## June 2005 Intake Paper 1 (FM1) [Examination date: 29 August 2006]

1. 
$$4\pi a^2$$

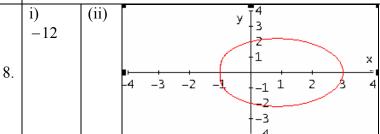
2. 
$$\frac{1}{r} - \frac{2}{r+2} + \frac{1}{r+3}$$
;  $\frac{7}{6} - \frac{1}{n+1} - \frac{1}{n+2} + \frac{1}{n+3}$ 

3. ii) 
$$\frac{16}{15\pi}$$

5. 
$$\frac{1}{12}$$

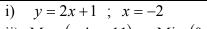
6. 
$$\frac{5\pi}{8}$$

7. i) 
$$y = \frac{3}{a}e^{ax} + \frac{1}{a}e^{ax}$$
; (ii)  $y = Ae^x + Be^{2x} + 3\cos x + \sin x$ 



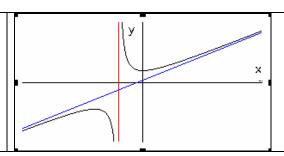


9. PROVE



ii) 
$$Max.(-4,-11)$$
;  $Min.(0,5)$ 

10. iii) Intersection (0, 5)



11E. i) 
$$\frac{15}{\sqrt{62}}$$
 (ii)  $\begin{pmatrix} \frac{71}{31} \\ \frac{40}{31} \\ \frac{58}{31} \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 7 \\ -3 \end{pmatrix}$  (iii)  $\frac{\sqrt{60294}}{62}$ 

110. a) 3; 
$$\begin{cases} \begin{pmatrix} 1 \\ 1 \\ 1 \\ -1 \end{pmatrix}$$
 (b) i)  $\lambda_1 = 1$ ,  $\mathbf{e}_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$ ;  $\lambda_2 = 2$ ,  $\mathbf{e}_2 = \begin{pmatrix} 3 \\ 1 \\ 0 \end{pmatrix}$ ;  $\lambda_3 = -3$ ,  $\mathbf{e}_3 = \begin{pmatrix} 1 \\ 8 \\ 5 \end{pmatrix}$