

CAMBRIDGE INTERNATIONAL EXAMINATIONS
International General Certificate of Secondary Education

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/22

Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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1	<p>rationalise the denominator to get $\frac{(2+\sqrt{5})^2(\sqrt{5}+1)}{5-1}$ or better</p> <p>squaring to get $\frac{(4+4\sqrt{5}+5)(\sqrt{5}+1)}{\text{their } 4}$ or better</p> <p>$\frac{29}{4} + \frac{13}{4}\sqrt{5}$ oe isw</p>	<p>M1</p> <p>M1</p> <p>A1 + A1</p>	<p>or squaring to get $\frac{(4+4\sqrt{5}+5)}{\sqrt{5}-1}$ or better</p> <p>or rationalising the denominator to get $\frac{\text{their}(9+4\sqrt{5})(\sqrt{5}+1)}{5-1}$ or better</p> <p>correct simplification</p> <p>Allow $\frac{29+13\sqrt{5}}{4}$ etc.</p>
2	<p>Correctly eliminate y</p> <p>$2x^2 + (k-9)x + 2 = 0$ oe</p> <p>Use $b^2 - 4ac$ oe</p> <p>Reach $\text{their}(k-9 = \pm 4)$ or solves $\text{their}(k^2 - 18k + 65) = 0$</p> <p>$k = 5$ and 13 cao</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>$-kx + 2 = 2x^2 - 9x + 4$ oe</p> <p>allow even if x terms not collected; condone $\dots = y$ provided later work implies it should be 0</p> <p>must be applied to a 3 term quadratic expression containing k as a coefficient; condone < 0 etc.</p> <p>condone $9 - k = \pm 4$; condone an inequality at this stage</p> <p>mark final answer, do not isw; A0 if inequalities for final answers</p>

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3	(i)	$3(-1)^3 - 14(-1)^2 - 7(-1) + d = 0$ with completion to $d = 10$	B1	<p>at least $-3 - 14 + 7 + d = 0$, $d = 10$; N.B. $= 0$ must be seen or implied by $\dots = d$ or $\dots = -d$, may be seen in following step.</p> <p>or convincingly showing $3(-1)^3 - 14(-1)^2 - 7(-1) + 10 = 0$; at least $-3 - 14 + 7 + 10 = 0$</p> <p>or correct synthetic division at least as far as</p> $ \begin{array}{r rrrr} -1 & 3 & -14 & -7 & 10 \\ & & -3 & 17 & -10 \\ \hline & 3 & -17 & 10 & \end{array} $
	(ii)	$3x^2 - 17x + 10$ isw or $a = 3, b = -17, c = 10$ isw	B2, 1, 0	<p>–1 each error; must be seen or referenced in (ii) even if found in (i) or (iii)</p>
	(iii)	$(x+1)(x-5)(3x-2)$ $-1, 5, \frac{2}{3}$	M1 A1	<p>for factorising quadratic ft correct; condone omission of $(x+1)$ or for ft correct use of formula or ft correct completing the square</p> <p>If M0 then SC1 for all three roots stated without working or verified/found by trials</p>

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4	(i)	$12\left(x - \frac{1}{4}\right)^2 + \frac{17}{4}$ isw	B3, 2, 1, 0	<p>one mark for each of p, q, r correct in a correctly formatted expression; allow correct equivalent values;</p> <p>If B0 then SC2 for $12\left(x - \frac{1}{4}\right) + \frac{17}{4}$ or</p> <p>SC1 for correct 3 values seen in incorrect format e.g.</p> <p>$12\left(x - \frac{1}{4}x\right) + \frac{17}{4}$ or</p> <p>$12\left(x^2 - \frac{1}{4}\right) + \frac{17}{4}$</p> <p>or for a correct completed square form of the original expression in a different but correct format. e.g.</p> <p>$3\left(2x - \frac{1}{2}\right)^2 + \frac{17}{4}$</p>
	(ii)	<p><i>their</i> $\frac{4}{17}$ or <i>their</i> 0.235</p> <p><i>their</i> $x = \frac{1}{4}$ oe</p>	<p>B1ft</p> <p>B1ft</p>	<p>strict ft ; <i>their</i> $\frac{4}{17}$ must be a proper fraction or decimal rounded to 3sig figs or more or truncated to 4 figs or more</p> <p>strict ft ; x must be correctly attributed</p>
	(i)	$1 - 20x + 160x^2$	B2, 1, 0	<p>–1 each error</p> <p>if B0 then M1 for 3 correct terms seen; may be unsimplified e.g.</p> <p>1, $5(-4x)$, $\frac{5 \times 4}{2}(-4x)^2$</p>
5	(ii)	$a + (\text{their} - 20) = -23$ soi	M1	condone sign errors only; must be <i>their</i> –20 from (i)
		$a = -3$	A1	validly obtained
		$b + (\text{their} - 20)a + (\text{their} 160) = 222$ soi	M1	condone sign errors only ; must be <i>their</i> –20 and <i>their</i> 160 from (i) and <i>their</i> a if used
		$b = 2$	A1	validly obtained

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6	(a) (i)	1	B1	
	(ii)	$x = -1$ or -2	B1 + B1	as final answers
	(b)	$\frac{\log_3 5}{\log_3 a}$ seen or implied	B1*	may be implied by $2 \log_3 15 - \log_3 5$
		$2 \log_3 15 = \log_3 15^2$ seen or implied	B1	
		$\log_3 15^2 - \log_3 5 = \log_3 \left(\frac{15^2}{5} \right)$	B1dep*	not from wrong working
		$\log_3 45$ cao	B1	must be 45 not e.g. $\frac{225}{5}$; with no wrong working seen
7	(i)	$x^4(3e^{3x}) + 4x^3e^{3x}$ isw	B1 + B1	each term of the sum correct; must be a sum of two terms
	(ii)	$\frac{1}{2 + \cos x} \times (-\sin x)$ isw	B2	or B1 for $\frac{1}{2 + \cos x} \times (k \pm \sin x)$ and k a constant
	(iii)	$\frac{d}{dx}(\sin x) = \cos x$ soi	B1	
		$\frac{d}{dx}(1 + \sqrt{x}) = \frac{1}{2}x^{-\frac{1}{2}}$ soi	B1	
		$\frac{(1 + \sqrt{x}) \text{ their } \cos x - \left(\text{their } \frac{1}{2} x^{-\frac{1}{2}} \right) \sin x}{(1 + \sqrt{x})^2}$ isw	B1ft	for correct form of quotient rule ft their $\cos x$ and their $\frac{1}{2}x^{-\frac{1}{2}}$; allow correct use of product and chain rules to obtain $\sin x \left(- (1 + \sqrt{x})^2 \times \frac{1}{2} x^{\frac{1}{2}} \right) +$ $\cos x (1 + \sqrt{x})^{-1}$ oe

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8	Substitution of either $x - 5$ or $y + 5$ into equation of curve and brackets expanded	M1	condone one sign error in either equation of curve or expansion of brackets; condone omission of $= 0$, BUT $x - 5$ or $y + 5$ must be correct
	$2x^2 - 8x - 10 [= 0]$ or $2y^2 + 12y [= 0]$ obtained	A1	
	Solving their quadratic	M1	dep on a valid substitution attempt
	$(-1, -6)$ oe and $(5, 0)$ oe isw	A1*+A1*	or A1 for correct pair of x coordinates or correct pair of y coordinates
	$\sqrt{72}$ or $6\sqrt{2}$ cao isw	B1dep*	
9	(i)	B2	or B1 for $(2x + 1)^{\frac{1}{2}+1}$
	$[y =] \frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} (+c)$ oe		
	$10 = \frac{2}{6} (2(4)+1)^{\frac{3}{2}} + c$ oe	M1	for valid attempt to find c ; condone slips e.g. omission of power or sign error
	$y = \frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + c$ seen and $c = 1$ or	A1	must have $y = \dots$; condone $f(x) = \dots$
	$y = \frac{(2x+1)^{\frac{3}{2}}}{2 \times \frac{3}{2}} + 1$ isw		
	(ii)		
	$\int \left(\frac{1}{3} (2x+1)^{\frac{3}{2}} + 1 \right) dx = \frac{1}{15} (2x+1)^{\frac{5}{2}} + x (+const)$	B1 + B1	B1 for $(2x+1)^{\frac{3}{2}+1}$, B1 for $\frac{1}{15} (2x+1)^{\frac{5}{2}}$
	$\left[\frac{1}{15} (2x+1)^{\frac{5}{2}} + x \right]_0^{1.5} =$	B1ft	B1 ft <i>their</i> c from (i) provided $c \neq 0$
	$\left[\frac{1}{15} (2(1.5)+1)^{\frac{5}{2}} + (1.5) \right] - \left[\frac{1}{15} (2(0)+1)^{\frac{5}{2}} + 0 \right]$	M1	for a genuine attempt to find $F(1.5) - F(0)$ in an attempt to integrate <i>their</i> y ; if their $F(0)$ is 0 must see at least their $F(1.5) - 0$; condone $+c$ as long as their c is not numerical.
	$\frac{107}{30}$ oe isw	A1	if decimal 3.57 or more accurate e.g. 3.566

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10	(i)	Taking logs of both sides $\log y = \log A + x \log b$	M1	any base; must be an explicitly correct statement
			A1	correct form; any base; no recovery from incorrect method steps
	(ii)	b : awrt 3 to one sf isw or awrt 4 to one sf isw A : awrt 0.5 to one sf	B2	or M1 for $b = e^{\text{their gradient}}$ soi; their gradient must be correctly evaluated as rise/run
			B2	or B1 for $A = e^{-0.6}$ or SC1 for $A = e^{-0.3} = 0.7$ (giving an awrt 0.7)
	(iii)	Evidence of graph used at $\ln y = 5.4$ soi	M1	or $\frac{220}{\text{their}0.5} = (\text{their}4)^x$ or $5.39... = \text{their}(1.4)x + \text{their} -0.6$ or $\ln(220) = x \ln(\text{their}4) + \ln(\text{their}0.5)$
		awrt 4.4 to two sf	A1	

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11	(i)	$f(x) > 3$ or $[f(x) \in](3, \infty)$	B1	condone $y > 3$
	(ii)	$x + 1 = 2^y$ $f^{-1}(x) = \log_2(x + 1)$	M1 A1	or $y + 1 = 2^x$ mark final answer or $\log_2(y + 1) = x$ and $f^{-1}(x) = \log_2(x + 1)$ or for $f^{-1}(x) = \frac{\log(x + 1)}{\log 2}$ (any base for this form)
	(iii)	Domain $x > 3$ Range $f^{-1}(x) > 2$ $2^x(2^x - 1)$ oe isw $2^x(2^x - 1) = 0$ leading to $2^x = 0$, impossible oe $2^x = 1 \Rightarrow x = 0$ 0 is not in the domain (and so $gf(x) = 0$ has no solutions)	B1ft B1 B1 M1 A1	ft their range of f provided mathematically valid inequality or interval condone $f(x) > 2$ or $y > 2$ e.g. $(2^x - 1)^2 + (2x - 1)$ or $2^{2x} - 2 \times 2^x + 1 + 2^x - 1$ or $2^x = 0$ which is outside domain of gf or $2^x(2^x - 1) = 2^{2x} - 2^x = 0$ $[2^{2x} = 2^x] \Rightarrow x = 0$

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12	(i)	$\frac{dy}{dx} = 3x^2 - 18x + 24$ Solving their $3x^2 - 18x + 24 \geq 0$ by factorising or quadratic formula or completing the square Critical values 2 and 4 $x \leq 2, x \geq 4$	B1 M1 A1 A1	attempt at differentiation resulting in quadratic expression with two terms correct; allow = or \leq or $<$ or $>$ or ≥ 0 omitted here. A0 if spurious attempt to combine; mark final answer
	(ii)	Evaluating their $\frac{dy}{dx}$ at $x = 3$ Use of $m_1 m_2 = -1$ to get $m_{normal} = -\frac{1}{their(-3)}$ $y = 18$ soi $y - their18 = \left(their \frac{1}{3} \right) (x - 3)$ or $y = their \frac{1}{3} x + c$ and $c = their17$ isw $P(0, 17)$ cao	M1 M1 B1 A1ft B1	must be explicit statement of gradient of normal ; may be seen in equation ft <i>their m</i> provided a genuine attempt at m_{normal} ; no ft if $m = their m_{tangent}$