

## UNIT-II

### Syntax Analysis :-

\* Introduction.

\* Role of Syntax Analysis.

### Introduction :-

→ It is the second phase of the compilation.

• It checks for the syntax of language.

• Syntax analyzer takes the tokens from the lexical analyzer and groups them in some programming structure called "syntax tree or Parse tree".

• If any syntax cannot be recognized then the syntax error will be generated.

### Definition:-

. A passing com syntax analysis is a process which takes string " $w$ " and produce either a parse tree or generates the semantic error.

. It is also called "Parser".

Ex:- consider the source program statement  $a := b + 10$

Here the lexical analyzer reads the above statement and broken it into the set of tokens like 'A' is identifier

A - is identifier

$:=$  - Assignment Operator

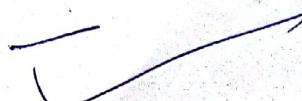
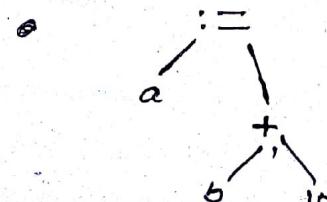
B - Identifier

$+$  - Assignment Operator

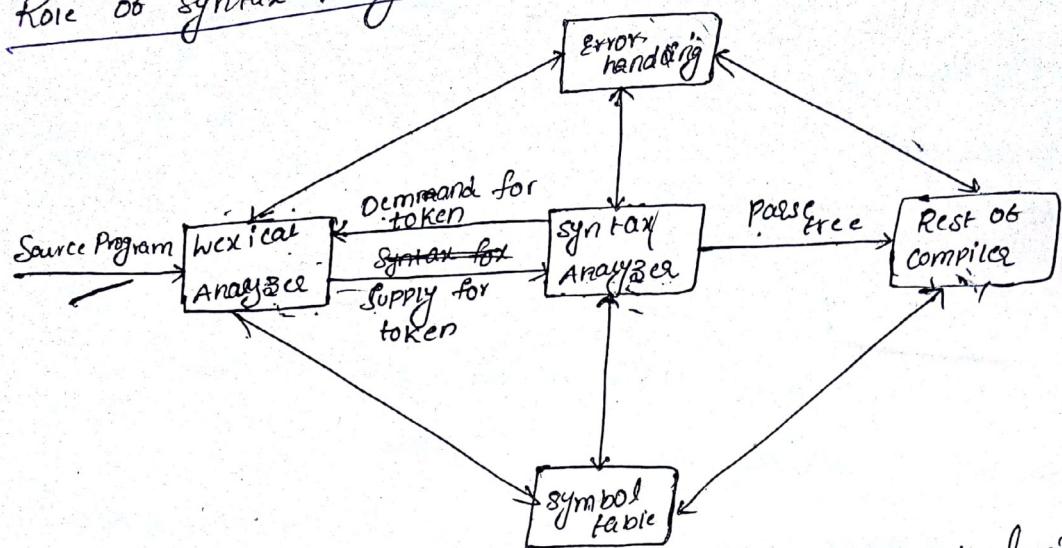
10 - number (or) Constant.

Now the syntax analyzer connect the above tokens from lexical analyzer and arrange them into a structure is called "Parse tree or Syntax tree".

$$\Rightarrow a := b + 10.$$



## Role of Syntax Analyzer : (or) Parser :-



In the process of compilation the parser and lexical analyzer work together that means.

- 1. When the parser requires string of tokens it invokes lexical analyzer.
- 2. In turn the lexical analyzer supply tokens to Syntax Analyzer.

→ The parser collects sufficient number of tokens and build a parse tree.

→ It finds syntactical errors at the time of construction of parse tree.

Parse tree.

→ These errors are recovered by Error handler.

## Context free Grammar:-

\* Introduction \* Derivation and Parse tree \* Ambiguous Grammars

→ Introduction,

A context free Grammar "G" is a four tuples like

$$G = (V, T, P, S)$$

$V \rightarrow$  set of nonterminal symbols.

$T \rightarrow$  set of terminal symbols.

$P \rightarrow$  set of Production rules of the form  $\alpha \rightarrow \beta$  where  $\alpha \in V$ ,  $\beta \in T^*$ .

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$S \rightarrow$  start symbol.

Ex:- Let the language  $W = a^n b^n, n \geq 1$

~~$a^n b^n$~~

minimum string = ab

$S \rightarrow \underline{a^n b^n}$

$\rightarrow \underline{a} a^{n-1} b^{n-1} b$

$\rightarrow a a a^{n-2} b^{n-2} b b$

P:  $S \rightarrow a^i S b^j$

$S \rightarrow \underline{a^i S b^j}$

$S \rightarrow \underline{a^i b^j}$

From the above  $G = (V, T, P, S)$  where is a context free grammar.

Where  $V \rightarrow$  set of {S}

$T \rightarrow$  set of {a, b}

$P \rightarrow$  {asb, ab}

$S \rightarrow$  start symbol {S}

→ Derivation and Parse tree :-

Derivation from 'S' means generation of a string 'W'

Form 'S'. For constructing derivation two things are

important.

1. Choice of non-terminal. Form several others.
2. choice of rule from production rules for corresponding non-terminal.

→ Definition of Derivation Tree.

Let  $G = (V, T, P, S)$  be a context free grammar.

The Derivation tree is a tree which can be constructed.

by following properties.

1. The root node has label 'S'.
2. Every vertex can be derived from {VUTS}

3. If there exist a vertex 'A' with children  $x_1, x_2, x_3, \dots, x_n$   
then there should be a production rule.

$$A \rightarrow x_1 x_2 x_3 \dots x_n$$

4. The leaf nodes are from set T, and internal nodes are  
from set  $\{S\}$ .

### → 1. Left Most Derivation (LMD)

In left most derivation the left most non terminal  
is replaced by a terminal (or) non-terminal in each step  
beginning with a start symbol.

### → Right Most Derivation (RMD):-

In Right most derivation the Right most non terminal  
is replaced by a terminal (or) non-terminal in each step  
beginning with a start symbol.

~~Ex:-~~ Consider the grammar given below

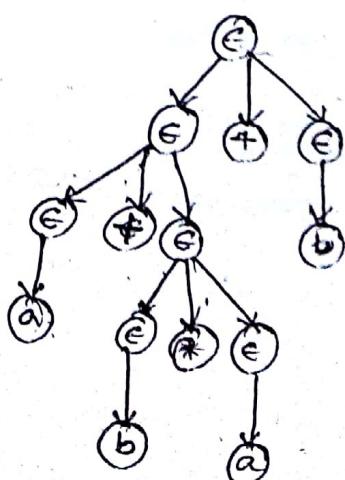
$$\begin{aligned} S &\rightarrow S + S \\ S &\rightarrow S * S \\ S &\rightarrow S / S \\ S &\rightarrow a/b \end{aligned}$$

Obtain 1. Left Most Derivation 2. Right Most Derivation  
3. Parse tree. for the input string a+b \* a+b.

### (a) Left Most Derivation:-

$$\begin{aligned} S &\rightarrow S + S \\ &\rightarrow S + S * S \\ &\rightarrow S + S + S \\ &\rightarrow S + S * S + S \\ &\rightarrow S + S * S + S * S \\ &\rightarrow S + S * S + S * S + S \\ &\rightarrow a + b * a + b \end{aligned}$$

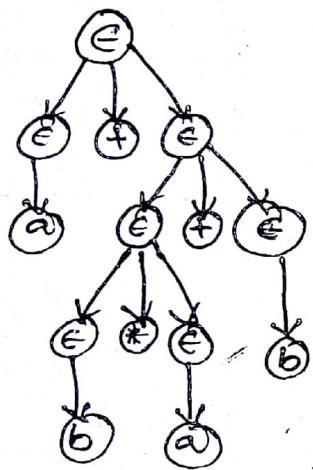
### Parse tree:-



Q. Right Most Derivation:-  $a+b \Rightarrow a+b$ .

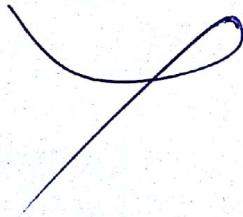
$$\begin{aligned}\epsilon &\rightarrow \epsilon + \epsilon \\&\rightarrow \epsilon + \epsilon + \underline{\epsilon} \\&\rightarrow \epsilon + \underline{\epsilon} + b \\&\rightarrow \cancel{\epsilon + a + b} \\&\rightarrow \epsilon + \epsilon * \underline{\epsilon} + b \\&\rightarrow \epsilon + \underline{\epsilon} * a + b \\&\rightarrow \epsilon + b * a + b \\&\rightarrow \cancel{a + b * a + b}\end{aligned}$$

Parse tree:-



Q. consider the grammar given below  $s \rightarrow (\omega) \mid a$   
 $\omega \rightarrow s, s \mid s$ .

Input string is  $(a, (a;a))$ .



→ writing a context-free Grammar:

- \* Lexical Analysis vs Syntax Analysis
- \* Classification of Parsing techniques.
- \* Problems with Parsing Techniques.

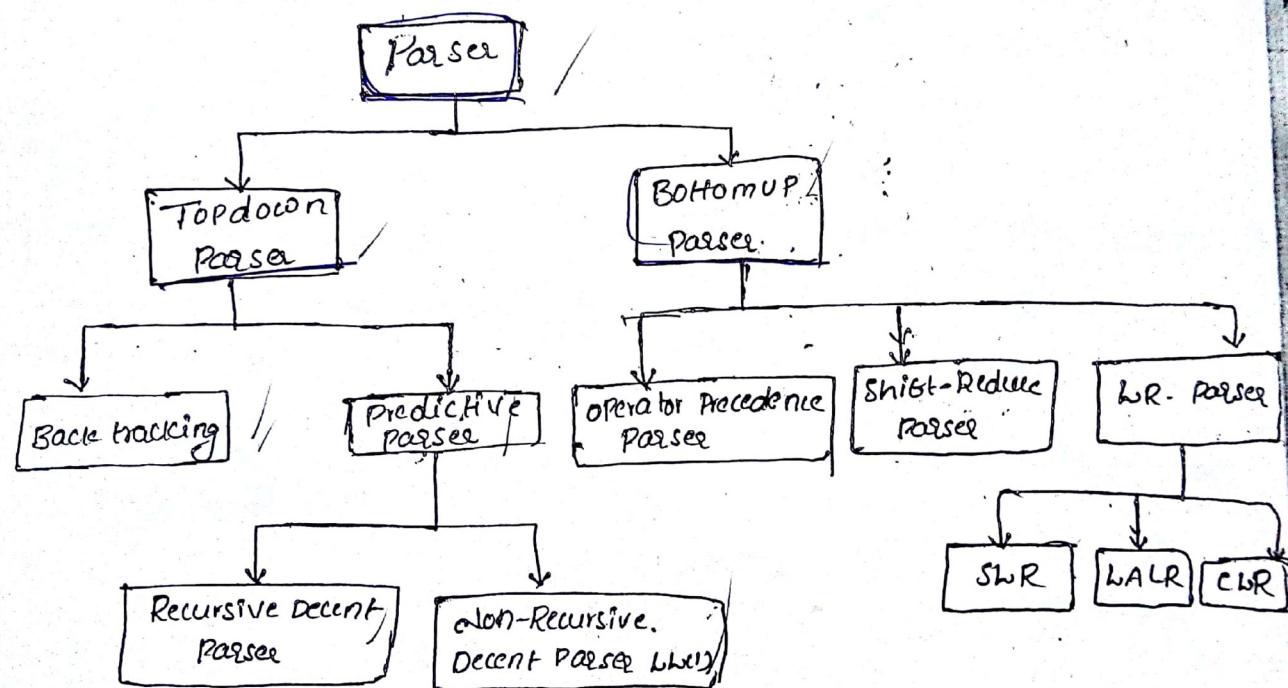
1. Back tracking.

2. Left Recursion.

3. Left factoring.

4. Ambiguity.

→ Classification of Parsing techniques:-



TOPDOWN Parser:-

The process of constructing a syntax tree (or) Parse tree from root node to leaf node is called "TOPDOWN Parser".

TOPDOWN parser classified into two types.

1. Backtracking    2. Predictive Parser.

→ Backtracking :-

Backtracking is a technique in which for expansion.

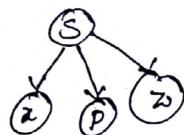
expansion of non terminal symbol we choose one alternative and if some mismatch occurs then we try another alternative if any.

Ex:- consider the grammar  $S \rightarrow xPz$   
 $P \rightarrow ywY$

also we obtain an input string  $xywz$  from the above.

Grammar:

$\rightarrow 1$



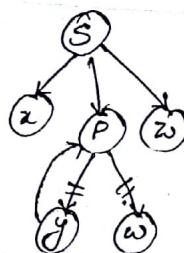
Here we take the first production

$S \rightarrow xPz$  then the

corresponding parse tree is  $S \rightarrow xPz$ .

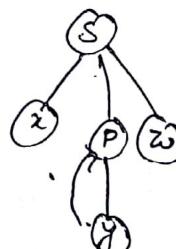
$\rightarrow 2$ . also non-terminal symbol 'p' is replaced by the first alternative of it that is  $P \rightarrow ywY$  then the parse tree is

$S \rightarrow xPz$   
 $P \rightarrow ywY$



This string doesn't derived the given input string. So ~~we move~~ we move backward to 'P' and remove the corresponding branch. From it. and apply another alternative of it. Then the corresponding tree is

$S \rightarrow xPz$   
 $P \rightarrow xyw$

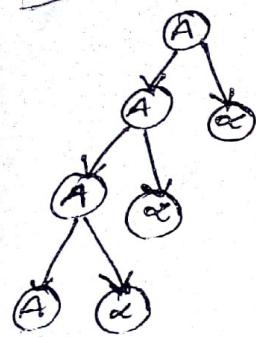


This parsing technique increases lot of overhead in implementation of parse tree. So we need to eliminate the backtracking by modifying the grammar.

→ Left Recursion:-

A left recursive grammar is a grammar which contains the production rule is like  $A \rightarrow A\alpha$  where  $A \in V$  and  $\alpha \in (V \cup T)^*$ .

If left recursion is present in the grammar then the top down parser can enter into infinity loop like



\*\*\* elimination of left Recursion—

To eliminate left Recursion we need to modified the grammar.

Let ' $G$ ' =  $(V, T, P, S)$  be a CFG with the productions rule having left recursion.

$$\begin{array}{l} A \rightarrow A\alpha \\ A \rightarrow B \end{array}$$

Then we eliminate

the left Recursion by rewriting: the production rule has

$$\begin{array}{l} 1. A \rightarrow BA' \\ 2. A' \rightarrow \alpha A' \\ 3. A' \rightarrow \epsilon \end{array}$$

$$\begin{array}{l} A \rightarrow A\alpha \\ A \rightarrow B \end{array}$$

Ex: consider the grammar

$$\begin{array}{l} E \rightarrow E + T \\ E \rightarrow T B \\ T \rightarrow T * F \\ T \rightarrow F \\ F \rightarrow (E) \\ F \rightarrow id \end{array} \quad \begin{array}{l} A \rightarrow A\alpha \\ A \rightarrow B \\ A \rightarrow A\alpha \\ A \rightarrow B \\ A \rightarrow A\alpha \\ A \rightarrow B \end{array} \quad \begin{array}{l} A \rightarrow A\alpha \\ A \rightarrow B \\ A \rightarrow A\alpha \\ A \rightarrow B \\ A \rightarrow A\alpha \\ A \rightarrow B \end{array}$$

$A = E, \alpha = +T,$

Eliminate left recursion from the given grammar.

$\Rightarrow A^*$   
 $A:$  Step 1:-  $E \rightarrow E + T \quad T \rightarrow T * E \quad F \rightarrow (E)$   
 $E \rightarrow T \quad T \rightarrow F \quad F \rightarrow id.$   
 we can map this grammar production rule with

the rule  $A \rightarrow A\alpha, A \rightarrow B$ . Where  $A = E$   
 $\alpha = +T$

$$\beta = T$$

know we can eliminate left Recursion

$$1. A \rightarrow BA'$$

$$\hookrightarrow E \rightarrow TE'$$

$$3. A' \rightarrow \epsilon$$

$$\hookrightarrow \epsilon' + \epsilon$$

$$2. A' \rightarrow \alpha A'$$

$$\hookrightarrow \epsilon' \rightarrow +TE'$$

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After eliminating left recursion the new Production

rules are:

$$\epsilon \rightarrow T\epsilon'$$

$$\epsilon' \rightarrow +TE'$$

$$\epsilon' \rightarrow \epsilon$$

$T \rightarrow FT^*$  similarly for the rules

$$T \rightarrow T * F$$

$$T \rightarrow F$$

we can map this grammar rule with the rule

$$A \rightarrow Ad$$

$$A \rightarrow B$$

where  $A = T$

$$d = *F$$

$$B = F$$

know we can eliminate left recursion.

1.  $A \rightarrow BA'$   
    $\hookrightarrow T \rightarrow FT'$

2.  $A' \rightarrow dA'$   
    $\hookrightarrow T' \rightarrow *FT'$

3.  $A' \rightarrow \epsilon$   
    $\hookrightarrow T' \rightarrow \epsilon$

Therefore the grammar without left recursion is

$$\epsilon \rightarrow T\epsilon'$$

$$\epsilon' \rightarrow +TE'$$

$$\epsilon' \rightarrow \epsilon$$

$$T \rightarrow FT'$$

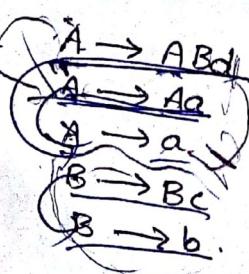
$$T' \rightarrow *FT'$$

$$T \rightarrow \epsilon$$

$$F \rightarrow (\epsilon)$$

$$F \rightarrow id$$

Q) Consider the Grammar



remove left recursion!

The

$$\begin{array}{lll}
 \text{Sol:-} & A \rightarrow ABd & A \rightarrow Aa \\
 & A \rightarrow a' & A \rightarrow a' \\
 & 1. A \rightarrow \alpha A' & 1. A \rightarrow \alpha A' \\
 & 2. A' \rightarrow BdA' & 2. A' \rightarrow \alpha A' \\
 & 3. A' \rightarrow \epsilon & 3. A' \rightarrow \epsilon \\
 & & B \rightarrow Bc \\
 & & B \rightarrow b \\
 & & 1. B \rightarrow bB' \\
 & & 2. B' \rightarrow cB' \\
 & & 3. B' \rightarrow \epsilon
 \end{array}$$

### → Left factoring :-

1. A Grammar may not be suitable for recursive decent Parsing even if there is no left recursion.
2. For example consider the grammar  $S \rightarrow iets | ietses | a$
3. A useful method for manipulating the grammar into a form suitable for recursive decent Parsing is left factoring.

### \* Left factoring :-

The process of factoring out the common prefix of alternatives let  $A \rightarrow \alpha B_1 | \alpha B_2 | \alpha B_3 | \dots | \alpha B_n$  are 'n' number of 'A' production rules. and ' $\alpha$ ' is not equal to null. after left factoring the grammar will become

$$\begin{array}{l}
 1. A \rightarrow \alpha A' \\
 2. A' \rightarrow B_1 | B_2 | B_3 | \dots | B_n
 \end{array}$$

Ex:- consider the Grammar

$$\begin{array}{l}
 S \rightarrow iets | ietses | a \\
 \epsilon \rightarrow b. \text{ do the left factoring on}
 \end{array}$$

above Grammar.

Sol:- consider the Production rule with common Prefix Part.

$$S \rightarrow \underbrace{iets}_\alpha | \underbrace{ietses}_\alpha | \dots | \alpha$$

after the new Productions are  $\alpha$

We can map the Grammar rules with the Rules

$$A \rightarrow \alpha B_1 | \alpha B_2$$

where  $A = S$ ,  $\alpha = iets$ ,  $B_1 = \epsilon$ ,  $B_2 = es$  After left factoring the new Production rules are

$$A \rightarrow \alpha A'$$

$$S \rightarrow iets S'$$

$$\begin{array}{l}
 2. A' \rightarrow B_1 | B_2 \\
 3. \frac{\epsilon S \rightarrow a}{\epsilon \rightarrow b}.
 \end{array}$$

∴ The grammar after left factoring is

$$S \rightarrow i \in \Sigma S'$$

$$S' \rightarrow \epsilon | \epsilon S$$

$$S \rightarrow a$$

$$\epsilon \rightarrow b.$$

Q, To the left factoring in the following Grammar.

$$A \rightarrow aAB | aA | a$$

$$B \rightarrow bB | b.$$

$$\text{Sol: } A \rightarrow aAB | aA | a$$

$$\text{where } \alpha = A$$

$$\alpha = a$$

$$B_1 = AB$$

$$B_2 = \alpha A$$

$$B_3 = \epsilon$$

After left factoring the new production rule is.

$$A \rightarrow \alpha A' \quad \text{Q, } A' \rightarrow B_1 | B_2 | B_3$$

$$A \rightarrow \alpha A' \quad A' \rightarrow AB | \alpha A | \epsilon.$$

$$B_1 = B$$

$$\alpha = b$$

$$B_2 = B$$

$$B_3 = \epsilon.$$

∴ the grammar after left factoring is.

$$A \rightarrow \alpha A'$$

$$A' \rightarrow AB | \alpha A | \epsilon.$$

$$A \leftrightarrow \alpha$$

$$B \rightarrow b \cdot B'$$

$$B' \rightarrow B | \epsilon.$$

→ Ambiguity:-

A Grammatical which has more than one left most derivation

(or) Right most derivation (or) Parse tree for the same input string is called "Ambiguous grammar."

Ex:- Consider the grammar which has more than one left most derivation for the input string ~~s+s+s~~ ~~s+s+s~~ ~~s+s+s~~.

$$A \rightarrow Ad$$

$$A \rightarrow B.$$

$$S \rightarrow S + S$$

(1)

1. LMD:-

$$S \rightarrow S + S$$

$$\rightarrow \underline{\alpha} + S$$

$$\rightarrow \underline{\alpha} + \underline{S} + S$$

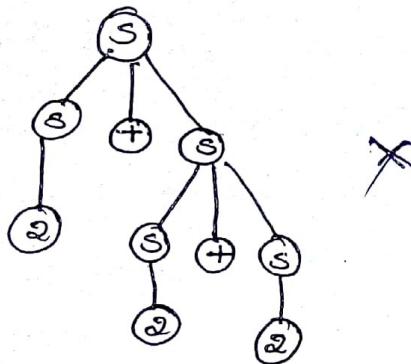
$$\rightarrow 2 + 2 + \underline{S}$$

$$\rightarrow 2 + 2 + 2.$$

$$A \rightarrow \alpha A$$

$$A \rightarrow B$$

Parse tree :-



✗ ea (doesn't current cal)

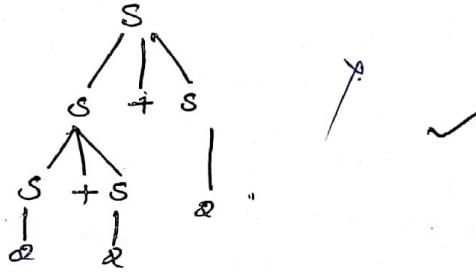
Q, LMD

Draw back :-

The computer may be confused at the time of computing mathematical expressions due to the grammar is Ambiguous.

Q, LMD :-

$$\begin{aligned} S &\rightarrow S + S \\ &\rightarrow S + S + S \\ &\rightarrow 2 + S + S \\ &\rightarrow 2 + 2 + S \\ &\rightarrow 2 + 2 + 2 \end{aligned}$$



for removing ambiguity

1. If the grammar is left associative operators (+, -, \*, /, %)

then induce Left Recursion

$$\begin{aligned} A &\rightarrow A\alpha \\ A &\rightarrow B \end{aligned}$$

2. If the grammar is Right associative operator (=, !, )

then induce the Right Recursion.

$$\begin{aligned} A &\rightarrow \alpha A \\ A &\rightarrow B \end{aligned}$$

Ex:- Consider the Grammar

$$S \rightarrow S + S$$

$$S \rightarrow S * S$$

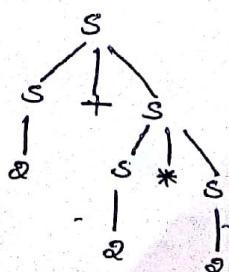
S → 2. And the SLP string is 2 + 2 \* 2.

WMD :- S → S + S

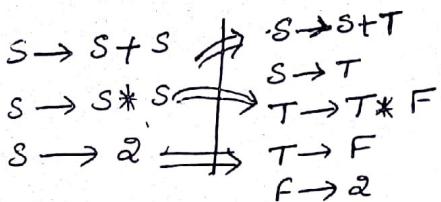
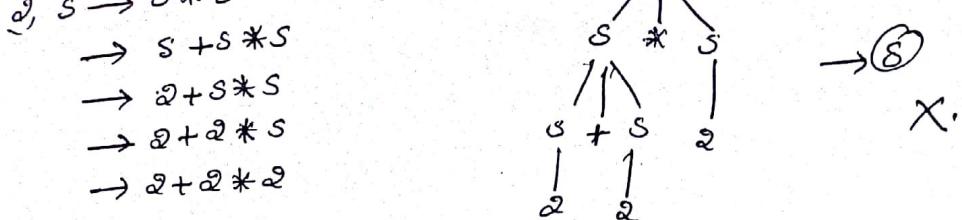
$$\rightarrow 2 + \underline{S}$$

$$\rightarrow 2 + 2 * \underline{S}$$

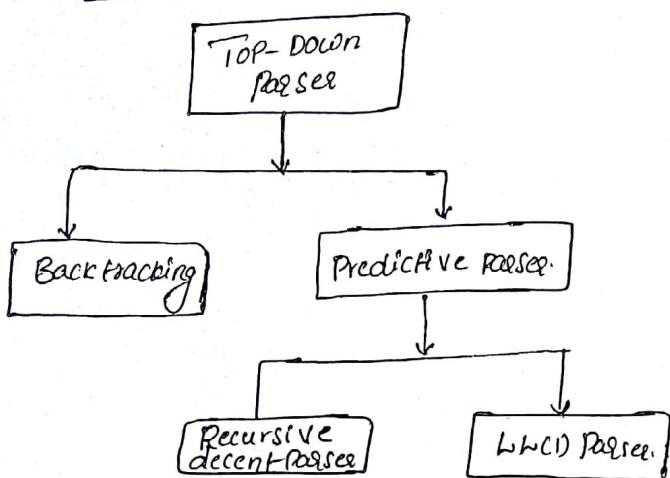
$$\rightarrow 2 + 2 * 2$$



✓ 8



$\rightarrow$  Top-down Parser:



Recursive decent Parser:

- A Parser that uses collection of recursive Procedures for parsing the given input string is called "Recursive decent Parser".
- In this type of Parser the CFG is used to build the recursive procedures.
- The RHS of the Production rule is directly converted to a program.
- for each non-terminal a separate procedure is written and body of the procedure is RHS of the corresponding non-terminal.

STEPS for Construction of Recursive decent Parser:

The RHS of the Production rule is directly converted into Program code symbol by symbol.

- Step 1 :- If the i/p symbol is non-terminal then a call to the procedure corresponding to that non-terminal symbol.
- Step 2 :- If the i/p symbol is terminal then it is matched with the locate symbol from the input.
- Step 3 :- If the production rule has many alternatives then all this alternatives as to be combined in to a single body of Procedure.
- Step 4 :- The Parser should be activated by a procedure corresponding to start symbol.

Ex :- construct a recursive decent parser for the following grammar.

$$\begin{array}{l}
 E \rightarrow E + T \\
 | \\
 E \rightarrow T \\
 | \\
 T \rightarrow TF \\
 | \\
 T \rightarrow F \\
 | \\
 F \rightarrow F^* / a / b
 \end{array}$$

Note :-

The recursive decent parser is works on a cFG with out left recursion.

Sol :- The Given grammar is

$$\begin{array}{l}
 E \rightarrow E + T \\
 | \\
 E \rightarrow T \\
 | \\
 T \rightarrow TF \\
 | \\
 T \rightarrow F \\
 | \\
 F \rightarrow F^* / a / b
 \end{array}$$

The above grammar. Constant left recursion.

So, before constructing RDP we should eliminate Left Recursion from the given grammar.

Elimination of left Recursion :-

$$\begin{array}{l}
 1. E \rightarrow E + T \\
 | \\
 E \rightarrow T \\
 | \\
 E \rightarrow TE' \\
 | \\
 E' \rightarrow +TE' \\
 | \\
 E' \rightarrow E
 \end{array}$$

$$\begin{array}{l}
 2. T \rightarrow TF \\
 | \\
 T \rightarrow F \\
 | \\
 T \rightarrow FT' \\
 | \\
 T' \rightarrow FT' \\
 | \\
 T' \rightarrow E
 \end{array}
 \quad
 \begin{array}{l}
 3. F \rightarrow F^* \\
 | \\
 F \rightarrow a \\
 | \\
 F \rightarrow aF' \\
 | \\
 F' \rightarrow *F \\
 | \\
 F' \rightarrow E
 \end{array}$$

$$\begin{array}{l}
 A \rightarrow A\alpha \Rightarrow A \rightarrow BA' \\
 | \\
 A \rightarrow B \quad A' \rightarrow \alpha A' \\
 | \\
 \alpha \rightarrow e
 \end{array}
 \quad
 \begin{array}{l}
 4. F \rightarrow F^* \\
 | \\
 F \rightarrow b \\
 | \\
 F \rightarrow bF' \\
 | \\
 F' \rightarrow *F' \\
 | \\
 F' \rightarrow E
 \end{array}$$

$\therefore$  the resultant Grammar with out left Recursion :-

RDP :-



$\epsilon \rightarrow T\epsilon'$  $\epsilon' \rightarrow +T\epsilon'$  $\epsilon' \rightarrow \epsilon$  $T \rightarrow FT'$  $T' \rightarrow FT'$  $T' \rightarrow \epsilon$  $F \rightarrow aF'$  $F' \rightarrow *F'$  $F' \rightarrow \epsilon$  $F \rightarrow bF'$ 

→ Construction of Recursive decent Parser :-

Procedure  $\epsilon()$ 

{

T();

ε'();

if (Lookahead == \$)

printf ("In string accepted");

else

printf ("In string rejected");

}

Procedure  $\epsilon'E'()$ 

{

if (lookahead == '+')

{

match ('+');

T();

ε'();

{

Else

{

null;

{

Procedure T()

{

F();

T'();

{

Procedure T'()

{ F(); } if (true)

{ T'(); }

```
else  
    null;  
}  
  
procedure F()  
{  
    if (lookahead == 'a')  
        match ('a');  
        F'();  
    }  
    else  
    {  
        if (lookahead == 'b')  
            match ('b');  
            F'();  
        }  
    }  
}
```

```
procedure F'()  
{  
    if (lookahead == '*')  
        match ('*');  
        F'();  
    }  
    else  
    {  
        null;  
    }  
}
```

```
procedure match (char c)  
{  
    if (lookahead == c)  
        lookahead++;  
    }  
}
```

## LW(1) Parser

\* Introduction.

\* Model of LW(1) Parser.

\* Construction of LW(1) Parser.

### (a) Introduction:-

\* Top-down parser.

\* Non-Recursive parser.

\* Predictive parser.

\* LW(1) means

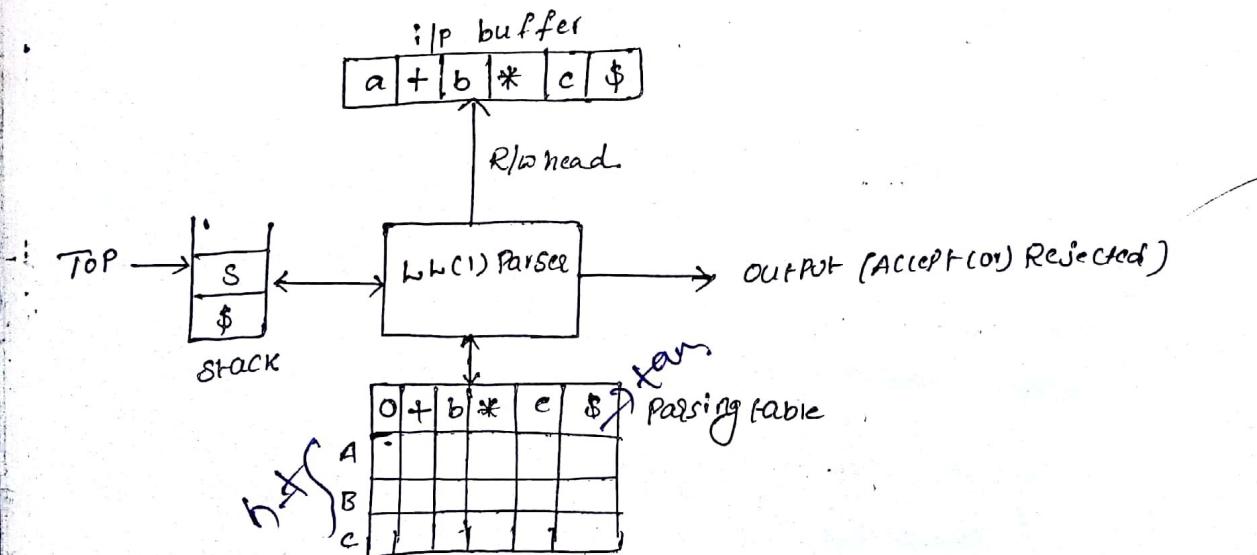
L → Reads the given i/p string from left side to right side.

L → Parse the given i/p string by using "left most derivation".

1 → Reads only one lookahead i/p symbol at a time.

\* It constants a "LW(1) Predictive Parsing table".

### (b) Model of LW(1) parser:-



It contains three data structures like

1. Input buffer. 2. Stack 3. Parsing table.

Input buffer :- LW(1) Parser uses input buffer to store the i/p tokens.

Stack :- LW(1) Parser uses stack to hold the left sentential form.

i.e., the symbols in the R.H.s<sup>of</sup> rule are placed (pushed) into the stack in reverse order that is from right to left.

Parsing table :- It is a two dimensional array contains called rows and columns. Rows represents non-terminals. Columns represent terminals. The table can be represented by  $M[A][J]$ .

where A is a non terminal.

a is a current i/p symbol.

## → Construction of Lw(1) Parser :-

Steps:-

1. computation of FIRST and FOLLOW functions.
2. construction of Lw(1) parser table using FIRST and FOLLOW.
3. construction of Lw(1) parsing algorithm using parser table.

### 1. Computation of FIRST and FOLLOW functions:-

1. FIRST function: FIRST is a set of Terminal symbols that are FIRST symbols appearing at RHS of Production rule.

Rule for computing FIRST function:-

1. If the terminal symbol 'a' then  $\text{FIRST}(a) = \{a\}$
2. If there is a rule ' $X \rightarrow e$ ' then  $\text{FIRST}(X) = \{e\}$
3. for the rule  $A \rightarrow x_1 x_2 x_3 \dots x_n$  then  $\text{FIRST}(A) = \{\text{FIRST}(x_1) \cup \text{FIRST}(x_2) \cup \text{FIRST}(x_3) \cup \dots \cup \text{FIRST}(x_n)\}$ .

Note: Lw. par.

Ex: Compute FIRST function on the following grammar.  $E \rightarrow E + T$   
 $E \rightarrow T$   
 $T \rightarrow T * F$   
 $T \rightarrow F$   
 $F \rightarrow (E)$   
 $F \rightarrow id.$

The grammar without left recursion is

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \\ E' &\rightarrow \epsilon \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \\ T' &\rightarrow \epsilon \\ F &\rightarrow (E) \\ F &\rightarrow id. \end{aligned}$$

Production rule	FIRST
$E \rightarrow TE'$	$\text{FIRST}(T) = \{e, id\}$
$E' \rightarrow +TE'/\epsilon$	$\{+, \epsilon\}$
$T \rightarrow FT'$	$\text{FIRST}(F) = \{c, id\}$
$T' \rightarrow *FT'/\epsilon$	$\{* , \epsilon\}$
$F \rightarrow (E)/id$	$\{c, id\}$

3, compute FIRST function for the following grammar  $S \rightarrow (L)/a$   
 $L \rightarrow L, S/L$

$$\begin{aligned} S &\rightarrow (L)/a \\ L &\rightarrow L, S/L \\ \downarrow & \\ L &\rightarrow SL' \\ L' &\rightarrow , SL' \\ L' &\rightarrow \epsilon \end{aligned}$$

The Grammar without left recursion is

$$\begin{aligned} S &\rightarrow (L)/a \\ L &\rightarrow SL' \\ L' &\rightarrow , SL' \\ L' &\rightarrow \epsilon \end{aligned}$$

Production rule	FIRST
$S \rightarrow (L)/a$	$\{\epsilon, a\}$
$L \rightarrow SL'$	$\text{FIRST}(L) = \{\epsilon, a\}$
$L' \rightarrow , SL'   \epsilon$	$\{\epsilon, \epsilon\}$

3, compute FIRST function on the following grammar.

$$S \rightarrow AaAb | BbBa$$

$$A \rightarrow \epsilon$$

$$B \rightarrow \epsilon$$

The given grammar doesn't contain left recursion.

Production rule	FIRST
$S \rightarrow AaAb   BbBa$	$\{a, b\}$
$A \rightarrow \epsilon$	$\{\epsilon\}$
$B \rightarrow \epsilon$	$\{\epsilon\}$

4, compute FIRST grammar

$$A \quad S \rightarrow aAB \quad (1) \quad B \rightarrow bA \quad (2) \quad \epsilon. \quad (3)$$

$$A \rightarrow aA \quad (1) \quad \epsilon$$

$$B \rightarrow bB \quad (2) \quad \epsilon$$

Production rule	FIRST
$S \rightarrow aAB   bA   \epsilon$	$\{a, b, \epsilon\}$
$A \rightarrow aAb   \epsilon$	$\{a, \epsilon\}$
$B \rightarrow bB   \epsilon$	$\{b, \epsilon\}$

## FOLLOW function:-

FOLLOW(A) is a set of terminal symbols that appear immediately to the right of A. i.e;

$$\text{FOLLOW}(A) = \{ a \mid s \rightarrow \alpha A \beta \}$$

where  $\alpha, \beta$  is grammar symbols.

a. is terminal symbols

## Rules for Computing FOLLOW:-

1.  $\text{FOLLOW}(S) = \{ \$ \}$  where  $S$  is the start symbol.
2. If there is a production rule  $A \rightarrow \alpha B \beta$  then  $\in$   
 $\text{FOLLOW}(B) = \text{FIRST}(\beta)$  accept ' $\epsilon$ ' in  $\text{FIRST}(\beta)$ .
3. If there is a production rule  $\cancel{A \rightarrow BB}$   $\text{FOLLOW}(B) = \text{FIRST}(\beta) \cup \text{FOLLOW}(A)$  if  $\text{FIRST}(\beta)$  contains  $\epsilon$ .
4. If there is a production rule of the form  $A \rightarrow \alpha B$  then  
 $\text{FOLLOW}(B) = \text{FOLLOW}(A)$ .

Ex:- find follow function on the following grammar.  $S \rightarrow Bb/cd$   
 $B \rightarrow AB/\epsilon$   
 $C \rightarrow cC/\epsilon$

Sol:-  $\text{FOLLOW}(S) = \{ \$ \}$

$$\text{FOLLOW}(B) = \{ b \}$$

$$\text{FOLLOW}(C) = \{ d \}$$

Ex:- compute ~~FIRST~~ and follow functions 'on the following grammar.'

$$\begin{array}{ll} S \rightarrow ABCDE & C \rightarrow C \\ A \rightarrow a\epsilon & b \rightarrow d\epsilon \\ B \rightarrow b\epsilon & \epsilon \rightarrow \epsilon \end{array}$$

Y

$$S \rightarrow ABCDE$$

Sol:-  $\text{FIRST}(S) = \text{FIRST}(A)$

$$A \rightarrow \underline{a} = \{ a \}$$

$$A \rightarrow \underline{\epsilon}$$

$$\begin{aligned} \text{FIRST}(A) &= \{ a \} \cup \{ \epsilon \} \\ &= \{ a, \epsilon \} \end{aligned}$$

$$B \rightarrow \underline{b}$$

$$B \rightarrow \underline{\epsilon}$$

$$\begin{aligned} \text{FIRST}(B) &= \{ b \} \cup \{ \epsilon \} \\ &= \{ b, \epsilon \} \end{aligned}$$

$$\begin{array}{l}
 C \rightarrow c \\
 C \rightarrow \epsilon \\
 \text{FIRST}(C) = \{c\} \cup \{\epsilon\} \\
 = \{c, \epsilon\}
 \end{array}
 \quad
 \begin{array}{l}
 D \rightarrow d \\
 D \rightarrow \epsilon \\
 \text{FIRST}(D) = \{d\} \cup \{\epsilon\} \\
 = \{d, \epsilon\}
 \end{array}$$

$$\begin{array}{l}
 E \rightarrow e \\
 E \rightarrow \epsilon \\
 \text{FIRST}(E) = \{e\} \cup \{\epsilon\} \\
 = \{e, \epsilon\}
 \end{array}$$

$$\begin{array}{l}
 S \rightarrow ABCDE \\
 S \rightarrow ABCDE
 \end{array}
 \quad
 \text{FIRST}(S) = \{a\}$$

$$\begin{array}{lll}
 S \rightarrow ECBDE & S \rightarrow BCDE & S \rightarrow ECDE \\
 S \rightarrow B CDE & S \rightarrow b CDE & S \rightarrow CDE \\
 \text{FIRST}(S) = \text{FIRST}(B) & \text{FIRST}(S) = \{b\} & \text{FIRST}(S) = \text{FIRST}(C) \\
 = \{b, \epsilon\} & & = \{c\}
 \end{array}$$

$$\therefore \text{FIRST}(S) = \{a\} \cup \{b\} \cup \{c\} \\
 = \{a, b, c\}$$

Computation of FOLLOW :-

$$\begin{array}{l}
 S \rightarrow ABCDE \\
 A \rightarrow a | \epsilon \\
 B \rightarrow b | \epsilon \\
 C \rightarrow c \\
 D \rightarrow d | \epsilon \\
 E \rightarrow e | \epsilon
 \end{array}$$

$$\text{FOLLOW}(S) = \{\$\}$$

$$\text{FOLLOW}(A) = \{b, c\}$$

$$\text{FOLLOW}(B) = \{c\}$$

$$\text{FOLLOW}(C) =$$

$$S \rightarrow ABCDE$$

$$\text{FOLLOW}(A) = \text{FIRST}(B)$$

$$= \{b, e\}$$

$$1, S \rightarrow A\underline{BCDE}$$

$$S \rightarrow A\underline{bcde}$$

$$\text{FOLLOW}(A) = \{b\}$$

$$2, S \rightarrow A\underline{BCDE}$$

$$S \rightarrow A\underline{c}DE$$

$$S \rightarrow A\underline{CD}E$$

$$\text{FOLLOW}(A) = \text{FIRST}(C)$$

$$= \{c\}$$

$$S \rightarrow ABCDE$$

$$\text{FOLLOW}(B) = \text{FIRST}(C)$$

$$= \{c\}$$

$$S \rightarrow AB\underline{CDE}$$

$$\text{FOLLOW}(C) = \text{FIRST}(D)$$

$$= \{d, e\}$$

$$① S \rightarrow ABCDE$$

$$S \rightarrow A\underline{B}cdE$$

$$\text{FOLLOW}(C) = \{d\}$$

$$② S \rightarrow ABCDE$$

$$S \rightarrow A\underline{B}cDE$$

$$S \rightarrow ABCE$$

→ Construction of LR(0) Parse Table:

Algorithm:-

CONSTRUCTION for the rule  $A \rightarrow \alpha$  of grammar 'G'.

Step1:- for each ' $\alpha$ ' in FIRST( $\alpha$ ) create entry ' $M[A, \alpha] = A \rightarrow \alpha$ '

where ' $\alpha$ ' is a terminal symbol.

Step2:- for ' $\epsilon$ ' in FIRST( $\alpha$ ) create entry ' $M[A, \epsilon] = A \rightarrow \alpha$ '.

where ' $b$ ' is a terminal symbol. In FOLLOW(A).

Step3:- If  $\epsilon$  in FIRST( $\alpha$ ) and  $\$ \in \text{FOLLOW}(A)$  then create entry  
in the table  $M[A, \$] = A \rightarrow \alpha$ .

Step4:- All the remaining entries in the table M are marked as  
syntax "SYNTAX ERRORS".

It means :- If re

Ex:- CONSTRUCT

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \mid e \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \mid e \\ F &\rightarrow (E) \mid id \end{aligned}$$

$$\rightarrow FIRST(E) = FIRST(T) = \{e, id\}$$

$$FIRST(T) = FIRST(F) = \{c, id\}$$

$$FIRST(E') = \{+, e\}$$

$$FIRST(T') = \{\ast, e\}$$

$$FIRST(F) = \{c, id\}$$

$$FOLLOW(E) = \{\$, \}\}$$

$$FOLLOW(E') = FOLLOW(E) = \{\$, \}\}$$

$$FOLLOW(T) = \{+, \$, \}\}$$

$$FOLLOW(T') = \{+, \$, \}\}$$

$$e \rightarrow TE'$$

$$\begin{aligned} FOLLOW(T) &= FIRST(E') \\ &= \{+, e\} \end{aligned}$$

$$e \rightarrow TE$$

$$e \rightarrow T$$

$$\begin{aligned} FOLLOW(T) &= FOLLOW(E) \\ &= \{\$, \} \end{aligned}$$

$$\therefore FOLLOW(T) = \{+, \$, \}\}$$

$$e' \rightarrow TE$$

$$e' \rightarrow +T$$

$$\begin{aligned} FOLLOW(T) &= FOLLOW(E') \\ &= \{\$\}\} \end{aligned}$$

$$T' \rightarrow * F e$$

$$T' \rightarrow * F$$

$$\begin{aligned} FOLLOW(F) &= FOLLOW(T') \\ &= \{+, \$, \}\} \end{aligned}$$

WJ

$$T^* \rightarrow * FT'$$

$$\begin{aligned} FOLLOW(F) &= FIRST(T') \\ &= \{\ast, e\} \end{aligned}$$

$$T \rightarrow FT'$$

$$\begin{aligned} FOLLOW(F) &= FIRST(T') \\ &= \{\ast, e\} \end{aligned}$$

$$T \rightarrow FT'$$

$$\begin{aligned} FOLLOW(T) &= FOLLOW(T') \\ &= \{+, \$, \}\} \end{aligned}$$

$$T \rightarrow F$$

$$T \rightarrow F$$

$$\begin{aligned} FOLLOW(F) &= FOLLOW(T) \\ &= \{+, \$, \}\} \end{aligned}$$

$$\therefore FOLLOW(F) = \{+, *, \$, \}\}$$

LAL(1) Parse Table :-

	+	*	(	)	id	\$
E			$E \rightarrow TE'$		$E \rightarrow TE'$	
E'	$E' \rightarrow +TE'$			$E' \rightarrow E$		$e' \rightarrow e$
T			$T \rightarrow FT'$		$T \rightarrow FT'$	
T'	$T' \rightarrow E$	$T' \rightarrow *FT'$		$T' \rightarrow e$		$T' \rightarrow e$
F			$F \rightarrow (E)$		$F \rightarrow id$	

$$\rightarrow E \rightarrow TE'$$

$$\begin{aligned} \Downarrow FIRST(TE') &= FIRST(T) \\ &= \{c, id\} \end{aligned}$$

$$E' \rightarrow +TE'$$

$$\begin{aligned} \Downarrow FIRST(+TE') &= FIRST(+T) \\ &= \{+\} \end{aligned}$$

$$3, E' \rightarrow E$$

$\Downarrow$

$FIRST(E) = \{e\}$

$\Rightarrow FOLLOW(E') = \{\$, )\}$

$$4, T \rightarrow FT$$

$\Downarrow$

$FIRST(FT) = FIRST(F)$   
 $= \{c, id\}$

$$5, T' \rightarrow *FT'$$

$\Downarrow$

$FIRST(*FT') = FIRST(*)$   
 $= \{* \}$

$$6, T' \rightarrow E$$

$\Downarrow$

$FIRST(E) = \{e\}$

$FOLLOW(T') = \{+, b, )\}$

7, F  $\rightarrow (E)$

$\Downarrow$

$FIRST((E)) = \{c\}$

$$F \rightarrow id$$

$\Downarrow$

$FIRST(id) = \{id\}$

WCD Parsing algorithm:-

consider the i/p string ~~id+id\*id.~~  $((a), a)$

stack	input-string	Action
\$ S	$((a), a)\$$	$S \rightarrow C(L)$
\$) L	$((a), a)\$$	POP
\$) L	$(a), a)\$$	$L \rightarrow SL^1$
\$) L	$(a), a)\$$	$S \rightarrow C(L)$
\$) L	$(a), a)\$$	POP
\$) L	$(a), a)\$$	$L \rightarrow SL^1$
\$) L	$a), a)\$$	$S \rightarrow a$
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	$L^1 \rightarrow \epsilon$
\$) L	$a), a)\$$	-
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	$L^1 \rightarrow SL^1$
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	$S \rightarrow a$
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	$L^1 \rightarrow \epsilon$
\$) L	$a), a)\$$	-
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	$L^1 \rightarrow \epsilon$
\$) L	$a), a)\$$	-
\$) L	$a), a)\$$	POP
\$) L	$a), a)\$$	accepted. X

- ① construct LL(1) parser table for the following grammar
- $S \rightarrow (L) / a$
- $L \rightarrow L, S / s$  and check the input string (a), a. is replaced or not by the LL(1) parser.

- ② construct LLL(1) parser table for the following grammar.

$$S \rightarrow PETSS'$$

$$S \rightarrow a$$

$$S' \rightarrow eS / \epsilon$$

$$\epsilon \rightarrow b.$$

### Error Recovery in Predictive Parser:-

→ An error is detected during predictive parsing when the terminal on the top of the stack does not match the next input symbol (or).

→ when non-terminal A on the top of the stack a is the next input symbol and parsing table entry  $E M[A, a]$  is empty.

→ the process of reducing number of errors in the parser table is called error recovery.

→ LLL(1) parser uses "panic mode" error recovery technique.

### "Panic mode Error recovery"

It is based on the idea of skipping symbols on the I/P until a synchronizing token is selected.

Synchronizing token: It is a set of terminals obtained from follow <sup>of</sup> non-terminal in the given grammar.

$$\text{ex: } \text{FOLLOW}(E) = \{ \$, \}, \{ \}$$

$$\text{FOLLOW}(E') = \{ \{ \}, \} \}$$

$$\text{FOLLOW}(T) = \{ +, \$, \} \}$$

$$\text{FOLLOW}(T') = \{ +, \$, \} \}$$

$$\text{FOLLOW}(F) = \{ *, +, \$, \} \}$$

After applying panic mode error recovery technique modified  
LHCD parse table is.

	+	*	(	)	id	\$
E			$\epsilon \rightarrow T\epsilon'$	sync	$\epsilon \rightarrow T\epsilon'$	sync
$E'$	$\epsilon' \rightarrow \epsilon T\epsilon'$			$\epsilon' \rightarrow \epsilon$		$\epsilon' \rightarrow \epsilon$
T	sync		$T \rightarrow FT'$	sync	$T \rightarrow FT'$	sync
$T'$	$T' \rightarrow E$	$T' \rightarrow F$		$T' \rightarrow E$		$T' \rightarrow E$
F	sync	sync	$F \rightarrow (E)$	sync	$F \rightarrow id$	sync

### Parsing Algorithm:-

\* If the parser look up the entry M [AA] as ablank then the iIP symbol 'a' skipped.

\* If the entry is 'sync' then the non-terminal at top of the stack is popped.

\* If the token on the top of the stack doesn't match the iIP symbol then we pop on the token from the stack.

Ex:- consider the iIP string + id \*\* id.

Stack	iIP string	Action
\$ E	+ id ** id \$	Skipped +
\$ E	id ** id \$	$\epsilon \rightarrow T\epsilon'$
\$ E' T	id ** id \$	$T \rightarrow FT'$
\$ E' T' F	id ** id \$	$F \rightarrow id$
\$ E' T' F	id ** id \$	Pop
\$ E' T' id	** id \$	$T' \rightarrow *FT'$
\$ E' T' id	* id \$	Pop
\$ E' T' F *	* id \$	syn, Pop
\$ E' T' F *	* id \$	$T' \rightarrow *FT'$
\$ E' T' F *	* id \$	Pop
\$ E' T' F *	id \$	$F \rightarrow id$
\$ E' T' id	id \$	Pop
\$ E' id	\$	$T' \rightarrow \epsilon$