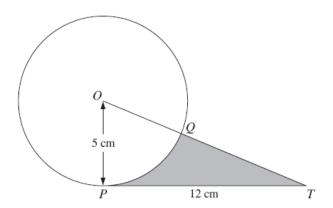
AS Final Exam: Revision 4 Circular Measure

P1 June 08

5



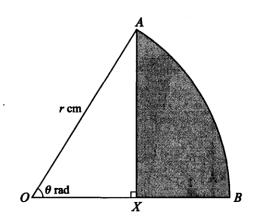
The diagram shows a circle with centre O and radius 5 cm. The point P lies on the circle, PT is a tangent to the circle and PT = 12 cm. The line OT cuts the circle at the point Q.

(i) Find the perimeter of the shaded region. [4]

(ii) Find the area of the shaded region. [3]

P1 Nov 08

7



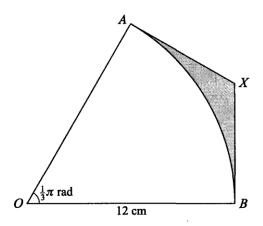
In the diagram, AB is an arc of a circle, centre O and radius r cm, and angle $AOB = \theta$ radians. The point X lies on OB and AX is perpendicular to OB.

(i) Show that the area, $A \text{ cm}^2$, of the shaded region AXB is given by

$$A = \frac{1}{2}r^2(\theta - \sin\theta\cos\theta).$$
 [3]

(ii) In the case where r = 12 and $\theta = \frac{1}{6}\pi$, find the perimeter of the shaded region AXB, leaving your answer in terms of $\sqrt{3}$ and π . [4]

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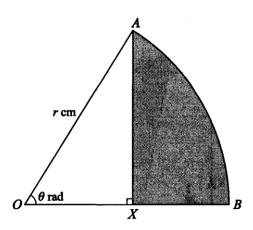


In the diagram, OAB is a sector of a circle with centre O and radius 12 cm. The lines AX and BX are tangents to the circle at A and B respectively. Angle $AOB = \frac{1}{3}\pi$ radians.

- (i) Find the exact length of AX, giving your answer in terms of $\sqrt{3}$. [2]
- (ii) Find the area of the shaded region, giving your answer in terms of π and $\sqrt{3}$. [3]

P1 Nov 07

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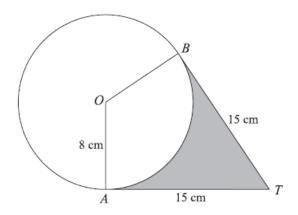
In the diagram, AB is an arc of a circle, centre O and radius r cm, and angle $AOB = \theta$ radians. The point X lies on OB and AX is perpendicular to OB.

(i) Show that the area, $A \text{ cm}^2$, of the shaded region AXB is given by

$$A = \frac{1}{2}r^2(\theta - \sin\theta\cos\theta).$$
 [3]

(ii) In the case where r = 12 and $\theta = \frac{1}{6}\pi$, find the perimeter of the shaded region AXB, leaving your answer in terms of $\sqrt{3}$ and π .

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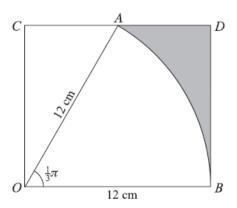


The diagram shows a circle with centre O and radius 8 cm. Points A and B lie on the circle. The tangents at A and B meet at the point T, and AT = BT = 15 cm.

- (i) Show that angle AOB is 2.16 radians, correct to 3 significant figures. [3]
- (ii) Find the perimeter of the shaded region. [2]
- (iii) Find the area of the shaded region. [3]

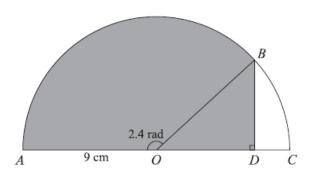
P1 Nov 06

3



In the diagram, AOB is a sector of a circle with centre O and radius 12 cm. The point A lies on the side CD of the rectangle OCDB. Angle $AOB = \frac{1}{3}\pi$ radians. Express the area of the shaded region in the form $a(\sqrt{3}) - b\pi$, stating the values of the integers a and b.

8

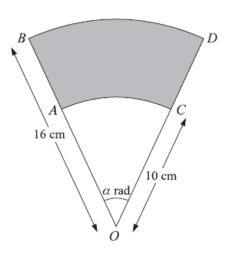


In the diagram, ABC is a semicircle, centre O and radius 9 cm. The line BD is perpendicular to the diameter AC and angle AOB = 2.4 radians.

- (i) Show that BD = 6.08 cm, correct to 3 significant figures. [2]
- (ii) Find the perimeter of the shaded region. [3]
- (iii) Find the area of the shaded region. [3]

P1 Nov 05

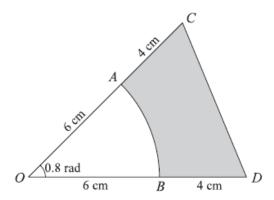
2



In the diagram, OAB and OCD are radii of a circle, centre O and radius 16 cm. Angle $AOC = \alpha$ radians. AC and BD are arcs of circles, centre O and radii 10 cm and 16 cm respectively.

- (i) In the case where $\alpha = 0.8$, find the area of the shaded region. [2]
- (ii) Find the value of α for which the perimeter of the shaded region is 28.9 cm. [3]

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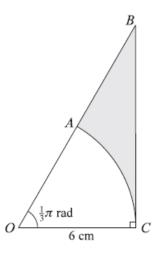


In the diagram, OCD is an isosceles triangle with $OC = OD = 10 \,\mathrm{cm}$ and angle $COD = 0.8 \,\mathrm{radians}$. The points A and B, on OC and OD respectively, are joined by an arc of a circle with centre O and radius $6 \,\mathrm{cm}$. Find

- (i) the area of the shaded region, [3]
- (ii) the perimeter of the shaded region. [4]

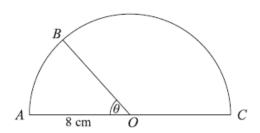
P1 Nov 04

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In the diagram, AC is an arc of a circle, centre O and radius 6 cm. The line BC is perpendicular to OC and OAB is a straight line. Angle $AOC = \frac{1}{3}\pi$ radians. Find the area of the shaded region, giving your answer in terms of π and $\sqrt{3}$.

9

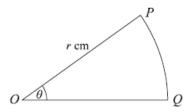


The diagram shows a semicircle ABC with centre O and radius 8 cm. Angle $AOB = \theta$ radians.

- (i) In the case where $\theta = 1$, calculate the area of the sector *BOC*. [3]
- (ii) Find the value of θ for which the perimeter of sector AOB is one half of the perimeter of sector BOC.
- (iii) In the case where $\theta = \frac{1}{3}\pi$, show that the exact length of the perimeter of triangle ABC is $(24 + 8\sqrt{3})$ cm.

P1 Nov 03

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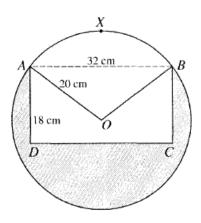


The diagram shows the sector OPQ of a circle with centre O and radius r cm. The angle POQ is θ radians and the perimeter of the sector is 20 cm.

(i) Show that
$$\theta = \frac{20}{r} - 2$$
. [2]

- (ii) Hence express the area of the sector in terms of r. [2]
- (iii) In the case where r = 8, find the length of the chord PQ. [3]

7



The diagram shows the circular cross-section of a uniform cylindrical log with centre O and radius 20 cm. The points A, X and B lie on the circumference of the cross-section and AB = 32 cm.

(i) Show that angle AOB = 1.855 radians, correct to 3 decimal places. [2]

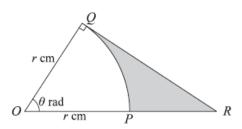
(ii) Find the area of the sector AXBO. [2]

The section AXBCD, where ABCD is a rectangle with $AD = 18 \,\mathrm{cm}$, is removed.

(iii) Find the area of the new cross-section (shown shaded in the diagram). [3]

P1 Nov 02

3



In the diagram, OPQ is a sector of a circle, centre O and radius r cm. Angle $QOP = \theta$ radians. The tangent to the circle at Q meets OP extended at R.

(i) Show that the area, $A \text{ cm}^2$, of the shaded region is given by $A = \frac{1}{2}r^2(\tan \theta - \theta)$. [2]

(ii) In the case where $\theta = 0.8$ and r = 15, evaluate the length of the perimeter of the shaded region.

[4]