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Cambridge International General Certificate of Secondary Education

MARK SCHEME for the May/June 2015 series

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0606 ADDITIONAL MATHEMATICS

0606/12 Paper 1, maximum raw mark 80

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Abbreviations

awrt	answers which round to
cao	correct answer only
.1	4 4 4

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

www without wrong working

1	$k^2 - 4(2k+5)$ (< 0) $k^2 - 8k - 20$ (< 0)	M1	use of $b^2 - 4ac$, (not as part of quadratic formula unless isolated at a later stage) with correct values for a , b and c
	(k-10)(k+2) (< 0) critical values of 10 and -2 -2 < k < 10	M1 A1 A1	Do not need to see < at this point attempt to obtain critical values correct critical values correct range
	Alternative 1:		
	$\frac{\mathrm{d}y}{\mathrm{d}x} = 2(2k+5)x+k$	M1	attempt to differentiate, equate to zero and substitute <i>x</i> value back in to obtain a <i>y</i> value
	When $\frac{dy}{dx} = 0$, $x = \frac{-k}{2(2k+5)}$, $y = \frac{8k+20-k^2}{4(2k+5)}$	M1	consider $y = 0$ in order to obtain critical values
	When $y = 0$, obtain critical values of 10 and -2 -2 < k < 10	A1 A1	correct critical values correct range
	Alternative 2:		
	$y = (2k+5) \left(\left(x + \frac{k}{2(2k+5)} \right)^2 - \frac{k^2}{4(2k+5)} \right) + 1$	M1	attempt to complete the square and consider $1 - \frac{k^2}{4(2k+5)}$ '
	Looking at $1 - \frac{k^2}{4(2k+5)} = 0$ leads to	M1	attempt to solve above = to 0, to obtain critical values
	critical values of 10 and -2 -2 < k < 10	A1 A1	correct critical values correct range

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2	$\frac{\tan\theta + \cot\theta}{\csc\theta} = \frac{\frac{\sin\theta}{\cos\theta} + \frac{\cos\theta}{\sin\theta}}{\frac{1}{\sin\theta}}$	M1	for $\tan \theta = \frac{\sin \theta}{\cos \theta}$, $\cot \theta = \frac{\cos \theta}{\sin \theta}$ and $\csc \theta = \frac{1}{\sin \theta}$; allow when used
	$= \frac{\sin^2 \theta + \cos^2 \theta}{\frac{\sin \theta \cos \theta}{\sin \theta}}$	M1	dealing correctly with fractions in the numerator; allow when seen
	$=\frac{1}{\cos\theta}$	M1	use of the appropriate identity; allow when seen
	$= \sec \theta$	A1	must be convinced it is from completely correct work (beware missing brackets)
	Alternative:		
	$\frac{\tan\theta + \cot\theta}{\csc\theta} = \frac{\frac{\tan^2\theta + 1}{\tan\theta}}{\csc\theta}$	M1	for either $\tan \theta = \frac{1}{\cot \theta}$ or
			$\cot \theta = \frac{1}{\tan \theta}$ and
	$=\frac{\sec^2\theta}{\tan\theta\frac{1}{\sin\theta}}$	M1	$cosec\theta = \frac{1}{sin \theta}$; allow when used dealing correctly with fractions in numerator; allow when seen
	$=\frac{\sec^2\theta}{\sec\theta}$	M1	use of the appropriate identity; allow when seen
	$= \sec \theta$	A1	must be convinced it is from completely correct work
3	$\mathbf{A}^{-1} = \frac{1}{2} \begin{pmatrix} 3 & -2 \\ -5 & 4 \end{pmatrix}$	B1	$\frac{1}{2}$ multiplied by a matrix
		B1	for matrix
	$ \begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & -2 \\ -5 & 4 \end{pmatrix} \begin{pmatrix} 8 \\ 9 \end{pmatrix} $	M1	attempt to use the inverse matrix, must be pre-multiplication
	$ \begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 6 \\ -4 \end{pmatrix} $		
	x = 3, y = -2	A1, A1	
L	I	l	<u>l</u>

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4	(i)	Area = $ \left(\frac{1}{2} \times 12^2 \times 1.7 \right) + \left(\frac{1}{2} \times 12^2 \sin(2\pi - 1.7 - 2.4) \right) $	B1,B1	B1 for sector area, allow unsimplified B1 for correct angle <i>BOC</i> , allow
			M1	unsimplified correct attempt at area of triangle, allow unsimplified using <i>their</i> angle <i>BOC</i> (Their angle <i>BOC</i> must not be 1.7 or 2.4)
		= awrt 181	A1	0. 2. 1)
	(ii)	$BC^{2} = 12^{2} + 12^{2} - (2 \times 12 \times 12 \cos 2.1832)$ or $BC = 2 \times 12 \times \sin\left(\frac{2\pi - 4.1}{2}\right)$	M1	correct attempt at <i>BC</i> , may be seen in (i), allow if used in (ii). Allow use of <i>their</i> angle <i>BOC</i> .
		BC = 21.296	A1	-
		Perimeter = $(12 \times 1.7) + 12 + 12 + 21.296$	B1 M1	for arc length, allow unsimplified for a correct 'plan' (an arc + 2 radii and BC)
		= 65.7	A1	20)
5	(a) (i)	20160	B1	
	(ii)	$3 \times {}^6P_4 \times 2$	B1,B1	B1 for 6P_4 (must be seen in a
	()	= 2160	,	product) B1 for all correct, with no further working
	(iii)	$5 \times 2 \times {}^6P_4$	B1,B1	B1 for 6P_4 (must be seen in a
		= 3600	B1	product) B1 for 5 (must be in a product) B1 for all correct, with no further working
		Alternative 1: ${}^{6}C_{4} \times 5! \times 2$	D1	
		= 3600	B2 B1	for ${}^6C_4 \times 5!$ for ${}^6C_4 \times 5! \times 2$
		Alternative 2:		,
		$(^{7}P_{5}-^{6}P_{5})\times 2$	B2	for $\left({}^{7}P_{5} - {}^{6}P_{5}\right)$
		= 3600	B1	for $(^7P_5 - ^6P_5) \times 2$
		Alternative 3:		
		$2!({}^{6}P_{4} + ({}^{6}P_{1} \times {}^{5}P_{3}) + ({}^{6}P_{2} \times {}^{4}P_{2}) + ({}^{6}P_{3} \times {}^{3}P_{1}) + {}^{6}P_{4})$	B2	4 terms correct or omission of 2! in
		= 3600	B1	each term all correct

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	(b) (i)	$^{14}C_4 \times ^{10}C_4$ or $^{14}C_8 \times ^8C_4$ (or numerical or factorial equivalent) = 210210	B1,B1	B1 for either ${}^{14}C_4$ or ${}^{14}C_8$ as part of a product B1 for correct answer, with no further working
	(ii)	${}^{8}C_{4} \times {}^{6}C_{4}$ = 1050	B1,B1	B1 for either 8C_4 or 6C_4 as part of a product B1 for correct answer with no further working
6	(i)	10ln4 or 13.9 or better	B1	
	(ii)	$\left(\frac{\mathrm{d}x}{\mathrm{d}t} = \right) \frac{20t}{t^2 + 4} - 4$		attempt to differentiate and equate to zero $\frac{20t}{t^2 + 4}$ or equivalent seen
		When $\frac{dx}{dt} = 0$, $\frac{20t}{t^2 + 4} = 4$ leading to $t^2 - 5t + 4 = 0$ t = 1, $t = 4$	DM1	attempt to solve their $\frac{dx}{dt} = 0$, must be a 2 or 3 term quadratic equation with real roots for both

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(iii)	$If (v =) \frac{20t}{t^2 + 4} - 4$		
	$(a=) \frac{20(t^2+4)-20t(2t)}{(t^2+4)^2}$	M1	attempt to differentiate their $\frac{dx}{dt}$
	(* ' ')	A1	$20(t^2+4)$
		A1	20t(2t)
	$20(4-t^2)$ or $80-20t^2$ or $4-t^2$ or equivalent	A1	$20(4-t^2)$ or $80-20t^2$ or $4-t^2$
	expression involving $-t^2$	D1	t = 2, dependent on obtaining first
	When acceleration is 0, $t = 2$ only	B1	and second A marks
	Alternative 1 for first 3 marks:		dx
	$If(v=) \frac{20t - 4t^2 - 16}{t^2 + 4}$	M1	attempt to differentiate their $\frac{dx}{dt}$
	$(a=)\frac{(t^2+4)(20-8t)-(20t-4t^2-16)(2t)}{(t^2+4)^2}$	A1	for $(t^2 + 4)(20 - 8t)$ for $(20t - 4t^2 - 16)(2t)$
	$\left(t^2+4\right)^2$	A1	for $(20t - 4t^2 - 16)(2t)$
	Alternative 2 for M1 mark:		
	If $(v =) 20t(t^2 + 4)^{-1} - 4$		dx
	$(a =) 20t \left(-2t \left(t^2 + 4\right)^{-2}\right) + 20 \left(t^2 + 4\right)^{-1}$	M1	attempt to differentiate their $\frac{dx}{dt}$
	Alternative 3 for the first 3 marks		
	If $(v =) (20t - 4t^2 - 16)(t^2 + 4)^{-1}$	M1	attempt to differentiate their $\frac{dx}{dx}$
	$(a =) (20t - 4t^2 - 16) (-2t(t^2 + 4)^{-2}) + (20 - 8t)(t^2 + 4)^{-1}$	A1	for $2t(20t-4t^2-15)$
	Numerator = $-2t(20t - 4t^2 - 16) + (20 - 8t)(t^2 + 4)$	A1	for $(20-8t)(t^2+4)$
7 (i)	$\overrightarrow{DA} = 3\mathbf{a} - \mathbf{b}$	B1	mark final answer, allow unsimplified
(ii)	$\overrightarrow{DB} = 7\mathbf{a} - \mathbf{b}$	B1	mark final answer, allow unsimplified
(iii)	$\overrightarrow{AX} = \lambda \left(4\mathbf{a} + \mathbf{b} \right)$	B1	mark final answer, allow unsimplified
(iv)	$\overrightarrow{DX} = 3\mathbf{a} - \mathbf{b} + \lambda \left(4\mathbf{a} + \mathbf{b} \right)$	M1	their (i) + their (iii) or equivalent
		A1	valid method or 3a – b + their (iii) Allow unsimplified

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(v)	$3\mathbf{a} - \mathbf{b} + \lambda (4\mathbf{a} + \mathbf{b}) = \mu (7\mathbf{a} - \mathbf{b})$ Equate like vectors: $3 + 4\lambda = 7\mu$ $-1 + \lambda = -\mu$ leads to $\lambda = \frac{4}{11}$, $\mu = \frac{7}{11}$	M1 DM1 A1,A1	equating their (iv) and $\mu \times$ their (ii) for an attempt to equate like vectors and attempt to solve 2 linear equations for λ and μ
8 (i)	$5e^{2x} - \frac{1}{2}e^{-2k} (+c)$	B1, B1	B1 for each term, allow unsimplified
(ii)	$\left(5e^{2k} - \frac{1}{2}e^{-2k}\right) - \left(5e^{-2k} - \frac{1}{2}e^{2k}\right)$	M1	use of limits provided integration has taken place. Signs must be correct if brackets are not included. allow any correct form
(iii)	$ \left(5e^{2k} - \frac{1}{2}e^{-2k}\right) \left(5e^{-2k} - \frac{1}{2}e^{2k}\right) = -60 $ or $ \frac{11}{2}e^{2k} - \frac{11}{2}e^{-2k} = -60 $	B1	correct expression from (ii) either simplified or unsimplified equated to – 60, must be first line seen.
	or equivalent leading to $11e^{2k} - 11e^{-2k} + 120 = 0$	DB1	must be convinced as AG
(iv)	$11y^{2} + 120y - 11 = 0$ $(11y - 1)(y + 11) = 0$ leading to $k = \frac{1}{2} \ln \frac{1}{11}, \ln \frac{1}{\sqrt{11}}, -\ln \sqrt{11}, -\frac{1}{2} \ln 11$	M1 DM1 A1	attempt to obtain a quadratic equation in y or e^{2k} and solve to get y or e^{2k} (only need positive solution) attempt to deal with e to get $k = 1$. any of given answers only.

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	I		
9	$\frac{\mathrm{d}y}{\mathrm{d}x} = 4 - 6\sin 2x$	M1,A1	M1 for attempt to differentiate A1 for all correct
	When $x = \frac{\pi}{4}$, $y = \pi$	B1	for y
	$\frac{dy}{dx} = -2$ so gradient of normal $= \frac{1}{2}$	DM1	for substitution of $x = \frac{\pi}{4}$ into <i>their</i>
			$\frac{dy}{dx}$ and use of ' $m_1m_2 = -1$ ', dependent on first M1
	Normal equation $y - \pi = \frac{1}{2} \left(x - \frac{\pi}{4} \right)$	DM1	correct attempt to obtain the equation of the normal, dependent on previous DM mark
	When $x = 0$, $y = \frac{7\pi}{8}$	A1	must be terms of π
	When $y = 0, x = -\frac{7\pi}{4}$	A1	must be terms of π
	$Area = \frac{1}{2} \times \frac{7\pi}{4} \times \frac{7\pi}{8} = \frac{49\pi^2}{64}$	B1ft	Follow through on <i>their x</i> and <i>y</i> intercepts; must be exact values
10 (a)	$\cos^2 3x = \frac{1}{2}$, $\cos 3x = (\pm)\frac{1}{\sqrt{2}}$		
10 (1)	$3x = 45^{\circ}, 135^{\circ}, 225^{\circ}, 315^{\circ}$	M1	complete correct method, dealing with sec and 3, correctly
	$x = 15^{\circ}, 45^{\circ}, 75^{\circ}, 105^{\circ}$	A1,A1	A1 for each correct pair
(b)	$3(\cot^{2} y + 1) + 5 \cot y - 5 = 0$ Leading to $3\cot^{2} y + 5 \cot y - 2 = 0 \text{ or}$	M1	use of a correct identity to get an equation in terms of one trig ratio only
	$2\tan^2 y - 5\tan y - 3 = 0$ $(3\cot y - 1)(\cot y + 2) = 0 \text{ or}$	M1	for $\cot y = \frac{1}{\tan y}$ to obtain either a
	$(\tan y - 3)(2\tan y + 1) = 0$		quadratic equation in tan y or solutions in terms of tan y; allow where appropriate
	$\tan y = 3, \tan y = \frac{1}{2}$	M1	for solution of a quadratic equation in terms of either tan y or cot y
	$y = 71.6^{\circ}, 251.6^{\circ}$ 153.4°, 333.4°	A1,A1	A1 for each correct 'pair'
(c)	$\sin\left(z + \frac{\pi}{3}\right) = \frac{1}{2}$	M1	completely correct method of solution
	$z + \frac{\pi}{3} = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}$	A1	one correct solution in range
	$z = \frac{\pi}{2}, \frac{11\pi}{6}$	M1	correct attempt to obtain a second solution within the range
	(allow 1.57, 5.76)	A1	second correct solution (and no other)