# Root

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LinearRegression	
LogisticRegression	
ML_Core	
PBblas	

# LinearRegression

Name	LinearRegression
Version	3.0.0
Description	Linear Regression Algorithm Bundle
License	http://www.apache.org/licenses/LICENSE-2.0
Copyright	Copyright (C) 2017 HPCC Systems
Authors	HPCCSystems
DependsOn	ML_Core, PBblas
Platform	6.2.0

## **Table of Contents**

### OLS.ecl

Ordinary Least Squares (OLS) Linear Regression aka Ordinary Linear Regression Regression learns a function that maps a set of input data (independents) to one or more output variables (dependents)

# LinearRegression.OLS

### **IMPORTS**

- ML\_Core
- ML\_Core.Types
- PBblas
- PBblas.Types
- PBblas.Converted
- PBblas.MatUtils
- ML\_Core.Math

## **DESCRIPTIONS**

MODULE: OLS

OLS

(DATASET(NumericField) X=empty\_data, DATASET(NumericField) Y=empty\_data)

#### Up

Ordinary Least Squares (OLS) Linear Regression aka Ordinary Linear Regression Regression learns a function that maps a set of input data (independents) to one or more output variables (dependents). The resulting learned function is known as the model. That model can then be used repetitively to predict (i.e. estimate) the output value(s) based on new input data. Two major use cases are supported: 1) Learn and return a model 2) Use an existing (e.g. persisted) model to predict new values for Y Of course, both can be done in a single run. Alternatively, the model can be persisted and used indefinitely for prediction of Y values, as long as the record format has not changed, and the original training data remains representative of the population. OLS supports any number of independent variables (Multiple Regression) and multiple dependent variables (Multivariate Regression). In this way, multiple variables' values can be predicted from the same input (i.e. independent) data. Training data is presented as

parameters to this module. When using a previously persisted model (use case 2 above), these parameters should be omitted. This module provides a rich set of analytics to assess the usefulness of the resulting linear regression model, and to determine the best subset of independent variables to include in the model. These include: For the whole model: - Analysis of Variance (ANOVA) - R-squared - Adjusted R-squared - F-Test - Akaike Information Criterion (AIC) For each coefficient: - Standard Error (SE) - T-statistic - P-value - Confidence Interval

Parameter X ||| The independent variable training data in DATASET(NumericField) format. Each observation (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number'). Omit this parameter when predicting from a persisted model.

**Parameter** Y ||| The dependent variable training data in DATASET(NumericField) format. Each observation (e.g. record) is identified by 'id', and each feature is identified by field number. Omit this parameter when predicting from a persisted model.

GetModel | Betas | Predict | makeRSQ | RSquared | AnovaRec | calcAnova | Anova | SE | TStat | AdjRSquared | AICRec | AIC | RangeVec | DistributionBase | TDistribution | FDistribution | NormalDistribution | pVal | ConfintRec | ConfInt | FTestRec | FTest |

#### ATTRIBUTE: GetModel

DATASET(Layout_Model)	GetModel
-----------------------	----------

#### Up

GetModel Returns the learned model that maps X's to Y's. In the case of OLS, the model represents a set of Betas which are the coefficients of the linear model: Beta0 \* 1 + Beta1 \* Field1 + Beta2 \* Field2 ... The ID of each model record specifies to which Y variable the coefficient applies. The Field Number ('number') indicates to which field of X the beta is to be applied. Field number 1 provides the intercept portion of the linear model and is always multiplied by 1. Note that if multiple work-items are provided within X and Y, there will be multiple models returned. The models can be separated by their work item id (i.e. 'wi'). A single model can be extracted from a myriad model by using e.g., model(wi=myWI\_id). GetModel should not be called when predicting using a previously persisted model (i.e. when training data was not passed to the module.

Return Model in DATASET(Layout\_Model) format

See ML core/Types.Layout Model

**OVERRIDE** True

#### **FUNCTION**: Betas

DATASET(NumericField)	Betas
(DATASET(Layout_Model) model=GetModel)	

#### Up

Return raw Beta values as numeric fields Extracts Beta values from the model. Can be used during training and prediction phases. For use during training phase, the 'model' parameter can be omitted. GetModel will be called to retrieve the model based on the training data. For use during prediction phase, a previously persisted model should be provided. The 'number' field of the returned NumericField records specifies to which Y the coefficient applies. The 'id' field of the returned record indicates the position of the Beta value. ID = 1 provides the Beta for the constant term (i.e. the Y intercept) while subsequent values reflect the Beta for each correspondingly numbered X feature. Feature 1 corresponds to Beta with 'id' = 2 and so on. If 'model' contains multiple work-items, Separate sets of Betas will be returned for each of the 'myriad' models (distinguished by 'wi').

**Parameter** model ||| Optional parameter provides a model that was previously retrieved using GetModel. If omitted, GetModel will be used as the model.

Return DATASET(NumericField) containing the Beta values.

#### **FUNCTION**: Predict

DATASET(NumericField)   Predict	
(DATASET(NumericField) newX, DATASET(Layout_Model) model=GetModel)	

#### Up

Predict the dependent variable values (Y) for any set of independent variables (X). Returns a predicted Y values for each observation (i.e. record) of X. This supports the 'myriad' style interface in that multiple independent work items may be present in 'newX', and multiple independent models may be provided in 'model'. The resulting predicted values will also be separable by work item (i.e. wi).

Parameter newX ||| The set of observations of independent variables in DATASET(NumericField) format.

**Parameter** model ||| Optional. A model that was previously returned from GetModel (above). Note that a model from a previous run will only be valid if the field numbers in X are the same as when the model was learned. If this parameter is omitted, the current model will be used.

**Return** An estimation of the corresponding Y value for each observation of newX. Returned in DATASET(NumericField) format with field number (i.e. 'number') indicating the dependent variable that is predicted.

**OVERRIDE** True

### TRANSFORM: makeRSQ

R2Rec makeRSQ	makeRSQ
(CoCoRec coco)	

Up

### ATTRIBUTE: RSquared

DATASET(R2Rec)	RSquared
----------------	----------

Up

RSquared Calculate the R-Squared Metric used to assess the fit of the regression line to the training data. Since the regression has chosen the best (i.e. least squared error) line matching the data, this can be thought of as a measurement of the linearity of the training data. R Squared generally varies between 0 and 1, with 1 indicating an exact linear fit, and 0 indicating that a linear fit will have no predictive power. Negative values are possible under certain conditions, and indicate that the mean(Y) will be more predictive than any linear fit. Moderate values of R squared (e.g. .5) may indicate that the relationship of X -> Y is non-linear, or that the measurement error is high relative to the linear correlation (e.g. many outliers). In the former case, increasing the dimensionality of X, such as by using polynomial variants of the features, may yield a better fit. R squared always increases when additional independent variables are added, so it should not be used to determine the optimal set of X variables to include. For that purpose, use Adjusted R Squared (below) which penalizes larger numbers of variables. Note that the result of this call is only meaningful during training phase (use case 1 above) as it is an analysis based on the training data which is not provided during a prediction-only phase.

**Return** DATASET(R2Rec) with one record per dependent variable, per work-item. The number field indicates the dependent variable and coresponds to the number field of the dependent (Y) variable to which it applies.

#### RECORD: AnovaRec

	AnovaRec
Up	

#### TRANSFORM: calcAnova

AnovaRec	calcAnova
(tmpRec le)	

Up

#### ATTRIBUTE: Anova

Anova	
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#### Up

ANOVA (Analysis of Variance) report Analyzes the sources of variance. Basic ANOVA equality: Model + Error = Total Determines how much of the variance of Y is explained by the regression model, versus how much is due to the error term (i.e. unexplained variance). This attribute is only meaningful during the training phase. Provides one record per work-item. Each record provides the following statistics: - Total\_SS - Total Sum of Squares (SS) variance of the dependent data - Model\_SS - The SS variance represented within the model - Error\_SS - The SS variance not reflected by the model (i.e. Total\_SS - Error\_SS) - Total\_DF - The total degrees of freedom within the dependent data - Model\_DF - Degrees of freedom of the model - Error\_DF - Degrees of freedom of the error component - Total\_MS - The Mean Square (MS) variance of the dependent data - Model\_MS - The Mean Square (MS) variance represented within the model - Error\_MS - The MS variance not reflected by the model - Model\_F - The F-Test statistic: Model\_MS / Error\_MS

**Return** DATASET(AnovaRec), one per work-item per dependent (Y) variable The number field indicates the dependent variable to which the analysis applies.

#### ATTRIBUTE: SE

DATASET(NumericField)	SE
-----------------------	----

#### Up

Standard Error of the Regression Coefficients Describes the variability of the regression error for each coefficient. Only meaningful during the training phase.

**Return** DATASET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The 'number' field indicates the dependent variable to which the coefficient applies.

#### ATTRIBUTE: TStat

DATASET(NumericField)	TStat
-----------------------	-------

#### Up

T-Statistic The T-statistic identifies the significance of the value of each regression coefficient. Its calculation is simply the value of the coefficient divided by the Standard Error of the coefficient. A larger absolute value of the T-statistic indicates that the coefficient is more significant. Only meaningful during the training phase.

**Return** DATSET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable to which the coefficient applies.

### ATTRIBUTE: AdjRSquared

DATASET(R2Rec)
----------------

Adjusted R2 Calculate Adjusted R Squared which is a scaled version of R Squared that does not arbitrarily increase with the number of features. Adjusted R2, rather than R2 should always be used when trying to determine the best set of features to include in a model. When adding features, R2 will always increase, whether or not it improves the predictive power of the model. Adjusted R2, however, will only increase with the predictive power of the model.

**Return** DATASET(R2Rec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

#### RECORD: AICRec

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Up

#### ATTRIBUTE: AIC

DATEACETT(ALCD)	AIC
DATASET(AICRec)	AIC

Up

Akaike Information Criterion (AIC) Information theory based criterion for assessing Goodness of Fit (GOF). Lower values mean better fit.

**Return** DATASET(AICRec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

## ${\bf RECORD: Range Vec}$

RangeVec

MODULE: Dist	tributionBase
--------------	---------------

DistributionBase
(t\_Count Nranges = 10000)

Up

Low | High | Density | RangeWidth | DensityV | CumulativeV | Cumulative | NTile | InvDensity | Discrete |

### ATTRIBUTE: Low

Low

Up

## ${\bf ATTRIBUTE: High}$

High

Up

## ${\bf FUNCTION: Density}$

t\_FieldReal Density
(t\_FieldReal t)

TT	
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ATTRIBUTE	:	RangeWidth
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RangeWidth

## ${\bf FUNCTION: Density V}$

DATASET(RangeVec)	DensityV
()	

Up

## ${\bf FUNCTION: Cumulative V}$

	CumulativeV
(	)

Up

## FUNCTION: Cumulative

t_FieldReal	Cumulative
(t_FieldReal t)	

FUNCTION: NTile
t_FieldReal NTile
(t_FieldReal Pc)
Up
FUNCTION : InvDensity
InvDensity
(t_FieldReal delta)
$\mathrm{Up}$
ATTRIBUTE : Discrete  Discrete
Discrete
$\mathrm{Up}$
MODULE : TDistribution
TDistribution
(t_Discrete v_in,t_Count NRanges = 10000)
${ m Up}$
Density

FUNCTION : Den	$\operatorname{sity} V$
DATASET(RangeVec)	DensityV
()	
Up	
OVERRIDE True	
FUNCTION: NTi	le
t_FieldReal NTile	
(t_FieldReal Pc)	
Up	
OVERRIDE True	
ATTRIBUTE : Dis	screte
Discrete	
Up	
INHERITED True	

FUNCTION: InvDensity
InvDensity
(t_FieldReal delta)
$\mathrm{Up}$
OVERRIDE True
ATTRIBUTE : High
High
${ m Up}$
OVERRIDE True
ATTRIBUTE : Low
Low
${ m Up}$
INHERITED True
ATTRIBUTE : RangeWidth
PangaWidth
RangeWidth

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## ${\bf FUNCTION: Density}$

t_FieldReal	Density
(t_FieldReal	t)

Up

**OVERRIDE** True

## ${\bf FUNCTION: Cumulative V}$

	CumulativeV
(	

Up

**OVERRIDE** True

## **FUNCTION**: Cumulative

t_FieldReal	Cumulative
(t_FieldReal	t)

Up

**OVERRIDE** True

MODI	$\Pi \mathbf{E}$	• FD	istrib	nition
コントくフェフリ	しししょしょ	` ロコノ	'156111	) ( ) ( ) ( ) ( )

MIODULE: FDistribution
FDistribution
(t_Discrete d1_in, t_Discrete d2_in, t_Count NRanges = 10000)
Up
DensityV   CumulativeV   Cumulative   NTile   InvDensity   Discrete   Low   High   RangeWidth   Density
${f FUNCTION: Density V}$
DATASET(RangeVec) DensityV
${ m Up}$
OVERRIDE True
${f FUNCTION: Cumulative V}$
CumulativeV
()
${ m Up}$
OVERRIDE True

FUN	CTION	: Cumui	lative
$\mathbf{r} \cup \mathbf{r}$	$\mathbf{O} + \mathbf{I} + \mathbf{O} + \mathbf{I}$	· Cumu.	ιαυινι

FUNCTION : Cumulative
t_FieldReal Cumulative
(t_FieldReal t)
$\mathrm{Up}$
OVERRIDE True
FUNCTION : NTile
t_FieldReal NTile
(t_FieldReal Pc)
$\mathrm{Up}$
OVERRIDE True
FUNCTION : InvDensity
InvDensity
(t_FieldReal delta)
${ m Up}$
INHERITED True

ATTRIBUTE : Discrete
Discrete
${ m Up}$
INHERITED True
ATTRIBUTE: Low
Low
$\mathrm{Up}$
INHERITED True
ATTRIBUTE : High
High
$\mathrm{Up}$
OVERRIDE True
${ m ATTRIBUTE}: { m RangeWidth}$
RangeWidth

ZO	710	$\mathbf{D}$	$\mathbf{D}$	T	T	Tours
しょい	/ P	H.	H.	11,	ľ	True

<b>FUNCTION</b>	:	Density
-----------------	---	---------

t_FieldReal	Density
(t_FieldReal	t)

**OVERRIDE** True

## MODULE: Normal Distribution

NormalDistribution
(t\_Count NRanges)

Up

Low | High | RangeWidth | DensityV | CumulativeV | Cumulative | NTile | InvDensity | Density | Density |

## ATTRIBUTE: Low

Low

Up

**INHERITED** True

ATTRIBUTE : High
High
$\mathrm{Up}$
INHERITED True
${f ATTRIBUTE}: {f RangeWidth}$
RangeWidth
$\mathrm{Up}$
OVERRIDE True
${f FUNCTION: Density V}$
DATASET(RangeVec) DensityV
${ m Up}$
OVERRIDE True
${\bf FUNCTION: Cumulative V}$
CumulativeV

Up	
OVERRIDE	True
FUNCTIO	N : Cumulative
t_FieldReal	Cumulative
(t_FieldReal	t)
Up	
OVERRIDE	True
FUNCTIO  t_FieldReal	NTile
(t_FieldReal	Pc)
Up	
OVERRIDE	True
FUNCTIO	${ m NN: InvDensity}$
InvDensity	
(t_FieldReal	delta)

ATTR	IBU	TE:	Discre	te

Discrete

Up

INHERITED True

### **FUNCTION**: Density

t_FieldReal	Density
(t_FieldReal	t)

Up

**OVERRIDE** True

## ATTRIBUTE: pVal

pVal

#### Up

P-Value Calculate the P-value for each coefficient, which is the probability that the coefficient is insignificant (i.e. actually zero). A low P-value (e.g. .05) provides evidence that the coefficient is significant in the model. A high P-value indicates that the coefficient value should, in fact, be zero. P-value is related to the T-Statistic, and can be thought of as a normalized version of the T-Statistic. Only meaningful during the training phase.

Return DATSET(NumericField), one record per Beta coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.
RECORD : ConfintRec
ConfintRec
Up
FUNCTION : ConfInt
ConfInt
(Types.t_fieldReal level)
$\mathrm{Up}$
Confidence Interval The Confidence Interval determines the upper and lower bounds of each estimated coefficient given a confidence level (level) that is required. For example, one could say that there is a 95% probability (level) that the coefficient of the first independent variable is between 2.05 and 3.62. This allows error margins to be determined with the desired confidence level. If the confidence interval spans zero, it implies that the coefficient may not be significant at the specified confidence level.
Parameter level     The level of confidence required, expressed as a percentage from 0.0 to 100.0
Return DATASET(ConfintRec) with one record per coefficient per dependent variable per work-item. The 'id' field is the coefficient number, with 1 being the Y intercept, 2 being the coefficient for the first feature, etc. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.
RECORD : FTestRec

 ${\rm FTestRec}$ 

#### ATTRIBUTE: FTest

DATASET(FTestRec)	FTest
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#### Up

F-Test Calculate the P-value for the full regression, which is the probability that all of the coefficients are insignificant (i.e. actually zero). A low P-value (e.g. .05) provides evidence that at least one coefficient is significant. A high P-value indicates that all the coefficient values should in fact be zero, implying that the regression has no statistically significant predictive power. P-value is related to the ANOVA F-Statistic, and can be thought of as a standardized version of the ANOVA F-Statistic. The F-Test and T-Test are similar, except that the T-test is used to test the significance of each coefficient, while the F-Test is used to test the significance of the entire regression. For simple linear regression (i.e. only one independent variable, the T-Test and F-Test are equivalent.

**Return** DATASET(FTestRec), one record per dependent variable per work-item. The number field indicates the dependent variable and corresponds to the number field of the dependent (Y) variable to which it applies.

# LogisticRegression

Name	LogisticRegression
Version	1.0.0
Description	Logistic Regression implementation
License	http://www.apache.org/licenses/LICENSE-2.0
Copyright	Copyright (C) 2017 HPCC Systems
Authors	HPCCSystems
DependsOn	ML_Core, PBblas
Platform	6.2.0

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Binomial confusion matrix

BinomialLogisticRegression.ecl

Binomial logistic regression using iteratively re-weighted least squares

Confusion.ecl

Detail confusion records to compare actual versus predicted response variable values

Constants.ecl

DataStats.ecl

Information about the datasets

Deviance\_Analysis.ecl

Compare deviance information for an analysis of deviance

Deviance Detail.ecl

Detail deviance for each observation

dimm.ecl

Matrix multiply when either A or B is a diagonal and is passed as a vector

Distributions.ecl

ExtractBeta.ecl

Extract the beta values form the model dataset

ExtractBeta\_CI.ecl

Extract the beta values form the model dataset

 $ExtractBeta\_pval.ecl$ 

Extract the beta values form the model dataset

ExtractReport.ecl

Extract Report records from model

LogitPredict.ecl

Predict the category values with the logit function and the supplied beta coefficients

LogitScore.ecl

Calculate the score using the logit function and the supplied beta coefficients

Model Deviance.ecl

Model Deviance

Null Deviance.ecl

Deviance for the null model, that is, a model with only an intercept

Types.ecl

# LogisticRegression.BinomialConfusion

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- ML\_Core.Types

## **DESCRIPTIONS**

### **FUNCTION**: BinomialConfusion

DATASET(Types.Binomial_Confusion_Summary)	BinomialConfusion
(DATASET(Core_Types.Confusion_Detail) d)	

#### Up

Binomial confusion matrix. Work items with multinomial responses are ignored by this function. The higher value lexically is considered to be the positive indication.

Parameter d || confusion detail for the work item and classifier

Return confusion matrix for a binomial classifier

# LogisticRegression.BinomialLogisticRegression

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Constants
- ML Core.Interfaces
- ML\_Core.Types

## **DESCRIPTIONS**

## ${\bf MODULE: Binomial Logistic Regression}$

BinomialLogisticRegression

(UNSIGNED max\_iter=200, REAL8 epsilon=Constants.default\_epsilon, REAL8 ridge=Constants.default\_ridge)

#### Up

Binomial logistic regression using iteratively re-weighted least squares.

Parameter max\_iter || maximum number of iterations to try

Parameter epsilon ||| the minimum change in the Beta value estimate to continue

Parameter ridge ||| a value to populate a diagonal matrix that is added to a matrix help assure that the matrix is invertible.

GetModel | Classify | Report |

### FUNCTION: GetModel

DATASET(Types.Layout_Model)	GetModel
(DATASET(Types.NumericField) of DATASET(Types.DiscreteField) cla	•

#### Up

Calculate the model to fit the observation data to the observed classes.

Parameter observations ||| the observed explanatory values

Parameter classifications ||| the observed classification used to build the model

Return the encoded model

**OVERRIDE** True

### **FUNCTION**: Classify

DATASET(Types.Classify_Result)	Classify
(DATASET(Types.Layout_Model) 1 DATASET(Types.NumericField) nev	

### Up

Classify the observations using a model.

Parameter model ||| The model, which must be produced by a corresponding getModel function.

Parameter new\_observations ||| observations to be classified

Return Classification with a confidence value

**OVERRIDE** True

## **FUNCTION**: Report

DATASET(Types.Confusion_Detail) Re	eport
(DATASET(Types.Layout_Model) model DATASET(Types.NumericField) observate DATASET(Types.DiscreteField) classification	ions,

## Up

Report the confusion matrix for the classifier and training data.

Parameter model ||| the encoded model

Parameter observations ||| the explanatory values.

Parameter classifications ||| the classifications associated with the observations

Return the confusion matrix showing correct and incorrect results

**OVERRIDE** True

# LogisticRegression.Confusion

## **IMPORTS**

- ML\_Core
- ML\_Core.Types
- LogisticRegression
- $\bullet \ \ Logistic Regression. Types$

## **DESCRIPTIONS**

## **FUNCTION**: Confusion

DATASET(Confusion_Detail)	Confusion
(DATASET(DiscreteField) depermental predicts)	endents, DATASET(DiscreteField)

### Up

Detail confusion records to compare actual versus predicted response variable values.

Parameter dependents ||| the original response values

Parameter predicts ||| the predicted responses

Return confusion counts by predicted and actual response values.

# LogisticRegression.Constants

## **IMPORTS**

## **DESCRIPTIONS**

**MODULE**: Constants

Constants

#### Up

 $limit\_card \mid default\_epsilon \mid default\_ridge \mid local\_cap \mid id\_base \mid id\_iters \mid id\_delta \mid id\_correct \mid id\_incorrect \mid id\_stat\_set \mid id\_betas \mid id\_betas\_coef \mid id\_betas\_SE \mid base\_builder \mid base\_max\_iter \mid base\_epsilon \mid base\_ind\_vars \mid base\_dep\_vars \mid base\_obs \mid builder\_irls\_local \mid builder\_irls\_global \mid builder\_softmax \mid$ 

## ATTRIBUTE: limit\_card

UNSIGNED2 | limit card

Up

### ATTRIBUTE : default\_epsilon

REAL8 default\_epsilon

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ATTRIBUTE	:	default	ridge
	•	actaate	1145

REAL8	default_ridge				
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## ${\bf ATTRIBUTE: local\_cap}$

UNSIGNED4	local_cap	
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Up

## ${\bf ATTRIBUTE: id\_base}$

id\_base

Up

## ${\bf ATTRIBUTE: id\_iters}$

id\_iters

ATTRIBUTE : id_delta
id_delta
${ m Up}$
ATTRIBUTE : id_correct
id_correct
Up
ATTRIBUTE : id_incorrect
id_incorrect
${ m Up}$
ATTRIBUTE : id_stat_set
id_stat_set
${ m Up}$
ATTRIBUTE : id_betas
id_betas

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ATTRIBUTE : id_betas_coef	
id_betas_coef	
${ m Up}$	
ATTRIBUTE : id_betas_SE	
id_betas_SE	
${ m Up}$	
ATTRIBUTE : base_builder	
base_builder	
${ m Up}$	
ATTRIBUTE : base_max_iter	
base_max_iter	
$\mathrm{Up}$	

ATTRIBUTE : base_epsilon
base_epsilon
${ m Up}$
ATTRIBUTE : base_ind_vars
base_ind_vars
${ m Up}$
ATTRIBUTE : base_dep_vars
base_dep_vars
${ m Up}$
ATTRIBUTE : base_obs
base_obs
${ m Up}$
${\bf ATTRIBUTE: builder\_irls\_local}$
builder_irls_local



# ${\bf ATTRIBUTE:builder\_irls\_global}$

builder\_irls\_global

Up

# ${\bf ATTRIBUTE: builder\_softmax}$

 $builder\_softmax$ 

# LogisticRegression.DataStats

### **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- LogisticRegression.Constants
- ML\_Core.Types

### **DESCRIPTIONS**

### **FUNCTION**: DataStats

DATASET(Types.Data_Info)	DataStats
(DATASET(Core_Types.Numer DATASET(Core_Types.Discrete field_details=FALSE)	

#### Up

Information about the datasets. Without details the range for the x and y (independent and dependent) columns. Note that a column of all zero values cannot be distinguished from a missing column. When details are requested, the cardinality, minimum, and maximum values are returned. A zero cardinality is returned when the field cardinality exceeds the Constants.limit\_card value.

Parameter indep || data set of independent variables

Parameter dep || data set of dependent variables

Parameter field details || Boolean directive to provide field level info

# $Logistic Regression. Deviance \_Analysis$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types

## **DESCRIPTIONS**

FUNCTION: Deviance\_Analysis

DATASET(Types.AOD_Record)	Deviance_Analysis
(DATASET(Types.Deviance_Record) proposed, DATASET(Types.Deviance_Record) base)	

#### Up

Compare deviance information for an analysis of deviance.

Parameter proposed ||| the proposed model

Parameter base ||| the base model for comparison

Return the comparison of the deviance between the models

# $Logistic Regression. Deviance\_Detail$

## **IMPORTS**

- ML\_Core
- ML\_Core.Types
- LogisticRegression
- ullet Logistic Regression. Types

## **DESCRIPTIONS**

 $FUNCTION: Deviance\_Detail$ 

DATASET(Types.Observation_Deviance)	Deviance_Detail
(DATASET(Core_Types.DiscreteField) de DATASET(Types.Raw_Prediction) predict	

#### Up

Detail deviance for each observation.

Parameter dependents ||| original dependent records for the model

Parameter predicts ||| the predicted values of the response variable

**Return** the deviance information by observation and the log likelihood of the predicted result.

# LogisticRegression.dimm

## **IMPORTS**

- $\bullet$  std.BLAS
- $\bullet$  std.BLAS.Types

## **DESCRIPTIONS**

#### EMBED: dimm

Types.matrix_t dimm		
(BOOLEAN transposeA, BOOLEAN transposeB, BOOLEAN diagonalA,		
BOOLEAN diagonalB, Types.dimension_t n, Types.dimension_t n,		
Types.dimension_t k, Types.value_t alpha, Types.matrix_t A, Types.matrix_t B, Types.value_t beta=0.0, Types.matrix_t C=[])		

#### Up

Matrix multiply when either A or B is a diagonal and is passed as a vector. alpha\*op(A) op(B) + beta\*C where op() is transpose

Parameter transposeA ||| true when transpose of A is used

Parameter transposeB ||| true when transpose of B is used

Parameter diagonalA ||| true when A is the diagonal matrix

Parameter diagonalB ||| true when B is the diagonal matrix

Parameter m ||| number of rows in product

Parameter n ||| number of columns in product

Parameter k ||| number of columns/rows for the multiplier/multiplicand

Parameter alpha ||| scalar used on A

 $\mathbf{Parameter}\ A\ |||\ \mathrm{matrix}\ A$ 

 $\textbf{Parameter} \;\; B \; ||| \; matrix \; B$ 

 $\textbf{Parameter}\;\; \text{beta}\; |||\; \text{scalar}\; \text{for matrix}\; C$ 

 $\textbf{Parameter} \ \ C \ ||| \ \ \text{matrix} \ \ C \ \ \text{or empty}$ 

# LogisticRegression.Distributions

### **IMPORTS**

- ML\_Core.Constants
- ML Core.Math

### **DESCRIPTIONS**

#### **MODULE**: Distributions

Distributions

#### Up

Normal\_CDF | Normal\_PPF | T\_CDF | T\_PPF | Chi2\_CDF | Chi2\_PPF |

### FUNCTION: Normal\_CDF

REAL8	Normal_CDF
(REAL8	$\mathbf{x}$ )

#### Up

Cumulative Distribution of the standard normal distribution, the probability that a normal random variable will be smaller than x standard deviations above or below the mean. Taken from C/C++ Mathematical Algorithms for Scientists and Engineers, n. Shammas, McGraw-Hill, 1995

Parameter x ||| the number of standard deviations

### FUNCTION: Normal\_PPF

REAL8 Normal\_PPF
(REAL8 x)

#### Up

Normal Distribution Percentage Point Function. Translated from C/C++ Mathematical Algorithms for Scientists and Engineers, N. Shammas, McGraw-Hill, 1995

Parameter x || probability

#### FUNCTION: T\_CDF

REAL8 T\_CDF
(REAL8 x, REAL8 df)

#### Up

Students t distribution integral evaluated between negative infinity and x. Translated from NIST SEL DATAPAC Fortran TCDF.f source

Parameter x | | | value of the evaluation

Parameter df || degrees of freedom

### **FUNCTION**: T\_PPF

REAL8 T\_PPF
(REAL8 x, REAL8 df)

#### Up

Percentage point function for the T distribution. Translated from NIST SEL DATAPAC Fortran TPPF.f source

### FUNCTION: Chi2\_CDF

REAL8	Chi2_CDF
(REAL8 x, REAL8 df)	

#### Up

The cumulative distribution function for the Chi Square distribution. the CDF for the specified degrees of freedom. Translated from the NIST SEL DATAPAC Fortran subroutine CHSCDF.

### $FUNCTION : Chi2\_PPF$

REAL8	Chi2_PPF
(REAL8 x, REAL8 df)	

#### Up

The Chi Squared PPF function. Translated from the NIST SEL DATAPAC Fortran subroutine CHSPPF.

# ${\bf Logistic Regression. Extract Beta}$

## **IMPORTS**

- $\bullet \ \ Logistic Regression$
- LogisticRegression.Types
- ML\_Core.Types

## **DESCRIPTIONS**

FUNCTION: ExtractBeta

ExtractBeta

 $(DATASET(Core\_Types.Layout\_Model)\ mod\_ds)$ 

#### Up

Extract the beta values form the model dataset.

Parameter mod\_ds ||| the model dataset

**Return** a beta values as Model Coefficient records, zero as the constant term.

# $Logistic Regression. Extract Beta\_CI$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- $\bullet \ \mathrm{ML\_Core.Types}$

## **DESCRIPTIONS**

FUNCTION: ExtractBeta\_CI

DATASET(Types.Confidence_Model_Coef)	ExtractBeta_CI
(DATASET(Core_Types.Layout_Model) mo REAL8 level)	$\mathrm{d}_{-}\mathrm{d}\mathrm{s},$

#### Up

Extract the beta values form the model dataset.

Parameter mod\_ds ||| the model dataset

Parameter level ||| the significance value for the intervals

**Return** the beta values with confidence intervals term.

# $Logistic Regression. Extract Beta\_pval$

## **IMPORTS**

- $\bullet \ \ Logistic Regression$
- LogisticRegression.Types
- ML\_Core.Types

## **DESCRIPTIONS**

 ${\bf FUNCTION: ExtractBeta\_pval}$ 

DATASET(Types.pval_Model_Coef)	ExtractBeta_pval
(DATASET(Core_Types.Layout_Model) mod_ds)	

#### Up

Extract the beta values form the model dataset.

Parameter mod\_ds ||| the model dataset

**Return** the beta values with p-values as Model Coefficient records, zero as the constant term.

# ${\bf Logistic Regression. Extract Report}$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- LogisticRegression.Constants
- $\bullet \ \mathrm{ML\_Core.Types}$

## **DESCRIPTIONS**

### FUNCTION: ExtractReport

DATASET(Types.Model_Report)	ExtractReport
(DATASET(Core_Types.Layout_Model) mod_ds)	

#### Up

Extract Report records from model

Parameter mod\_ds ||| the model dataset

Return the model report dataset

# Logistic Regression. Logit Predict

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- ML\_Core.Types

## **DESCRIPTIONS**

### ${\bf FUNCTION: LogitPredict}$

DATASET(Classify_Result)	LogitPredict
(DATASET(Model_Coef) coef, DATASET(NumericField) independents)	

#### Up

Predict the category values with the logit function and the the supplied beta coefficients.

Parameter coef ||| the model beta coefficients

Parameter independents ||| the observations

Return the predicted category values and a confidence score

# ${\bf Logistic Regression. Logit Score}$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types
- ML\_Core.Types

## **DESCRIPTIONS**

## ${\bf FUNCTION: Logit Score}$

DATASET(Raw_Prediction)	LogitScore
(DATASET(Model_Coef) coef, DATASET(NumericField) independents)	

### Up

Calculate the score using the logit function and the supplied beta coefficients.

Parameter coef ||| the model beta coefficients

Parameter independents ||| the observations

Return the raw prediction value

# $Logistic Regression. Model\_Deviance$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types

## **DESCRIPTIONS**

FUNCTION: Model\_Deviance

DATASET(Types.Deviance_Record)   Model_Deviance
(DATASET(Types.Observation_Deviance) od, DATASET(Types.Model_Coef) mod)

#### Up

Model Deviance.

Parameter od ||| observation deviance record

Parameter mod || model co-efficients

Return model deviance

# $Logistic Regression. Null\_Deviance$

## **IMPORTS**

- LogisticRegression
- LogisticRegression.Types

## **DESCRIPTIONS**

FUNCTION: Null\_Deviance

DATASET(Types.Deviance_Record)	Null_Deviance	
(DATASET(Types.Observation_Deviance) od)		

#### Up

Deviance for the null model, that is, a model with only an intercept.

Parameter od || Observation Deviance record set.

Return a data set of the null model deviances for each work item and classifier.

# LogisticRegression.Types

## **IMPORTS**

• ML\_Core.Types

### **DESCRIPTIONS**

MODULE: Types

Types	

#### Up

t\_Universe | Field\_Desc | Data\_Info | NumericField\_U | DiscreteField\_U | Layout\_Column\_Map | Classifier\_Stats | Model\_Report | Binomial\_Confusion\_Summary | Model\_Coef | Confidence\_Model\_Coef | pval\_Model\_Coef | Raw\_Prediction | Observation\_Deviance | Deviance\_Record | AOD\_Record |

### $ATTRIBUTE: t\_Universe$

t\_Universe

$\operatorname{RECORD}: \operatorname{Field\_Desc}$
Field_Desc
${ m Up}$
RECORD : Data_Info
Data_Info
$\mathrm{Up}$
$RECORD: NumericField\_U$
NumericField_U
${ m Up}$
${f RECORD: DiscreteField\_U}$
DiscreteField_U
$\mathrm{Up}$
RECORD : Layout_Column_Map
Lavout Column Map

Up	
RECORD : Classifier_Stats	
Classifier_Stats	
${ m Up}$	
$RECORD: Model\_Report$	
Model_Report	
${ m Up}$	
RECORD : Binomial_Confusion_Summary	
Binomial_Confusion_Summary	
${ m Up}$	
RECORD : Model_Coef	
Model_Coef	
$_{ m Up}$	

RECORD : Confidence_Model_Coef
Confidence_Model_Coef
$\mathrm{Up}$
RECORD : pval_Model_Coef
pval_Model_Coef
$\mathrm{Up}$
RECORD : Raw_Prediction
Raw_Prediction
$\mathrm{Up}$
RECORD : Observation_Deviance
Observation_Deviance
Up
RECORD : Deviance_Record
Deviance_Record



# ${\tt RECORD: AOD\_Record}$

AOD\_Record

# $ML\_Core$

Name	ML_Core
Version	3.1.0
Description	Common definitions for Machine Learning
License	See LICENSE.TXT
Copyright	Copyright (C) 2017 HPCC Systems
Authors	HPCCSystems
Platform	6.2.0

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# $ML\_Core.AppendID$

# **IMPORTS**

# **DESCRIPTIONS**

MACRO: AppendID

AppendID
(dIn,idfield,dOut)

# ${\bf ML\_Core.AppendSeqID}$

# **IMPORTS**

# **DESCRIPTIONS**

 ${\bf MACRO: AppendSeqID}$ 

	AppendSeqID
(0	$\operatorname{IIn,idfield,dOut})$

# ML\_Core.Config

<u>IMPORTS</u>
DESCRIPTIONS

MODULE · Config

ATTRIBUTE: Discrete

IVI (	ODULE: Config
	Config
Up	
Ma	xLookup   Discrete   RoundingError
ΛП	TRIBUTE : MaxLookup
AJ	TRIBUTE: WaxLookup
	MaxLookup
Up	
-	

Up

Discrete

# ${\bf ATTRIBUTE: Rounding Error}$

RoundingError

# $ML\_Core.Constants$

TN	$\mathbf{IP}$	$\mathbf{O}$	$R$ $\Gamma$	$\Gamma S$
<b>T</b> T V		$\mathbf{\mathcal{I}}$	101	$\perp$

# **DESCRIPTIONS**

Constants

Up

Useful constants

Pi | Root\_2 |

### ATTRIBUTE: Pi

Pi

Up

Constant PI

## ATTRIBUTE: Root\_2

Root\_2

## Up

Constant square root of 2

# $ML\_Core.Discretize$

## **IMPORTS**

- ML\_Core
- ML\_Core.Types

## **DESCRIPTIONS**

MODULE: Discretize

Discretize

Up

c\_Method | r\_Method | i\_ByRounding | ByRounding | i\_ByBucketing | ByBucketing | i\_ByTiling | ByTiling | Do |

### $ATTRIBUTE: c\_Method$

c Method

$RECORD: r\_Method$	
r_Method	
Up	
FUNCTION: i_ByRounding	
i_ByRounding	
(SET OF Types.t_FieldNumber f, REAL Scale=1.0,REAL Delta=0.0)	
Up	
FUNCTION : ByRounding	
FUNCTION : ByRounding  ByRounding	
ByRounding	
ByRounding (DATASET(Types.NumericField) d,REAL Scale=1.0, REAL Delta=0.0)	
ByRounding  (DATASET(Types.NumericField) d,REAL Scale=1.0, REAL Delta=0.0)  Up	

ByBucketing
(DATASET(Types.NumericField) d, Types.t\_Discrete N=ML\_Core.Config.Discrete)

Up

### FUNCTION: i\_ByTiling

 $i\_ByTiling$ 

(SET OF Types.t\_FieldNumber f, Types.t\_Discrete N=ML\_Core.Config.Discrete)

Up

### **FUNCTION: ByTiling**

ByTiling

 $(DATASET(Types.NumericField)\ d,\ Types.t\_Discrete\ N=ML\_Core.Config.Discrete)$ 

Up

### **FUNCTION: Do**

Do

 $(DATASET(Types.NumericField)\ d,\ DATASET(r\_Method)\ to\_do)$ 

# ML\_Core.FieldAggregates

## **IMPORTS**

- ML\_Core
- ML\_Core.Types
- ML\_Core.Utils
- std.system.ThorLib

## **DESCRIPTIONS**

MODULE : FieldAggregates

FieldAggregates
(DATASET(Types.NumericField) d)

Up

Simple | SimpleRanked | Medians | MinMedNext | Buckets | BucketRanges | Modes | Cardinality | RankedInput | NTiles | NTileRanges |

## ATTRIBUTE: Simple

Simple

ATTRIBUTE : SimpleRanked
SimpleRanked
Up
ATTRIBUTE : Medians
Medians
$\mathrm{Up}$
${\bf ATTRIBUTE: MinMedNext}$
MinMedNext
${ m Up}$
FUNCTION : Buckets
Buckets
(Types.t_Discrete n)
$\mathrm{Up}$

# ${\bf FUNCTION: Bucket Ranges}$

BucketRanges
(Types.t_Discrete n)
$_{ m Up}$
ATTRIBUTE : Modes
Modes
Up
ATTRIBUTE : Cardinality
Cardinality
${ m Up}$
f ATTRIBUTE: Ranked Input
RankedInput
Up

# FUNCTION: NTiles

	NTiles
(Types.t_Discrete n)	

Up

# ${\bf FUNCTION: NTile Ranges}$

	NTileRanges
('	Types.t_Discrete n)

# ${\bf ML\_Core.FromField}$

## **IMPORTS**

## **DESCRIPTIONS**

MACRO: From Field

FromField

(dIn,lOut,dOut,dMap=")

# $ML\_Core.Generate$

## **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

## **DESCRIPTIONS**

MODULE: Generate

Generate

Up

tp\_Method | MethodName | ToPoly |

 ${\bf ATTRIBUTE: tp\_Method}$ 

tp\_Method

### ${\bf FUNCTION: Method Name}$

	MethodName
(	$tp\_Method x)$

Up

## FUNCTION: ToPoly

ToPoly

 $({\tt DATASET}({\tt Types.NumericField})~{\tt seedCol},~{\tt UNSIGNED}~{\tt maxN=6})$ 

# $ML\_Core.ToField$

## **IMPORTS**

## **DESCRIPTIONS**

MACRO: ToField

ToField

(dIn, dOut, idfield=", wifield=", wivalue=", datafields=")

# ML\_Core.Types

### **IMPORTS**

## **DESCRIPTIONS**

MODULE: Types

Types

Up

### ${\bf ATTRIBUTE: t\_RecordID}$

 $t\_RecordID$ 

Up

### ${\bf ATTRIBUTE: t\_FieldNumber}$

 $t_FieldNumber$ 

Up	
${ m ATTRIBUTE: t\_FieldReal}$	
t_FieldReal	
$\mathrm{Up}$	
$f ATTRIBUTE: t\_FieldSign$	
t_FieldSign	
${ m Up}$	
ATTRIBUTE : t_Discrete  t_Discrete	
Up	
ATTRIBUTE : t_Item	
t_Item	
Up	

ATTRIBUTE : t_Count
t_Count
${ m Up}$
ACCEPTED TO THE STATE OF THE ST
ATTRIBUTE : t_Work_Item
t_Work_Item
$\mathrm{Up}$
RECORD : AnyField
AnyField
${ m Up}$
${f RECORD}: {f Numeric Field}$
NumericField
$\mathrm{Up}$
${f RECORD: Discrete Field}$
DiscreteField

Up	
$RECORD: Layout\_Model$	
Layout_Model	
${ m Up}$	
RECORD : Classify_Result	
Classify_Result	
Up	
RECORD : l_result	
l_result	
m Up	
RECORD : Confusion_Detail  Confusion_Detail	

RECORD : ItemElement
ItemElement
Up
ATTRIBUTE : t_node
t_node
Up
ATTRIBUTE : t_level
t_level
${ m Up}$
RECORD : NodeID
NodeID
$\mathrm{Up}$

## Interfaces

## **Table of Contents**

### IClassify.ecl

Interface definition for Classification

#### IRegression.ecl

Interface Definition for Regression Modules Regression learns a function that maps a set of input data to one or more output variables

# ML\_Core.Interfaces.IClassify

### **IMPORTS**

- ML\_Core
- ML\_Core.Types

## **DESCRIPTIONS**

MODULE: IClassify

IClassify

#### Up

Interface definition for Classification. Actual implementation modules will probably take parameters.

GetModel | Classify | Report |

#### FUNCTION: GetModel

DATASET(Types.Layout_Model)	GetModel
(DATASET(Types.NumericField) classification (DATASET(Types.DiscreteField) classification (DATASET(Types.DiscreteField) classification (DATASET(Types.DiscreteField))	·

#### Up

Calculate the model to fit the observation data to the observed classes.

Parameter observations ||| the observed explanatory values

Parameter classifications ||| the observed classification used to build the model

Return the encoded model

#### **FUNCTION**: Classify

DATASET(Types.Classify_Result)	Classify
(DATASET(Types.Layout_Model) model, DATASET(Types.NumericField) new_observations)	

#### Up

Classify the observations using a model.

Parameter model ||| The model, which must be produced by a corresponding getModel function.

Parameter new\_observations ||| observations to be classified

Return Classification with a confidence value

### **FUNCTION**: Report

DATASET(Types.Confusion_Detail)	Report
(DATASET(Types.Layout_Model) model DATASET(Types.NumericField) observation DATASET(Types.DiscreteField) classification of the control of the	rvations,

#### Up

Report the confusion matrix for the classifier and training data.

Parameter model ||| the encoded model

**Parameter** observations ||| the explanatory values.

Parameter classifications ||| the classifications associated with the observations

 ${\bf Return}\,$  the confusion matrix showing correct and incorrect results

## ML\_Core.Interfaces.IRegression

### **IMPORTS**

- ML\_Core
- ML\_Core.Types

### **DESCRIPTIONS**

### **MODULE**: IRegression

IRegression

(DATASET(NumericField) X=empty\_data, DATASET(NumericField) Y=empty\_data)

#### Up

Interface Definition for Regression Modules Regression learns a function that maps a set of input data to one or more output variables. The resulting learned function is known as the model. That model can then be used repetitively to predict (i.e. estimate) the output value(s) based on new input data.

**Parameter** X ||| The independent data in DATASET(NumericField) format. Each statistical unit (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number').

**Parameter** Y ||| The dependent variable(s) in DATASET(NumericField) format. Each statistical unit (e.g. record) is identified by 'id', and each feature is identified by field number (i.e. 'number').

### GetModel | Predict |

#### ATTRIBUTE: GetModel

DATASET(Layout_Model)	GetModel
-----------------------	----------

#### Up

Calculate and return the 'learned' model The model may be persisted and later used to make predictions using 'Predict' below.

Return DATASET(LayoutModel) describing the learned model parameters

#### **FUNCTION**: Predict

DATASET(NumericField)	Predict
(DATASET(NumericField)	newX, DATASET(Layout_Model) model)

#### Up

Predict the output variable(s) based on a previously learned model

Parameter newX || DATASET(NumericField) containing the X values to b predicted.

**Return** DATASET(NumericField) containing one entry per observation (i.e. id) in newX. This represents the predicted values for Y.

## Math

### Table of Contents

#### Beta.ecl

Return the beta value of two positive real numbers, x and y

#### Distributions.ecl

#### DoubleFac.ecl

The 'double' factorial is defined for ODD n and is the product of all the odd numbers up to and including that number

#### Fac.ecl

Factorial function

#### gamma.ecl

Return the value of gamma function of real number x A wrapper for the standard C tgamma function

#### log\_gamma.ecl

Return the value of the log gamma function of the absolute value of X

#### lowerGamma.ecl

Return the lower incomplete gamma value of two real numbers,

#### NCK.ecl

#### Poly.ecl

Evaluate a polynomial from a set of co-effs

#### StirlingFormula.ecl

Stirling's formula

#### upperGamma.ecl

Return the upper incomplete gamma value of two real numbers, x and y

# $ML\_Core.Math.Beta$

## **IMPORTS**

• ML\_Core.Math

## **DESCRIPTIONS**

**FUNCTION**: Beta

	Beta
(	REAL8 x, REAL8 y)

#### Up

Return the beta value of two positive real numbers, x and y

**Parameter**  $x \mid\mid\mid$  the value of the first number

Parameter y ||| the value of the second number

Return the beta value

## ML Core.Math.Distributions

### **IMPORTS**

- ML\_Core.Constants
- ML Core.Math

### **DESCRIPTIONS**

#### **MODULE**: Distributions

Distributions

#### Up

Normal\_CDF | Normal\_PPF | T\_CDF | T\_PPF | Chi2\_CDF | Chi2\_PPF |

### FUNCTION: Normal\_CDF

REAL8	Normal_CDF
(REAL8	$\mathbf{x}$ )

#### Up

Cumulative Distribution of the standard normal distribution, the probability that a normal random variable will be smaller than x standard deviations above or below the mean. Taken from C/C++ Mathematical Algorithms for Scientists and Engineers, n. Shammas, McGraw-Hill, 1995

**Parameter** x ||| the number of standard deviations

### FUNCTION: Normal\_PPF

REAL8 Normal\_PPF
(REAL8 x)

#### Up

Normal Distribution Percentage Point Function. Translated from C/C++ Mathematical Algorithms for Scientists and Engineers, N. Shammas, McGraw-Hill, 1995

Parameter x || probability

#### FUNCTION: T\_CDF

REAL8 T\_CDF
(REAL8 x, REAL8 df)

#### Up

Students t distribution integral evaluated between negative infinity and x. Translated from NIST SEL DATAPAC Fortran TCDF.f source

Parameter x | | | value of the evaluation

Parameter df ||| degrees of freedom

### **FUNCTION**: T\_PPF

REAL8 T\_PPF
(REAL8 x, REAL8 df)

#### Up

Percentage point function for the T distribution. Translated from NIST SEL DATAPAC Fortran TPPF.f source

### FUNCTION: Chi2\_CDF

REAL8	Chi2_CDF
(REAL8 x, REAL8 df)	

#### Up

The cumulative distribution function for the Chi Square distribution. the CDF for the specified degrees of freedom. Translated from the NIST SEL DATAPAC Fortran subroutine CHSCDF.

### $FUNCTION : Chi2\_PPF$

REAL8	Chi2_PPF
(REAL8 x, REAL8 df)	

#### Up

The Chi Squared PPF function. Translated from the NIST SEL DATAPAC Fortran subroutine CHSPPF.

# $ML\_Core. Math. Double Fac$

### **IMPORTS**

### **DESCRIPTIONS**

### EMBED: DoubleFac

REAL8	DoubleFac
(INTEGER2 i)	

#### Up

The 'double' factorial is defined for ODD n and is the product of all the odd numbers up to and including that number. We are extending the meaning to even numbers to mean the product of the even numbers up to and including that number. Thus DoubleFac(8) = 8\*6\*4\*2 We also defend against i < 2 (returning 1.0)

Parameter i ||| the value used in the calculation

**Return** the factorial of the sequence, declining by 2

# $ML\_Core.Math.Fac$

## **IMPORTS**

## **DESCRIPTIONS**

EMBED: Fac

REAL8	Fac
(UNSIGNED2 i)	

### Up

Factorial function

 $\mathbf{Parameter} \ i \ ||| \ the \ value \ used, \ (i)(i\text{--}1)(i\text{--}2)\dots(2)$ 

Return the factorial i!

# $ML\_Core.Math.gamma$

## **IMPORTS**

## **DESCRIPTIONS**

### EMBED: gamma

REAL8	gamma
(REAL8 x)	

#### Up

Return the value of gamma function of real number x A wrapper for the standard C tgamma function.

Parameter  $x \parallel \parallel$  the input x

**Return** the value of GAMMA evaluated at x

# $ML\_Core.Math.log\_gamma$

## **IMPORTS**

## **DESCRIPTIONS**

EMBED: log\_gamma

REAL8	log_gamma
(REAL8 x)	

#### Up

Return the value of the log gamma function of the absolute value of X. A wrapper for the standard C lgamma function. Avoids the race condition found on some platforms by taking the absolute value of the of the input argument.

Parameter  $x \parallel \parallel$  the input x

**Return** the value of the log of the GAMMA evaluated at ABS(x)

# $ML\_Core.Math.lowerGamma$

## **IMPORTS**

## **DESCRIPTIONS**

### EMBED: lowerGamma

REAL8	lowerGamma
(REAL8 x, REAL8 y)	

#### Up

Return the lower incomplete gamma value of two real numbers, x and y

 $\textbf{Parameter} \ \, x \ ||| \ \, \text{the value of the first number} \\$ 

Parameter y ||| the value of the second number

Return the lower incomplete gamma value

# $ML\_Core.Math.NCK$

## **IMPORTS**

 $\bullet$  ML\_Core.Math

## **DESCRIPTIONS**

**FUNCTION: NCK** 

REAL8 NCK	
(INTEGER2 N, INTEGER2 K)	

# ML\_Core.Math.Poly

## **IMPORTS**

## **DESCRIPTIONS**

EMBED: Poly

REAL8	Poly
(REAL8 x, SET OF REAL8 Coeffs)	

#### Up

Evaluate a polynomial from a set of co-effs. Co-effs 1 is assumed to be the HIGH order of the equation. Thus for  $ax^2+bx+c$  - the set would need to be Coef := [a,b,c];

Parameter x ||| the value of x in the polynomial

Parameter Coeffs ||| a set of coefficients for the polynomial. The ALL set is considered to be all zero values

**Return** value of the polynomial at x

# $ML\_Core.Math.StirlingFormula$

## **IMPORTS**

- $\bullet$  ML\_Core.Math
- ML\_Core.Constants

## **DESCRIPTIONS**

FUNCTION: StirlingFormula

StirlingFormula
(REAL x)

#### Up

Stirling's formula

Parameter  $x \parallel \parallel$  the point of evaluation

Return evaluation result

# $ML\_Core.Math.upperGamma$

## **IMPORTS**

## **DESCRIPTIONS**

### ${\bf EMBED: upper Gamma}$

REAL8	upperGamma
(REAL8 x, REAL8 y)	

#### Up

Return the upper incomplete gamma value of two real numbers, x and y.

Parameter x ||| the value of the first number

Parameter y ||| the value of the second number

Return the upper incomplete gamma value

# Tests

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# $ML\_Core.Tests.Check\_Dist$

## **IMPORTS**

- $\bullet \ \mathrm{ML\_Core.Math.Distributions}$
- ML\_Core
- python

## **DESCRIPTIONS**

 $ATTRIBUTE: Check\_Dist$ 

Check\_Dist

# $ML\_Core. Tests. field\_aggregates$

## **IMPORTS**

- ML\_Core
- $\bullet$  ML\_Core.Types

## **DESCRIPTIONS**

 ${\bf ATTRIBUTE: field\_aggregates}$ 

field\_aggregates

# $ML\_Core. Tests. generate$

## **IMPORTS**

 $\bullet$  ML\_Core

## **DESCRIPTIONS**

 ${\bf ATTRIBUTE: generate}$ 

generate

# $ML\_Core.Tests.test\_appends$

## **IMPORTS**

- $\bullet$  ML\_Core
- ullet std.system.thorlib

## **DESCRIPTIONS**

ATTRIBUTE: test\_appends

test\_appends

# $ML\_Core.Tests.test\_discrete$

## **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

## **DESCRIPTIONS**

 ${\bf ATTRIBUTE: test\_discrete}$ 

test\_discrete

# $ML\_Core.Tests.to\_from$

## **IMPORTS**

- $\bullet$  ML\_Core
- $\bullet$  ML\_Core.Types

## **DESCRIPTIONS**

ATTRIBUTE: to\_from

to\_from

## $ML\_Core.Tests.Validate\_Betas$

### **IMPORTS**

- ML\_Core
- ML\_Core.Math
- python

### **DESCRIPTIONS**

 ${\bf ATTRIBUTE: Validate\_Betas}$ 

Validate\_Betas

Up

## $ML\_Core. Tests. Validate\_Gammas$

### **IMPORTS**

- ML\_Core
- ML\_Core.Math
- python

### **DESCRIPTIONS**

 ${\bf ATTRIBUTE: Validate\_Gammas}$ 

Validate\_Gammas

Up

## Utils

### **Table of Contents**

#### Fat.ecl

Will take a potentially sparse file d and fill in the missing

#### FatD.ecl

Will take a potentially sparse file d and fill in the missing

#### Gini.ecl

Creates a file of pivot/target pairs with a Gini impurity value

#### SequenceInField.ecl

Given a file which is sorted by the work item identifier and INFIELD (and possibly other values), add sequence numbers within the range of each infield

## $ML\_Core.Utils.Fat$

### **IMPORTS**

• ML\_Core.Types

### **DESCRIPTIONS**

### **FUNCTION**: Fat

DATASET(Types.NumericField)	Fat
(DATASET(Types.NumericField) d0, Types.t_FieldReal v=0)	

#### Up

Will take a potentially sparse file d and fill in the missing with value v for Numeric Field datasets

Parameter d0 || They myriad format Numeric Field dataset to be filled

Parameter v || The value to assign missing records

Return A full Numeric Field dataset with every field populated

## $ML\_Core.Utils.FatD$

### **IMPORTS**

• ML\_Core.Types

### **DESCRIPTIONS**

### FUNCTION: FatD

DATASET(Types.DiscreteField)	FatD
(DATASET(Types.DiscreteField) d0, Types.t_Discrete v=0)	

#### Up

Will take a potentially sparse file d and fill in the missing with value v for Discrete Field datasets

Parameter d0 || They myriad format Discrete Field dataset to be filled

Parameter v || The value to assign missing records

Return A full Discrete Field dataset with every field populated

## ML\_Core.Utils.Gini

### **IMPORTS**

### **DESCRIPTIONS**

#### MACRO: Gini

Gini

(infile, pivot, target, wi\_name='wi')

#### Up

Creates a file of pivot/target pairs with a Gini impurity value.

Parameter infile ||| the input file, any type with a work item field

Parameter pivot ||| the name of the pivot field

Parameter target ||| the name of the field used as the target

Parameter wi\_name ||| the name of the work item field, default is "wi" return A table by Work Item and Pivot value giving count and Gini impurity value

## ML\_Core.Utils.SequenceInField

#### **IMPORTS**

### **DESCRIPTIONS**

### MACRO: SequenceInField

SequenceInField
(infile,infield,seq,wi\_name='wi')

#### Up

Given a file which is sorted by the work item identifier and INFIELD (and possibly other values), add sequence numbers within the range of each infield. Slighly elaborate code is to avoid having to partition the data to one value of infield per node and to work with very large numbers of records where a global count project would be inappropriate. This is useful for assigning rank positions with the groupings.

Parameter infile ||| the input file, any type

Parameter infield ||| field name of grouping field

Parameter seq ||| name of the field to receive the sequence number

Parameter wi\_name || | work item field name, default is wi

**Return** a file of the same type with sequence numbers applied

### **PBblas**

Name	PBblas
Version	3.0.1
Description	Parallel Block Basic Linear Algebra Subsystem
License	http://www.apache.org/licenses/LICENSE-2.0
Copyright	Copyright (C) 2016, 2017 HPCC Systems
Authors	HPCCSystems
DependsOn	ML_Core
Platform	6.2.0

### Table of Contents

#### Apply2Elements.ecl

Apply a function to each element of the matrix Use PBblas. IElement Func as the prototype function

#### asum.ecl

Absolute sum – the "Entrywise" 1-norm

#### axpy.ecl

Implements alpha\*X + Y

#### Constants.ecl

#### Converted.ecl

Module to convert between ML\_Core/Types Field layouts (i.e.

#### ExtractTri.ecl

Extract the upper or lower triangle from the composite output from getrf (LU Factorization)

#### gemm.ecl

Extended Parallel Block Matrix Multiplication Module Implements: Result = alpha \* op(A)op(B) + beta \* C

#### getrf.ecl

LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks

#### HadamardProduct.ecl

Element-wise multiplication of X \* Y

#### IElementFunc.ecl

Function prototype for a function to apply to each element of the

#### MatUtils.ecl

Provides various utility attributes for manipulating cell-based matrixes

#### potrf.ecl

Implements Cholesky factorization of A = U\*\*T \* U if Triangular. Upper requested or A = L \* L\*\*T if Triangular. Lower is requested

#### scal.ecl

Scale a matrix by a constant Result is alpha \* X This supports a "myriad" style interface in that X may be a set of independent matrices separated by different work-item ids

#### tran.ecl

Transpose a matrix and sum into base matrix

#### trsm.ecl

Partitioned block parallel triangular matrix solver

#### Types.ecl

Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes

#### Vector2Diag.ecl

Convert a vector into a diagonal matrix

## PBblas.Apply2Elements

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS

### **DESCRIPTIONS**

### **FUNCTION: Apply2Elements**

DATASET(Layout_Cell)	Apply2Elements
(DATASET(Layout_Cell) X, IElementFunc f)	

#### Up

Apply a function to each element of the matrix Use PBblas. IElementFunc as the prototype function. Input and outure may be a single matrix, or myriad matrixes with different work item ids.

Parameter X | | A matrix (or multiple matrices) in Layout\_Cell form

 $\mathbf{Parameter}\ \ \mathbf{f}\ |||\ \mathbf{A}\ \mathbf{function}\ \mathbf{based}\ \mathbf{on}\ \mathbf{the}\ \mathbf{IElementFunc}\ \mathbf{prototype}$ 

Return A matrix (or multiple matrices) in Layout\_Cell form

See PBblas/IElementFunc

See PBblas/Types.Layout\_Cell

## PBblas.asum

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.BLAS

### **DESCRIPTIONS**

#### **FUNCTION**: asum

DATASET(Layout_Norm)	asum
(DATASET(Layout_Cell) X)	

#### Up

Absolute sum – the "Entrywise" 1-norm Compute SUM(ABS(X))

Parameter X | | Matrix or set of matrices in Layout\_Cell format

Return DATASET(Layout\_Norm) with one record per work item

See PBblas/Types.Layout\_Cell

## PBblas.axpy

### **IMPORTS**

- PBblas
- PBblas.Types

### **DESCRIPTIONS**

**FUNCTION**: axpy

DATASET(Layout_Cell)	axpy
(value_t alpha, DATASET(Layout_Cell) X, DATASET(Layout_Cell) Y)	

#### Up

Implements alpha\*X + Y X and Y must have same shape

Parameter alpha || || Scalar multiplier for the X matrix

Parameter X | | X matrix in DATASET(Layout\_Cell) form

Parameter Y | | Y matrix in DATASET(Layout\_Call) form

Return Matrix in DATASET(Layout\_Cell) form

See PBblas/Types.layout\_cell

### PBblas.Constants

### **IMPORTS**

### **DESCRIPTIONS**

**MODULE**: Constants

Constants

Up

Block\_Minimum | Block\_NoSplit | Block\_Maximum | Block\_Vec\_Rows | Dimension\_Incompat | Dimension\_IncompatZ | Distribution\_Error | Distribution\_ErrorZ | Not\_Square | Not\_SquareZ | Not\_PositiveDef | Not\_PositiveDefZ | Not\_Single\_Block | Not\_Single\_BlockZ | Not\_Block\_Vector | Not\_Block\_VectorZ |

### ATTRIBUTE: Block\_Minimum

Block\_Minimum

Up

### ATTRIBUTE: Block\_NoSplit

Block\_NoSplit

${ m Up}$
ATTRIBUTE : Block_Maximum
Block_Maximum
${ m Up}$
ATTRIBUTE : Block_Vec_Rows
Block_Vec_Rows
m Up
ATTRIBUTE : Dimension_Incompat
Dimension_Incompat
Up
ATTRIBUTE : Dimension_IncompatZ
Dimension_IncompatZ

Up

ATTRIBUTE : Distribution_Error	
Distribution_Error	
${ m Up}$	
ATTRIBUTE : Distribution_ErrorZ	
Distribution_ErrorZ	
Up	
ATTRIBUTE : Not_Square	
Not_Square	
${ m Up}$	
ATTRIBUTE : Not_SquareZ	
Not_SquareZ	
Up	
ATTRIBUTE : Not_PositiveDef	
Not PositiveDef	

Up
${\bf ATTRIBUTE: Not\_Positive Def Z}$
Not_PositiveDefZ
${ m Up}$
ATTRIBUTE : Not_Single_Block
Not_Single_Block
Up
ATTRIBUTE : Not_Single_BlockZ
Not_Single_BlockZ
Up
${\bf ATTRIBUTE: Not\_Block\_Vector}$

# Up

 $Not\_Block\_Vector$ 

### ${\bf ATTRIBUTE: Not\_Block\_Vector Z}$

Not_Block_VectorZ	
-------------------	--

Up

### PBblas.Converted

### **IMPORTS**

- PBblas
- PBblas.Types
- ML\_Core.Types

### **DESCRIPTIONS**

MODULE: Converted

Converted

Up

Module to convert between ML\_Core/Types Field layouts (i.e. NumericField and DiscreteField) and PBblas matrix layout (i.e. Layout\_Cell)

NFToMatrix | DFToMatrix | MatrixToNF | MatrixToDF |

#### **FUNCTION: NFToMatrix**

DATASET(Layout\_Cell) NFToMatrix
(DATASET(NumericField) recs)

Up

Convert NumericField dataset to Matrix

Parameter recs || Record Dataset in DATASET(NumericField) format

Return Matrix in DATASET(Layout\_Cell) format

See PBblas/Types.Layout\_Cell

 ${f See}$  ML\_Core/Types.NumericField

#### **FUNCTION: DFToMatrix**

DATASET(Layout_Cell)	DFToMatrix
(DATASET(DiscreteField) recs)	

#### Up

Convert DiscreteField dataset to Matrix

Parameter recs || Record Dataset in DATASET(DiscreteField) format

Return Matrix in DATASET(Layout\_Cell) format

See PBblas/Types.Layout\_Cell

See ML Core/Types.DiscreteField

#### **FUNCTION:** MatrixToNF

DATASET(NumericField)	MatrixToNF
(DATASET(Layout_Cell) mat)	

#### Up

Convert Matrix to NumericField dataset

Parameter mat || Matrix in DATASET(Layout\_Cell) format

Return NumericField Dataset

See PBblas/Types.Layout\_Cell

### **FUNCTION**: MatrixToDF

DATASET(DiscreteField)	MatrixToDF
(DATASET(Layout_Cell) mat)	

Up

Convert Matrix to DiscreteField dataset

Parameter mat || Matrix in DATASET(Layout\_Cell) format

Return DiscreteField Dataset

See PBblas/Types.Layout\_Cell

See ML\_Core/Types.DiscreteField

### PBblas.ExtractTri

### **IMPORTS**

- PBblas
- std.BLAS
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted

### **DESCRIPTIONS**

#### FUNCTION: ExtractTri

DATASET(Layout_Cell)	ExtractTri
(Triangle tri, Diagonal dt, DATASET(Layout_Cell) A)	

#### Up

Extract the upper or lower triangle from the composite output from getrf (LU Factorization).

Parameter tri || Triangle type: Upper or Lower (see Types.Triangle)

Parameter dt | Diagonal type: Unit or non unit (see Types.Diagonal)

Parameter A | | Matrix of cells. See Types.Layout\_Cell

**Return** Matrix of cells in Layout\_Cell format representing a triangular matrix (upper or lower)

See Std.PBblas.Types

1	9	n
T	o	U

## PBblas.gemm

#### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- std.BLAS
- PBblas.internal.MatDims
- $\bullet$  std.system.Thorlib

### **DESCRIPTIONS**

### FUNCTION: gemm

```
DATASET(Layout_Cell) gemm

(BOOLEAN transposeA, BOOLEAN transposeB, value_t alpha,
DATASET(Layout_Cell) A_in, DATASET(Layout_Cell) B_in,
DATASET(Layout_Cell) C_in=emptyC, value_t beta=0.0)
```

#### Up

Extended Parallel Block Matrix Multiplication Module Implements: Result = alpha \* op(A)op(B) + beta \* C. op is No Transpose or Transpose. Multiplies two matrixes A and B, with an optional pre-multiply transpose for each Optionally scales the product by the scalar "alpha". Then adds an optional C matrix to the product after scaling C by the scalar "beta". A, B, and C are specified as DATASET(Layout\_Cell), as is the Resulting matrix. Layout\_Cell describes a sparse matrix stored as a list of x, y, and value. This interface also provides a "Myriad" capability allowing multiple similar operations to be performed on independent sets of matrixes in parallel. This is done by use of the work-item id (wi\_id) in each cell of the matrixes. Cells with the same will dare considered part of the same matrix. In the myriad form,

each input matrix A, B, and (optionally) C can contain many independent matrixes. The wi\_ids are matched up such that each operation involves the A, B, and C with the same wi\_id. A and B must therefore contain the same set of wi\_ids, while C is optional for any wi\_id. The same parameters: alpha, beta, transposeA, and transposeB are used for all work-items. The result will contain cells from all provided work-items. Result has same shape as C if provided. Note that matrixes are not explicitly dimensioned. The shape is determined by the highest value of x and y for each work-item.

Parameter transposeA | Boolean indicating whether matrix A should be transposed before multiplying

Parameter transposeB ||| Same as above but for matrix B

Parameter alpha ||| Scalar multiplier for alpha \* A \* B

Parameter A\_in || 'A' matrix (multiplier) in Layout\_Cell format

Parameter B\_in || Same as above for the 'B' matrix (multiplicand)

Parameter C\_in || Same as above for the 'C' matrix (addend). May be omitted.

Parameter beta || A scalar multiplier for beta \* C, scales the C matrix before addition. May be omitted.

**Return** Result matrix in Layout\_Cell format.

See PBblas/Types.Layout\_Cell

## PBblas.getrf

#### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- std.BLAS
- PBblas.internal.MatDims
- std.system.Thorlib

### **DESCRIPTIONS**

FUNCTION: getrf

DATASET(Layout_Cell)	getrf
(DATASET(Layout_Cell) A)	

#### Up

LU Factorization Splits a matrix into Lower and Upper triangular factors Produces composite LU matrix for the diagonal blocks. Iterates through the matrix a row of blocks and column of blocks at a time. Partition A into M block rows and N block columns. The A11 cell is a single block. A12 is a single row of blocks with N-1 columns. A21 is a single column of blocks with M-1 rows. A22 is a sub-matrix of M-1 x N-1 blocks. | A11 A12 | | L11 0 | | U11 U12 | | A21 A22 | == | L21 L22 | \* | 0 U22 | | L11\*U11 L11\*U12 | == | L21\*U11 L21\*U12 + L22\*U22 | Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi\_id). Note: The returned matrix includes both the upper and lower factors. This matrix can be used directly by trsm which will only use the part

indicated by trsm's 'triangle' parameter (i.e. upper or lower). To extract the upper or lower triangle explicitly for other purposes, use the ExtractTri function. When passing the Lower matrix to the triangle solver (trsm), set the "Diagonal" parameter to "UnitTri". This is necessary because both triangular matrixes returned from this function are packed into a square matrix with only one diagonal. By convention, The Lower triangle is assumed to be a Unit Triangle (diagonal all ones), so the diagonal contained in the returned matrix is for the Upper factor and must be ignored (i.e. assumed to be all ones) when referencing the Lower triangle.

Parameter A ||| The input matrix in Types.Layout\_Cell format

Return Resulting factored matrix in Layout\_Cell format

See Types.Layout\_Cell

See ExtractTri

### PBblas.HadamardProduct

### **IMPORTS**

- PBblas
- PBblas.internal
- PBblas.internal.MatDims
- PBblas.Types
- PBblas.internal.Types
- PBblas.internal.Converted
- std.BLAS
- std.system.Thorlib

### **DESCRIPTIONS**

#### **FUNCTION**: HadamardProduct

DATASET(Layout_Cell)	HadamardProduct
(DATASET(Layout_Cell) X, DATASET(Layout_Cell) Y)	

#### Up

Element-wise multiplication of X \* Y. Supports the "myriad" style interface – X and Y may contain multiple separate matrixes. Each X will be multiplied by the Y with the same work-item id. Note: This performs element-wise multiplication. For dot-product matrix multiplication, use PBblas.gemm.

Parameter X || A matrix (or multiple matrices) in Layout\_Cell form

Parameter Y || A matrix (or multiple matrices) in Layout\_Cell form

 ${\bf Return}\,$  A matrix (or multiple matrices) in Layout\_Cell form

 ${\bf See}\ {\bf PBblas/Types.Layout\_Cell}$ 

## PBblas.IElementFunc

### **IMPORTS**

• PBblas

### **DESCRIPTIONS**

#### **FUNCTION: IElementFunc**

value_t	IElementFunc
(value_t v, dimension_t r, dimension_t c)	

#### Up

Function prototype for a function to apply to each element of the distributed matrix Base your function on this prototype:

Parameter v || Input value

Parameter r || Row number (1 based)

Parameter c || Column number (1 based)

Return Output value

See PBblas/Apply2Elements

## PBblas.MatUtils

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims

### **DESCRIPTIONS**

MODULE: MatUtils

MatUtils

Up

Provides various utility attributes for manipulating cell-based matrixes

See Std/PBblas/Types.Layout\_Cell

GetWorkItems | InsertCols | Transpose |

#### **FUNCTION**: GetWorkItems

DATASET(Layout_WI_ID)	GetWorkItems
(DATASET(Layout_Cell) cells)	

#### Up

Get a list of work-item ids from a matrix containing one or more work items

Parameter cells || A matrix in Layout\_Cell format

Return DATASET(Layout\_WI\_ID), one record per work-item

See PBblas/Types.Layout\_Cell

See PBblas/Types.Layout\_WI\_ID

### FUNCTION: InsertCols

DATASET(Layout_Cell)	InsertCols
(DATASET(Layout_Cell) insert_val=1)	M, UNSIGNED cols_to_insert=1, value_t

#### Up

Insert one or more columns of a fixed value into a matrix. Columns are inserted before the first original column. This attribute supports the myriad interface. Multiple independent matrixes can be represented by M.

Parameter M ||| the input matrix

Parameter cols\_to\_insert ||| the number of columns to insert, default 1

Parameter insert\_val || the value for each cell of the new column(s), default 0

**Return** matrix in Layout\_Cell format with additional column(s)

### **FUNCTION**: Transpose

DATASET(Layout_Cell)	Transpose
(DATASET(Layout_Cell) M)	

#### Up

Transpose a matrix This attribute supports the myriad interface. Multiple independent matrixes can be represented by M.

Parameter M || A matrix represented as DATASET(Layout\_Cell)

Return Transposed matrix in Layout\_Cell format

See PBblas/Types.Layout\_Cell

## PBblas.potrf

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.system.Thorlib

### **DESCRIPTIONS**

### **FUNCTION**: potrf

```
DATASET(Layout_Cell) potrf

(Triangle tri, DATASET(Layout_Cell) A_in)
```

#### Up

Implements Cholesky factorization of  $A = U^{**}T^*U$  if Triangular.Upper requested or  $A = L^*L^{**}T$  if Triangular.Lower is requested. The matrix A must be symmetric positive definite.

So, use Cholesky on the first block to get L11. L21 = A21\*L11\*\*T\*\*-1 which can be found by dtrsm on each column block A22' is A22 - L21\*L21\*\*T

Based upon PB-BLAS: A set of parallel block basic linear algebra subprograms by Choi and Dongarra

This module supports the "Myriad" style interface, allowing many independent problems to be worked on at once. The A matrix can contain multiple matrixes to be factored, indicated by different values for work-item id (wi\_id).

Parameter tri || Types. Triangle enumeration indicating whether we are looking for the Upper or the Lower factor

Parameter A\_in || The matrix or matrixes to be factored in Types.Layout\_Cell format

Return Triangular matrix in Layout\_Cell format

See Std.PBblas.Types.Layout\_Cell

See Std.PBblas.Types.Triangle

## PBblas.scal

### **IMPORTS**

- PBblas
- PBblas.Types

### **DESCRIPTIONS**

#### **FUNCTION**: scal

DATASET(Layout_Cell) scal	
(value_t alpha, DATASET(Layout_Cell) X)	

#### Up

Scale a matrix by a constant Result is alpha \* X This supports a "myriad" style interface in that X may be a set of independent matrices separated by different work-item ids.

Parameter alpha || A scalar multiplier

Parameter X ||| The matrix(es) to be scaled in Layout\_Cell format

Return Matrix in Layout\_Cell form, of the same shape as X

See PBblas/Types.Layout\_Cell

### PBblas.tran

### **IMPORTS**

- PBblas
- PBblas.Types
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.BLAS
- std.system.Thorlib

### **DESCRIPTIONS**

#### **FUNCTION**: tran

```
DATASET(Layout_Cell) tran

(value_t alpha, DATASET(Layout_Cell) A, value_t beta=0,
DATASET(Layout_Cell) C=empty_c)
```

#### Up

Transpose a matrix and sum into base matrix result  $\leq$  = alpha \* A\*\*t + beta \* C, A is n by m, C is m by n A\*\*T (A Transpose) and C must have same shape

Parameter alpha || || Scalar multiplier for the A\*\*T matrix

Parameter A || A matrix in DATASET(Layout\_Cell) form

Parameter beta || || Scalar multiplier for the C matrix

 $\textbf{Parameter} \ \ C \ ||| \ \ C \ \ matrix \ in \ \ DATASET(Layout\_Call) \ form$ 

See PBblas/Types.layout\_cell

### PBblas.trsm

### **IMPORTS**

- PBblas
- PBblas.Types
- std.BLAS
- PBblas.internal
- PBblas.internal.Types
- PBblas.internal.MatDims
- PBblas.internal.Converted
- std.system.Thorlib

### **DESCRIPTIONS**

#### FUNCTION: trsm

DATASET(Layout_Cell)	trsm
, , ,	LEAN transposeA, Diagonal diag, value_t alpha, A_in, DATASET(Layout_Cell) B_in)

#### Up

Partitioned block parallel triangular matrix solver. Solves for X using: AX = B or XA = B A is is a square triangular matrix, X and B have the same dimensions. A may be an upper triangular matrix (UX = B or XU = B), or a lower triangular matrix (LX = B or XL = B). Allows optional transposing and scaling of A. Partially based upon an approach discussed by MJ DAYDE, IS DUFF, AP CERFACS. A Parallel Block implementation of Level-3 BLAS for MIMD Vector Processors ACM Tran. Mathematical Software, Vol 20, No 2, June 1994 pp 178-193 and other papers about PB-BLAS by Choi and Dongarra This module supports the "Myriad" style interface, allowing many independent problems to be worked on

at once. Corresponding A and B matrixes are related by a common work-item identifier (wi\_id) within each cell of the matrix. The returned X matrix will contain cells for the same set of work-items as specified for the A and B matrices.

**Parameter** s | | Types. Side enumeration indicating whether we are solving AX = B or XA = B

**Parameter** tri ||| Types. Triangle enumeration indicating whether we are solving an Upper or Lower triangle.

Parameter transposeA || Boolean indicating whether or not to transpose the A matrix before solving

Parameter diag ||| Types. Diagonal enumeration indicating whether A is a unit matrix or not. This is primarily used after factoring matrixes using getrf (LU factorization). That module produces a factored matrix stored within the same space as the original matrix. Since the diagonal is used by both factors, by convention, the Lower triangle has a unit matrix (diagonal all 1's) while the Upper triangle uses the diagonal cells. Setting this to UnitTri, causes the contents of the diagonal to be ignored, and assumed to be 1. NotUnitTri should be used for most other cases.

Parameter alpha || Multiplier to scale A

Parameter A\_in || The A matrix in Layout\_Cell format

Parameter B\_in || The B matrix in Layout\_Cell format

Return X solution matrix in Layout\_Cell format

See Types.Layout\_Cell

See Types.Triangle

See Types.Side

## PBblas.Types

### **IMPORTS**

- ML\_Core
- ML\_Core.Types

### **DESCRIPTIONS**

MODULE: Types

Types

#### Up

Types for the Parallel Block Basic Linear Algebra Sub-programs support WARNING: attributes marked with WARNING can not be changed without making corresponding changes to the C++ attributes.

 $\label{local_dimension_t} $$ dimension_t \mid partition_t \mid work\_item\_t \mid value\_t \mid m\_label\_t \mid Triangle \mid Diagonal \mid Side \mid t\_mu\_no \mid Layout\_Cell \mid Layout\_Norm \mid $$$ 

### ATTRIBUTE : dimension\_t

dimension t

#### Up

Type for matrix dimensions. Uses UNSIGNED four as matrixes are not designed to support more than 4 B rows or columns.

$\mathbf{AT}$	$egin{array}{ll}  ext{TRIBUTE}:  ext{partition\_t} \end{array}$
I	artition_t
Up	
	e for partition id – only supports up to 64K partitions
$\mathbf{AT}$	$egin{array}{ll} \Gamma RIBUTE: work\_item\_t \end{array}$
V	vork_item_t
Up Type	$_{ m e}$ for work-item id – only supports up to 64K work items
	$egin{array}{ll} \mathbf{TRIBUTE: value\_t} \ & \mathbf{raine\_t} \ & raine\_$
Up Type	e for matrix cell values WARNING: type used in C++ attribute

Up

 $m\_label\_t$ 

 $ATTRIBUTE: m\_label\_t$ 

Type for matrix label. Used for Matrix dimensions (see Layout_Dims) and for partitions (see Layout_Part)
ATTRIBUTE : Triangle
Triangle
$\mathrm{Up}$
Enumeration for Triangle type WARNING: type used in C++ attribute
ATTRIBUTE : Diagonal
Diagonal
${ m Up}$
Enumeration for Diagonal type WARNING: type used in C++ attribute
ATTRIBUTE : Side
Side
$\mathrm{Up}$
Enumeration for Side type WARNING: type used in C++ attribute
ATTRIBUTE : t_mu_no
t_mu_no

#### Up

Type for matrix universe number Allow up to 64k matrices in one universe

#### RECORD: Layout\_Cell

Layout\_Cell

#### Up

Layout for Matrix Cell Main representation of Matrix cell at interface to all PBBlas functions. Matrixes are represented as DATASET(Layout\_Cell), where each cell describes the row and column position of the cell as well as its value. Only the non-zero cells need to be contained in the dataset in order to describe the matrix since all unspecified cells are considered to have a value of zero. The cell also contains a work-item number that allows multiple separate matrixes to be carried in the same dataset. This supports the "myriad" style interface that allows the same operations to be performed on many different sets of data at once. Note that these matrixes do not have an explicit size. They are sized implicitly, based on the maximum row and column presented in the data. A matrix can be converted to an explicit dense form (see matrix\_t) by using the utility module MakeR8Set. This module should only be used for known small matrixes (< 1M cells) or for partitions of a larger matrix. The Converted module provides utility functions to convert to and from a set of partitions (See Layout\_parts).

Field wi\_id || Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

Field x || 1-based row position within the matrix

Field y | | 1-based column position within the matrix

Field v | | Real value for the cell

See matrix t

See Std/PBblas/MakeR8Set.ecl

See Std/PBblas/Converted.ecl WARNING: Used as C++ attribute. Do not change without corresponding changes to MakeR8Set.

### $RECORD: Layout\_Norm$

Layout\_Norm

### Up

Layout for Norm results.

**Field** wi\_id ||| Work Item Number – An identifier from 1 to 64K-1 that separates and identifies individual matrixes

 ${f Field}\ {f v}\ |||\ {f Real}\ {f value}\ {f for\ the\ norm}$ 

## PBblas.Vector2Diag

### **IMPORTS**

- PBblas
- PBblas.internal
- PBblas.internal.MatDims
- PBblas.Types
- PBblas.internal.Types
- PBblas.Constants

### **DESCRIPTIONS**

#### FUNCTION: Vector2Diag

DATASET(Layout_Cell)	Vector2Diag
(DATASET(Layout_Cell) X)	

#### Up

Convert a vector into a diagonal matrix. The typical notation is D = diag(V). The input X must be a 1 x N column vector or an N x 1 row vector. The resulting matrix, in either case will be N x N, with zero everywhere except the diagonal.

Parameter X || A row or column vector (i.e. N x 1 or 1 x N) in Layout\_Cell format

Return An N x N matrix in Layout Cell format

See PBblas/Types.Layout\_cell