


July 2007 Intake Paper 1 (FM1) [Examination date: 28 August 2008]

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| 1. | PROVE |
| 2. | PROVE |
| 3. | $\left(\frac{727}{737}, \frac{-490}{737}, \frac{58}{737}\right)$ |
| 4. | $27u^4 - 27u^3 + 90u^2 - 19u + 42 = 0$ |
| 5. | $\left(\frac{4}{5}, \frac{2}{7}\right)$ |
| 6. | <p>i) Asymptotes : $y = 4$, $x = 6$ and $x = \frac{-3}{2}$</p> <p>ii) Critical points : $\left(-4, \frac{23}{5}\right)$ and $\left(0, \frac{7}{3}\right)$</p> |
| 7. | $\frac{16\sqrt{2}-8}{3}$ |
| 8. | $(n-1)I_n = (n-2)I_{n-2} - \csc^{n-2} x \cot x$; $I_3 = \frac{-1}{2} \ln \csc x + \cot x - \frac{1}{2} \csc x \cot x + C$; $I_4 = \frac{-2}{3} \cot x - \frac{1}{3} \csc^2 x \cot x + C$ |
| 9. | $\frac{-1}{32} \cos 6\theta + \frac{3}{16} \cos 4\theta - \frac{15}{32} \cos 2\theta + \frac{5}{16}$; $\frac{5}{16}$ |
| 10. | $10r^4 + 20r^2 + 2$; $\frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{6n^5+15n^4+10n^3-1}{30}$ |
| 11E. | <p>i) </p> <p>ii) $r_{\max} = 2$ at $\theta = \frac{\pi}{2}$</p> <p>iii) $\frac{\pi + \sqrt{3}}{2}$</p> |
| 11O. | $\frac{d^2 z}{dx^2} + 5 \frac{dz}{dx} + 4z = 3e^{7x}$; $y = \left(Ae^{-x} + Be^{-4x} + \frac{3}{88}e^{7x}\right)^{\frac{1}{5}}$ |