## July 2003 Intake Paper 1 (FM1) [Examination date: 3 September 2004]

1. 
$$a = 30$$
,  $b = 14$ ,  $c = -3$ ,  $d = -1$ 

2. 
$$y = x + a - 3, x = -3$$

$$3. \left\{ \begin{pmatrix} 2\\45\\-49 \end{pmatrix}, \begin{pmatrix} 13\\7\\-14 \end{pmatrix} \right\}$$

$$\lambda_{1} = 1, \mathbf{e}_{1} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}; \quad \lambda_{2} = 3, \mathbf{e}_{2} = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}; \quad \lambda_{3} = 4, \mathbf{e}_{3} = \begin{pmatrix} 5 \\ 3 \\ -3 \end{pmatrix}; \quad \mathbf{Q} = \begin{pmatrix} 1 & 1 & 5 \\ 0 & 1 & 3 \\ 0 & 0 & -3 \end{pmatrix};$$

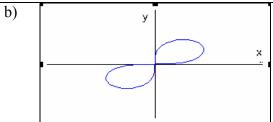
c)  $\sqrt{2}$ 

$$\mathbf{D} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 243 & 0 \\ 0 & 0 & 1024 \end{pmatrix}$$

5. 
$$\frac{28}{15}$$

8.

7. a) 
$$m = 3$$



9. b) 
$$\frac{1}{\theta}\sec\theta - \frac{4}{\theta^3}\sec\theta + \frac{2}{\theta}\sec^3\theta$$

10. 
$$\sin^6 \theta = \frac{-1}{32} \cos 6\theta + \frac{3}{16} \cos 4\theta - \frac{15}{32} \cos 2\theta + \frac{5}{16} ; \frac{5}{16} - \frac{11}{12\pi}$$

11. 
$$\begin{vmatrix} b & 3 \\ 4 \\ -5 \end{vmatrix}$$
; c) 6

12E. a) 
$$\frac{14}{3}$$
; b)  $\frac{5\sqrt{3}}{8}$ 

12O. 
$$A = -4.901 \times 10^9$$
;  $B = 1.590 \times 10^9$ ;  $1.874 \times 10^9$