THE VEDIC NAKSATRAS – A REAPPRAISAL

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In the calendar of Vedānga Jyotisa the position of the sun and the moon is identified by a lunar mansion (or a sector of the ecliptic) and the distance from the leading edge of this sector (bhāmśa). It has been generally accepted that the position and the extent of these lunar mansions are defined by the naksatras (background stars and asterisms). In this paper it is shown that the jāvādi arrangement of naksatras, given in Vedānga Jyotisa, defines an invariant frame of reference that is anchored to the ecliptic and not to the background stars. Fixed and absolute coordinates of the lunar mansions or naksatra-sectors can be determined within this frame of reference. Unlike all previous determinations of coordinates of *naksatra*-sectors, these coordinates are independent of the stellar coordinates found in the post-Vedic texts like Paitāmahasiddhānta. In the coordinate system defined by the jāvādi arrangement of naksatras, the position of the sun and the moon is also independent of the coordinates of the background stars. This analysis suggest that between 2000 BC and 1500 BC the Vedic New Year started in spring.

Key words: *Jāvādi* arrangement, *Nakṣatras*, *Vedānga Jyotiṣa*, Vedic New Year.

1. Introduction

In the Vedic texts the word *nakṣatra* indicates both a star (and an asterism) and a lunar mansion. The moon is supposed to conjoin each night with the twenty-seven (sometimes twenty-eight) *nakṣatras* (stars or asterisms) or reside in the twenty-seven lunar mansions. It is very likely that the mansions were identified by nearby stars. It is impossible to identify the origins of *nakṣatras* or their identification by stars but some names, which appear in the lists of *nakṣatras* given in the later

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Saṃhitās and the Brāhmaṇas, can be traced back to the earliest Vedic text – Rgveda Saṃhitā (RV). In addition, statements like "soma is stationed in the vicinity of nakṣatra" (RV.X.85.2) suggests that even in this early text the position of the moon in the sky may have been defined by reference to the stars. Pioneering work on Vedic nakṣatras was done in the nineteenth century 1,2,3,4 but most of this work is based on interpretation of nakṣatras as stars or asterism. This discussion has been one-sided possibly because the stars were seen to provide the only possible fixed (and absolute) frame of reference against which the motion of the moon could be observed and calibrated. The Vedic texts have aided and abetted this one-sided discussion by not distinguishing between the lunar mansions and their stellar markers. To avoid the confusion caused by the dual use of the word nakṣatra, in this paper, the stars and asterisms are referred to as 'nakṣatras' and the lunar mansions are referred to as 'nakṣatra-sectors'.

The identification of stars and asterisms of the *nakṣatras* is fraught with difficulties and uncertainties. The Vedic texts provide little or no information to identify the stellar markers; neither relative position nor the shape of an asterism are given. The number of stars in each *nakṣatra* is of some help, that is, *nakṣatras* whose names are dual probably have two stars and plural names suggest a group of stars. In South Asia, coordinates of stars are only given in astronomical texts produced after fifth century AD. The oldest catalogue of coordinates of one (prominent) star, the yogatārā of the nakṣatra, is given in the Paitāmahasiddhānta of the Visnudharmottarapurāna. The provenance of this text is disputed^{5,6} but that is of no concern here. Suffice it to say that there is a gap of over a thousand years between the Vedic texts and this catalogue of coordinates. This gap should be borne in mind in arriving at conclusions based on the coordinates of the yogatārās. All attempts till date to identify the nakṣatras and their yogatārās are based either explicitly or implicitly on the coordinates given in the Paitāmahasiddhānta and the siddhānta is silent on the procedure by which these coordinates were obtained. Moreover, these coordinates – polar longitude and latitude – are very inaccurate; they are mostly expressed as integer degrees.

The lists of *nakṣatras* given in one of the earliest *Saṃhitā* and *Vedānga Jyotiṣa* (a text of the late Vedic period) are given in Table 1. These lists are broadly similar but differ in detail; the names and the number of *nakṣatras* differ from list to list but every list in the Vedic texts starts with *kṛttikās*. Twenty-seven *nakṣatras* are common to all lists; the *nakṣatra* left out is *Abhijit*. The stellar counterparts, in modern astronomical catalogues, of *yogatārās* were

	MS II.13.20	VJ RJ.25-28		MS II.13.20	VJ RJ.25-28
1	Kṛttikâs	Kṛttikâs	15	Anūrâdhâ	Anurâdhâs
2	Rohini	Rohinī	16	Jyesthâ	Jyesthâ
3	Invaka	Mṛgaśirṣa	17	Mūla	Mūla
4	Bâhu	Ârdrâ	18	Âsâdhâs	Pūrvâ Âsâdhâs
5	Punarvasus	Punarvasus	19	Âs âdh âs	Uttrâ Âsâdhâs
6	Tisya	Pusya		Abhijit	·
7	Âśresâs	Âśresâs	20	Śronâ	Śronâ
8	Maghâs	Maghâs	21	Śravisthâs	Śravisthâs
9	Phalgunis	Phalgunis	22	Śatabhisaj	Śatabhisaj
10	Phalgunis	Phalgunis	23	Prosthapadas	Pūrva-Prosthapadas
11	Hasta	Hasta	24	Prosthapadas	Uttara-Prosthapadas
12	Citrâ	Citrâ	25	Revati	Revati
13	Nistyâ	Svâti	26	Aśvayuj	Aśvayujau
14	Viśâkhâs	Viśâkhâs	27	Bharaṇis	Bharanis

Table 1. List of naksatras in one of the earliest Samhitâs and a late Vedic text

MS - Maitrâyanīya Samhitâ

VJ - Vedânga Jyotişa

RJ - Rgveda recension

identified in the late nineteenth century and recently these attempts have been reassessed and refined^{5,7}. In this paper, an attempt is made to determine the absolute coordinates of the *nakṣatra*-sectors without an appeal to *Paitāmahasiddhānta*. This procedure has the advantage that the conclusions are based only on the Vedic texts and are not affected by the corrupt and inaccurate intrusions in the South Asian astronomy and calendric system from times far removed from the Vedic period. In Section 2 the *jāvādi* arrangement of *nakṣatras* in *Vedān ga Jyotiṣa* is discussed and derived. In Section 3 the equatorial and ecliptic coordinates of the *nakṣatra*-sectors are derived and the discussion of the results and conclusions are given in Section 4.

2. The *Jāvādi* arrangement of *nakṣatras*

The *Vedānga* (arm or limb of the Veda) *Jyotiṣa* (*VJ*) is the earliest South Asian text devoted exclusively to the calendar. The text is a manual for determining the proper times for Vedic ceremonies. This text has survived in two recensions – a *Rgveda* recension (*RJ*) called *Arca-Jyotiṣa* and a *Yajurveda* recension (*YJ*) called *Yājuṣa-Jyotiṣa*. The *Rgveda* recension is considered to be the older of the two recensions. The differences between the two recensions are small and of no relevance to this paper. The verses in the text do not follow a thematic or logical order and verses on similar topics are scattered in different parts of the text. This

Table 2. The jâvâdi arrangement of naksatra

	Abbrev- iations	nakṣatra		Abbrev- iations	nakṣatra
1	jau	aśvayu jau (aśvin i)	14	mâ	Arya mâ uttraphâlguṇis
2	drâ	âr drâ	15	dhâḥ	anurâ dhâh
3	gah	bha gaḥ (pūrvaphâlgunis)	16	n ah	śrava nah
4	khe	viśâ khe	17	re ·	re vatī
5	śve	viś ve devâh uttarâṣâḍhâs	18	mr	mrgasirsa
6	hih	a hir budhnyah	19	ghâh	ma ghâh
	•	(uttra prostapadâs)		•	•
7	ro	ro hinī	20	svâ	svâ tī
8	s â	âśre șâ	21	pah	â pah (puvâṣâdhâs)
9	cit	cit râ	22	jah	a ja ejapât
				•	(pūrva prostapadâs)
10	$m\bar{u}$	mū la	23	kr	kr ttikâs
11	sa	śatabhi sa j	24	syah	pu syah
12	n yah	bhara nyah	25	ha .	ha sta
13	$s\bar{u}$	punarva sū	26	jye	jye şthâ
		-	27	sthâh	śravi sthâh

suggests that the present versions of VJ are not the original versions. VJ came to the attention of early Indologists like Sir William Jones and in the nineteenth and twentieth century various attempts, of varying degree of success, were made to interpret it 8,9,10,11,12 . In 1979 a complete interpretation and translation of VJ was produced and this, along with the critical editions of both the Rgvedic and Vajurvedic recensions (from twenty manuscripts) was published in 1984 by the Indian National Science Academy¹³. The discussion in this paper is based on this edition and translation of VJ.

The calendar of *VJ* is based on an 'intercalation period' of 1830 days or five tropical years of 366 days each. This intercalation period is called a *yuga*. This period is synchronized with five synodic years by intercalating two synodic months, that is, the intercalated 'synodic *yuga*' is composed of sixty-two synodic months (i.e. 1830.86 days). This intercalation period starts every five years around winter solstice "when the sun and the moon are in the *nakṣatra* Śraviṣṭhās" (*RJ*.5-6 – verses #5-6 in the *R̄gveda* recension, *YJ*.6-7 – verses #6-7 in the *Yājuṣa* recension) i.e. when the new moon is in *nakṣatra* Śraviṣṭhās around winter solstice. Two lists of *nakṣatras* are given in *VJ*; in *RJ*.25-28 and *YJ*.32-35 a list of *nakṣatras* is identified by their presiding deity. This list is very similar

to the lists of *nakṣatras* given in the earlier *Saṃhitās* and the *Brāhmaṇas* and is reproduced in Table 1. In *RJ*.14 and *YJ*.18, *VJ* introduces a different list of *nakṣatras* identified by either an abbreviation of the name of the *nakṣatra* or an abbreviation of the name of the presiding deity of the *nakṣatra*. This arrangement of the *nakṣatras* is called the " $j\bar{a}v\bar{a}di$ (jau $\bar{a}di$ beginning with jau) arrangement". In *RJ*.18, *YJ*.39, *VJ* states that the sun stays in each *nakṣatra* 13 and $^{5}/_{9}$ days. These verses unambiguously state that in *VJ* a *nakṣatra* is not considered to be a star or an asterism but a sector of the ecliptic and this sector is 13.33° wide. There is also an implicit assumption here that all sectors are of equal width.

The *jāvādi* arrangement of *nakṣatras* is given in Table 2; the abbreviation, as given in *VJ*, are given in columns #2 and #5 and the *nakṣatra* or the deity and the *nakṣatra* are given in columns #3 and #6 and the *VJ* abbreviations are highlighted in these names. *VJ* does not give the scheme or the algorithm used to obtain this arrangement. An inspection of the list of *nakṣatras* in Table1 and the list in the *jāvādi* arrangement (Table 2.) suggests that the *nakṣatras* in the arrangement are every fifth *nakṣatra* from Table 1 starting from Śraviṣṭhās (*nakṣatra* number #21). That is, Śraviṣṭhās is assumed to be *nakṣatra* number #0 and the fifth *nakṣatra* is *Aśvayujau* and the fifth after that is *Ārdrā* and so on to choose twenty-seven *nakṣatras*. This of course prompts the question, why choose every fifth *nakṣatra*. A pedestrian answer could be "the Āryan predilection for numbers five"! A rational explanation for the choice of *nakṣatras* of the *jāvādi* arrangement is likely to be as follows. This derivation was presented and discussed by Thibaut ¹⁴, it is reproduced here to make more comprehensible the derivation of the absolute coordinates of *nakṣatra*(-sectors) that follows.

In a yuga (the five year Vedic intercalation period) there are

62 lunations/lunar months

67 sidereal months (both these numbers are given in the VJ)

Therefore, in 1 lunation there are 67÷62 sidereal months

Or 1 lunation = $1^{5}/_{62}$ sidereal months

In a sidereal month the moon passes by 27 nakṣatras

Therefore in 1 lunation the moon passes by $27 \times 1^{5}/_{62}$ nakṣatras

 $= 29^{22}/_{124}$ naksatras

Thus the separation of successive new (or full) moons is $29^{22}/_{124}$ nakṣatras. And the separation between a new and full (or full and new) moon (or a pakṣa) is $14^{73}/_{124}$ nakṣatras.

To obtain the jāvādi arrangement of nakṣatra-sectors an 'origin' from which the *nakṣatra* of a full or a new moon is counted is required. As discussed above, the VJ yuga commences with new moon in Śravisthās (around winter solstice) and this is the origin for $j\bar{a}v\bar{a}di$ arrangement. Thus starting from new moon in Śravisthās, it is possible to obtain the *nakṣatra*-sectors at successive full moons and new moons in a *yuga* by the scheme given above; the *nakṣatras* are from the list of *naksatras* in Table 1. For example, the *naksatra*-sector of the first full moon after the start of a yuga will be the fourteenth nakṣatra counted from Śravisthās. If the *nakṣatra*-sector is divided into 124 parts then the first full moon will be in the 73rd part of the fourteenth *nakṣatra*-sector. Similarly, the first new moon after the start of a yuga will be in the 22nd part of the twenty-ninth nakṣatra-sector. However, there are only twenty-seven nakṣatras-sector therefore this new moon will be in the (29 - 27) or the second *nakṣatra*-sector. The division of the *nakṣatra*-sector into 124 parts is implicit in VJ and each part is called a *bhāmśa*, but an explicit definition of a *bhāmśa* is not given in *VJ*. The nakṣatras-sector of the new moon and full moon (and the location of the moon within a *nakṣatras*-sector in terms of the number of *bhāṃśas*) of the sixty-two lunations of a yuga are given in Table 3. These nakṣatra-sectors and bhāṃśas are obtained by assuming that the 'length' of a synodic month is $29^{22}/_{124}$ naksatras i.e. 29.52502 days (the modern value for the mean length of the synodic month is 29.53059 days). The *nakṣatras*-sectors of the $j\bar{a}v\bar{a}di$ arrangement are selected from this list of new-moon and full-moon *nakṣatras*-sectors. The *nakṣatras*sector when the moon is in the first twenty-seven bhāmśa are selected (the sequence of *nakṣatra*-sectors repeats after the twenty-seventh *nakṣatra*sector) for the arrangement, these *nakṣatra*-sectors are highlighted in Table 3. Equivalently the position of a *nakṣatra*-sector in the *jāvādi* arrangement is given by X where

$$B \equiv X \text{ modulo } (27)$$

where B is the *bhāṃśa* given in Table 3. For example, the first full moon of a *yuga* is in the *nakṣatra*-sector Maghā at *bhāṃśa* #73, then the position of *nakṣatra*-sector Maghā in the *jāvādi* arrangement, by the above equation

Table 3. The bhâmśa and the nakṣatra at new moon and full moon of sixty-two synodic months of a yuga. The jâvâdi arrangement of naksatras is high-lighted

No:	io: Ne		New moon		Full moon		No:	New moon		Full moon			
	#1	#2	#3	#1	#2	#3		#1	#2	#3	#1	#2	#3
1	0	0	śravisthâ	14	73	maghâ	32	13	62	âślesâ	1	11	śatabhisaj
2	2	22	p. prostapadâ	16	95	u. phâlguṇ̄i	33	15	84	p. phâlguṇi	3	33	u. prostapadâ
3	4	44	revati	18	117	citrâ	34	17	106	hasta	5	55	asvayujau
4	6	66	bharaṇi	21	15	anurâdhâ	35	20	4	viśâkhe	7	77	kṛttikâ
5	8	88	rohini	23	37	mūla	36	22	26	jyeṣṭhâ	9	99	mṛgasirsa
6	10	110	ârdrâ	25	59	u. âṣâdhâ	37	24	48	p. âṣâdhâ	11	121	punarvasū
7	13	8	âśleṣâ	0	81	śravisthâ	38	26	70	śravana	14	19	maghâ
8	15	30	p. phâlgunī	2	103	p. prostapadâ	39	1	92	śatabhisaj	16	41	u. phâlgunī
9	17	52	hasta	5	1	asvayujau	40	3	114	u. prostapadâ	18	63	citrâ
10	19	74	svâti	7	23	krttikâ	41	6	12	bharaṇi	20	85	viśâkhe
11	21	96	anurâdhâ	9	45	mrgasirsa	42	8	34	rohini	22	107	jyesthâ
12	23	118	mūla	11	67	punarvasū	43	10	56	ârdrâ	25	5	u. âsâdhâ
13	26	16	śravaņa	13	89	âślesâ	44	12	78	pusya	0	27	śravisthâ
14	1	38	śatabhisaj	15	111	p. phâlgunī	45	14	100	maghâ	2	49	p. prostapadâ
15	3	60	u. prostapadâ	18	9	citrâ	46	16	122	u. phâlguṇi	4	71	revati
16	5	82	asvayujau	20	31	viśâkhe	47	19	20	svâtī	6	93	bharaṇī
17	7	104	krttikâ	22	53	jyesthâ	48	21	42	anurâdhâ	8	115	rohini
18	10	2	ârdrâ	24	75	p. âsâdhâ	49	23	64	mūla	11	13	punarvasu
19	12	24	puṣya	26	97	śravana	50	25	86	u. âsâdhâ	13	35	âślesâ
20	14	46	maghâ	1	119	śatabhisaj	51	0	108	śravisthâ	15	57	p. phâlguṇ̄i
21	16	68	u. phâlguṇ̄i	4	17	revatī	52	3	6	u. prostapadâ	17	79	hasta
22	18	90	citrâ	6	39	bharaṇi	53	5	28	asvayujau	19	101	svâtī
23	20	112	viśâkhe	8	61	rohini	54	7	50	krttikâ	21	123	anurâdhâ
24	23	10	mūla	10	83	ârdrâ	55	9	72	mrgasirsa	24	21	p. âsâdhâ
25	25	32	u. âsâdhâ	12	105	pusya	56	11	94	punarvasū	26	43	śravana
26	0	54	śravisthâ	15	3	p. phâlguṇī	57	13	116	âślesâ	1	65	śatabhisak
27	2	76	p. prostapadâ	17	25	hasta	58	16	14	u. phâlguṇā	3	87	u. prostapadâ
28	4	98	revati	19	47	svâtī	59	18	36	citrâ	5	109	asvayujau
29	6	120	bharani	21	69	anurâdhâ	60	20	58	viśâkhe	8	7	rohini
30	9	18	mrgasirsa	23	91	mūla	61	22	80	jyesthâ	10	29	ârdrâ
31	11	40	punarvasū	25	113	u. âsâdhâ	62	24	102	p. âsâdhâ	12	51	pusya

#1: nakṣatra number as counted from śraviṣṭhâ, see Table 1; #2: bhâmśa of the new and full moon; #3. nakṣatra

 $(73 \div 27 \text{ remainder } 19)$ is at #19 as given in Table 2. The *bhāṃśas* of the new and full moons in Table 3 can similarly be 'reduced' to obtain the position of the *nakṣatra*-sector of the moon in the $j\bar{a}v\bar{a}di$ arrangement. The *nakṣatra*-sectors of the jāvādi arrangement are rearranged in Table 4 to demonstrate that, as stated above, the selected *nakṣatra*-sectors are the *nakṣatra*-sector of the full moon and the new moon in the first twenty-seven *bhāṃśas* following the new moon in Śravisthās at the start of a *yuga*. It is not entirely clear why the composer(s) of VJ chose to arrange the *nakṣatra*-sectors of the $j\bar{a}v\bar{a}di$ arrangement in the bhāmśa sequence. The jāvādi arrangement or the derivation of the jāvādi arrangement emphasises the primary usage of the word *nakṣatra* in the calendric system of VJ – the *nakṣatras* are wide sectors of the ecliptic and are evenly distributed along the path of the moon or they are *nakṣatra*-sectors and these are anchored to the ecliptic and are independent of the background stars. Since every yuga starts around winter solstice when the new moon is in naksatra Śravisthās, the *nakṣatra*-sectors (and the *bhāṃśas*) define the fixed (and absolute) position of the full moon and new moon in every yuga. In other words, the $j\bar{a}$ *vādi* arrangement defines a coordinate system along the ecliptic with the origin around winter solstice when the new moon is in naksatra Śravisthās.

Table 4. The jāvādi arrangement of naksatra arranged in the bhāmśa sequence

					<u> </u>
	Full M	loon		New M	oon
N	В	nakṣatra	N	В	nakṣatra
9	1	âsvayujau	18	2	ârdrâ
26	3	p. phâlguṇ̄i	35	4	viśâkhâ
43	5	u. âsâdhâ	52	6	u. prostapada
60	7	rohini	7	8	âśleşâs
15	9	citrâ	24	10	mūlâ
32	11	śatabhisaj	41	12	bharan ya
49	13	punarvasu	58	14	u. phâlgunī
4	15	anurâdhâ	13	16	śravana
21	17	revatī	30	18	mrgasirsa
38	19	maghâ	47	20	svâti
55	21	p. âṣâdhâ	2	22	p. prostapada
10	23	krttikâ	19	24	pusya
17	25	hasta	36	26	jyesthâ
44	27	śravisthâ			

N – Full moon and new moon number from Table 3;

B – bhāmśa

3. Naksatras – absolute coordinates of lunar mansions

The *jāvādi* arrangement (and the procedure to obtain the arrangement) gives the location of the (new and full) moon in a *nakṣatra*-sector and if the (ecliptic or equatorial) coordinates of the moon are determined then the (ecliptic or equatorial) coordinates of a point in the *nakṣatra*-sector are established. The coordinates of the full moons in a *yuga* are determined as follows;

- Determine the date(s) of the new-moon at or around winter solstice.
- Determine the separation in days between the new moon at winter solstice and the following full moons in a *yuga*.
- Convert the separation to coordinates of the full-moon. The reference frame for this conversion is the standard reference frame with the origin at the first point of Aries.
- The *nakṣatra*-sector of this full-moon is given by the scheme for *jāvādi* arrangement and is given in Table 3.

The currently used zero point (the first point of Aries) is used to obtain the coordinates of the full moon because the origin that may have been used by the Āryas is not known. However, as will be shown below, the Āryas may have (unwittingly) used the vernal equinox as the origin. Two procedures have been followed to determine the coordinates of the full moons in a yuga. In the first method, the dates of the new moon at or within one day of the winter solstice between 1900 AD and 2000 AD were obtained from the available calendars. The dates of the sixty-two full moons following each of these new-moons were also obtained from these calendars. In the second method, the dates of the new moon at or within one day of the winter solstice between 1500 BC and 500 BC were obtained by first calculating the dates of the winter solstice, that is, dates of minimum declination of the sun each year. The separation between the sun and the moon was calculated for each date and the dates when the separation was within five degree (i.e. the sun and the moon were in conjunction) were retained. These dates were considered to be the dates of the new moon at winter solstice. For each new moon date the following sixty-two dates when the sun and the moon were in opposition (i.e. about 180° apart or full moon) were determined, these were considered to be the dates of the full moons of a yuga. For both methods, the dates determined were in Julian days and for the second method the currently available orbital parameters of the earth and moon were used. The separation

between the new moon at winter solstice and the following full moons was converted to equatorial and ecliptic coordinates. For the two periods considered, the coordinates for each full moon in a yuga were averaged to obtain the spread (root mean square deviation) in the mean value. The full moon number, the corresponding nakṣatra-sector, bhāmśa and the ecliptic and the equatorial coordinates of the moon determined for the 1500 BC to 500 BC period, are given in Table 5. The computed nakṣatra-sector and the bhāmśa at each full moon can be compared with the corresponding parameters given in Table 3, the match between the *nakṣatra*-sectors is prefect but the *bhāṃśas* differ. This is because in computing the *nakṣatra*-sectors and the *bhāṃśas* of Table 3 a fixed value (the mean length) of the synodic month was used but in the computations for the period of 1500 BC to 500 BC the length of the synodic month varies (slightly) because of the changes in the speed of the moon in its orbit. The mean ecliptic coordinates of the first twelve full moons in a yuga determined for both the 1500 BC to 500 BC period and for the 1900 AD to 2000 AD period are plotted in Fig. 1. It is important to emphasise that the coordinates determined and given in Table 5 are the coordinates of the (full) moon; the *nakṣatra*-sector of the moon is obtained from the procedure followed to obtain the $j\bar{a}v\bar{a}di$ arrangement

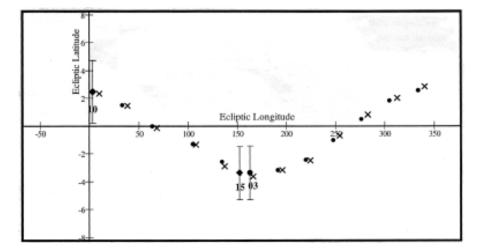


Fig. 1. The ecliptic longitude and latitude of first twelve full-moons of a *yuga*. The 'lay-out' of the positions of all subsequent full moons of the *yuga* will be similar but slightly shifted to the left. The data obtained for the 1500 BC to 500BC period are shown by crosses and the data for 1900 AD to 2000 AD period are shown by dots. To avoid crowding only representative error bars are shown. The *nakṣatra* of full moon #10 is Kṛttikās. The *nakṣatra* of full-moon #3 and #15 is *Citrā*.

Table 5. Ecliptic and equatorial coordinates of the first twenty-seven full moons of a *yuga* and their respective *nakṣatras* or lunar mansions. The equatorial coordinates of the centre of the *nakṣatra*-sectors are given and for comparison the coordinates of the *yogatârâs* determined by Pingree and Morrissey (1989) and Abhyankar (1991) are included

			1	E-11		C = -	C n-s P & M (1989)			A (1991)		
			11 - /	Full-moon c		C n-s			· · · · · · · · · · · · · · · · · · ·			
	nakṣatra	FM	bhāṃśa	L	α	α	α	mag	α	mag		
				В	δ	δ	δ J(2000)		δ J(2000)			
1	Krttikâ	10	3	3.22 ± 0.72	1.96±1.26	00 35 48+	03 47 29	2.87	03 47 29	2.87		
	•			2.45 ± 2.24	3.54±1.99	04 45 04	+24 06 18		+24 06 18			
2	Rohini	23	55	22.20±0.61	20.01±1.53	01 28 09+	04 35 55+	0.85	04 35 55+	0.85		
	•			1.21±3.16	9.90±2.85	07 37 34	16 30 33		16 30 33			
3	Mrgaśirsa	11	37	33.28 ± 0.87	30.44±1.66	02 17 16	05 35 08	3.66	05 35 08	3.66		
				1.50±3.03	14.20±2.71	+12 55 11	+09 56 03		+09 56 03			
4	Ârdrâ	24	90	52.37±0.61	49.98±1.33	03 13 42	05 55 10	0.50	06 37 42	1.93		
				-0.43 ± 3.41	18.23±3.23	+14 56 33	+07 24 25		+16 23 57			
5	Punarvasu	12	72	63.61±0.70	61.51±1.31	04 6 13	07 45 19	1.15	07 45 19	1.15		
				-0.01 ± 3.40	21.19±3.26	+18 14 24	+28 01 34		+28 01 34			
6	Pusya	25	1	82.58 ± 0.75	82.02±0.91	05 02 58	08 44 41	3.94	08 44 41	3.94		
	•			-2.01 ± 2.90	21.60±2.89	+19 18 55	+18 09 15		+18 09 15			
7	Âślesâ	13	104	93.65 ± 0.82	93.93±0.82	05 59 23	08 46 47	3.38	08 55 23	3.11		
	•			-1.67 ± 3.12	22.10±3.15	+19 58 45	+06 25 08		+05 56 44			
8	Mâgha	1	81	104.72 ± 0.75	105.87±0.63	06 53 46	10 08 23	1.35	10 08 23	1.35		
				-1.31 ± 3.26	21.69±3.30	+19 33 36	+11 58 02		+11 58 02			
9	Purva	14	7	123.42 ± 0.90	125.08±0.82	07 50 35	11 14 06	2.56	11 14 06	2.56		
	Phâlguni			-2.93 ± 2.32	16.84±2.37	+17 37 18	+20 31 25		+20 31 25			
10	Uttra _	2	104	134.14 ± 0.82	135.91±0.72	08 43 07	11 49 04	2.14	11 49 04	2.14		
	Phâlguni			-2.62 ± 2.57	14.33±2.62	+14 36 46	+14 34 19		+14 34 19			
11	Hasta	27	55	141.92±0.97	143.22±1.23	09 35 31	12 29 52	2.95	12 15 48	2.59		
				-3.45 ± 1.96	11.16±1.82	+10 41 36	-16 30 56		-17 32 31			
12	Citrâ	3	1	163.16±0.93	163.22±1.09	10 27 55	13 25 12	0.98	13 25 12	0.98		
				-3.38 ± 1.91	3.59±1.83	+07 00 40	-11 10 57		-11 10 57			
13	Svâti	28	73	170.71 ± 1.05	170.34±1.74	11 16 57	14 15 40	-0.04	14 15 40	-0.04		
				-2.90 ± 2.62	1.07±2.22	+01 28 40	+19 12 37		+19 12 37			
14	Viśâkhe	16	45	181.30±0.94	179.92±1.53	12 09 09	15 12 13	4.54	14 50 41	5.15		
				-3.15 ± 2.44	-3.41±2.12	- 01 58 19	-19 47 30		-15 59 50			
15	Anurâdhâ	4	12	191.56±1.02	189.32±1.45	12 57 14	16 00 20	2.32	16 00 20	2.32		
				-3.20 ± 2.24	-7.58±1.99	- 08 00 46	-22 37 17		-22 37 17			

16	Jyesthâ	17	55	209.38±0.95	206.49±1.86	13 50 21	16 29 24	0.96	16 29 24	0.96
	••			-2.05±3.14	-13.34 ± 2.73	-10 40 44	-26 25 53		-26 25 53	
17	Mūla	5	27	219.75±0.96	216.44±1.62	14 41 41	17 27 21	4.29	17 33 36	1.63
				-2.44±2.91	-17.27±2.66	-15 28 51	-29 52 01		-37 06 14	
18	Pūrvâsâdhâ	18	66	237.36±0.95	234.83±1.64	15 37 55	18 20 59	2.70	18 20 59	2.70
	•			-0.64±3.37	-20.50±3.16	-20 05 40	-29 49 40		-29 49 40	
19	Uttrâsâdhâ	6	41	247.88±0.74	245.85 ± 1.17	16 33 10	18 55 16	2.02	18 55 16	2.02
	•			-1.03±3.37	-22.98±3.29	-20 16 54	-26 17 46		-26 17 46	
20	Śravanâ	19	81	265.52±0.68	265.13 ± 0.80	17 29 34	19 50 47	0.77	20 37 33	3.63
	•			0.92±3.07	-22.81 ± 3.07	-20 38 29	+08 52 06		+14 35 43	
21	Śravisthâ	7	53	276.00±0.78	276.53 ± 0.76	18 28 00	20 39 38	3.77	19 55 18	3.71
	••			0.48±3.23	-23.19±3.26	-20 49 49	+15 54 43		+06 24 24	
22	Śatabhisaj	20	96	293.96±0.72	295.52 ± 0.71	19 24 10	22 52 37	3.74	22 57 39	1.16
	•			2.09±2.31	-19.59 ± 2.33	-19 32 05	-07 34 47		-29 37 20	
23	Purva	8	74	304.52±0.57	306.49 ± 0.78	20 19 52	23 04 45	2.49	23 04 45	2.49
	Prosthapada	a		1.81±2.55	-17.67±2.52	-16 52 09	+15 12 19		+15 12 19	
24	Uttra	33	16	312.05±0.82	313.84 ± 1.01	21 13 33	00 08 23	2.06	00 13 14	2.83
	Prosthapada	a		2.60±1.97	-14.94±1.89	-14 21 16	+29 05 26		+15 11 01	
25	Revati	21	117	322.73±0.74	324.28 ± 0.97	22 6 54	01 13 44	5.24	00 08 23	2.06
				2.61±1.90	-11.68±1.81	- 09 39 08	+07 34 31		+29 05 26	
26	Asvayujau	9	97	333.61±0.72	334.65 ± 0.84	22 58 45	01 53 32	4.75	01 53 32	4.75
				2.55±1.93	-7.96±1.89	- 06 27 21	+19 17 37		+19 17 37	
27	Bharani	22	21	352.26±0.61	352.00 ± 1.21	23 44 07	02 43 27	4.66	02 49 59	3.63
				2.30±2.44	-1.01 ± 2.20	+ 00 47 09	+27 42 26		+27 15 38	

P & M (1989) : Pingree and Morrissey (1989) $\alpha,\ \delta$: right ascension and declination 9) A (1991) : Abhyankar (1991) L, B : ecliptic longitude and latitude C n-s: Centre of the naksatra-sectors

J(2000): reference epoch and equinox FM: The full-moon number

Table 6. The width of the nakṣatra-sectors (in degrees)

nakṣatra	FM	bhāṃśa	L	FM	bhāṃśa	L	WNS
Kṛttikâ	10	23	10.17	35	77	15.98	13.34
Rohini	23	61	27.49	48	115	33.45	13.69
Rohini	48	115	33.45	60	7	21.23	14.03
Mrgaśirsa	11	45	38.32	36	99	44.53	14.26
Ârdrâ	24	83	55.91	61	29	50.48	12.47
Punarvasū	12	67	67.90	37	121	73.74	13.41
Punarvasū	37	121	73.74	49	13	61.69	13.84
Pusya	25	105	85.34	62	51	79.22	14.05
Âślesâ	13	89	96.13	50	35	91.45	10.75
Mâgha	1	73	107.91	38	19	102.49	12.45
Purva Phâlguṇ̄i	14	111	125.68	26	3	113.58	13.89
Purva Phâlguṇi	26	3	113.58	51	57	119.71	14.08
Uttra Phâlguṇ̄	2	95	137.33	39	41	131.45	13.50
Hasta	27	25	143.26	52	79	149.37	14.03
Citrâ	3	117	166.12	15	9	154.32	13.55
Citrâ	15	9	154.32	40	63	160.53	14.26
Svâti	28	47	171.62	53	101	177.76	14.10
Viśâkhe	16	31	183.87	41	85	189.36	12.61
Anurâdhâ	4	15	195.82	29	69	201.47	12.97
Anurâdhâ	29	69	201.47	54	123	207.27	13.32
Jyesthâ	17	53	212.80	42	107	218.70	13.55
Mūla	5	37	224.49	30	91	229.90	12.42
Purvâṣâdḥâ	18	75	242.20	55	21	235.78	14.74
Uttrâṣâdḥâ	6	59	254.28	31	113	259.81	12.70
Uttrâsâdhâ	31	113	259.81	43	5	247.40	14.25
Śravanâ	19	97	271.29	56	43	265.19	14.01
Śravisthâ	7	81	282.63	44	27	277.04	12.84
Śravisthâj	20	119	300.29	32	11	288.25	13.82
Śatabhisaj	32	11	288.25	57	65	294.02	13.25
Purva Prostapada	8	103	312.37	45	49	305.56	15.64
Uttra Prostapada	33	33	317.99	58	87	323.20	11.96
Revatī	21	17	329.53	46	71	335.34	13.34
Asvayujau	9	1	340.56	34	55	346.52	13.69
Asvayujau	34	55	346.52	59	109	352.28	13.23
Bharaṇi	22	39	358.21	47	93	3.71	12.62

Mean Width of the Nakṣatra Sector 12.65±3.28

L: Ecliptic Longitude; WNS: Width of the Naksatra Sector in degrees

of *nakṣatras*. The coordinates of the full moon and the *nakṣatra*-sector of this moon are obtained by independent methods. These lunar positions do not change with epoch because they are not affected by precession of the equinox (this is demonstrated by the agreement between the values obtained for the two periods). If background stars are used to identify the *nakṣatra*-sectors in which the moon is full (or new) each *yuga*, then the positions of the stellar markers will be epochdependent, because of the precession of the equinox; the same set of stars will not identify the same *nakṣatra*-sector at different epochs.

It can be seen from Table 3 that the full moon (and new moon) can occur in the same *nakṣatra*-sector at different times in a *yuga* i.e. in a *yuga* different full moons (identified by full moon numbers in Table 3) can occur in the same naksatra-sector, but they occur at different bhāmśas. For example, full moon three, fifteen and forty occur in the *nakṣatra*-sector Citrā (positions of full moon #3 and #15 are shown in Fig. 1) but at bhāmśa 117, 9 and 63 respectively. In Table 6 are collated all *nakṣatra*-sectors in which there are multiple occurrences of the full moon during a yuga and the full moon number, the bhāmśa and the ecliptic longitude (obtained by the first method described above) of the full moon are given. The size of the nakṣatra-sector calculated from ecliptic longitudes of pairs of full-moons in the same *nakṣatra*-sector is also given in this table. The mean width of the *naksatra*-sector is 12.65±3.28 degrees. The mean width obtained from the ecliptic longitude of the full moon determined by the second method above is 11.38±5.07 degrees. These values are consistent with the width of the *nakṣatra*-sector given in *VJ* (*RJ*.18, *YJ*.39) and discussed above. The spread in the mean values also demonstrates that the *nakṣatra*-sectors are of equal width. The (equatorial) coordinates of the centre of each naksatra-sector are given in Table 5. For comparison the coordinates of the *yogatārās* of the nakṣatras^{15,16} are also given in this table. VJ emphasises the importance of the bhāmśas and gives algorithms for calculating the bhāmśas of the sun and the moon but the method to empirically determine the *bhāmśa* (of the sun or the moon) at any particularly time is not given. Since VJ describes the use of a clepsydra (water-clock) it is very likely that the Āryas determined the *bhāṃśa* by timing the passage of the moon across a *nakṣatra*-sector.

5. DISCUSSION AND CONCLUSIONS

The *jāvādi* arrangement of *nakṣatras* in *Vedānga Jyotiṣa* enables the invariant positions of the *nakṣatra*-sectors to be determined. This arrangement is

unique to VJ and no trace of it is found in any of the earlier Vedic texts. However, this arrangement casts light on some of the aspects of calendar of these earlier Vedic texts. The tenth full moon, which is in the *naksatra*-sector Krttikās (Table 4 and 5.), will be in autumn (*śarad*) (this is determined by counting the number of lunations from the first full moon after the new moon at winter solstice). The sun will occupy this position six months later that is the sun will be in the *naksatra*sector Kıttikās in spring (vasanta). In the northern hemisphere the vernal equinox is in spring, the *jāvādi* arrangement thus states that (around) vernal equinox the sun is in the *nakṣatra*-sector Kṛttikās. In the early Vedic texts, spring (*vasanta*) is described as "the mouth of the seasons" or the seasonal cycle starts with spring. It would appear that at the time of these early Vadic texts the (Vedic) seasonal year commenced in spring (around vernal equinox) when the sun was in the nakṣatra-sector Kṛttikās. This hypothesis is confirmed by the absolute position of the *nakṣatra*-sector Kṛttikās. The ecliptic longitude of the tenth full moon which is in the *nakṣatra*-sector Kṛttikās is almost 0° (Table 5.) that is, this *nakṣatra*sector is close to vernal equinox. The start of the seasonal cycle in spring with the sun in Krttikās is consistent with the myth of Skanda (the year) with its six heads (seasons) who was born when agni/sun was in Krttikās¹⁷. In this respect the Āryas would appear to be similar to a number of early cultures in which the food gathering and agricultural season started when the sun was 'close' to the Pleiades (Kıttikās) or around vernal equinox in the northern hemisphere and around autumnal equinox in the southern hemisphere¹⁸.

In the calculation of the coordinates of the full moons in a *yuga* the origin was assumed to be the first point of Aries or vernal equinox and a *nakṣatra* would be expected to be close to this origin or close to vernal equinox. That this *nakṣatra* should be the Kṛttikās is perhaps not entirely fortuitous; the start of the seasonal year discussed above suggests that the Āryas set-up their scheme of *nakṣatra* with origin at vernal equinox i.e. the *nakṣatra* of the sun at vernal equinox was considered to be the first *nakṣatra* and this was Kṛttikās. This explains why all lists of *nakṣatras* in Vedic texts start with Kṛttikās.

The use of the word *nakṣatras* both as *nakṣatra*-sectors and as asterisms suggests that the Āryas may have identified the *nakṣatra*-sectors by the stars in proximity of these sectors. This method of identification of *nakṣatra*-sectors would be more reproducible then counting the number of full or new moons from the start of every *yuga*. The stellar identifiers of the *nakṣatras* are not given in

the Vedic text including VJ. An exception may be the Kṛttikās; the mythology, the number of stars, the position in the list of *nakṣatras* and the comparison with other cultures suggests that the identification of the Kṛttikās with the Pleiades is unambiguous. Like other cultures the Āryas could have used the heliacal rising or setting of the Pleiades (Kṛttikās) to herald the seasonal cycle and the New Year.

To identify the epoch when the Vedic New Year was in spring it is necessary to identify the (precessed) coordinates of the Pleiades at this epoch. To determine this epoch it is necessary to consider the *Cāturmāsya* (or seasonal) sacrifices. In the post-*Rgvedic* texts the 'dates' of the performance of these three sacrifices are identified by the conjunction of the full moon and three prescribed *nakṣatras*. The autumn sacrifice, *Sākamedha*, was performed when the full moon was in Kṛttikās ^{19,20}. In Figure 2 are shown the ecliptic longitude and latitude of the tenth full moon of a *yuga*; as discussed above, this full moon is in autumn (*śarad*). Also shown in Figure 2 are the coordinates of seven principle stars of the Pleiades precessed to eleven evenly spaced epochs (250 years apart) between 3000 BC and 500 BC. Between 2000 BC and 1500 BC the

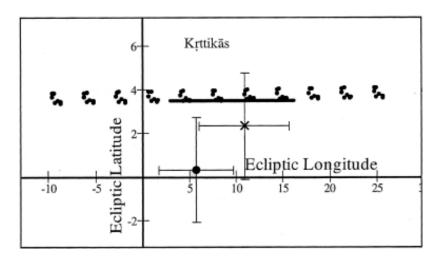


Fig. 2. The coordinates of seven brightest stars of the Pleiades (Kṛttikās) precessed to eleven epochs (250 years apart) between 3000 BC and 500 BC. In this diagram, the ecliptic is the line along latitude 0°. The 'bar' is the width of the *nakṣatra*-sector Kṛttikās. For clarity, the *nakṣatra*-sector is off-set from the ecliptic. The ecliptic longitude and latitude of the 10th full moon in a *yuga* are shown. The mean coordinates obtained for 1900 AD to 2000 AD period are plotted as a large dot and those obtained for 1500 BC to 500 BC period are plotted as a cross. The error bars denote the spread in the coordinates over the period for which the coordinates have been calculated (see text for details).

Kṛttikās conjoin the autumn full moon and during this period the sun will be in Kṛttikās in spring (*vasanta*). During this epoch the *nakṣatra Kṛttikās* are also in the *nakṣatra*-sector Kṛttikās (shown in Fig. 2). At vernal equinox at this epoch the Pleiades will rise after sun-rise but set after sun-set. Few (fifteen to twenty) days later they will rise before sun-rise and set before sun-set. Thus around vernal equinox between 2000 BC and 1500 BC the Kṛttikās/Pleiades would have been observed to rise and set heliacally and this would have been (perhaps) a good omen to start a New Year.

A number of passages in various Vedic texts suggest that during the Vedic period there was also a tradition to start a New Year at winter solstice. As discussed above, in the calendar of *Vedānga Jyotisa*, the *yuga* starts at winter solstice "when the sun and the moon are in Śravisthās". The parameters of the calendar of *Vedānga Jyotisa* depend on this start of the *yuga*. It is possible that the New Year in spring was an earlier tradition (in conformity with most other early cultures) and the New Year at winter solstice was a later development. It is equally possible that these were two parallel traditions. It would have been possible for the composer(s) of *Vedānga Jyotisa* to rearrange the list of *naksatras* to start with Śravisthās but they clearly opted to retain the arrangement of nakṣatras given in the earlier texts. The jāvādi arrangement of nakṣatras appears to have been devised to create an absolute and fixed frame of reference that is anchored to the ecliptic. Background stars could be and most probably were used to identify the sectors of this reference frame. However, because of precession of the equinox, over time these stellar identifiers will have moved out of their original sectors.

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