July 2004 Intake Paper 1 (FM1) [Examination date: 24 August 2005]

2.
$$2cis\left(\frac{-\pi}{10}\right)$$
; $2cis\left(\frac{3\pi}{10}\right)$; $2cis\left(\frac{7\pi}{10}\right)$; $2cis\left(\frac{-\pi}{2}\right)$; $2cis\left(\frac{-9\pi}{10}\right)$

3.
$$\sin \frac{k\pi}{15}$$
, $k=1,2,4,5,7$

4. i)
$$(x+1)e^x$$
; $(x+2)e^x$; $(x+3)e^x$; (ii) $(x+n)e^x$

5.
$$\begin{vmatrix} i & 1 & 0 & 0 \\ 1 & -1 & 0 \\ \frac{-1}{a} & 0 & \frac{1}{a} \end{vmatrix}$$
; (ii)
$$\begin{vmatrix} 1 & -1 & -1 \\ 1 & -2 & \frac{-3}{2} \\ \frac{-1}{a} & \frac{1}{a} & \frac{3}{2a} \end{vmatrix}$$

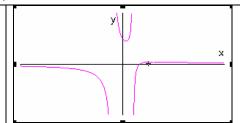
(ii)
$$\frac{2\sqrt{3}}{9}a$$

8. i)
$$(11-2a)\mathbf{x} + (10+5a)\mathbf{y} - 25\mathbf{z} + 25a = 0$$
 (ii) $a = -132$

i)
$$x = \pm 1, y = 0$$

9. ii) Min.
$$\left(\frac{1}{3}, 4\frac{1}{2}\right)$$
;

Max.
$$\left(3, \frac{1}{2}\right)$$



10. i) 2 (ii) 2;
$$\begin{cases} 2 \\ 4 \\ 1 \\ 0 \end{cases}, \begin{pmatrix} -1 \\ 2 \\ 0 \\ 1 \end{pmatrix}$$
 (iii)
$$\begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 4 \\ 1 \\ 0 \end{pmatrix} + \beta \begin{pmatrix} -1 \\ 2 \\ 0 \\ 1 \end{pmatrix}$$

11.
$$\lambda_{1} = 1, \mathbf{e}_{1} = \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} ; \quad \lambda_{2} = 3, \mathbf{e}_{2} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} ;$$

$$\lambda_{3} = 5, \mathbf{e}_{3} = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} ; \quad \mathbf{P} = \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix} ;$$

$$\lambda_3 = 5$$
, $\mathbf{e}_3 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}$; $\mathbf{P} = \begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{pmatrix}$;

$$\mathbf{D} = \begin{pmatrix} (1-k)^n & 0 & 0 \\ 0 & (3-k)^2 & 0 \\ 0 & 0 & (5-k)^n \end{pmatrix}$$

12E.
$$A\cos 3x^2 + B\sin 3x^2 - \frac{2}{3}$$

120.
$$\left(\frac{2e-5}{e-2}, \frac{e^2-5}{8e^2-16e}\right)$$