item$ 

ATTRIBUTE: t Item

Up

 $attribute: t\_Count$ 

 $ATTRIBUTE: t\_Count$ 

Up

 $attribute: t_Work_Item$ 

 $ATTRIBUTE: t\_Work\_Item$ 

Up

record: AnyField

RECORD: AnyField

#### record: NumericField

RECORD: NumericField

Up

record: Discrete Field

RECORD: Discrete Field

Up

 ${\bf record: Layout\_Model}$ 

 $RECORD: Layout\_Model$ 

Up

 $record: Classify\_Result$ 

 $RECORD: Classify\_Result$ 

Up

 $record: l\_result$ 

 $RECORD: l\_result$ 

Up

record: Confusion\_Detail

 $RECORD: Confusion\_Detail$ 

Up

record: ItemElement

 $\label{eq:RECORD: ItemElement} \textbf{RECORD: ItemElement}$ 

Up

attribute: t\_node

 $ATTRIBUTE: t\_node$ 

Up

attribute: t\_level

 $ATTRIBUTE: t\_level$ 

record : NodeID

RECORD: NodeID

## $ML\_Core.FieldAggregates$

#### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet \ \mathrm{ML\_Core.Types}$
- $\bullet$  ML\_Core. Utils
- $\bullet$  std.system.ThorLib

### **DESCRIPTIONS**

module: FieldAggregates

 $\operatorname{MODULE}: \operatorname{FieldAggregates}(\operatorname{DATASET}(\operatorname{Types.NumericField})$ d) Up

- 1. Simple
- 2. SimpleRanked
- 3. Medians
- 4. MinMedNext
- 5. Buckets
- 6. BucketRanges
- 7. Modes
- 8. Cardinality
- 9. RankedInput
- 10. NTiles
- 11. NTileRanges

attribute : Simple ATTRIBUTE : Simple

attribute: SimpleRanked

 ${\bf ATTRIBUTE: Simple Ranked}$ 

Up

attribute: Medians

ATTRIBUTE : Medians

Up

attribute: MinMedNext

ATTRIBUTE : MinMedNext

Up

function: Buckets

FUNCTION : Buckets(Types.t\_Discrete n)

Up

function: BucketRanges

 $FUNCTION: BucketRanges(Types.t\_Discrete\ n)$ 

Up

attribute: Modes

ATTRIBUTE : Modes

Up

attribute: Cardinality

ATTRIBUTE : Cardinality

Up

attribute: RankedInput

 ${\bf ATTRIBUTE: Ranked Input}$ 

Up

function: NTiles

FUNCTION: NTiles(Types.t\_Discrete n)

### function: NTile Ranges

 $\begin{array}{l} FUNCTION: NTileRanges(Types.t\_Discrete\ n) \\ Up \end{array}$ 

## $ML\_Core.Generate$

#### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet \ \mathrm{ML\_Core.Types}$

### **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: Generate} \\ \mathbf{MODULE: Generate} \end{array}$ 

Up

- 1. tp\_Method
- 2. MethodName
- 3. ToPoly

attribute : tp\_Method
ATTRIBUTE : tp\_Method

Up

function: Method Name

 $\begin{aligned} & FUNCTION: MethodName(tp\_Method~x) \\ & Up \end{aligned}$ 

СP

function: ToPoly

 $FUNCTION: ToPoly(DATASET(Types.NumericField) \ seedCol, \ UNSIGNED \ maxN=6)$ 

# $ML\_Core.Discretize$

### $\underline{\mathbf{IMPORTS}}$

- $\bullet$  ML\_Core
- $\bullet \ \mathrm{ML\_Core.Types}$

### **DESCRIPTIONS**

module: Discretize

MODULE: Discretize

Up

- 1. c\_Method
- 2. r\_Method
- 3. i\_ByRounding
- 4. ByRounding
- 5. i\_ByBucketing
- 6. ByBucketing
- $7. \ i\_ByTiling$
- 8. ByTiling
- 9. Do

attribute: c\_Method

 $ATTRIBUTE: c\_Method$ 

Up

 $record: r\_Method$ 

 $RECORD: r\_Method$ 

#### function: i\_ByRounding

#### function: ByRounding

 $FUNCTION: By Rounding (DATASET (Types.Numeric Field) \ d, REAL\ Scale = 1.0,\ REAL\ Delta = 0.0) \ Up$ 

#### function: i\_ByBucketing

 $FUNCTION: i\_ByBucketing (SET\ OF\ Types.t\_FieldNumber\ f,\ Types.t\_Discrete\ N=ML\_Core.Config.Discrete)\ Up$ 

#### function: ByBucketing

 $FUNCTION: By Bucketing (DATASET (Types.Numeric Field) \ d, \ Types.t\_Discrete \ N=ML\_Core. Config. Discrete) \ Up$ 

#### function: i\_ByTiling

#### function: ByTiling

 $FUNCTION: By Tiling (DATASET (Types.Numeric Field) \ d, \ Types.t\_Discrete \ N=ML\_Core. Config. Discrete) \ Up$ 

#### function: Do

 $FUNCTION: Do(DATASET(Types.NumericField) \ d, \ DATASET(r\_Method) \ to\_do) \\ Up$ 

# $ML\_Core.FromField$

### $\underline{\mathbf{IMPORTS}}$

### **DESCRIPTIONS**

macro: FromField

MACRO: FromField(dIn,lOut,dOut,dMap=")

# $ML\_Core.AppendID$

### $\underline{\mathbf{IMPORTS}}$

### **DESCRIPTIONS**

macro: AppendID

MACRO: AppendID(dIn, idfield, dOut)

## $ML\_Core.Constants$

### **IMPORTS**

### **DESCRIPTIONS**

```
module: Constants

MODULE: Constants
Up

Useful constants

1. Pi
2. Root_2

attribute: Pi
ATTRIBUTE: Pi
Up

Constant PI

attribute: Root_2

ATTRIBUTE: Root_2
Up
```

## Tests

### **Table of Contents**

file: to\_from.ecl
file: Validate\_Betas.ecl
file: test\_discrete.ecl
file: test\_appends.ecl
file: Validate\_Gammas.ecl
file: field\_aggregates.ecl
file: Check\_Dist.ecl
file: generate.ecl

# $ML\_Core.Tests.to\_from$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

### **DESCRIPTIONS**

attribute : to\_from
ATTRIBUTE : to\_from

# $ML\_Core.Tests.Validate\_Betas$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Math
- python

### **DESCRIPTIONS**

 $attribute: Validate\_Betas$ 

 $ATTRIBUTE: Validate\_Betas$ 

## $ML\_Core.Tests.test\_discrete$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

### **DESCRIPTIONS**

 $attribute: test\_discrete$ 

 ${\bf ATTRIBUTE: test\_discrete}$ 

# $ML\_Core.Tests.test\_appends$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  std.system.thorlib

### **DESCRIPTIONS**

 $attribute: test\_appends$ 

 $ATTRIBUTE: test\_appends$ 

# $ML\_Core. Tests. Validate\_Gammas$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Math
- python

### **DESCRIPTIONS**

 $attribute: Validate\_Gammas$ 

 $ATTRIBUTE: Validate\_Gammas$ 

# $ML\_Core. Tests. field\_aggregates$

### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

### **DESCRIPTIONS**

 $attribute: field\_aggregates$ 

 ${\bf ATTRIBUTE: field\_aggregates}$ 

## $ML\_Core.Tests.Check\_Dist$

### **IMPORTS**

- $\bullet \ \mathrm{ML\_Core.Math.Distributions}$
- $\bullet$  ML\_Core
- python

### **DESCRIPTIONS**

 $attribute: Check\_Dist$ 

 $ATTRIBUTE: Check\_Dist$ 

# ${\bf ML\_Core. Tests. generate}$

### **IMPORTS**

 $\bullet$  ML\_Core

### **DESCRIPTIONS**

attribute : generate
ATTRIBUTE : generate

## Interfaces

#### **Table of Contents**

file : IRegression.ecl Interface Definition for Regression Modules Regression learns a function that maps a

set of input data to one or more output variables

 ${\it file: IClassify.ecl\ Interface\ definition\ for\ Classification}$ 

### ML\_Core.Interfaces.IRegression

#### **IMPORTS**

- ML\_Core
- ML\_Core.Types

#### DESCRIPTIONS

module: IRegression

 $\begin{aligned} & MODULE: IRegression(DATASET(NumericField) \ X=empty\_data, DATASET(NumericField) \ Y=empty\_data) \\ & Up \end{aligned}$ 

Interface Definition for Regression Modules Regression learns a function that maps a set of input data to one or more output variables. The resulting learned function is known as the model. That model can then be used repetitively to predict (i.e. estimate) the output value(s) based on new input data.

**Parameter**: X ||| The independent data in DATASET(NumericField) format. Each statistical unit (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number').

**Parameter**: Y ||| The dependent variable(s) in DATASET(NumericField) format. Each statistical unit (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number').

- 1. GetModel
- 2. Predict

#### attribute: GetModel

 $\begin{array}{lll} & \text{ATTRIBUTE}: \text{DATASET(Layout\_Model)} \text{ GetModel} \\ & \text{Up} \end{array}$ 

Calculate and return the 'learned' model The model may be persisted and later used to make predictions using 'Predict' below.

Return: DATASET(LayoutModel) describing the learned model parameters

#### function: Predict

 $FUNCTION: DATASET(NumericField) \ Predict(DATASET(NumericField) \ newX, \ DATASET(Layout\_Model) \\ model) \\ Up$ 

Predict the output variable(s) based on a previously learned model

Parameter: newX || DATASET(NumericField) containing the X values to b predicted.

 $\mathbf{Return}: \, \mathrm{DATASET}(\mathrm{NumericField}) \, \, \mathrm{containing} \, \, \mathrm{one} \, \, \mathrm{entry} \, \, \mathrm{per} \, \, \mathrm{observation} \, \, (\mathrm{i.e.} \, \, \mathrm{id}) \, \, \mathrm{in} \, \, \mathrm{new} X. \, \, \mathrm{This} \, \, \mathrm{represents} \, \, \mathrm{the} \, \, \mathrm{predicted} \, \, \mathrm{values} \, \, \mathrm{for} \, \, Y.$ 

### ML\_Core.Interfaces.IClassify

#### **IMPORTS**

- ML\_Core
- ML\_Core.Types

#### DESCRIPTIONS

module : IClassify
MODULE : IClassify
Up

Interface definition for Classification. Actual implementation modules will probably take parameters.

- 1. GetModel
- 2. Classify
- 3. Report

#### function: GetModel

 $FUNCTION: DATASET(Types.Layout\_Model) \ GetModel(DATASET(Types.NumericField) \ observations, \\ DATASET(Types.DiscreteField) \ classifications) \\ Up$ 

Calculate the model to fit the observation data to the observed classes.

Parameter: observations ||| the observed explanatory values

Parameter: classifications ||| the observed classification used to build the model

Return: the encoded model

#### function: Classify

 $FUNCTION: DATASET(Types.Classify\_Result) \ Classify(DATASET(Types.Layout\_Model) \ model, \ DATASET(Types.Numnew\_observations) \\ Up$ 

Classify the observations using a model.

Parameter: model ||| The model, which must be produced by a corresponding getModel function.

Parameter: new\_observations ||| observations to be classified

**Return**: Classification with a confidence value

#### function: Report

FUNCTION: DATASET(Types.Confusion\_Detail) Report(DATASET(Types.Layout\_Model) model, DATASET(Types.Nur.observations, DATASET(Types.DiscreteField) classifications)

Up

Report the confusion matrix for the classifier and training data.

 $\mathbf{Parameter}: \mathbf{model} \ ||| \ \mathbf{the} \ \mathbf{encoded} \ \mathbf{model}$ 

 ${\bf Parameter}:$  observations ||| the explanatory values.

 $\mathbf{Parameter}:$  classifications ||| the classifications associated with the observations

Return: the confusion matrix showing correct and incorrect results

## Utils

#### **Table of Contents**

file: SequenceInField.ecl Given a file which is sorted by the work item identifier and INFIELD (and possibly

other values), add sequence numbers within the range of each infield file: FatD.ecl Will take a potentially sparse file d and fill in the missing file: Fat.ecl Will take a potentially sparse file d and fill in the missing file: Gini.ecl Creates a file of pivot/target pairs with a Gini impurity value

## ML\_Core.Utils.SequenceInField

#### **IMPORTS**

#### **DESCRIPTIONS**

macro: SequenceInField

MACRO: SequenceInField(infile,infield,seq,wi\_name='wi')

Up

Given a file which is sorted by the work item identifier and INFIELD (and possibly other values), add sequence numbers within the range of each infield. Slighly elaborate code is to avoid having to partition the data to one value of infield per node and to work with very large numbers of records where a global count project would be inappropriate. This is useful for assigning rank positions with the groupings.

Parameter: infile ||| the input file, any type Parameter: infield ||| field name of grouping field

Parameter: seq ||| name of the field to receive the sequence number

Parameter: wi\_name ||| work item field name, default is wi Return: a file of the same type with sequence numbers applied

## $ML\_Core.Utils.FatD$

#### **IMPORTS**

 $\bullet$  ML\_Core.Types

#### **DESCRIPTIONS**

function: FatD

 $FUNCTION: DATASET(Types.DiscreteField) \ FatD(DATASET(Types.DiscreteField) \ d0, \ Types.t\_Discrete \ v=0)$ 

Up

Will take a potentially sparse file d and fill in the missing with value v for Discrete Field datasets

Parameter: d0 || They myriad format Discrete Field dataset to be filled

Parameter: v ||| The value to assign missing records

Return: A full Discrete Field dataset with every field populated

## $ML\_Core.Utils.Fat$

#### **IMPORTS**

 $\bullet$  ML\_Core.Types

#### **DESCRIPTIONS**

function: Fat

 ${\tt FUNCTION}: {\tt DATASET}({\tt Types.NumericField})$   ${\tt Fat}({\tt DATASET}({\tt Types.NumericField})$   ${\tt d0},$   ${\tt Types.t\_FieldReal}$   ${\tt v=0})$   ${\tt Up}$ 

Will take a potentially sparse file d and fill in the missing with value v for Numeric Field datasets

Parameter: d0 || They myriad format Numeric Field dataset to be filled

Parameter: v ||| The value to assign missing records

Return: A full Numeric Field dataset with every field populated

## $ML\_Core.Utils.Gini$

### **IMPORTS**

#### **DESCRIPTIONS**

macro: Gini

MACRO : Gini(infile, pivot, target, wi\_name='wi')

Up

Creates a file of pivot/target pairs with a Gini impurity value. **Parameter**: infile ||| the input file, any type with a work item field

 $\mathbf{Parameter}:$  pivot ||| the name of the pivot field

 $\mathbf{Parameter}$ : target ||| the name of the field used as the target

Parameter: wi\_name ||| the name of the work item field, default is "wi" return A table by Work Item and

Pivot value giving count and Gini impurity value

## Math

#### **Table of Contents**

file: StirlingFormula.ecl Stirling's formula

file: NCK.ecl

file: upperGamma.ecl Return the upper incomplete gamma value of two real numbers, x and y

file: Beta.ecl Return the beta value of two positive real numbers, x and y

 $\label{eq:continuous} \textbf{file: } \textbf{gamma.ecl} \ \textbf{Return the value of } \textbf{gamma function of real number } \textbf{x} \ \textbf{A} \ \textbf{wrapper for the standard} \ \textbf{C} \ \textbf{tgamma function}$ 

file: log\_gamma.ecl Return the value of the log gamma function of the absolute value of X

file: Fac.ecl Factorial function

file: lowerGamma.ecl Return the lower incomplete gamma value of two real numbers,

file: DoubleFac.ecl The 'double' factorial is defined for ODD n and is the product of all the odd numbers up to and including that number

file: Poly.ecl Evaluate a polynomial from a set of co-effs

file: Distributions.ecl

# $ML\_Core. Math. Stirling Formula$

### **IMPORTS**

- $\bullet$  ML\_Core.Math
- $\bullet$  ML\_Core. Constants

## **DESCRIPTIONS**

function: Stirling Formula

 $FUNCTION: StirlingFormula(REAL\ x)$ 

Up

Stirling's formula

**Parameter** : x ||| the point of evaluation

Return: evaluation result

# $ML\_Core.Math.NCK$

### **IMPORTS**

 $\bullet$  ML\_Core.Math

## **DESCRIPTIONS**

function: NCK

FUNCTION: REAL8 NCK(INTEGER2 N, INTEGER2 K)

Up

## $ML\_Core.Math.upperGamma$

### **IMPORTS**

#### **DESCRIPTIONS**

embed: upperGamma

EMBED: REAL8 upperGamma(REAL8 x, REAL8 y)

Up

Return the upper incomplete gamma value of two real numbers, x and y.

Parameter: x ||| the value of the first number
Parameter: y ||| the value of the second number
Return: the upper incomplete gamma value

# $ML\_Core.Math.Beta$

### **IMPORTS**

 $\bullet$  ML\_Core.Math

### **DESCRIPTIONS**

function: Beta

FUNCTION : Beta(REAL8 x, REAL8 y)

Up

Return the beta value of two positive real numbers, x and y

 $\begin{array}{lll} \textbf{Parameter}: & x \mid \mid \mid \text{the value of the first number} \\ \textbf{Parameter}: & y \mid \mid \mid \text{the value of the second number} \end{array}$ 

Return: the beta value

# $ML\_Core.Math.gamma$

## **IMPORTS**

### **DESCRIPTIONS**

embed: gamma

EMBED : REAL8 gamma(REAL8 x)

Up

Return the value of gamma function of real number x A wrapper for the standard C tgamma function.

 $\mathbf{Parameter}: x \mid\mid\mid the \ input \ x$ 

 ${\bf Return}$  : the value of GAMMA evaluated at x

## $ML\_Core.Math.log\_gamma$

### **IMPORTS**

#### **DESCRIPTIONS**

embed: log\_gamma

EMBED : REAL8 log\_gamma(REAL8 x)

Up

Return the value of the log gamma function of the absolute value of X. A wrapper for the standard C lgamma function. Avoids the race condition found on some platforms by taking the absolute value of the of the input argument.

**Parameter** :  $x \parallel \parallel$  the input x

 ${f Return}$ : the value of the log of the GAMMA evaluated at ABS(x)

# $ML\_Core.Math.Fac$

## $\underline{\mathbf{IMPORTS}}$

### **DESCRIPTIONS**

embed : Fac

EMBED: REAL8 Fac(UNSIGNED2 i)

 $\operatorname{Up}$ 

Factorial function

**Parameter** : i ||| the value used, (i)(i-1)(i-2)...(2)

Return: the factorial i!

## $ML\_Core.Math.lowerGamma$

### **IMPORTS**

### **DESCRIPTIONS**

embed: lowerGamma

 ${\bf EMBED: REAL8\ lowerGamma(REAL8\ x,\ REAL8\ y)}$ 

Up

Return the lower incomplete gamma value of two real numbers, x and y

Parameter: x ||| the value of the first number Parameter: y ||| the value of the second number Return: the lower incomplete gamma value

## $ML\_Core. Math. Double Fac$

### **IMPORTS**

#### **DESCRIPTIONS**

embed: DoubleFac

EMBED: REAL8 DoubleFac(INTEGER2 i)

Up

The 'double' factorial is defined for ODD n and is the product of all the odd numbers up to and including that number. We are extending the meaning to even numbers to mean the product of the even numbers up to and including that number. Thus DoubleFac(8) = 8\*6\*4\*2 We also defend against i < 2 (returning 1.0)

**Parameter**: i ||| the value used in the calculation **Return**: the factorial of the sequence, declining by 2

## ML\_Core.Math.Poly

### **IMPORTS**

#### **DESCRIPTIONS**

embed: Poly

EMBED: REAL8 Poly(REAL8 x, SET OF REAL8 Coeffs)

Up

Evaluate a polynomial from a set of co-effs. Co-effs 1 is assumed to be the HIGH order of the equation. Thus for  $ax^2+bx+c$  - the set would need to be Coef := [a,b,c];

 $\mathbf{Parameter}: x \mid\mid\mid the \ value \ of \ x \ in \ the \ polynomial$ 

Parameter: Coeffs ||| a set of coefficients for the polynomial. The ALL set is considered to be all zero

values

 ${f Return}$ : value of the polynomial at x

## ML\_Core.Math.Distributions

#### **IMPORTS**

- ML Core.Constants
- ML\_Core.Math

#### **DESCRIPTIONS**

module: Distributions

MODULE : Distributions

Up

- 1. Normal CDF
- 2. Normal PPF
- 3. T\_CDF
- 4. T\_PPF
- 5. Chi2\_CDF
- 6. Chi<sub>2</sub> PPF

function: Normal\_CDF

FUNCTION : REAL8 Normal\_CDF(REAL8 x) Up

Cumulative Distribution of the standard normal distribution, the probability that a normal random variable will be smaller than x standard deviations above or below the mean. Taken from C/C++ Mathematical Algorithms for Scientists and Engineers, n. Shammas, McGraw-Hill, 1995

Parameter: x ||| the number of standard deviations

function: Normal\_PPF

 $\begin{aligned} & FUNCTION: REAL8 \ Normal\_PPF(REAL8 \ x) \\ & Up \end{aligned}$ 

Normal Distribution Percentage Point Function. Translated from C/C++ Mathematical Algorithms for Scientists and Engineers, N. Shammas, McGraw-Hill, 1995

**Parameter** : x ||| probability

function: T CDF

FUNCTION: REAL8 T\_CDF(REAL8 x, REAL8 df)

Up

Students t distribution integral evaluated between negative infinity and x. Translated from NIST SEL

DATAPAC Fortran TCDF.f source

 $\begin{array}{ll} \textbf{Parameter}: \ x \ ||| \ value \ of \ the \ evaluation \\ \textbf{Parameter}: \ df \ ||| \ degrees \ of \ freedom \end{array}$ 

 $function : T_PPF$ 

FUNCTION: REAL8 T\_PPF(REAL8 x, REAL8 df)

Up

Percentage point function for the T distribution. Translated from NIST SEL DATAPAC Fortran TPPF.f source

function: Chi2\_CDF

 $FUNCTION: REAL8\ Chi2\_CDF(REAL8\ x,\ REAL8\ df)$ 

Up

The cumulative distribution function for the Chi Square distribution. the CDF for the specified degrees of freedom. Translated from the NIST SEL DATAPAC Fortran subroutine CHSCDF.

function: Chi2 PPF

FUNCTION: REAL8 Chi2\_PPF(REAL8 x, REAL8 df)

Up

The Chi Squared PPF function. Translated from the NIST SEL DATAPAC Fortran subroutine CHSPPF.

## LogisticRegression

Name: LogisticRegression Version: 1.0.0 Description: Logistic Regression implementation License: http://www.apache.org/licenses/LICENSE-2.0 Copyright: Copyright (C) 2017 HPCC Systems Authors: HPCCSystems DependsOn: ML Core, PBblas Platform: 6.2.0

#### Table of Contents

file: Deviance\_Analysis.ecl Compare deviance information for an analysis of deviance

file: LogitPredict.ecl Predict the category values with the logit function and the the supplied beta coefficients

file: Deviance\_Detail.ecl Detail deviance for each observation

file: Types.ecl file: Constants.ecl file: Distributions.ecl

file: Null Deviance.ecl Deviance for the null model, that is, a model with only an intercept

file: ExtractReport.ecl Extract Report records from model

file: ExtractBeta\_CI.ecl Extract the beta values form the model dataset

file: dimm.ecl Matrix multiply when either A or B is a diagonal and is passed as a vector

file: BinomialConfusion.ecl Binomial confusion matrix

file: Model\_Deviance.ecl Model Deviance

file: LogitScore.ecl Calculate the score using the logit function and the supplied beta coefficients file: Confusion.ecl Detail confusion records to compare actual versus predicted response variable values

file: ExtractBeta.ecl Extract the beta values form the model dataset

file: BinomialLogisticRegression.ecl Binomial logistic regression using iteratively re-weighted least squares

file: DataStats.ecl Information about the datasets

file: ExtractBeta pval.ecl Extract the beta values form the model dataset

## LogisticRegression.Deviance\_Analysis

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types

#### **DESCRIPTIONS**

function: Deviance\_Analysis

 $FUNCTION: DATASET(Types.AOD\_Record) \ Deviance\_Analysis(DATASET(Types.Deviance\_Record) \ proposed, \ DATASET(Types.Deviance\_Record) \ base) \\ Up$ 

Compare deviance information for an analysis of deviance.

Parameter: proposed ||| the proposed model

Parameter: base ||| the base model for comparison

**Return**: the comparison of the deviance between the models

## ${\bf Logistic Regression. Logit Predict}$

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- ML\_Core.Types

#### **DESCRIPTIONS**

function: LogitPredict

 $FUNCTION: DATASET(Classify\_Result) \ LogitPredict(DATASET(Model\_Coef) \ coef, \ DATASET(NumericField) \ independents)$ 

Up

Predict the category values with the logit function and the supplied beta coefficients.

Parameter: coef ||| the model beta coefficients Parameter: independents ||| the observations

Return: the predicted category values and a confidence score

## LogisticRegression.Deviance\_Detail

#### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types
- LogisticRegression
- LogisticRegression.Types

#### **DESCRIPTIONS**

function: Deviance\_Detail

 $FUNCTION: DATASET(Types.Observation\_Deviance) \ Deviance\_Detail(DATASET(Core\_Types.DiscreteField) \ dependents, \ DATASET(Types.Raw\_Prediction) \ predicts) \ Up$ 

Detail deviance for each observation.

**Parameter**: dependents ||| original dependent records for the model **Parameter**: predicts ||| the predicted values of the response variable

Return: the deviance information by observation and the log likelihood of the predicted result.

## LogisticRegression.Types

#### **IMPORTS**

 $\bullet \ \mathrm{ML\_Core.Types}$ 

#### **DESCRIPTIONS**

```
\begin{array}{l} \textbf{module: Types} \\ \textbf{MODULE: Types} \\ \textbf{Up} \end{array}
```

- 1. t\_Universe
- 2. Field Desc
- 3. Data\_Info
- 4. NumericField\_U
- $5. \ DiscreteField\_U$
- 6. Layout\_Column\_Map
- 7. Classifier\_Stats
- 8. Model\_Report
- 9. Binomial\_Confusion\_Summary
- 10. Model\_Coef
- 11. Confidence\_Model\_Coef
- 12. pval\_Model\_Coef
- 13. Raw\_Prediction
- 14. Observation\_Deviance
- 15. Deviance\_Record
- 16. AOD\_Record

 $attribute: t\_Universe$ 

 $\begin{array}{l} {\bf ATTRIBUTE: t\_Universe} \\ {\bf Up} \end{array}$ 

 $record : Field\_Desc$ 

 ${\tt RECORD:Field\_Desc}$ 

Up

record: Data\_Info

 $RECORD: Data\_Info$ 

Up

record: NumericField\_U

 $RECORD: NumericField\_U$ 

Up

 $record: DiscreteField\_U$ 

 $RECORD: DiscreteField\_U$ 

Up

record : Layout\_Column\_Map

 $RECORD: Layout\_Column\_Map$ 

Up

record : Classifier\_Stats

RECORD : Classifier Stats

Up

record: Model\_Report

 $RECORD : Model\_Report$ 

Up

record: Binomial\_Confusion\_Summary

RECORD: Binomial\_Confusion\_Summary

Up

record: Model\_Coef

 $RECORD : Model\_Coef$ 

Up

 ${\bf record: Confidence\_Model\_Coef}$ 

 $RECORD: Confidence\_Model\_Coef$ 

Up

 $record: pval\_Model\_Coef$ 

 $RECORD: pval\_Model\_Coef$ 

Up

record: Raw\_Prediction

RECORD : Raw Prediction

Up

 $record: Observation\_Deviance$ 

 ${\tt RECORD: Observation\_Deviance}$ 

Up

record : Deviance\_Record

 ${\tt RECORD: Deviance\_Record}$ 

Up

record: AOD\_Record

 ${\tt RECORD: AOD\_Record}$ 

Up

# ${\bf Logistic Regression. Constants}$

### **IMPORTS**

#### **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: Constants} \\ \mathbf{MODULE: Constants} \\ \mathbf{Up} \end{array}$ 

- 1. limit\_card
- 2. default\_epsilon
- 3. default\_ridge
- 4. local\_cap
- 5. id\_base
- 6. id\_iters
- $7. \ id\_delta$
- 8. id\_correct
- 9. id\_incorrect
- 10. id\_stat\_set
- 11. id\_betas
- 12. id\_betas\_coef
- 13. id\_betas\_SE
- 14. base\_builder
- 15. base\_max\_iter
- 16. base\_epsilon
- 17. base\_ind\_vars
- 18. base\_dep\_vars
- 19. base\_obs
- 20. builder\_irls\_local
- 21. builder\_irls\_global
- 22. builder\_softmax

attribute: limit card

 $ATTRIBUTE: UNSIGNED2\ limit\_card$ 

Up

attribute: default\_epsilon

 $ATTRIBUTE: REAL8 \ default\_epsilon$ 

Up

attribute : default\_ridge

 ${\bf ATTRIBUTE: REAL 8 \ default\_ridge}$ 

 $\operatorname{Up}$ 

attribute: local\_cap

ATTRIBUTE : UNSIGNED4 local\_cap

Up

attribute: id\_base

 $ATTRIBUTE: id\_base$ 

Up

attribute: id\_iters

ATTRIBUTE : id iters

Up

attribute: id\_delta

ATTRIBUTE : id delta

Up

attribute: id\_correct

 $ATTRIBUTE: id\_correct$ 

Up

 $attribute: id\_incorrect$ 

ATTRIBUTE : id\_incorrect

Up

```
attribute: id_stat_set
```

 $ATTRIBUTE: id\_stat\_set$ 

Up

#### attribute : id\_betas

 ${\bf ATTRIBUTE: id\_betas}$ 

Up

#### attribute: id\_betas\_coef

 $ATTRIBUTE: id\_betas\_coef$ 

Up

#### attribute: id\_betas\_SE

 $ATTRIBUTE: id\_betas\_SE$ 

Up

#### attribute : base\_builder

 $ATTRIBUTE: base\_builder$ 

Up

#### $attribute: base\_max\_iter$

ATTRIBUTE : base\_max\_iter

Up

#### attribute : base\_epsilon

 $ATTRIBUTE: base\_epsilon$ 

Up

#### attribute: base\_ind\_vars

 $ATTRIBUTE: base\_ind\_vars$ 

Up

#### attribute: base\_dep\_vars

 $ATTRIBUTE: base\_dep\_vars$ 

Up

attribute: base\_obs

 ${\bf ATTRIBUTE: base\_obs}$ 

Up

attribute: builder\_irls\_local

 $ATTRIBUTE: builder\_irls\_local$ 

Up

 $attribute: builder\_irls\_global$ 

 $ATTRIBUTE: builder\_irls\_global$ 

Up

 $attribute: builder\_softmax$ 

 $ATTRIBUTE: builder\_softmax$ 

 $\operatorname{Up}$ 

## LogisticRegression.Distributions

#### **IMPORTS**

- ML Core.Constants
- ML\_Core.Math

#### **DESCRIPTIONS**

module: Distributions

 ${\bf MODULE: Distributions}$ 

Up

- 1. Normal CDF
- 2. Normal PPF
- 3. T\_CDF
- 4. T\_PPF
- 5. Chi2\_CDF
- 6. Chi<sub>2</sub> PPF

function: Normal\_CDF

FUNCTION : REAL8 Normal\_CDF(REAL8 x) Up

Cumulative Distribution of the standard normal distribution, the probability that a normal random variable will be smaller than x standard deviations above or below the mean. Taken from C/C++ Mathematical Algorithms for Scientists and Engineers, n. Shammas, McGraw-Hill, 1995

Parameter: x ||| the number of standard deviations

function: Normal\_PPF

 $\begin{aligned} & FUNCTION: REAL8 \ Normal\_PPF(REAL8 \ x) \\ & Up \end{aligned}$ 

Normal Distribution Percentage Point Function. Translated from C/C++ Mathematical Algorithms for Scientists and Engineers, N. Shammas, McGraw-Hill, 1995

**Parameter** : x ||| probability

function: T CDF

 $FUNCTION: REAL8\ T\_CDF(REAL8\ x,\ REAL8\ df)$ 

Up

Students t distribution integral evaluated between negative infinity and x. Translated from NIST SEL

DATAPAC Fortran TCDF.f source

 $\begin{array}{ll} \textbf{Parameter}: \ x \ ||| \ value \ of \ the \ evaluation \\ \textbf{Parameter}: \ df \ ||| \ degrees \ of \ freedom \end{array}$ 

 $function : T_PPF$ 

FUNCTION: REAL8 T\_PPF(REAL8 x, REAL8 df)

Up

Percentage point function for the T distribution. Translated from NIST SEL DATAPAC Fortran TPPF.f source

function: Chi2\_CDF

 $FUNCTION: REAL8\ Chi2\_CDF(REAL8\ x,\ REAL8\ df)$ 

Up

The cumulative distribution function for the Chi Square distribution. the CDF for the specified degrees of freedom. Translated from the NIST SEL DATAPAC Fortran subroutine CHSCDF.

function: Chi2 PPF

FUNCTION: REAL8 Chi2\_PPF(REAL8 x, REAL8 df)

Up

The Chi Squared PPF function. Translated from the NIST SEL DATAPAC Fortran subroutine CHSPPF.

# $Logistic Regression. Null\_Deviance$

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types

#### **DESCRIPTIONS**

function: Null\_Deviance

 $\label{eq:function} FUNCTION: DATASET(Types.Deviance\_Record) \ Null\_Deviance(DATASET(Types.Observation\_Deviance) \\ od) \\ Up$ 

Deviance for the null model, that is, a model with only an intercept.

**Parameter** : od || Observation Deviance record set.

Return: a data set of the null model deviances for each work item and classifier.

# ${\bf Logistic Regression. Extract Report}$

#### **IMPORTS**

- ullet LogisticRegression
- $\bullet$  Logistic Regression. Types
- ullet Logistic Regression. Constants
- $\bullet \ \mathrm{ML\_Core.Types}$

### **DESCRIPTIONS**

function: ExtractReport

 $FUNCTION: DATASET(Types.Model\_Report) \ ExtractReport(DATASET(Core\_Types.Layout\_Model) \ mod\_ds) \ Up$ 

Extract Report records from model  $Parameter : mod_ds | | |$  the model dataset

**Return**: the model report dataset

## LogisticRegression.ExtractBeta\_CI

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- ML\_Core.Types

#### **DESCRIPTIONS**

function: ExtractBeta\_CI

 $FUNCTION: DATASET(Types.Confidence\_Model\_Coef) \ ExtractBeta\_CI(DATASET(Core\_Types.Layout\_Model) \\ mod\_ds, \ REAL8 \ level) \\ Up$ 

Extract the beta values form the model dataset.

 $\mathbf{Parameter} : \bmod \_ ds \mid\mid\mid the \bmod el \ dataset$ 

**Parameter**: level ||| the significance value for the intervals **Return**: the beta values with confidence intervals term.

## LogisticRegression.dimm

#### **IMPORTS**

- std.BLAS
- $\bullet$  std.BLAS.Types

#### DESCRIPTIONS

#### embed: dimm

EMBED: Types.matrix\_t dimm(BOOLEAN transposeA, BOOLEAN transposeB, BOOLEAN diagonalA, BOOLEAN diagonalB, Types.dimension\_t m, Types.dimension\_t n, Types.dimension\_t k, Types.value\_t alpha, Types.matrix\_t A, Types.matrix\_t B, Types.value\_t beta=0.0, Types.matrix\_t C=[])
Up

Matrix multiply when either A or B is a diagonal and is passed as a vector. alpha\*op(A) op(B) + beta\*C where op() is transpose

Parameter: transposeA ||| true when transpose of A is used Parameter: transposeB ||| true when transpose of B is used Parameter: diagonalA ||| true when A is the diagonal matrix Parameter: diagonalB ||| true when B is the diagonal matrix

Parameter: m ||| number of rows in product
Parameter: n ||| number of columns in product

Parameter: k || number of columns/rows for the multiplier/multiplicand

Parameter: alpha ||| scalar used on A

Parameter : A ||| matrix A Parameter : B ||| matrix B

Parameter: beta ||| scalar for matrix C Parameter: C ||| matrix C or empty

## LogisticRegression.BinomialConfusion

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- ML\_Core.Types

### **DESCRIPTIONS**

function: BinomialConfusion

 $FUNCTION: DATASET (Types. Binomial\_Confusion\_Summary) \\ BinomialConfusion (DATASET (Core\_Types. Confusion\_Dataset (Core\_Types. Core\_Types. Confusion\_Dataset (Core\_Types. Core\_Types. Core$ 

Binomial confusion matrix. Work items with multinomial responses are ignored by this function. The higher value lexically is considered to be the positive indication.

Parameter: d ||| confusion detail for the work item and classifier

Return: confusion matrix for a binomial classifier

## $Logistic Regression. Model\_Deviance$

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types

## **DESCRIPTIONS**

 $function: Model\_Deviance$ 

 $FUNCTION: DATASET(Types.Deviance\_Record) \ Model\_Deviance(DATASET(Types.Observation\_Deviance) \\ od, \ DATASET(Types.Model\_Coef) \ mod) \\ Up$ 

Model Deviance.

Parameter : od ||| observation deviance record

 $\mathbf{Parameter} : \bmod ||| \bmod el \ co\text{-efficients}$ 

Return: model deviance

# ${\bf Logistic Regression. Logit Score}$

### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- ML\_Core.Types

#### **DESCRIPTIONS**

function: LogitScore

 $FUNCTION: DATASET(Raw\_Prediction) \ LogitScore(DATASET(Model\_Coef) \ coef, \ DATASET(NumericField) \ coef, \ DATASET(Numeric$ 

 $\frac{1}{2} \left( \frac{1}{2} \right) = \frac{1}{2} \left( \frac{1}{2} \right) = \frac{1}$ 

Up

Calculate the score using the logit function and the the supplied beta coefficients.

 $\begin{array}{l} \textbf{Parameter}: \ coef \ ||| \ the \ model \ beta \ coefficients \\ \textbf{Parameter}: \ independents \ ||| \ the \ observations \end{array}$ 

 ${f Return}$ : the raw prediction value

## LogisticRegression.Confusion

#### **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types
- LogisticRegression
- $\bullet$  Logistic Regression. Types

#### **DESCRIPTIONS**

function: Confusion

 $FUNCTION: DATASET(Confusion\_Detail) \ Confusion(DATASET(DiscreteField) \ dependents, \ DATASET(DiscreteField) \ predicts) \ Up$ 

Detail confusion records to compare actual versus predicted response variable values.

Parameter: dependents ||| the original response values

 ${\bf Parameter}: \ {\rm predicts} \ ||| \ {\rm the} \ {\rm predicted} \ {\rm responses}$ 

Return: confusion counts by predicted and actual response values.

# ${\bf Logistic Regression. Extract Beta}$

#### **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- $\bullet$  ML\_Core.Types

### **DESCRIPTIONS**

function: ExtractBeta

 $FUNCTION: ExtractBeta(DATASET(Core\_Types.Layout\_Model) \ mod\_ds) \\ Up$ 

Extract the beta values form the model dataset.

 $\mathbf{Parameter} : \bmod \_ \mathrm{ds} \ ||| \ \mathrm{the} \ \mathrm{model} \ \mathrm{dataset}$ 

Return: a beta values as Model Coefficient records, zero as the constant term.

# LogisticRegression.BinomialLogisticRegression

#### **IMPORTS**

- LogisticRegression
- LogisticRegression.Constants
- ML\_Core.Interfaces
- ML\_Core.Types

#### DESCRIPTIONS

#### module: BinomialLogisticRegression

$$\label{eq:module} \begin{split} & MODULE: Binomial Logistic Regression (UNSIGNED\ max\_iter=200, REAL8\ epsilon=Constants.default\_epsilon, REAL8\ ridge=Constants.default\_ridge) \\ & Up \end{split}$$

Binomial logistic regression using iteratively re-weighted least squares.

Parameter: max iter || maximum number of iterations to try

Parameter: epsilon ||| the minimum change in the Beta value estimate to continue

Parameter: ridge ||| a value to populate a diagonal matrix that is added to a matrix help assure that the matrix is invertible.

- 1. GetModel
- 2. Classify
- 3. Report

#### function: GetModel

 $FUNCTION: DATASET(Types.Layout\_Model) \ GetModel(DATASET(Types.NumericField) \ observations, \\ DATASET(Types.DiscreteField) \ classifications) \\ Up$ 

Calculate the model to fit the observation data to the observed classes.

**Parameter**: observations ||| the observed explanatory values

Parameter: classifications ||| the observed classification used to build the model

Return: the encoded model

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

### function: Classify

 $FUNCTION: DATASET(Types.Classify\_Result) \ Classify(DATASET(Types.Layout\_Model) \ model, \ DATASET(Types.Numnew\_observations)$ 

Up

Classify the observations using a model.

Parameter: model ||| The model, which must be produced by a corresponding getModel function.

Parameter: new\_observations ||| observations to be classified

Return: Classification with a confidence value

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

#### function: Report

 $FUNCTION: DATASET(Types.Confusion\_Detail) \ Report(DATASET(Types.Layout\_Model) \ model, \ DATASET(Types.Number various, \ DATASET(Types.Discrete Field) \ classifications) \\ Up$ 

Report the confusion matrix for the classifier and training data.

Parameter: model ||| the encoded model

Parameter: observations ||| the explanatory values.

Parameter: classifications ||| the classifications associated with the observations

Return: the confusion matrix showing correct and incorrect results

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

# ${\bf Logistic Regression. Data Stats}$

### **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- LogisticRegression.Constants
- ML\_Core.Types

### **DESCRIPTIONS**

function: DataStats

FUNCTION : DATASET(Types.Data\_Info) DataStats(DATASET(Core\_Types.NumericField) indep, DATASET(Core\_Typedep, BOOLEAN field\_details=FALSE)

Up

Information about the datasets. Without details the range for the x and y (independent and dependent) columns. Note that a column of all zero values cannot be distinguished from a missing column. When details are requested, the cardinality, minimum, and maximum values are returned. A zero cardinality is returned when the field cardinality exceeds the Constants.limit\_card value.

Parameter: indep || data set of independent variables
Parameter: dep || data set of dependent variables

Parameter: field\_details || Boolean directive to provide field level info

# $Logistic Regression. Extract Beta\_pval$

# **IMPORTS**

- LogisticRegression
- $\bullet$  Logistic Regression. Types
- ML\_Core.Types

# **DESCRIPTIONS**

function: ExtractBeta\_pval

 $FUNCTION: DATASET(Types.pval\_Model\_Coef) \ ExtractBeta\_pval(DATASET(Core\_Types.Layout\_Model) \ mod\_ds) \ Up$ 

Extract the beta values form the model dataset.

 $\mathbf{Parameter} : \bmod \_ \mathrm{ds} \ ||| \ \mathrm{the} \ \mathrm{model} \ \mathrm{dataset}$ 

 ${f Return}$ : the beta values with p-values as Model Coefficient records, zero as the constant term.

# LinearRegression

# **Table of Contents**

file: OLS.ecl Ordinary Least Squares (OLS) Linear Regression aka Ordinary Linear Regression Regression learns a function that maps a set of input data (independents) to one or more output variables (dependents)

# LinearRegression.OLS

### **IMPORTS**

- ML\_Core
- ML\_Core.Types
- PBblas
- PBblas.Types
- PBblas.Converted
- PBblas.MatUtils
- ML Core.Math

#### **DESCRIPTIONS**

module: OLS

 $\label{eq:module} \begin{aligned} & \text{MODULE}: \text{OLS}(\text{DATASET}(\text{NumericField}) \ X \text{=} \text{empty\_data}, \ \text{DATASET}(\text{NumericField}) \ Y \text{=} \text{empty\_data}) \\ & \text{Up} \end{aligned}$ 

Ordinary Least Squares (OLS) Linear Regression aka Ordinary Linear Regression Regression learns a function that maps a set of input data (independents) to one or more output variables (dependents). The resulting learned function is known as the model. That model can then be used repetitively to predict (i.e. estimate) the output value(s) based on new input data. Two major use cases are supported: 1) Learn and return a model 2) Use an existing (e.g. persisted) model to predict new values for Y Of course, both can be done in a single run. Alternatively, the model can be persisted and used indefinitely for prediction of Y values, as long as the record format has not changed, and the original training data remains representative of the population. OLS supports any number of independent variables (Multiple Regression) and multiple dependent variables (Multivariate Regression). In this way, multiple variables' values can be predicted from the same input (i.e. independent) data. Training data is presented as parameters to this module. When using a previously persisted model (use case 2 above), these parameters should be omitted. This module provides a rich set of analytics to assess the usefulness of the resulting linear regression model, and to determine the best subset of independent variables to include in the model. These include: For the whole model:

- Analysis of Variance (ANOVA) - R-squared - Adjusted R-squared - F-Test - Akaike Information Criterion (AIC) For each coefficient: - Standard Error (SE) - T-statistic - P-value - Confidence Interval

**Parameter**: X ||| The independent variable training data in DATASET(NumericField) format. Each observation (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number'). Omit this parameter when predicting from a persisted model.

**Parameter**: Y ||| The dependent variable training data in DATASET(NumericField) format. Each observation (e.g. record) is identified by 'id', and each feature is identified by field number. Omit this parameter when predicting from a persisted model.

- 1. GetModel
- 2. Betas
- 3. Predict
- 4. makeRSQ
- 5. RSquared
- 6. AnovaRec
- 7. calcAnova
- 8. Anova
- 9. **SE**
- 10. TStat
- 11. AdjRSquared
- 12. AICRec
- 13. AIC
- 14. RangeVec
- 15. DistributionBase
- 16. TDistribution
- 17. FDistribution
- 18. NormalDistribution
- 19. pVal
- 20. ConfintRec
- 21. ConfInt
- 22. FTestRec
- 23. FTest

#### attribute: GetModel

 $\begin{array}{lll} {\bf ATTRIBUTE: DATASET(Layout\_Model)~GetModel} \\ {\bf Up} \end{array}$ 

GetModel Returns the learned model that maps X's to Y's. In the case of OLS, the model represents a set of Betas which are the coefficients of the linear model: Beta0 \* 1 + Beta1 \* Field1 + Beta2 \* Field2 ... The ID of each model record specifies to which Y variable the coefficient applies. The Field Number ('number') indicates to which field of X the beta is to be applied. Field number 1 provides the intercept portion of the linear model and is always multiplied by 1. Note that if multiple work-items are provided within X and Y, there will be multiple models returned. The models can be separated by their work item id (i.e. 'wi'). A single model can be extracted from a myriad model by using e.g., model(wi=myWI\_id). GetModel should not be called when predicting using a previously persisted model (i.e. when training data was not passed to the module.

Return: Model in DATASET(Layout\_Model) format

See: ML\_core/Types.Layout\_Model

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

#### function: Betas

 $FUNCTION: DATASET(NumericField) \ Betas(DATASET(Layout\_Model) \ model=GetModel) \ Up$ 

Return raw Beta values as numeric fields Extracts Beta values from the model. Can be used during training and prediction phases. For use during training phase, the 'model' parameter can be omitted. Get-Model will be called to retrieve the model based on the training data. For use during prediction phase, a previously persisted model should be provided. The 'number' field of the returned NumericField records specifies to which Y the coefficient applies. The 'id' field of the returned record indicates the position of the Beta value. ID = 1 provides the Beta for the constant term (i.e. the Y intercept) while subsequent values reflect the Beta for each correspondingly numbered X feature. Feature 1 corresponds to Beta with 'id' = 2 and so on. If 'model' contains multiple work-items, Separate sets of Betas will be returned for each of the 'myriad' models (distinguished by 'wi').

**Parameter**: model ||| Optional parameter provides a model that was previously retrieved using GetModel. If omitted, GetModel will be used as the model.

**Return**: DATASET(NumericField) containing the Beta values.

#### function: Predict

 $FUNCTION: DATASET(NumericField) \ Predict(DATASET(NumericField) \ newX, DATASET(Layout\_Model) \\ model=GetModel) \\ Up$ 

Predict the dependent variable values (Y) for any set of independent variables (X). Returns a predicted Y values for each observation (i.e. record) of X. This supports the 'myriad' style interface in that multiple independent work items may be present in 'newX', and multiple independent models may be provided in 'model'. The resulting predicted values will also be separable by work item (i.e. wi).

**Parameter**: newX ||| The set of observations of independent variables in DATASET(NumericField) format. **Parameter**: model ||| Optional. A model that was previously returned from GetModel (above). Note that a model from a previous run will only be valid if the field numbers in X are the same as when the model was learned. If this parameter is omitted, the current model will be used.

**Return**: An estimation of the corresponding Y value for each observation of newX. Returned in DATASET(NumericField) format with field number (i.e. 'number') indicating the dependent variable that is predicted.

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

#### transform: makeRSQ

TRANSFORM : R2Rec makeRSQ(CoCoRec coco)Up

attribute: RSquared

 $\begin{array}{lll} {\rm ATTRIBUTE: DATASET(R2Rec) \ RSquared} \\ {\rm Up} \end{array}$ 

RSquared Calculate the R-Squared Metric used to assess the fit of the regression line to the training data. Since the regression has chosen the best (i.e. least squared error) line matching the data, this can be thought of as a measurement of the linearity of the training data. R Squared generally varies between 0 and 1, with 1 indicating an exact linear fit, and 0 indicating that a linear fit will have no predictive power. Negative values are possible under certain conditions, and indicate that the mean(Y) will be more predictive than any linear fit. Moderate values of R squared (e.g. .5) may indicate that the relationship of X -> Y is

non-linear, or that the measurement error is high relative to the linear correlation (e.g. many outliers). In the former case, increasing the dimensionality of X, such as by using polynomial variants of the features, may yield a better fit. R squared always increases when additional independent variables are added, so it should not be used to determine the optimal set of X variables to include. For that purpose, use Adjusted R Squared (below) which penalizes larger numbers of variables. Note that the result of this call is only meaningful during training phase (use case 1 above) as it is an analysis based on the training data which is not provided during a prediction-only phase.

**Return**: DATASET(R2Rec) with one record per dependent variable, per work-item. The number field indicates the dependent variable and coresponds to the number field of the dependent (Y) variable to which it applies.

#### record: AnovaRec

RECORD : AnovaRec

Up

#### transform: calcAnova

TRANSFORM: AnovaRec calcAnova(tmpRec le)

Up

#### attribute: Anova

ATTRIBUTE : Anova

Up

ANOVA (Analysis of Variance) report Analyzes the sources of variance. Basic ANOVA equality: Model + Error = Total Determines how much of the variance of Y is explained by the regression model, versus how much is due to the error term (i.e. unexplained variance). This attribute is only meaningful during the training phase. Provides one record per work-item. Each record provides the following statistics: - Total\_SS - Total Sum of Squares (SS) variance of the dependent data - Model\_SS - The SS variance represented within the model - Error\_SS - The SS variance not reflected by the model (i.e. Total\_SS - Error\_SS) - Total\_DF - The total degrees of freedom within the dependent data - Model\_DF - Degrees of freedom of the model - Error\_DF - Degrees of freedom of the error component - Total\_MS - The Mean Square (MS) variance of the dependent data - Model\_MS - The Mean Square (MS) variance represented within the model - Error\_MS - The MS variance not reflected by the model - Model\_F - The F-Test statistic: Model\_MS / Error\_MS

**Return**: DATASET(AnovaRec), one per work-item per dependent (Y) variable The number field indicates the dependent variable to which the analysis applies.

#### attribute: SE

ATTRIBUTE: DATASET(NumericField) SE

Up

Standard Error of the Regression Coefficients Describes the variability of the regression error for each coefficient. Only meaningful during the training phase.

**Return**: DATASET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The 'number' field indicates the dependent variable to which the coefficient applies.

attribute: TStat

 ${\bf ATTRIBUTE: DATASET(NumericField)\ TStat}$ 

Up

T-Statistic The T-statistic identifies the significance of the value of each regression coefficient. Its calculation is simply the value of the coefficient divided by the Standard Error of the coefficient. A larger absolute value of the T-statistic indicates that the coefficient is more significant. Only meaningful during the training phase.

**Return**: DATSET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable to which the coefficient applies.

### attribute: AdjRSquared

 $\begin{array}{lll} {\rm ATTRIBUTE:DATASET(R2Rec)\ AdjRSquared} \\ {\rm Up} \end{array}$ 

Adjusted R2 Calculate Adjusted R Squared which is a scaled version of R Squared that does not arbitrarily increase with the number of features. Adjusted R2, rather than R2 should always be used when trying to determine the best set of features to include in a model. When adding features, R2 will always increase, whether or not it improves the predictive power of the model. Adjusted R2, however, will only increase with the predictive power of the model.

**Return**: DATASET(R2Rec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

record: AICRec

RECORD : AICRec

Up

attribute: AIC

 $\begin{array}{l} {\rm ATTRIBUTE: DATASET(AICRec) \ AIC} \\ {\rm Up} \end{array}$ 

Akaike Information Criterion (AIC) Information theory based criterion for assessing Goodness of Fit (GOF). Lower values mean better fit.

**Return**: DATASET(AICRec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

record: RangeVec

RECORD: RangeVec

Up

module: DistributionBase

MODULE: DistributionBase(t Count Nranges = 10000)

- 1. Low
- 2. High
- 3. Density
- 4. RangeWidth
- 5. Density V
- 6. CumulativeV
- 7. Cumulative
- 8. NTile
- 9. InvDensity
- 10. Discrete

#### attribute: Low

 ${\bf ATTRIBUTE: Low}$ 

Up

# attribute: High

ATTRIBUTE : High

Up

#### function: Density

 $FUNCTION: t\_FieldReal\ Density(t\_FieldReal\ t)$ 

Up

### attribute: RangeWidth

 ${\bf ATTRIBUTE: RangeWidth}$ 

 $\operatorname{Up}$ 

# function: Density V

FUNCTION : DATASET(RangeVec) DensityV()

Up

#### function: CumulativeV

FUNCTION: CumulativeV()

```
function: Cumulative
```

 $\label{eq:function} \begin{aligned} & FUNCTION: t\_FieldReal \ Cumulative(t\_FieldReal \ t) \\ & Up \end{aligned}$ 

### function: NTile

 $\begin{array}{l} FUNCTION: t\_FieldReal\ NTile(t\_FieldReal\ Pc) \\ Up \end{array}$ 

#### function: InvDensity

 $\begin{array}{l} FUNCTION: InvDensity(t\_FieldReal\ delta) \\ Up \end{array}$ 

#### attribute: Discrete

ATTRIBUTE : Discrete

Up

#### module: TDistribution

 $\label{eq:module} \begin{aligned} & MODULE: TDistribution(t\_Discrete\ v\_in, t\_Count\ NRanges = 10000) \\ & \textbf{Up} \end{aligned}$ 

- 1. DensityV
- 2. NTile
- 3. Discrete
- 4. InvDensity
- 5. High
- 6. Low
- 7. RangeWidth
- 8. Density
- 9. CumulativeV
- 10. Cumulative

#### function: DensityV

 ${\bf FUNCTION: DATASET(RangeVec)\ DensityV()}$ 

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

function: NTile

 $FUNCTION: t\_FieldReal\ NTile(t\_FieldReal\ Pc)$ 

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

attribute: Discrete

 ${\bf ATTRIBUTE: Discrete}$ 

Up

 $\mathbf{INHERITED}: \mathbf{True}$ 

function: InvDensity

 $FUNCTION: InvDensity(t\_FieldReal\ delta)$ 

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

attribute: High

 ${\bf ATTRIBUTE: High}$ 

 $\operatorname{Up}$ 

**OVERRIDE**: True

attribute: Low

ATTRIBUTE : Low

Up

 $\mathbf{INHERITED}: \mathbf{True}$ 

attribute: RangeWidth

 ${\bf ATTRIBUTE: RangeWidth}$ 

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

function: Density

 $FUNCTION: t\_FieldReal\ Density(t\_FieldReal\ t)$ 

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

```
function: CumulativeV
FUNCTION: CumulativeV()
Up
   \mathbf{OVERRIDE}: \mathbf{True}
function: Cumulative
FUNCTION: t\_FieldReal\ Cumulative (t\_FieldReal\ t)
Up
   \mathbf{OVERRIDE}: \mathbf{True}
module: FDistribution
MODULE : FDistribution(t_Discrete d1_in, t_Discrete d2_in, t_Count NRanges = 10000)
Up
  1. DensityV
  2. CumulativeV
  3. Cumulative
  4. NTile
  5. InvDensity
  6. Discrete
  7. Low
  8. High
  9. RangeWidth
 10. Density
function: DensityV
FUNCTION: DATASET(RangeVec)\ DensityV()
Up
   \mathbf{OVERRIDE}: \mathrm{True}
function: CumulativeV
FUNCTION: CumulativeV()
Up
```

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

function: Cumulative

 $FUNCTION: t\_FieldReal\ Cumulative (t\_FieldReal\ t)$ 

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

function: NTile

 $FUNCTION: t\_FieldReal\ NTile(t\_FieldReal\ Pc)$ 

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

 ${\bf function: InvDensity}$ 

 $FUNCTION: InvDensity(t\_FieldReal\ delta)$ 

Up

INHERITED: True

attribute: Discrete

ATTRIBUTE : Discrete

Up

INHERITED: True

attribute: Low

ATTRIBUTE : Low

Up

 $\mathbf{INHERITED}: \mathrm{True}$ 

attribute: High

ATTRIBUTE : High

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

attribute: RangeWidth

ATTRIBUTE : RangeWidth

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

# function: Density

 $FUNCTION: t\_FieldReal\ Density(t\_FieldReal\ t)$ 

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

#### module: NormalDistribution

 $\begin{array}{l} MODULE: Normal Distribution(t\_Count\ NRanges) \\ Up \end{array}$ 

- 1. Low
- 2. High
- 3. RangeWidth
- 4. DensityV
- 5. CumulativeV
- 6. Cumulative
- 7. NTile
- 8. InvDensity
- 9. Discrete
- 10. Density

#### attribute: Low

ATTRIBUTE : Low

Up

INHERITED: True

attribute: High

ATTRIBUTE: High

Up

INHERITED: True

attribute: RangeWidth

 ${\bf ATTRIBUTE: RangeWidth}$ 

Up

 $\mathbf{OVERRIDE}: \mathbf{True}$ 

```
function: DensityV
FUNCTION: DATASET(RangeVec) DensityV()
Up
   \mathbf{OVERRIDE}: \mathbf{True}
function: CumulativeV
FUNCTION: CumulativeV()
Up
   \mathbf{OVERRIDE}: \mathbf{True}
function: Cumulative
FUNCTION: t\_FieldReal\ Cumulative (t\_FieldReal\ t)
Up
   \mathbf{OVERRIDE}: \mathbf{True}
function: NTile
FUNCTION: t\_FieldReal\ NTile(t\_FieldReal\ Pc)
Up
   OVERRIDE: True
function: InvDensity
FUNCTION: InvDensity(t\_FieldReal\ delta)
Up
   INHERITED: True
attribute: Discrete
ATTRIBUTE : Discrete
Up
   INHERITED: True
function: Density
FUNCTION: t\_FieldReal\ Density(t\_FieldReal\ t)
```

Up

 $\mathbf{OVERRIDE}: \mathrm{True}$ 

attribute : pVal

ATTRIBUTE : pVal

Up

P-Value Calculate the P-value for each coefficient, which is the probability that the coefficient is insignificant (i.e. actually zero). A low P-value (e.g. .05) provides evidence that the coefficient is significant in the model. A high P-value indicates that the coefficient value should, in fact, be zero. P-value is related to the T-Statistic, and can be thought of as a normalized version of the T-Statistic. Only meaningful during the training phase.

**Return**: DATSET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

record: ConfintRec

RECORD : ConfintRec

Up

function: ConfInt

 $FUNCTION: ConfInt(Types.t\_fieldReal\ level)$ 

Up

Confidence Interval The Confidence Interval determines the upper and lower bounds of each estimated coefficient given a confidence level (level) that is required. For example, one could say that there is a 95% probability (level) that the coefficient of the first independent variable is between 2.05 and 3.62. This allows error margins to be determined with the desired confidence level. If the confidence interval spans zero, it implies that the coefficient may not be significant at the specified confidence level.

Parameter: level ||| The level of confidence required, expressed as a percentage from 0.0 to 100.0

**Return**: DATASET(ConfintRec) with one record per coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

record: FTestRec

RECORD : FTestRec

Up

attribute: FTest

ATTRIBUTE: DATASET(FTestRec) FTest

Up

F-Test Calculate the P-value for the full regression, which is the probability that all of the coefficients are insignificant (i.e. actually zero). A low P-value (e.g. .05) provides evidence that at least one coefficient is significant. A high P-value indicates that all the coefficient values should in fact be zero, implying that the regression has no statistically significant predictive power. P-value is related to the ANOVA F-Statistic, and can be thought of as a standardized version of the ANOVA F-Statistic. The F-Test and T-Test are

similar, except that the T-test is used to test the significance of each coefficient, while the F-Test is used to test the significance of the entire regression. For simple linear regression (i.e. only one independent variable, the T-Test and F-Test are equivalent.

**Return**: DATASET(FTestRec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

# **PBblas**

Name: PBblas Version: 3.0.1 Description: Parallel Block Basic Linear Algebra Subsystem License: http://www.apache.org/licenses/LICENSE-2.0 Copyright: Copyright (C) 2016, 2017 HPCC Systems Authors: HPCCSystems DependsOn: ML Core Platform: 6.2.0

#### Table of Contents

file: ExtractTri.ecl Extract the upper or lower triangle from the composite output from getrf (LU Factorization)

file: Types.ecl Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes

file: tran.ecl Transpose a matrix and sum into base matrix

file: MatUtils.ecl Provides various utility attributes for manipulating cell-based matrixes

file : gemm.ecl Extended Parallel Block Matrix Multiplication Module Implements: Result = alpha \* op(A)op(B) + beta \* C

file : getrf.ecl LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks

file: Constants.ecl

file: axpy.ecl Implements alpha\*X + Y

file: Converted.ecl Module to convert between ML\_Core/Types Field layouts (i.e

file: HadamardProduct.ecl Element-wise multiplication of X \* Y

file: Apply2Elements.ecl Apply a function to each element of the matrix Use PBblas.IElementFunc as the prototype function

file: IElementFunc.ecl Function prototype for a function to apply to each element of the

file: potrf.ecl Implements Cholesky factorization of  $A = U^{**}T^{*}U$  if Triangular. Upper requested or  $A = L^{**}T$  if Triangular. Lower is requested

file: asum.ecl Absolute sum - the "Entrywise" 1-norm

file: trsm.ecl Partitioned block parallel triangular matrix solver

file: scal.ecl Scale a matrix by a constant Result is alpha \* X This supports a "myriad" style interface in

that X may be a set of independent matrices separated by different work-item ids

file: Vector2Diag.ecl Convert a vector into a diagonal matrix

# PBblas.ExtractTri

### **IMPORTS**

- PBblas
- $\bullet$  std.BLAS
- PBblas.Types
- PBblas.internal
- ullet PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted

#### DESCRIPTIONS

function: ExtractTri

 $FUNCTION: DATASET(Layout\_Cell) \ ExtractTri(Triangle \ tri, \ Diagonal \ dt, \ DATASET(Layout\_Cell) \ A) \\ Up$ 

Extract the upper or lower triangle from the composite output from getrf (LU Factorization).

 $\begin{array}{l} \textbf{Parameter}: \ tri \ ||| \ Triangle \ type: \ Upper \ or \ Lower \ (see \ Types.Triangle) \\ \textbf{Parameter}: \ dt \ ||| \ Diagonal \ type: \ Unit \ or \ non \ unit \ (see \ Types.Diagonal) \end{array}$ 

Parameter : A || Matrix of cells. See Types.Layout\_Cell

Return: Matrix of cells in Layout\_Cell format representing a triangular matrix (upper or lower)

 $\mathbf{See}: \mathbf{Std.PBblas.Types}$ 

# PBblas.Types

### **IMPORTS**

- ML\_Core
- $\bullet \ \mathrm{ML\_Core.Types}$

# **DESCRIPTIONS**

 $\begin{array}{ll} \mathbf{module: Types} \\ \mathbf{MODULE: Types} \\ \mathbf{Up} \end{array}$ 

Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes.

```
    dimension_t
    partition_t
    work_item_t
    value_t
    m_label_t
    Triangle
    Diagonal
    Side
    t_mu_no
    Layout_Cell
    Layout_Norm
    attribute: dimension_t
```

ATTRIBUTE : dimension\_t

Up

Type for matrix dimensions. Uses UNSIGNED four as matrixes are not designed to support more than 4 B rows or columns.

```
attribute: partition t
ATTRIBUTE : partition_t
Up
  Type for partition id – only supports up to 64K partitions
attribute: work item t
ATTRIBUTE : work\_item\_t
Up
  Type for work-item id – only supports up to 64K work items
attribute: value_t
ATTRIBUTE: value\_t
Up
  Type for matrix cell values WARNING: type used in C++ attribute
attribute: m label t
ATTRIBUTE : m_label_t
Up
  Type for matrix label. Used for Matrix dimensions (see Layout_Dims) and for partitions (see Lay-
out Part)
attribute: Triangle
ATTRIBUTE: Triangle
Up
  Enumeration for Triangle type WARNING: type used in C++ attribute
attribute: Diagonal
ATTRIBUTE: Diagonal
Up
  Enumeration for Diagonal type WARNING: type used in C++ attribute
attribute: Side
ATTRIBUTE: Side
Up
```

Enumeration for Side type WARNING: type used in C++ attribute

attribute : t\_mu\_no
ATTRIBUTE : t\_mu\_no

Up

Type for matrix universe number Allow up to 64k matrices in one universe

record: Layout Cell

 $\begin{array}{l} {\rm RECORD: Layout\_Cell} \\ {\rm \bf Up} \end{array}$ 

Layout for Matrix Cell Main representation of Matrix cell at interface to all PBBlas functions. Matrixes are represented as DATASET(Layout\_Cell), where each cell describes the row and column position of the cell as well as its value. Only the non-zero cells need to be contained in the dataset in order to describe the matrix since all unspecified cells are considered to have a value of zero. The cell also contains a work-item number that allows multiple separate matrixes to be carried in the same dataset. This supports the "myriad" style interface that allows the same operations to be performed on many different sets of data at once. Note that these matrixes do not have an explicit size. They are sized implicitly, based on the maximum row and column presented in the data. A matrix can be converted to an explicit dense form (see matrix\_t) by using the utility module MakeR8Set. This module should only be used for known small matrixes (< 1M cells) or for partitions of a larger matrix. The Converted module provides utility functions to convert to and from a set of partitions (See Layout parts).

Field: wi\_id || Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

**Field**:  $x \parallel \parallel 1$ -based row position within the matrix **Field**:  $y \parallel \parallel 1$ -based column position within the matrix

Field: v | | | Real value for the cell

 $See : matrix\_t$ 

See: Std/PBblas/MakeR8Set.ecl

See: Std/PBblas/Converted.ecl WARNING: Used as C++ attribute. Do not change without corresponding changes to MakeR8Set.

record : Layout\_Norm

 $RECORD : Layout\_Norm Up$ 

Layout for Norm results.

Field: wi\_id ||| Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

Field: v ||| Real value for the norm

# PBblas.tran

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.BLAS
- std.system.Thorlib

# **DESCRIPTIONS**

function: tran

FUNCTION : DATASET(Layout\_Cell) tran(value\_t alpha, DATASET(Layout\_Cell) A, value\_t beta=0, DATASET(Layout\_Cell) C=empty\_c) Up

Transpose a matrix and sum into base matrix result  $\leq$  = alpha \* A\*\*t + beta \* C, A is n by m, C is m by n A\*\*T (A Transpose) and C must have same shape

Parameter: A ||| A matrix in DATASET(Layout\_Cell) form

 $\begin{array}{l} \textbf{Parameter}: \ beta \ ||| \ Scalar \ multiplier \ for \ the \ C \ matrix \\ \textbf{Parameter}: \ C \ ||| \ C \ matrix \ in \ DATASET(Layout\_Call) \ form \end{array}$ 

Return: Matrix in DATASET(Layout\_Cell) form alpha \* A\*\*T + beta \* C

 $\mathbf{See}: \mathrm{PBblas/Types.layout\_cell}$ 

# PBblas.MatUtils

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims

#### **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: MatUtils} \\ \mathbf{MODULE: MatUtils} \\ \mathbf{Up} \end{array}$ 

Provides various utility attributes for manipulating cell-based matrixes  $\bf See: Std/PBblas/Types.Layout\_Cell$ 

- 1. GetWorkItems
- 2. InsertCols
- 3. Transpose

#### function: GetWorkItems

 $FUNCTION: DATASET(Layout\_WI\_ID) \ GetWorkItems(DATASET(Layout\_Cell) \ cells) \ Up$ 

Get a list of work-item ids from a matrix containing one or more work items

Parameter: cells || A matrix in Layout Cell format

Return: DATASET(Layout\_WI\_ID), one record per work-item

See: PBblas/Types.Layout\_Cell See: PBblas/Types.Layout\_WI\_ID

#### function: InsertCols

 $FUNCTION: DATASET(Layout\_Cell) \ InsertCols(DATASET(Layout\_Cell) \ M, \ UNSIGNED \ cols\_to\_insert=1, \\ value\_t \ insert\_val=1) \\ Up$ 

Insert one or more columns of a fixed value into a matrix. Columns are inserted before the first original column. This attribute supports the myriad interface. Multiple independent matrixes can be represented by  $\mathbf{M}$ 

 $\mathbf{Parameter}: \mathbf{M} \mid\mid\mid \mathbf{the} \ \mathbf{input} \ \mathbf{matrix}$ 

Parameter: cols\_to\_insert ||| the number of columns to insert, default 1

**Parameter**: insert val ||| the value for each cell of the new column(s), default 0

Return: matrix in Layout Cell format with additional column(s)

#### function: Transpose

 $FUNCTION: DATASET(Layout\_Cell) \ Transpose(DATASET(Layout\_Cell) \ M) \ Up$ 

Transpose a matrix This attribute supports the myriad interface. Multiple independent matrixes can be represented by M.

Parameter: M ||| A matrix represented as DATASET(Layout\_Cell)

Return: Transposed matrix in Layout\_Cell format

 $\mathbf{See}: \ PBblas/Types.Layout\_Cell$ 

# PBblas.gemm

#### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- std.BLAS
- PBblas.internal.MatDims
- std.system.Thorlib

#### **DESCRIPTIONS**

#### function: gemm

 $FUNCTION: DATASET(Layout\_Cell) \ gemm(BOOLEAN \ transposeA, BOOLEAN \ transposeB, value\_t \ alpha, DATASET(Layout\_Cell) \ A_in, DATASET(Layout\_Cell) \ B_in, DATASET(Layout\_Cell) \ C_in=emptyC, value\_t \ beta=0.0) \ Up$ 

Extended Parallel Block Matrix Multiplication Module Implements: Result = alpha \* op(A)op(B) + beta \* C. op is No Transpose or Transpose. Multiplies two matrixes A and B, with an optional pre-multiply transpose for each Optionally scales the product by the scalar "alpha". Then adds an optional C matrix to the product after scaling C by the scalar "beta". A, B, and C are specified as DATASET(Layout\_Cell), as is the Resulting matrix. Layout\_Cell describes a sparse matrix stored as a list of x, y, and value. This interface also provides a "Myriad" capability allowing multiple similar operations to be performed on independent sets of matrixes in parallel. This is done by use of the work-item id (wi\_id) in each cell of the matrixes. Cells with the same wi\_id are considered part of the same matrix. In the myriad form, each input matrix A, B, and (optionally) C can contain many independent matrixes. The wi\_ids are matched up such that each operation involves the A, B, and C with the same wi\_id. A and B must therefore contain the same set of wi\_ids, while C is optional for any wi\_id. The same parameters: alpha, beta, transposeA, and transposeB are used for all work-items. The result will contain cells from all provided work-items. Result has same shape as C if provided. Note that matrixes are not explicitly dimensioned. The shape is determined by the highest value of x and y for each work-item.

Parameter: transposeA ||| Boolean indicating whether matrix A should be transposed before multiplying

Parameter: transposeB ||| Same as above but for matrix B Parameter: alpha ||| Scalar multiplier for alpha \* A \* B

**Parameter**: A\_in ||| 'A' matrix (multiplier) in Layout\_Cell format **Parameter**: B\_in ||| Same as above for the 'B' matrix (multiplicand)

Parameter: C\_in || Same as above for the 'C' matrix (addend). May be omitted.

 $\label{eq:parameter:def} \textbf{Parameter}: beta \mid\mid\mid A \ scalar \ multiplier \ for \ beta \ ^*C, \ scales \ the \ C \ matrix \ before \ addition. \ May be omitted. \\ \textbf{Return}: \ Result \ matrix \ in \ Layout\_Cell \ format.$ 

See: PBblas/Types.Layout\_Cell

# PBblas.getrf

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- std.BLAS
- PBblas.internal.MatDims
- std.system.Thorlib

#### **DESCRIPTIONS**

function: getrf

 $\label{eq:function} FUNCTION: DATASET(Layout\_Cell) \ getrf(DATASET(Layout\_Cell) \ A) \\ Up$ 

LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks. Iterates through the matrix a row of blocks and column of blocks at a time. Partition A into M block rows and N block columns. The A11 cell is a single block. A12 is a single row of blocks with N-1 columns. A21 is a single column of blocks with M-1 rows. A22 is a sub-matrix of M-1 x N-1 blocks. L21\*U12 + L22\*U22 | Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi id). Note: The returned matrix includes both the upper and lower factors. This matrix can be used directly by trsm which will only use the part indicated by trsm's 'triangle' parameter (i.e. upper or lower). To extract the upper or lower triangle explicitly for other purposes, use the ExtractTri function. When passing the Lower matrix to the triangle solver (trsm), set the "Diagonal" parameter to "UnitTri". This is necessary because both triangular matrixes returned from this function are packed into a square matrix with only one diagonal. By convention, The Lower triangle is assumed to be a Unit Triangle (diagonal all ones), so the diagonal contained in the returned matrix is for the Upper factor and must be ignored (i.e. assumed to be all ones) when referencing the Lower triangle.

Parameter: A ||| The input matrix in Types.Layout\_Cell format

Return: Resulting factored matrix in Layout\_Cell format

See: Types.Layout Cell

See : ExtractTri

# PBblas.Constants

# **IMPORTS**

# **DESCRIPTIONS**

 $\begin{array}{l} \mathbf{module: Constants} \\ \mathbf{MODULE: Constants} \\ \mathbf{Up} \end{array}$ 

- 1. Block\_Minimum
- 2. Block\_NoSplit
- 3. Block\_Maximum
- 4. Block\_Vec\_Rows
- 5. Dimension\_Incompat
- ${\bf 6. \ Dimension\_IncompatZ}$
- 7. Distribution Error
- 8. Distribution\_ErrorZ
- 9. Not\_Square
- 10. Not\_SquareZ
- 11. Not\_PositiveDef
- 12. Not\_PositiveDefZ
- 13. Not\_Single\_Block
- 14. Not\_Single\_BlockZ
- 15. Not\_Block\_Vector
- 16. Not\_Block\_VectorZ

attribute : Block\_Minimum

 $ATTRIBUTE: Block\_Minimum$ 

attribute: Block NoSplit

 $ATTRIBUTE: Block\_NoSplit$ 

Up

 $attribute: Block\_Maximum$ 

 $ATTRIBUTE: Block\_Maximum$ 

Up

attribute: Block\_Vec\_Rows

ATTRIBUTE : Block Vec Rows

Up

attribute: Dimension\_Incompat

 $ATTRIBUTE: Dimension\_Incompat$ 

Up

attribute: Dimension\_IncompatZ

 $ATTRIBUTE: Dimension\_IncompatZ$ 

Up

attribute: Distribution\_Error

 $ATTRIBUTE: Distribution\_Error$ 

Up

attribute: Distribution\_ErrorZ

 $ATTRIBUTE: Distribution\_ErrorZ$ 

Up

attribute: Not\_Square

ATTRIBUTE : Not\_Square

Up

attribute: Not\_SquareZ

 $ATTRIBUTE: Not\_SquareZ$ 

 $attribute: Not\_PositiveDef$ 

 ${\tt ATTRIBUTE: Not\_PositiveDef}$ 

Up

 $attribute: Not\_PositiveDefZ$ 

 $ATTRIBUTE: Not\_PositiveDefZ$ 

Up

 $attribute: Not\_Single\_Block$ 

 $ATTRIBUTE: Not\_Single\_Block$ 

Up

attribute: Not\_Single\_BlockZ

 $ATTRIBUTE: Not\_Single\_BlockZ$ 

Up

 $attribute: Not\_Block\_Vector$ 

 $ATTRIBUTE: Not\_Block\_Vector$ 

Up

attribute: Not\_Block\_VectorZ

 $ATTRIBUTE: Not\_Block\_VectorZ$ 

# PBblas.axpy

# **IMPORTS**

- PBblas
- PBblas.Types

# **DESCRIPTIONS**

```
function: axpy
```

 $FUNCTION: DATASET(Layout\_Cell) \ axpy(value\_t \ alpha, DATASET(Layout\_Cell) \ X, DATASET(Layout\_Cell) \ Y) \\ Up$ 

$$\label{eq:local_state} \begin{split} & \textbf{Parameter}: \ alpha^*X + Y \ X \ and \ Y \ must \ have \ same \ shape \\ & \textbf{Parameter}: \ alpha \ ||| \ Scalar \ multiplier \ for \ the \ X \ matrix \\ & \textbf{Parameter}: \ X \ ||| \ X \ matrix \ in \ DATASET(Layout\_Cell) \ form \\ & \textbf{Parameter}: \ Y \ ||| \ Y \ matrix \ in \ DATASET(Layout\_Call) \ form \end{split}$$

Return: Matrix in DATASET(Layout\_Cell) form

 $\mathbf{See}: \mathrm{PBblas}/\mathrm{Types.layout\_cell}$ 

# PBblas.Converted

### **IMPORTS**

- PBblas
- PBblas.Types
- $\bullet$  ML\_Core.Types

#### **DESCRIPTIONS**

module : Converted

MODULE : Converted

Up

Module to convert between ML\_Core/Types Field layouts (i.e. NumericField and DiscreteField) and PBblas matrix layout (i.e. Layout\_Cell)

- 1. NFToMatrix
- 2. DFToMatrix
- 3. MatrixToNF
- 4. MatrixToDF

function: NFToMatrix

 $FUNCTION: DATASET(Layout\_Cell) \ NFToMatrix(DATASET(NumericField) \ recs) \\ Up$ 

Convert NumericField dataset to Matrix

Parameter: recs ||| Record Dataset in DATASET(NumericField) format

Return: Matrix in DATASET(Layout\_Cell) format

See: PBblas/Types.Layout\_Cell See: ML Core/Types.NumericField

function: DFToMatrix

FUNCTION: DATASET(Layout\_Cell) DFToMatrix(DATASET(DiscreteField) recs)

Convert DiscreteField dataset to Matrix

Parameter: recs || Record Dataset in DATASET(DiscreteField) format

Return: Matrix in DATASET(Layout\_Cell) format

See: PBblas/Types.Layout\_Cell See: ML\_Core/Types.DiscreteField

#### function: MatrixToNF

 $FUNCTION: DATASET(NumericField) \ MatrixToNF(DATASET(Layout\_Cell) \ mat) \\ Up$ 

Convert Matrix to NumericField dataset

Parameter: mat || Matrix in DATASET(Layout Cell) format

Return: NumericField Dataset
See: PBblas/Types.Layout\_Cell
See: ML\_Core/Types.NumericField

#### function: MatrixToDF

 $FUNCTION: DATASET(DiscreteField) \ MatrixToDF(DATASET(Layout\_Cell) \ mat) \\ Up$ 

Convert Matrix to DiscreteField dataset

Parameter: mat || Matrix in DATASET(Layout\_Cell) format

Return : DiscreteField Dataset See : PBblas/Types.Layout\_Cell See : ML\_Core/Types.DiscreteField

# PBblas.HadamardProduct

### **IMPORTS**

- PBblas
- PBblas.internal
- PBblas.internal.MatDims
- PBblas.Types
- PBblas.internal.Types
- PBblas.internal.Converted
- std.BLAS
- std.system.Thorlib

# **DESCRIPTIONS**

function: HadamardProduct

 $FUNCTION: DATASET(Layout\_Cell) \ HadamardProduct(DATASET(Layout\_Cell) \ X, DATASET(Layout\_Cell) \ Y) \\ Up$ 

Element-wise multiplication of X \* Y. Supports the "myriad" style interface – X and Y may contain multiple separate matrixes. Each X will be multiplied by the Y with the same work-item id. Note: This performs element-wise multiplication. For dot-product matrix multiplication, use PBblas.gemm.

Parameter: X ||| A matrix (or multiple matrices) in Layout\_Cell form Parameter: Y ||| A matrix (or multiple matrices) in Layout\_Cell form

Return : A matrix (or multiple matrices) in Layout\_Cell form

See: PBblas/Types.Layout\_Cell

# PBblas.Apply2Elements

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS

# **DESCRIPTIONS**

function: Apply2Elements

 $FUNCTION: DATASET(Layout\_Cell) \ Apply2Elements(DATASET(Layout\_Cell) \ X, \ IElementFunc \ f) \ Up$ 

Apply a function to each element of the matrix Use PBblas. IElementFunc as the prototype function.

Input and ouput may be a single matrix, or myriad matrixes with different work item ids.

 $\label{eq:parameter: X | | A matrix (or multiple matrices) in Layout\_Cell form \\ \textbf{Parameter}: f | | | A function based on the IElementFunc prototype \\ \textbf{Return}: A matrix (or multiple matrices) in Layout\_Cell form \\ \end{aligned}$ 

See: PBblas/IElementFunc See: PBblas/Types.Layout\_Cell

# PBblas.IElementFunc

# **IMPORTS**

• PBblas

# **DESCRIPTIONS**

function: IElementFunc

 $FUNCTION: value\_t \ IElementFunc(value\_t \ v, \ dimension\_t \ r, \ dimension\_t \ c) \\ Up$ 

Function prototype for a function to apply to each element of the distributed matrix Base your function on this prototype:

 $\mathbf{Parameter}: \mathbf{v} \mid\mid\mid \mathbf{Input} \ \mathbf{value}$ 

Parameter: r ||| Row number (1 based)
Parameter: c ||| Column number (1 based)

Return: Output value

 ${f See}: {f PBblas/Apply2Elements}$ 

# PBblas.potrf

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.system.Thorlib

# **DESCRIPTIONS**

function: potrf

 $FUNCTION: DATASET(Layout\_Cell) \ potrf(Triangle \ tri, \ DATASET(Layout\_Cell) \ A\_in) \\ Up$ 

Implements Cholesky factorization of  $A = U^{**}T^*U$  if Triangular. Upper requested or  $A = L^*L^{**}T$  if Triangular. Lower is requested. The matrix A must be symmetric positive definite.

```
 \begin{array}{l} \mid \text{A11 A12} \mid \mid \text{L11 0} \mid \mid \text{L11**T L21**T} \mid \\ \mid \text{A21 A22} \mid == \mid \text{L21 L22} \mid * \mid \text{0 L22} \mid \\ \mid \text{L11*L11**T L11*L21**T} \mid \\ == \mid \text{L21*L11**T L21*L21**T} + \text{L22*L22**T} \mid \\ \end{array}
```

So, use Cholesky on the first block to get L11. L21 = A21\*L11\*\* $T^{**}$ -1 which can be found by dtrsm on each column block A22' is A22 - L21\* $L21^{**}$ T

Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra

This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi id).

**Parameter** : tri ||| Types.Triangle enumeration indicating whether we are looking for the Upper or the Lower factor

Parameter: A in || The matrix or matrixes to be factored in Types.Layout Cell format

Return: Triangular matrix in Layout\_Cell format See: Std.PBblas.Types.Layout\_Cell See: Std.PBblas.Types.Triangle

# PBblas.asum

# **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- $\bullet$  PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- $\bullet$  std.BLAS

# **DESCRIPTIONS**

function: asum

 $\label{eq:function} FUNCTION: DATASET(Layout\_Norm) \ asum(DATASET(Layout\_Cell) \ X) \\ Up$ 

Absolute sum – the "Entrywise" 1-norm Compute SUM(ABS(X)) **Parameter**:  $X \parallel \parallel Matrix$  or set of matrices in Layout\_Cell format **Return**: DATASET(Layout\_Norm) with one record per work item

 $\mathbf{See}: \mathrm{PBblas}/\mathrm{Types}.\mathrm{Layout}\_\mathrm{Cell}$ 

# PBblas.trsm

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.system.Thorlib

### **DESCRIPTIONS**

function: trsm

FUNCTION : DATASET(Layout\_Cell) trsm(Side s, Triangle tri, BOOLEAN transposeA, Diagonal diag, value\_t alpha, DATASET(Layout\_Cell) A\_in, DATASET(Layout\_Cell) B\_in)
Up

Partitioned block parallel triangular matrix solver. Solves for X using: AX = B or XA = B A is is a square triangular matrix, X and B have the same dimensions. A may be an upper triangular matrix (UX = B or XU = B), or a lower triangular matrix (LX = B or XL = B). Allows optional transposing and scaling of A. Partially based upon an approach discussed by MJ DAYDE, IS DUFF, AP CERFACS. A Parallel Block implementation of Level-3 BLAS for MIMD Vector Processors ACM Tran. Mathematical Software, Vol 20, No 2, June 1994 pp 178-193 and other papers about PB-BLAS by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. Corresponding A and B matrixes are related by a common work-item identifier (wi\_id) within each cell of the matrix. The returned X matrix will contain cells for the same set of work-items as specified for the A and B matrices.

Parameter: s \$|||\$ Types. Side enumeration indicating whether we are solving AX = B or XA = B

 $\textbf{Parameter}: \ tri \ ||| \ Types. Triangle \ enumeration \ indicating \ whether \ we \ are \ solving \ an \ Upper \ or \ Lower \ triangle.$ 

Parameter: transpose A ||| Boolean indicating whether or not to transpose the A matrix before solving Parameter: diag ||| Types. Diagonal enumeration indicating whether A is a unit matrix or not. This is primarily used after factoring matrixes using getrf (LU factorization). That module produces a factored matrix stored within the same space as the original matrix. Since the diagonal is used by both factors, by convention, the Lower triangle has a unit matrix (diagonal all 1's) while the Upper triangle uses the diagonal cells. Setting this to UnitTri, causes the contents of the diagonal to be ignored, and assumed to be 1. NotUnitTri should be used for most other cases.

 $\mathbf{Parameter}:$ alpha ||| Multiplier to scale A

Parameter : A\_in ||| The A matrix in Layout\_Cell format Parameter : B\_in ||| The B matrix in Layout\_Cell format

 ${\bf Return}:$  X solution matrix in Layout\_Cell format

 $\begin{tabular}{ll} \bf See: Types.Layout\_Cell\\ \bf See: Types.Triangle\\ \bf See: Types.Side \end{tabular}$ 

# PBblas.scal

# **IMPORTS**

- PBblas
- PBblas.Types

# **DESCRIPTIONS**

function: scal

 $\label{eq:function} FUNCTION: DATASET(Layout\_Cell) \ scal(value\_t \ alpha, \ DATASET(Layout\_Cell) \ X) \\ Up$ 

Scale a matrix by a constant Result is alpha \* X This supports a "myriad" style interface in that X may be a set of independent matrices separated by different work-item ids.

Parameter : alpha ||| A scalar multiplier

Parameter: X ||| The matrix(es) to be scaled in Layout\_Cell format

**Return**: Matrix in Layout\_Cell form, of the same shape as X

 $\mathbf{See}: \mathrm{PBblas/Types.Layout\_Cell}$ 

# PBblas.Vector2Diag

### **IMPORTS**

- PBblas
- PBblas.internal
- PBblas.internal.MatDims
- PBblas.Types
- ullet PBblas.internal.Types
- PBblas.Constants

### **DESCRIPTIONS**

function: Vector2Diag

 $FUNCTION: DATASET(Layout\_Cell) \ Vector 2 Diag(DATASET(Layout\_Cell) \ X) \\ Up$ 

Convert a vector into a diagonal matrix. The typical notation is D = diag(V). The input X must be a 1 x N column vector or an N x 1 row vector. The resulting matrix, in either case will be N x N, with zero everywhere except the diagonal.

Parameter: X ||| A row or column vector (i.e. N x 1 or 1 x N) in Layout\_Cell format

Return : An N x N matrix in Layout\_Cell format

 ${\bf See}: {\bf PBblas/Types.Layout\_cell}$