

Example:

Solve the system of linear equations using the Elimination Algorithm:

$$(a) \begin{cases} x + 3y = 4 \\ 2x - y = 1 \\ x - y = 0 \end{cases}$$

$$(b) \begin{cases} 5x - 2y = -9 \\ x - 3y = -7 \\ 3x + 2y = 1 \end{cases}$$

Example:

Solve the system of linear equations using the Elimination

Algorithm:

$$(a) \begin{cases} 2x_1 + 3x_2 = 1 \\ 3x_1 + 5x_2 = 0 \\ x_1 + x_2 = 1 \end{cases}$$

$$(b) \begin{cases} x + 2y = 1 \\ -x + 2y = 3 \\ 2x + 3y = 0 \end{cases}$$

Example:

Solve the system of linear equations using the Elimination Algorithm:

$$(a) \begin{cases} x - 2y + z = 2 \\ 2x - 3y + 4z = 5 \\ -x + 3y + 2z = 1 \end{cases}$$

$$(b) \begin{cases} 4x_1 - 4x_2 + 3x_3 = 5 \\ x_1 - 2x_2 + x_3 = 3 \\ 2x_1 - x_2 + 5x_3 = 12 \end{cases}$$

Example:

Solve the system of linear equations using the Elimination Algorithm:

$$(a) \begin{cases} x + y - z = 1 \\ 2x + 3y + z = 6 \\ 5x + 7y + z = 13 \end{cases}$$

$$(b) \begin{cases} 2x_1 + x_2 + x_3 = 2 \\ 8x_1 + 3x_2 + 5x_3 = 4 \\ 3x_1 + x_2 + 2x_3 = -2 \end{cases}$$

Example :

A system of linear equations is given by
$$\begin{cases} x + y - z = 1 \\ 2x + 3y + z = 6. \\ 5x + 7y + z = k \end{cases}$$

Find the value of k for which the system has solution.

Find the solution in this case.

Example:

Solve the system of linear equations
$$\begin{cases} x + y + z = 2 \\ 2x + (a + 1)y + az = 3 \\ 3x + (a - 2)y + 3z = a + 1 \end{cases},$$

where $a \in \mathbb{R}$, completely for $x, y, z \in \mathbb{R}$.

Example:

Find the value of k for which the system of linear equations

$$\begin{cases} x + 2y + 3z = 7 \\ 2x + y + 4z = 4k^2 - 3, \text{ where } k \in \mathbb{R}, \text{ does not have a unique} \\ 2x - 2y + kz = 6k \end{cases}$$

solution. Find the solution in this case.

Homework

Please attempt all the questions in the following slides.

Questions are to be discussed on the next day of the instruction.

Example:

Solve the system of linear equations $\begin{cases} 2x - y - 6z = 6 \\ x + y - z = 4 \\ x - 2y + 3z = -6 \end{cases}$

for $x, y, z \in \mathbb{R}$.

Example:

Solve the system of linear equations using the Elimination Algorithm:

$$(a) \begin{cases} x - y + z = 2 \\ 2x + 3y - z = 4 \\ 3x + 7y - 3z = 5 \end{cases}$$

$$(b) \begin{cases} x_1 + x_2 - x_3 = 0 \\ 2x_1 + 3x_2 + x_3 = 0 \\ 5x_1 + 7x_2 + x_3 = 0 \end{cases}$$

Example:

Solve the system of linear equations $\begin{cases} x + y = 2 \\ 2x - y = 7 \\ 3x - ay = 2 \end{cases}$, where $a \in \mathbb{R}$,

completely for $x, y \in \mathbb{R}$.

Example :

A system of linear equations is given by
$$\begin{cases} ax + y + z = 2 \\ 2x - z = 3 \\ x + y + 2z = a \end{cases}.$$

(a) Show that the system has a unique solution if $a \neq 3$.

Find the solution in this case.

(b) Determine whether there is any solution if $a = 3$.

Example :

A system of linear equations is given by
$$\begin{cases} x + y + z = 3 \\ x + 2y + kz = 6 \\ x + ky + (k + 2)z = 9 \end{cases} .$$

- (a) Find the values of k such that the system does not have a unique solution.
- (b) Solve the system for each of these values of k .

Example :

A system of linear equations is given by
$$\begin{cases} 2x + ay - z = 0 \\ 3x + 4y - (a + 1)z = 13 \\ 10x + 8y + (a - 4)z = 26 \end{cases} .$$

(a) Find the values of a such that the system does not have a unique solution.

(b) Solve the system for each of these values of a .

Example :

A system of linear equations is given by
$$\begin{cases} x + ky + kz = 0 \\ kx + y + kz = 0. \\ kx + ky + z = 0 \end{cases}$$

- (a) Find the values of k such that the system does not have a unique solution .
- (b) Solve the system completely for $x, y, z \in \mathbb{R}$.

Example:

A system of linear equations is given by
$$\begin{cases} -y + z = kx \\ y + z = ky \\ 2z = kz \end{cases}.$$

- (a) Find the values of k such that the system has an infinite number of solutions for x , y and z .
- (b) Solve the system for each of these values of k .