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### **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**International General Certificate of Secondary Education** 

## MARK SCHEME for the October/November 2012 series

# 0606 ADDITIONAL MATHEMATICS

**0606/22** Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2012 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol 
   <sup>↑</sup> implies that the A or B mark indicated is allowed for work correctly following
   on from previously incorrect results. Otherwise, A or B marks are given for correct work
   only. A and B marks are not given for fortuitously "correct" answers or results obtained from
   incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2, 1, 0 means that the candidate can earn anything from 0 to 2.

Page 3	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

The following abbreviations may be used in a mark scheme or used on the scripts:

AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)

### **Penalties**

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through \" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy.
- OW –1,2 This is deducted from A or B marks when essential working is omitted.
- PA –1 This is deducted from A or B marks in the case of premature approximation.
- S –1 Occasionally used for persistent slackness usually discussed at a meeting.
- EX –1 Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

1 $7x + 5 = 3x - 13$ x = -4.5 o.e. 7x + 5 = 3x + 13 x = 0.8 o.e. OR Square and Equate $10x^2 + 37x - 36(=0)$ o.e. (5x - 4)(2x + 9)[=0] x = 0.8 and $x = -4.5ORPlot y =  7x + 5 Plot y =  3x - 13 x = 0.8x = -4.5$	M1 Equate and attempt to solve A1 M1 Equate A1 Mark final answers [4] M1 Both expressions must have 3 terms A1 Three terms M1 Factorise or formula of three term A1 quadratic.  M1 Shape and intercepts must be correct M1 Shape and intercepts must be correct A1 A1
2 $\left(\frac{dA}{dr}\right) = 4\pi r + 10\pi$ Use $\frac{dA}{dt} = \frac{dA}{dr} \times \frac{dr}{dt}$ with $r = 6$ 6.8	B1,B1 M1 Their $\frac{dA}{dr}$ A1 Rounds to 6.8
3 Rearrange to $ax^2 + bx + c = 0$ (2x-1)(2x-7)[< 0] 0.5 and 3.5 0.5 < x < 3.5	$\begin{array}{c c} M1 \\ M1 \\ A1 \\ A1 \\ & \text{not} \leqslant \text{ mark final statement.} \end{array}$
4 (i) $8 (2^3)$ or $56$ $-448(x^5)$ (ii) $1120(x^4)$ $2 \times \text{their } 1120 \text{ and their } -448 \text{ used}$ $1792(x^5)$	B1 B1 Mark final answer  [2] B1 M1 A1 [3]
<ul> <li>5 (i) Evidence of 6, 5, 4, and 3 only 360</li> <li>(ii) Evidence of 2 × 3 for outside digits Evidence of 4 × 3 for inside digits 72</li> </ul>	M1 Numbers listed but not added.  [2] B1 B1 B1 B1 [3]
6 (i) Express as powers of 2 Correctly reaches $3x + 2y = 6$ (ii) Express as powers of 5 $y = 3x - 4$ o.e. Attempt to solve simultaneous equations $x = \frac{14}{9}$ and $y = \frac{2}{3}$	M1 A1 AG [2] M1 Both correct $5^2$ and $5^{3x-6}$ o.e.  A1 Three terms M1 Equations must be linear A1 [4] Accept decimals that round to correct 3sf

Page 5	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

7	(i)	$\sec^2 4x$	M1	One term only
	(**)	× 4	A1 [2]	
	(ii)	$x + \tan 4x$	B1 M1	No additional terms
	<b></b>	÷ 4	A1 [3]	isw
	(iii)	Correct use of limits	M1	Expression must have 2 integrated terms in <i>x</i> from (ii).
		$k = \frac{1}{8}$	A1 [2]	Rounds to 0.125. Accept $\frac{\pi}{8}$ or $0.125\pi$
8	(i)	$\left(b=\right)\frac{7-4}{8-2}=\left[\frac{1}{2}\right]$	B1 M1	Finding gradient Finding y intercept
		$(\lg a)=3$	M1	$\lg y = c + m \lg x \text{ is sufficient}$
		lgy = lga + blgx  or  lgy - 4 = b(lgx - 2) or $lgy = 3 + 0.5lgx$		
		$a = 1000 \text{ or } 10^3$	A1	
		$y = 1000x^{0.5} \text{ or } 1000\sqrt{x}$	A1 [5]	
	(ii)	m = 1	B1	
	(iii)	<i>c</i> = 6	[1] B1	
			[1]	
9	(i)	80	B1	Correct triangle
		420 OR		
		420		
		$\sin \alpha  \sin 40$	M1	Use of sine or cosine rule in any triangle
		$\frac{\sin 40}{80} = \frac{\sin 40}{420}$		with some of $80,420$ , their $v$ and an angle.
		$\alpha = 7.03 \text{ or } 7$	A1 A1√	
		Bearing 223 $(230 - \alpha)$	[4]	
	(ii)	$\frac{v}{\sin their 133} = \frac{420}{\sin 40}$	M1	Use of sine or cosine rule in any triangle with 80 or 420 or both.
		v = 478	A1	
		Use time $\frac{1000}{v}$	M1	v calculated from a triangle
		2.09 hours or 2 hours 5minutes	A1 [4]	Units required

Page 6	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

10 (0)	T	3.61	Y 6 11 1
10 (i)	Integrate to find $v$ $v = 4t - t^2(+c)$	M1 A1	Increase of powers seen at least once
	Use $t = 0$ , $v = 12$ to find $c = 12$	B1	
	$v = 4t - t^2 + 12$	M1	Solve three term quadratic
	t = 6	A1	Do not penalize $t = -2$ .
	, ,	[5]	20 1100 penuming (
(ii)	Integrate to find <i>s</i>	M1	Increase of powers on at least 2 terms
	$2^2 t^3$	A1√	3 terms
	$s = 2t^2 - \frac{t^3}{3} + 12t$	A1	cao
	s = 72	[3]	Cao
		[6]	
11 (a)	$\tan x = -2.25$	B1	
	114	B1	Rounds to 114.0 isw
	294	B1√	Their 114 + 180 from tan function isw
-		[3]	
(b)	Uses $\csc y = \frac{1}{\sin y}$	B1	Seen anywhere
	Forms quadratic in $\sin y$ : $12\sin^2 y + \sin y - 1$	M1	Must be 3 terms
	[= 0]	3.54	
	$(4\sin y - 1)(2\sin y + 1)[= 0]$	M1	Factorise or formula of 3 term quadratic.
	14.5 and 199.5	A1	Any 2 values isw
	165.5 and 340.5	A1	The other 2 values isw
(c)	(-) 2	[5]	
	$\cos\left(\frac{z}{3}\right) = \frac{3}{5}$	B1	
	(3) 5		
	$\frac{z}{3} = 0.927$	M1	Solves their equation in radians
	9	A 1	isw
	z = 2.78 to 2.79 inc $z = 16.1$	A1 A1	Rounds to isw
	2 – 10.1	[4]	Rounds to isw
		[۳]	
12 EITH	IER		
	1	M1	Integrate: $e^{-\frac{x}{4}}$ seen
(i)	$yAe^{-\frac{-x}{4}x}(+c)$	A1	integrate : e seen
	A = -4	DM1	
	Substitute (0, 10)	21/11	
	$\frac{1}{x}$		
	$y = 14 - 4e^{-\frac{1}{4}x}$	A1	
	14 - 4e	A1	
		[5]	
(ii)	Tangent at A is $y - 10 = x$	B1	
	Gradient tangent at <i>B</i> is e	B1	
	-		
	Tangent at B is $y+4e-14=ex+4e$	B1√	With their gradient and answer to (i)
	Solve equations of tangents	M1	Two linear equations
	$x = \frac{4}{}$ o.e.		
	$x = \frac{1-e}{1-e}$ o.e.	A1	
		[5]	

Page 7	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2012	0606	22

12 OR (i)	$\frac{\mathrm{d}y}{\mathrm{d}x} = -\frac{1}{3}e^{-\frac{1}{3}x}$	M1	$Ae^{-\frac{x}{3}}$ only one term
	at $(0, 9) \frac{dy}{dx} = -\frac{1}{3}$	A1	
	Grad normal = 3	M1	Use of $m_1$ $m_2 = -1$
	Point $Q$ is $(-3, 0)$	A1	Condone $x = -3$
		[4]	
(ii)	Area rectangle 24 + 3e (32.1)	M1	Their $3 \times \text{their} (8 + e)$
	$\int_{-3}^{0} 8 + e^{-\frac{x}{3}} dx$	M1	Integrate: $8x$ and $e^{-\frac{x}{3}}$ seen
	$= \left[ 8x - 3e^{-\frac{x}{3}} \right]_{-3}^{0}$	A1	
	21+3e (29.1)	M1	Correct use of limits their –3 and 0
	Shaded area =3	A1	
		A1	
		[6]	