

Quiz 3

⚠ This is a preview of the published version of the quiz

Started: Jun 22 at 9:11pm

Quiz Instructions



Question 1 1 pts

Which of the following statement is correct about the expectation for two random variables X and Y?

☐

$E[XY] = E[X] E[Y]$ if X and Y are independent.

☐

$E[XY] = E[X] E[Y]$ for any X and Y

☐

$E[X + Y] = E[X] + E[Y]$ only when X and Y are uncorrelated.

☐

$E[X + Y] = E[X] + E[Y]$ only when X and Y are independent.



Question 2 1 pts

Which of the following statement is correct about the variance and covariance for two random variables X and Y?

☐

All of them!



$\text{Var}(X + Y) = \text{Var}(X) + \text{Var}(Y)$ if X and Y are independent



$\text{Var}(X + Y) = \text{Var}(X) + \text{Var}(Y) + 2\text{Cov}(X, Y)$ for any X and Y



$\text{Var}(X + Y + c) = \text{Var}(X) + \text{Var}(Y)$ if X and Y are independent and c is a constant.



Question 3 1 pts

If I toss a fair die 100 times and count the number of times I get the each faces from 1 to 6 and denote them as X_1 to X_6 . What is the distribution of random vector $\mathbf{X} = (X_1, \dots, X_6)$?



A multinomial with $n=100$, and p_1 to p_6 all equal to $1/6$.



A binomial with $n=100$, and $p=1/6$.



A Bernoulli with $p=1/6$.



An unknown distribution $>_<$



Question 4 1 pts

If X and Y follow a bivariate Normal (Gaussian) distribution, which of the following statement is correct?



All of them!



The marginal distribution of X and Y are both normal.



The conditional distribution of $X | Y$ and $Y | X$ are both normal.



For any constant a and b , define a new random variable $Z = aX + bY$, and Z is also normal.



Question 5 1 pts

Let X_1, X_2, \dots, X_n be i.i.d. random variables from Bernoulli(p).

Define

$$Y_1 = X_1 \cdot X_2,$$

$$Y_2 = X_2 \cdot X_3,$$

....

$$Y_{n-1} = X_{n-1} \cdot X_n,$$

$$Y_n = X_n \cdot X_1.$$

$$Y = Y_1 + Y_2 + \dots + Y_n$$

Which of the following is correct?



$$E[Y] = np^2$$



$$E[Y] = n(1-p^2)$$



$$\text{Var}[Y] = np^2$$



$$\text{Var}[Y] = n(1-p^2)$$

Not saved

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