

D. Tables

Table 1 Units with special names and symbols¹

ALL VALUES DECIMAL

Unit Category	Dimension	The Universal Unit Systems			
		with the Rydberg constant(u)		Harmonic System (\pm)	
base units that are not natural units	length	$_{\text{u}}\text{m}$	272.102883 mm	$\pm \text{h}^2$	272.352206 mm
	time	$_{\text{u}}\text{s}$	390.267520 ms	$\pm \text{n}$	390.625115 ms
	energy	$_{\text{u}}\text{J}$	64.143275 mJ	$\pm \text{J}$	64.084556 mJ
	temperature ³	$_{\text{u}}\text{K}$	58.441041 μK	$\pm \text{K}$	58.387542 μK
base units that are natural units	plane angle	rad	($2/\pi$) arc sin(1)		
	logarithm	neper	log(e)		
	amount of substance	$\text{\scriptsize \#}\text{mol}$ or N_A^{-1}	mol / $6.02214076 \times 10^{23}$. In this context ' \scriptsize \# ' is equivalent to '3-' and ' \scriptsize \# mol' is called 'natural mol.'		
	impedance	$\text{\scriptsize \#}\Omega$ or Z_p	29.979245796 Ω ($=1\text{sr}/(\epsilon_0 c_0)^4$) $\text{\scriptsize \#}\Omega$ is called 'natural ohm' or more simply 'nohm.'		
derived units of electromagnetic quantities	charge	$\pm \text{C}$	28.896578 mC (may be called 'universal Coulomb' (or 'Clio' ⁶))		
	electric current	$_{\text{u}}\text{A}$	74.043001 mA	$\pm \text{A}$	73.975219 mA
	field strength	$_{\text{u}}\text{E}$ ^{5,6}	272.113988 mA/m	$\pm \text{E}$	271.616007 mA/m
	flux density	$_{\text{u}}\text{T}$	390.283447 mC/m ²	$\pm \text{T}$	389.569211 mC/m ²
derived units of dynamical quantities	mass	$_{\text{u}}\text{g}$	131.950082 g	$\pm \text{l}_{(\text{x}006\text{C})}$	131.829289 g
	power	$_{\text{u}}\text{W}$	164.357196 mW	$\pm \text{W}$	164.056415 mW
	force	$_{\text{u}}\text{N}$	235.731701 mN	$\pm \text{N}$	235.300301 mN
	Pressure	$_{\text{u}}\text{P}$	3.183843 Pa	$\pm \text{P}$	3.172201 Pa

¹ Please see also https://github.com/suchowan/a_converter/blob/master/doc/dozenal_com/univunit-e.pdf for details. A web-based unit converter is available at <http://hosil.org/cgi-bin/conv.cgi>. This converter also teaches us the representation of units that belong to various unit systems.

² 'harmon'($\pm \text{h}$), 'nic'($\pm \text{n}$), 'looloh'⁸($\pm \text{l}$, ' l ' can also be a cursive ' ℓ ' (x2113), the suffix ' h ' representing the Harmonic System's identity), and 'nohm'($\text{\scriptsize \#}\Omega$) constitutes a quartet.

³ The unit of thermodynamic temperature has been changed. The new unit is one-1,0000;th of the old unit in the paper <http://dozenal.com> along with the introduction of the Earth local extension.

⁴ If we adopt the elementary charge as one of the definition constants, $\pm \text{Q}$ is used in substitution for $\text{\scriptsize \#}\Omega$.

⁵ See electromagnetic units in §3.2.2 of the paper <http://dozenal.com>, and https://github.com/suchowan/a_converter/blob/master/doc/dozenal_com/electromagnetism.pdf.

⁶ The unit symbol E (Ørsted) is associated with the CGS system. In this paper, we adopt metric unit names based on the scientists' names as is.

However, under the Harmonic System, an alternative proposal suggests replacing these units with the names of Muses bearing the same initials — namely, Newton→**Nete**, Pascal→(Polymnia→)**Polym**, Coulomb→**Clio**, Ampere→**Aoide**, Ørsted→**Erato**, Tesla→**Thalia**, and Kelvin→**Kalliope**. Notably, Polym derives from Polymnia, the Muse of sacred song; a lute piece titled Polymnia was composed by Vincenzo Galilei (father of Galileo), symbolically linking musical and scientific traditions of harmonic proportion. This proposal has two advantages: (1) it does not honor any individual, and (2) it allows the omission of redundant 'harmonic' terms. The unit converter for this proposal is available at http://hosil.org/cgi-bin/conv_muse.cgi.

This proposal also renames units for which no corresponding Muse is found, such as Joule→**Juno**, Watt→(Walküre→)**Walku**, naper→(Nephelē→)**nephe**, dirac→**diana**, and Ω hm→**Ω(Omega)**. Since no suitable Muse exists for Joule, Watt, or naper, the proposal instead borrows names from Roman, Norse, and Greek mythology. Moreover, because of the electromagnetic symmetry required to pair $\text{\scriptsize \#}\Omega$ and Ω (see the 3rd part of p. 20), ' Ω (Omega)' is adopted without a Muse equivalent.

Non-coherent	defining constants	wave number	R_∞	10,973,731.568157/m (is called 'Rydberg')
		velocity	c_0 or γ	299,792,458 m/s (defined, and is called 'light')
		action	\hbar	$6.62607015 \times 10^{-34} \text{ Js}/2\pi$ (is called 'quantum')
		heat capacity	k_B	$1.380649 \times 10^{-23} \text{ J/K}$ (is called 'Boltzmann')
	supplementary constants	the total solid angle of a hypersphere	Ω_k	$\frac{2\pi^{\frac{k+1}{2}}}{\Gamma(\frac{k+1}{2})} \text{ rad}^k$ $k=0,1,2$ $\Omega_0=2$ $\Omega_1=2\pi \text{ rad}$ (is called 'cycle') $\Omega_2=4\pi \text{ sr}$ (is called 'turn')
		logarithm of an integer	$\tilde{\Omega}_k$	$\log(2^k)$ $k=1(\text{bit}), 2(\text{figure}), 4(\text{nibble}), 8(\text{byte}), \dots$ $z=\log_2(12.)$
		amount of substance	$\pm\text{mol}$	132.007620 mol ($=12^{24}/N_A$) ($\pm\text{mol}$ may be called 'universal mol')
		elementary charge	e	$1.6021766340 \times 10^{-19} \text{ C}$ (e is called 'electron') ($=\sqrt{\frac{\alpha\hbar}{\Omega_n}}$)

Table 2 Physical, material and astronomical constants⁷

ALL VALUES DOZENAL

Constant Symbols and Name (UNDERLINE INDICATES CONSTANT MAINTAINS SAME VALUE BETWEEN SYSTEMS u AND h)		Constant Value expressed by the Universal Unit Systems		Exponent N of $\times 10^N$	Unit Symbol (u and h prefixes omitted)
		with the Rydberg constant (u)	Harmonic System (h)		
R_∞	Rydberg constant	1	1;00170000	6;	Ω_1/m
c_0	<u>the speed of light in vacuum</u>	1		8;	m/s
\hbar	<u>quantum of action</u>	1		-26;	J s
k_B	<u>Boltzmann constant</u>	1		-20;	J/K
N_A	<u>Avogadro constant</u>	1		20;	mol^{-1}
R	<u>gas constant</u>	1		0;	$\text{J}/(\text{mol K})$
u	unified atomic mass unit	1;00090610	1;00240733	-20;	g^8
a_B	Bohr Radius	1;005E85684	1;00447X74	-9;	m
α	<u>fine structure constant</u>	1;0739940472		-2;	-
e	<u>elementary charge</u>	1;0374439E14	9	-14;	C
m_e	electron mass	0;E4692217E0	0;E48324X245	-23;	g

⁷ If CODATA (2022) values are required, see <http://physics.nist.gov/cuu/Constants/index.html>.

⁸ Because $u\text{g}$ is approximately 100×10^{-10} ; u , I add dedicated name 'looloh' (lú:lou/əʊv, $\pm l$) to mass unit of the Harmonic System.

⁹ This value equals $12\sqrt{\alpha}$ and matches the ratio 41. : 40. within an error of 0.009 %. The ratio 41. : 40. is termed the Fine Harmonic Ratio, named after the fine-structure constant α .

σ	<u>Stefan-Boltzmann constant</u>	1;E82E28		-1E;	W/(m ² K ⁴)
m_G	gravitic meter ($\sqrt{2E} / l_p$)	1;00186	1;00016	-27;	m
l_p	Planck length	2;0445E	2;04134	-28;	m
F_p	Planck force ($\hbar c_0 / l_p^2$)	2;XE206	2;XEE32($\div 2;E$) ¹⁰	35;	N
G	Newtonian constant of gravitation (c_0^4/F_p)	4;15768	4;14663	-X;	(m ⁴ /s ⁴)/N
θ_W	<u>weak mixing angle</u>	E;304		-2;	Ω_1
V_m	molar volume of an ideal gas under standard conditions	1;02X469	1;025665	2;	m ³ /mol
	black-body radiation at the ice point	0;EX2466	0;EX8784	2;	W/m ²
	maximum density of water	1;088183	1;092X47 ($\div 15;/14;$)	2;	g/m ³
	density of ice at the ice point	0;E7E9	0;E85E	2;	g/m ³
	specific heat of water ¹¹	0;6052	0;6045 ($\div 1/2$)	0;	J/(g K)
	surface tension of water at 25°C	0;EE68	0;EEE4	-1;	N/m
atm	standard atmosphere	1;65008E	1;659967 ($\div 1;66$)	4;	P
g_n	standard gravitational acceleration	5;5X54XE9	5;5E21264 ($\div E;/2$)	0;	m/s ²
r_E	gravitational radius of Earth	2;41E8982X0X	2;418030652	-2;	m
au	astronomical unit	8;X67575535	8;X55509X31	X;	m
	astronomical unit	9;E91731X53		-3;	$c_0 s_E$ day

Table 3 Power prefixes

name	symbol	TeX text	value	name	symbol	TeX text	value
dirac ¹²	$\text{\textcircled{v}\#}$	dirac	10;				
hyper	#(x266F)	hyper	10;⁴	sub	$\text{\textcircled{b}}$ (x266D)	sub	10;⁻⁴
cosmic	+	_+	10;⁸(=U)	atomic	-	_-	U⁻¹
di-cosmic	2+	_{2+}	U ²	di-atomic	2-	_{2-}	U ⁻²
ter-cosmic	3+	_{3+}	U ³	ter-atomic	3-	_{3-}	U ⁻³
tetra-cosmic	4+	_{4+}	U ⁴	tetra-atomic	4-	_{4-}	U ⁻⁴
penta-cosmic	5+	_{5+}	U ⁵	penta-atomic	5-	_{5-}	U ⁻⁵
hexa-cosmic	6+	_{6+}	U ⁶	hexa-atomic	6-	_{6-}	U ⁻⁶
hepta-cosmic	7+	_{7+}	U ⁷	hepta-atomic	7-	_{7-}	U ⁻⁷

¹⁰ If this is expressed as 2;E, the error from CODATA (2018) becomes -6;61(-6.51) times standard deviation.

¹¹ This corresponds to the definition of the thermodynamic calorie.

¹² ‘dirac’ is only used when expressing the unit of the Gravitic System with the Harmonic System. (i.e., gravitic meter = tetra-atomic dirac harmon, gravitic second = penta-atomic dirac nic, gravitic gram = atomic dirac looloh)

Table 4 Examples of natural scale quantity representation ¹³

quantity	symbol	value	refer to
2E; penta-cosmic Newton	2E;s+N	2E; $\times U^5$ [harmonic] Newton	the Planck force
6;di-cosmic nic	6;2+n	6; $\times U^2$ [harmonic]nic[second]	the age of the universe
cosmic hyper bit [Boltzmann]	+# $\tilde{\Omega}_1[kb]$	$U^{1\cdot\cdot 4}\log 2^1$ [Boltzmann]	1.01 Tera Byte(=2 ⁴³ .bit)
cosmic harmon	+h	U^1 harmon[ic meter]	the speed of light in vacuum
ato[mic]l[ight]	-γ	harmon[ic meter]/ [harmonic]nic[second]	U^{-1} light(=2.51 km / hour)
atomic unino[]h[armon]	1;'[0].h	$U^{1\cdot\cdot 1}$ harmon[ic meter]	the Bohr radius
di-atomic Coulomb	2-C	U^{-2} [universal] Coulomb	the elementary charge
di-atomic effective Watt	2- \bar{W}	U^{-2} [harmonic]effective Watt	a photon power (540.THz)
ter-atomic looloh	3-l	U^{-3} looloh	the unified atomic mass unit
2; tetra-atomic harmon	2;4-h	2; $\times U^{-4}$ harmon[ic meter]	the Planck length

Table 5 The Earth local extension for the Harmonic Universal Unit System

category		name / description		symbol	plain text	value
Non-coherent calendar time	units	year		$\tilde{\odot}_{(x263C)}$	year	$\tilde{\odot} = 365.\text{days}$
		month		$\tilde{\mathfrak{D}}_{(x263D)}$	month	$\tilde{\mathfrak{D}} = 10;^{-1} \tilde{\odot}$
		day		$\tilde{\sigma}_{(x00B0)}$	day	$\Omega_1 = \tilde{\sigma} = 10; \tilde{\gamma} = 100; \tilde{\eta} = 1000; \tilde{m} = 10^4$
		unino day		$\tilde{\tau}_{(x2032)}$	unitia	'day' corresponds to 86,400. s at the beginning of year 1900.
		dino day		$\tilde{\tau}_{(x2033)}$	ditia	
		terno day (tertiary 12 divisions of one day)		$\tilde{\tau}_{(x2034)}$	tertia	
		nodus		$\tilde{\star}_{(x2606)}$	nodus	$\tilde{\sigma} = 2^{+7} \tilde{\star}$
		terno nodus → terno n(odus) → ternon		$\tilde{\nabla}_{(x25BD)}$	ternon	$\tilde{\nabla} = 10;^{-3} \tilde{\star}$
		hexaon nodus → hex(a)o(n) n(odus) → hexon		$\tilde{\mathfrak{G}}_{(x232C)}$	hexon	$\tilde{\mathfrak{G}} = 2^{+6} \tilde{\odot} = 1;003628 \times 10;^{+6} \tilde{\star}$
		difference between thermodynamic temperature and $T_E(=118,2354; \pm K (-74.36^\circ C, -101.85^\circ F))$		${}^\circ H$	deg H	1,0000; $\pm K(\div 1.210724 K \div 23./19. K)$
Non-coherent unit and constants		approximate formula				100; 0000°H is 99.9839 °C
		$C = \frac{1E}{17}; {}^\circ H - 62; 4$	${}^\circ H = \frac{17}{1E}; C + 51; 5$			78; 0000°H is 37.0262°C
						61; 0000°H is 14.0224°C
						51; 5026°H is 0.0000°C
						99.9839 °C is the boiling point of water at the standard atmosphere.
		supple- mentary constants	the gravitational acceleration of the Earth (is called 'gee [of Earth]')	g_E	g_E or gee	$5;611X615$ harmon/nic ² g_E is defined as $c_0^2 r_E(m_E \text{ rad})^{-2}$
			the rotation period of the Earth (is called '[Earth] solar') at the beginning of year 1900.	s_E	s_E or solar	0;EEEEEE15336X nic/ ternon (=86400 s / Ω_1) (This should be 'coordinated'.)
			the meridian length of the Earth (is called '[Earth] meridian')	m_E	m_E or meridian	4124,216E; harmon/ Ω_1

¹³ The part enclosed with '[]' can be omitted in Table 4 and Table 5.

¹⁴ This is the notation explained at the end of Appendix C.

\bar{W} corresponds to 1;di-cosmic photon energy(540.THz) / nic and 115.667212 lumen.

¹⁵ Units for quantity weighted by dimensionless human sensitivity are indicated by 'effective' and symbolled by overline.

\bar{W} corresponds to 1;di-cosmic photon energy(540.THz) / nic and 115.667212 lumen.