

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

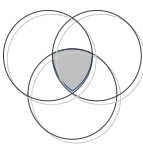
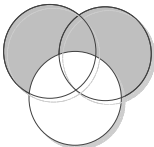
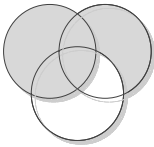
Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2014 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

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1	$\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta(1 + \sin \theta) + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		M1	M1 for attempt to obtain a single fraction
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’
	<p>Alternative solution:</p> $\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{(1 + \sin \theta)(1 - \sin \theta)}$ $= \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{\cos^2 \theta}$ $= \frac{\sin \theta}{\cos \theta} + \frac{(1 - \sin \theta)}{\cos \theta}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		M1	M1 for multiplication by $(1 - \sin \theta)$
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’
	<p>Alternative solution:</p> $\text{LHS} = \frac{\tan \theta(1 + \sin \theta) + \cos \theta}{1 + \sin \theta}$ $= \frac{\frac{\sin \theta}{\cos \theta} + \frac{\sin^2}{\cos \theta} + \cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta + \sin^2 \theta + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	M1	M1 for attempt to obtain a single fraction
		B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’

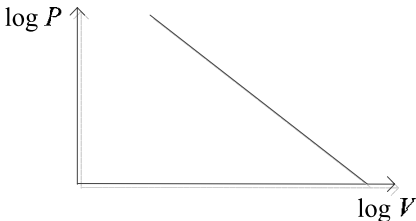
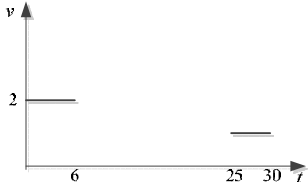
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2	(i)	$ a = \sqrt{4^2 + 3^2} = 5$ $ b + c = \sqrt{(-3)^2 + 4^2} = 5$	M1	M1 for finding the modulus of either a or b + c
	(ii)	$\lambda \begin{pmatrix} 4 \\ 3 \end{pmatrix} + \mu \begin{pmatrix} 2 \\ 2 \end{pmatrix} = 7 \begin{pmatrix} -5 \\ 2 \end{pmatrix}$ $4\lambda + 2\mu = -35$ and $3\lambda + 2\mu = 14$ leading to $\lambda = -49$, $\mu = 80.5$	A1 M1 DM1 A1	A1 for completion M1 for equating like vectors and obtaining 2 linear equations DM1 for solution of simultaneous equations A1 for both
3	(a)	(i)  (ii)  (iii) 	B1 B1 B1	B1 for each
	(b) (i)	2	B1	
	(ii)	0	B1	
4		$k(4x - 3) = 4x^2 + 8x - 8$ $4x^2 + x(8 - 4k) + 3k - 8 = 0$ $b^2 - 4ac = (8 - 4k)^2 - 16(3k - 8)$ $= 16k^2 - 112k + 192$ $b^2 - 4ac < 0$, $k^2 - 7k + 12 < 0$ critical values $k = 3, 4$ $\therefore 3 < k < 4$	M1 DM1 DM1 A1 A1	M1 for equating the line and the curve and attempt to obtain a quadratic equation in k DM1 for use of $b^2 - 4ac$ with k DM1 for solution of a 3 term quadratic equation, dependent on both previous M marks A1 for both critical values A1 for the range
	(i)	$\frac{dy}{dx} = 2xe^{x^2}$	B1B1	B1 for e^{x^2} , B1 for $2xe^{x^2}$
	(ii)	$\frac{1}{2}e^{x^2}$	M1A1	M1 for ke^{x^2} A1 for $\frac{1}{2}e^{x^2}$
	(iii)	$\left(\frac{1}{2}e^4\right) - \left(\frac{1}{2}\right) = 26.8$	DM1 A1	DM1 for correct use of limits A1 for 26.8, allow exact value

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6	(i)	$\mathbf{AB} = \begin{pmatrix} 10 & 19 \\ 32 & 37 \\ 14 & 14 \end{pmatrix}$	M1 A1	M1 for at least 3 correct elements of a 3×2 matrix A1 for all correct
	(ii)	$\mathbf{B}^{-1} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix}$	B1 B1	B1 for $\frac{1}{7}$, B1 for $\begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix}$
	(iii)	$2 \begin{pmatrix} 2 & 1 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -3 \\ -22 \end{pmatrix}$	M1	M1 for obtaining in matrix form
		$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} -1.5 \\ -11 \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 3.5 \\ -17.5 \end{pmatrix}$ $x = 0.5, y = -2.5$	M1 A1	M1 for pre-multiplying by \mathbf{B}^{-1} A1 for both
7	(i)	$y = 2x^2 - \frac{1}{x+1} (+c)$ when $x = \frac{1}{2}, y = \frac{5}{6}$ so $\frac{5}{6} = \frac{1}{2} - \frac{2}{3} + c$ leading to $c = 1$ $\left(y = 2x^2 - \frac{1}{x+1} + 1 \right)$	B1 B1 M1 A1	B1 for each correct term M1 for attempt to find $+c$, must have at least 1 of the previous B marks Allow A1 for $c = 1$
	(ii)	When $x = 1, y = \frac{5}{2}$ $\frac{dy}{dx} = \frac{17}{4}$ so gradient of normal $= -\frac{4}{17}$ Equation of normal $y - \frac{5}{2} = -\frac{4}{17}(x - 1)$ $(8x + 34y - 93 = 0)$	M1 B1 DM1 A1	M1 for using $x = 1$ in their (i) to find y B1 for gradient of normal DM1 for attempt at normal equation A1 – allow unsimplified (fractions must not contain decimals)

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8	(i)	$\log p = n \log V + \log k$ <table><tr><td>$\ln V$</td><td>2.30</td><td>3.91</td><td>4.61</td><td>5.30</td></tr><tr><td>$\ln p$</td><td>4.55</td><td>2.14</td><td>1.10</td><td>0.10</td></tr></table> <table><tr><td>$\lg V$</td><td>1</td><td>1.70</td><td>2</td><td>2.30</td></tr><tr><td>$\lg p$</td><td>1.98</td><td>0.93</td><td>0.48</td><td>0.04</td></tr></table> 	$\ln V$	2.30	3.91	4.61	5.30	$\ln p$	4.55	2.14	1.10	0.10	$\lg V$	1	1.70	2	2.30	$\lg p$	1.98	0.93	0.48	0.04	B1	B1 for statement, but may be implied by later work.
	$\ln V$	2.30	3.91	4.61	5.30																			
	$\ln p$	4.55	2.14	1.10	0.10																			
	$\lg V$	1	1.70	2	2.30																			
$\lg p$	1.98	0.93	0.48	0.04																				
(ii)	Use of gradient = n $n = -1.5$ (allow -1.4 to -1.6)	M1 A2,1,0	M1 for plotting a suitable graph –1 for each error in points plotted																					
(iii)	Allow 13 to 16	DM1 A1	DM1 for equating numerical gradient to n																					
		DM1 A1	DM1 for use of <i>their</i> graph or substitution into <i>their</i> equation.																					
9	(a)	Distance travelled = area under graph $= \frac{1}{2}(60 + 20) \times 12 = 480$	M1 A1	M1 for realising that area represents distance travelled and attempt to find area																				
	(b)		B1 B1 B1	B1 for velocity of 2 ms ^{–1} for 0 ≤ t ≤ 6 B1 for velocity of zero for <i>their</i> ‘6’ to <i>their</i> ‘25’ B1 for velocity of 1 ms ^{–1} for 25 ≤ t ≤ 30																				
	(c) (i)	$v = 4 - \frac{16}{t + 1}$ When $v = 0$, $t = 3$	M1 DM1 A1	M1 for attempt at differentiation DM1 for equating velocity to zero and attempt to solve																				
	(ii)	$a = \frac{16}{(t + 1)^2}$ $0.25(t + 1)^2 = 16$ $t = 7$	M1 A1	M1 for attempt at differentiation and equating to 0.25 with attempt to solve																				

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10 (a)	1 digit even numbers	2	B1	
	2 digit even numbers	$4 \times 2 = 8$	B1	
	3 digit even numbers	$3 \times 3 \times 2 = 18$	B1	
	Total = 28		B1	
	(b) (i)			
	3M 5W = 35		B1	
	4M 4W = 175		B1	
	5M 3W = 210		B1	
	Total = 420		B1	B1 for addition to obtain final answer, must be evaluated.
	or ${}^{12}C_8 - 6M\ 2W - 7M\ 1W$			or: as above, final B1 for subtraction to get final answer
(ii)	Oldest man in, oldest woman out and vice-versa			
	${}^{10}C_7 \times 2 = 240$		B1, B1	B1 for ${}^{10}C_7$, B1 for realising there are 2 identical cases
	Alternative:			
	1 man out	1 woman in		
	6 men	4 women		
	6M 1W : ${}^6C_6 \times {}^4C_1 = 4$			
	5M 2W : ${}^6C_5 \times {}^4C_2 = 36$			
	4M 3W : ${}^6C_4 \times {}^4C_3 = 60$			
	3M 4W : ${}^6C_3 \times {}^4C_4 = 20$			
	Total = 120		B1	All separate cases correct for B1
	There are 2 identical cases to consider, so 240 ways in all.		B1	B1 for realising there are 2 identical cases, which have integer values

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11	(a)	$5\sin 2x + 3\cos 2x = 0$ $\tan 2x = -0.6$ $2x = 149^\circ, 329^\circ$ $x = 74.5^\circ, 164.5^\circ$ Alternatives: $\sin(2x + 31^\circ) = 0$ or $\cos(2x - 59^\circ) = 0$	M1 DM1 A1,A1 M1	In each case the last A mark is for a second correct solution and no extra solutions within the range M1 for use of tan DM1 for dealing with $2x$ correctly A1 for each M1 for either, then mark as above
	(b)	$2\cot^2 y + 3\operatorname{cosec} y = 0$ $2(\operatorname{cosec}^2 y - 1) + 3\operatorname{cosec} y = 0$ $2\operatorname{cosec}^2 y + 3\operatorname{cosec} y - 2 = 0$ $(2\operatorname{cosec} y - 1)(\operatorname{cosec} y + 2) = 0$ One valid solution $\operatorname{cosec} y = -2, \sin y = -\frac{1}{2}$ $y = 210^\circ, 330^\circ$ Alternative: $2\frac{\cos^2 y}{\sin^2 y} + \frac{3}{\sin y} = 0$ leads to $2\sin^2 y - 3\sin y - 2 = 0$ and $\sin y = -\frac{1}{2}$ only $y = 210^\circ, 330^\circ$	M1 M1 M1 A1,A1 M1 M1 A1A1	M1 for use of correct identity M1 for attempt to factorise a 3 term quadratic equation A1 for each M1 for use of $\cot y = \frac{\cos y}{\sin y}$ and $\operatorname{cosec} y = \frac{1}{\sin y}$ M1 for attempt to factorise a 3 term quadratic equation
	(c)	$3\cos(z + 1.2) = 2$ $\cos(z + 1.2) = \frac{2}{3}$ $(z + 1.2) = 0.8411, 5.442, 7.124$ $z = 4.24, 5.92$	M1 A1 A1A1	M1 for correct order of operations to end up with 0.8411 radians or better A1 for one of 5.441 or 7.124 (or better) A1 for each valid solution