- (h) $x < -\frac{1}{3}\sqrt{21}$ or $x > \frac{1}{3}\sqrt{21}$
- (i) True for no x
- (j) True for all x
- (k) $x < -\frac{3}{4}$ or $x > \frac{1}{3}$
- $\frac{1}{6}(7 \sqrt{37}) \le x \le \frac{1}{6}(7 + \sqrt{37})$

Miscellaneous exercise 5 (page 72)

- 1 $-6 \le x \le 7$
- 2 -4 < x < 2
- 3 -4 < x < 3
- 4 -1 < x < 0 or x > 1
- 5 $-3 \le x \le 0 \text{ or } x \ge 2$
- 6 (a) k < 0 or k > 8
 - (b) $-1\frac{1}{2} < k < 1\frac{1}{2}$ provided $k \ne 0$ (if k = 0 the equation is linear, and has just one root)
 - (c) k < -2 or k > 2
- 7 (a) $0 \le k < 5$
- (b) k = 0
- (c) $-\frac{8}{25} < k < 0$
- **8** $k \le 0 \text{ or } k \ge \frac{4}{9}$
- $x < -2 \text{ or } x > \frac{2}{3}$
- 10 $-\frac{1}{2} < x < 0 \text{ or } x > 2$
- **11** (a) x < 2 or $x > 2\frac{1}{2}$ (b) $1 - \sqrt{6} < x < 1 + \sqrt{6}$

Revision exercise 1

(page 73)

- 1 (-4,-16)
- 3 $(x+5)^2+13$;
 - (a) 13, -5(b) $x \le -8$ or $x \ge -2$
- 5 (a) $\frac{1}{2} \le x \le 2$ (b) $-\frac{1}{2} < x < \frac{7}{2}$ (c) x > 6.3
- **6** 6 7 $\pm \sqrt{65}$
- 8 (0,0),(-1,-1),(1,1)
- 9 $\{(12(x+y)+15xy); 5z^2+8z-4=0, 0.4\}$
- 10 x+y=5; 7
- 11 (a) $x > \frac{4}{3}$ (b) $x > \frac{3}{2}$ (c) $x \le 0$ or $x \ge 5$
- 0.5
- 13 x = 1, y = 1 or x = 4, y = -1
- 14
- (2,1); the line is a tangent to the curve. 15
- 16 2x + 3y = 7, 3x 2y = 4; (4,4)
- (a) (3,-1) (b) 5 (c) $2\sqrt{6}-1$
- **18** (a) x < -1 or x > 2(b) -1 < x < 2 or x > 3
- 19 $2\sqrt{19}$ cm
- **20** x = 7, 3y + x = 10; (7,1); all $5\sqrt{2}$; 30; $2\sqrt{5}$

- **21** 5, y = 1; $2\sqrt{2}$, y = x + 1
- **22** 3, -18, 35; $3(x-3)^2 + 8$; 8
- **23** -2, 0
- **24** 1.52, -8.52
- **25** (a) $\left(\frac{c}{a}\right)^{\frac{3}{2}}$ (b) $\frac{c^2}{a^2}\sqrt{\frac{c}{a}}$

6 Differentiation

Exercise 6A (page 77)

- 1 y = 3x 2
- **2** (a) 2.001
- (b) 1.9999
- (c) 4.002
- (d) 3.999
- (e) 6.000 001
- (f) 5.999 99

Exercise 6B (page 79)

- 1 (a) 2 (b) 8
 - (f) -7
- (c) 0 (g) 2p
- (h) 4p (c) 0
- **2** (a) 2 (b) 8

(e) -0.4

- (d) -4(h) 4p

(d) -4

- (f) (e) -0.4
- (g) 2p
- 3 4 and -4
- **4** (a) y = 4x 4
- (b) y = -2x + 1
- (c) y = 2x 3 and y = -2x 3
- (d) y = -2
- 5 (a) 2y = -x + 3(b) 4y = x + 22
 - (c) x = 0
 - (d) $2y\sqrt{c} = -x + \sqrt{c}(4c+1)$
- 6 12y = -4x + 33
- 7 4y = 4x + 3
- 8 $\left(-2\frac{1}{4},5\frac{1}{16}\right)$

Exercise 6C (page 82)

- 1 (a) 2x
- (b) 2x-1
- (c) 8x
- (d) 6x 2
- $(e)^{-3}$
- (f) 1-4x
- (h) $\sqrt{2} 2\sqrt{3}x$ 4-6x(g)
- **2** (a) 3
- (b) -6x
- (c) 0
- (d) 2 + 6x
- (e) -2x
- (f) 6-6x
- (g) 2-4x(h) 4x+13 (a) 6
 - (b) 3
- - (d) 8 (c) -3(g) 4 (h) -17
 - (e) -8(f) -6
 - (b)
- (c) $-\frac{3}{2}$
- **4** (a) (f) $\frac{1}{2}$ (d) -1(e)
- **5** (a) y = -2x - 1
- (b) y = -x
 - (c) y = 2x 1
- (d) y = 6x + 10
- (e) y = 1
- (f) y = 0
- **6** (a) 2y = x 3
- (b) 4y = -x + 1(d) x = 0
- (c) 8y = -x 58(e) 2y = x + 9
- (f) $x = \frac{1}{2}$
- 7 4y = 4x 1

- **8** y = 0
- 9 y = -2x
- 10 12y = 12x 17
- 11 x = 1
- 12 7y = -x + 64
- **14** (a) 0.499 875... (b) 0.500 012...
 - (c) 0.249 968 ... (d) 0.250 015 ...
 - (e) 0.999 999 ... (f) 1.000 001 ...

Exercise 6D (page 86)

- 1 (a) $3x^2 + 4x$
- (b) $-6x^2 + 6x$
- (c) $3x^2 12x + 11$
- (d) $6x^2 6x + 1$
- (e) $4x 24x^3$
- (f) $-3x^2$
- **2** (a) -10 (b) 6

-4 ^{4}p

4p

ĴХ

-17

- (c) 58 (f) 12

(e) 8

- (d) -13 (a) -2, 2

- (f) No values

- (e) $-1, -\frac{1}{3}$ (f) No value (a) $\frac{1}{\sqrt{x}}$ (b) $\frac{1}{\sqrt{x}} + 1$ (c) $1 \frac{1}{4\sqrt{x}}$ (d) $1 \frac{1}{\sqrt{x}}$ (e) $1 + \frac{1}{x^2}$ (f) 2^x (g) $1 \frac{2}{x^2}$ (h) 1
- (f) $2x+1-\frac{1}{x^2}$

- 5 y = 4x + 2
- 6 y = x + 2
- 4y = x + 4
- 8 4y = -x + 4
- 9 x = 1
- 11 y = -2x 6
- 12 $y = -a^2x$, $y = 2a^2x + 2a^3$, $y = 2a^2x 2a^3$
- **13** $(\frac{1}{2},-2)$
- **14** (a) $-\frac{1}{4x^2}$ (b) $-\frac{6}{x^3}$

- (d) $\frac{3}{4\sqrt[4]{x}}$ (e) $\frac{2}{\sqrt[3]{x^2}}$ (f) $-\frac{2}{\sqrt{x^3}}$
- (g) $-\frac{3}{x^2} \frac{1}{x^4}$ (h) $10\sqrt{x^3}$
- (j) $-\frac{1}{6\sqrt[3]{x^4}}$ (k) $\frac{4-x}{x^3}$ (l) $\frac{3x-1}{4\sqrt[4]{x^5}}$
- 15 3y x = 4, y + 3x = 28
- **16** $(0,12), (\frac{3}{4},0)$

Exercise 6E (page 93)

- 1 $f'(p) = 3p^2$
- 2 $f'(p) = 8p^7$
- 3 $f'(p) = -\frac{2}{p^3}$

Miscellaneous exercise 6 (page 94)

- 1 y = 13x 16
- **2** (a) -9
- (b) $-\frac{19}{3}$, 3
- 3 80y = 32x 51
- 4 $\left(-3, -\frac{1}{3}\right)$
- 6 $\left(-\frac{1}{3}, -4\frac{17}{27}\right)$, (2,13)
- 7 x+19y-153=0
- **8** 13
- 9 (2,12)
- **10** 2
- 11 Both curves have gradient 12.
- **12** –183
- 13 mn = -1

7 Applications of differentiation

Exercise 7A (page 96)

3 (a)



Exercise 7B (page 103)

- 1 (a) $2x-5, x \ge \frac{5}{2}$
- (b) $2x+6, x \ge -3$
- (c) $-3-2x, x \le -\frac{3}{2}$
- (d) $6x 5, x \ge \frac{5}{6}$
- 2 (a) $2x+4, x \le -2$
- (e) $10x + 3, x \ge -\frac{3}{10}$ (f) $-4 6x, x \le -\frac{2}{3}$
- (b) $2x-3, x \le \frac{3}{2}$ (d) $4x-8, x \le 2$
- (c) $-3+2x, x \le \frac{3}{2}$ (e) $7-4x, x \ge \frac{7}{4}$
- (f) $-5-14x, x \ge -\frac{5}{14}$
- 3 (a) $3x^2 12, x \le -2 \text{ and } x \ge 2$
 - (b) $6x^2 18, x \le -\sqrt{3} \text{ and } x \ge \sqrt{3}$
 - (c) $6x^2 18x 24$, $x \le -1$ and $x \ge 4$
 - (d) $3x^2 6x + 3$, all x
 - (e) $4x^3 4x, -1 \le x \le 0$ and $x \ge 1$
 - (f) $4x^3 + 12x^2, x \ge -3$
 - (g) $3-3x^2, -1 \le x \le 1$
 - (h) $10x^4 20x^3$, $x \le 0$ and $x \ge 2$
 - (i) $3(1+x^2)$, all x

- 4 (a) $3x^2 27, -3 \le x \le 3$
 - (b) $4x^3 + 8x, x \le 0$
 - (c) $3x^2 6x + 3$, none
 - (d) $12-6x^2$, $x \le -\sqrt{2}$ and $x \ge \sqrt{2}$
 - (e) $6x^2 + 6x 36, -3 \le x \le 2$
 - (f) $12x^3 60x^2, x \le 5$
 - (g) $72x 8x^3, -3 \le x \le 0 \text{ and } x \ge 3$
 - (h) $5x^4 5, -1 \le x \le 1$
 - (i) $nx^{n-1} n$; $x \le 1$ if n is even, $-1 \le x \le 1$ if n is odd
- **5** (a) $\frac{1}{2}x^{1/2}(5x-3)$; $0 < x < \frac{3}{5}$; $x \ge \frac{3}{5}$
 - (b) $\frac{1}{4}x^{-1/4}(3-14x)$; $x \ge \frac{3}{14}$; $0 \le x \le \frac{3}{14}$
 - (c) $\frac{1}{3}x^{-1/3}(5x+4); -\frac{4}{5} \le x \le 0;$ $x \le -\frac{4}{5} \text{ and } x \ge 0$
 - (d) $\frac{13}{5}x^{-2/5}(x^2-3); -\sqrt{3} \le x \le \sqrt{3};$ $x \le -\sqrt{3} \text{ and } x \ge \sqrt{3}$
 - (e) $1 \frac{3}{x^2}$; $-\sqrt{3} \le x < 0$ and $0 < x \le \sqrt{3}$; $x \le -\sqrt{3}$ and $x \ge \sqrt{3}$
 - (f) $\frac{x-1}{2x\sqrt{x}}$; $0 < x \le 1$; $x \ge 1$
- **6** (a) (i) (4,-12) (ii) minimum (iv) $f(x) \ge -12$
 - (b) (i) (-2,-7) (ii) minimum (iv) $f(x) \ge -7$
 - (c) (i) $\left(-\frac{3}{5}, \frac{1}{5}\right)$ (ii) minimum (iv) $f(x) \ge \frac{1}{5}$
 - (d) (i) (-3,13) (ii) maximum (iv) $f(x) \le 13$
 - (e) (i) (-3,0) (ii) minimum (iv) $f(x) \ge 0$
 - (f) (i) $\left(-\frac{1}{2},2\right)$ (ii) maximum (iv) $f(x) \le 2$
- 7 (a) (-4,213), maximum; (3,-130), minimum
 - (b) (-3,88), maximum; (5,-168), minimum
 - (c) (0,0), minimum; (1,1), neither
 - (d) (-2,65), maximum; (0,1), neither; (2,-63), minimum
 - (e) $\left(-\frac{1}{3}, -\frac{11}{27}\right)$, minimum; $\left(\frac{1}{2}, \frac{3}{4}\right)$, maximum
 - (f) (-1,0), neither
 - (g) (-1,-2), maximum; (1,2), minimum
 - (h) (3,27), minimum
 - (i) none
 - (j) $\left(\frac{1}{4}, -\frac{1}{4}\right)$, minimum
 - (k) $\left(6, \frac{1}{12}\right)$, maximum
 - (1) (-2,17), minimum
 - (m) (1,3), maximum
 - (n) (-1,-5), minimum
 - (o) (0,0), minimum; $(\frac{4}{5}, \frac{256}{3125})$, maximum
- **8** (a) $f(x) \ge \frac{3}{4}$
 - (b) $f(x) \ge -16$
 - (c) $f(x) \le -2, f(x) \ge 2$

Exercise 7C (page 109)

- 1 (a) Gradient of road
 - (b) Rate of increase of crowd
 - (c) Rate of increase (or decrease if negative) of magnetic force with respect to distance
 - (d) Acceleration of particle
 - (e) Rate of increase of petrol consumption with respect to speed
- 2 (a) $\frac{dp}{dh}$, p in millibars, h in metres
 - (b) $\frac{d\theta}{dt}$, θ in degrees C, t in hours
 - (c) $\frac{dh}{dt}$, h in metres, t in hours
 - (d) $\frac{dW}{dt}$, W in kilograms, t in weeks
- 3 (a) 6t+7 (b) $1-\frac{1}{2\sqrt{x}}$
 - (c) $1 \frac{6}{y^3}$ (d) $2t \frac{1}{2t\sqrt{t}}$
 - (e) 2t+6 (f) $12s^5-6s$
 - (g) 5 (h) $-\frac{2}{r^3}-1$
- 4 (a) Velocity
 - (b) (i) Increasing (ii) Decreasing
 - (c) 9, occurs when velocity is zero and direction of motion changes
- $5 (a) \frac{\mathrm{d}x}{\mathrm{d}t} = c$
 - (b) $\frac{dA}{dt} = kA$; A stands for the amount deposited
 - (c) $\frac{dx}{dt} = f(\theta)$; x stands for diameter, θ for air temperature
- 6 80 km h^{-1}
- 7 20 m
- **8** 36
- 9 $4\sqrt{5}$
- 10 Greatest $V = 32\pi$ when r = 4, least V = 0 when r = 0 or h = 0
- 11 25
- **12** (b) 1800 m²
- 13 0 < x < 20, 7.36 cm
- **14** 20 cm
- **15** (b) 38 400 cm³ (to 3 s.f.)
- **16** 2420 cm³ (to 3 s.f.)

Miscellaneous exercise 7 (page 110)

- 1 Maximum at (-2,-4); minimum at (2,4); y increases with x for $x \le -2$ and $x \ge 2$
- $\frac{\mathrm{d}n}{\mathrm{d}t} = kn$ (b) $\frac{\mathrm{d}\theta}{\mathrm{d}t} = -k\theta$
 - $\frac{\mathrm{d}\theta}{\mathrm{d}\theta} = -k(\theta \beta)$
- $(20-4t) \text{ m s}^{-1}, -4 \text{ m s}^{-2}; \text{ for } 0 \le t \le 5$
- 5 (a) 20 m
- (b) $6 \,\mathrm{s}$ (c) $40 \,\mathrm{m \, s}^{-1}$
- 50 6

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- (b) $40\frac{1}{2}$ cm² 7 (a) $9\sqrt{2}$ cm
- (a) (-1,-7),(2,20)
 - (b) Graph crosses the x-axis three times.
 - (c) y = -5 has three intersections with graph.
 - (d) (i) -20 < k < 7 (ii) k < -20 and k > 7
- 9 (-2,4), (2,-28); $-28 \le k \le 4$
- **10** $\left(-\frac{2}{3}, \frac{4}{27}\right)$, (0,0); $0 < k < \frac{4}{27}$
- **11** (-1,5),(2,-22), (0,10);
 - (a) 5 < k < 10 (b) -22 < k < 5 and k > 10
- **12** $\left(\frac{1}{3}, \frac{4}{27}\right)$, (1,0); $k < -\frac{2}{3\sqrt{3}}$ and $k > \frac{2}{3\sqrt{3}}$
- **13** (a) $P = 2x + 2r + \frac{1}{2}\pi r$, $A = \frac{1}{4}\pi r^2 + rx$ (b) $x = \frac{1}{4}r(4-\pi)$
- **14** Maximum at $(2,\frac{1}{4})$
 - (a) $(2,5\frac{1}{4})$
 - (b) $(3,\frac{1}{2})$; that is, when x-1=2
- **16** (a) 1100 20x (b) £x(1100 20x)
 - (c) £(24 000 400x); £37.50
- 17 (a) The gradient at P' is the negative of the gradient at P. So f'(-p) = -f'(p). The derivative of an even function is odd.

8 Sequences

Exercise 8A (page 115)

- **1** (a) 7,14,21,28,35
- (b) 13,8,3,-2,-7
- (c) 4,12,36,108,324 (d) 6,3,1.5,0.75,0.375
- (e) 2, 7, 22, 67, 202
- (f) 1,4,19,364,132499
- **2** (a) $u_1 = 2, u_{r+1} = u_r + 2$
 - (b) $u_1 = 11, u_{r+1} = u_r 2$
 - (c) $u_1 = 2, u_{r+1} = u + 4$
 - (d) $u_1 = 2, u_{r+1} = 3u_r$
 - (e) $u_1 = \frac{1}{3}, u_{r+1} = \frac{1}{3}u_r$
 - (f) $u_1 = \frac{1}{2}a, u_{r+1} = \frac{1}{2}u_r$
 - (g) $u_1 = b 2c, u_{r+1} = u_r + c$
 - (h) $u_1 = 1, u_{r+1} = -u_r$

- (i) $u_1 = \frac{p}{q^3}, u_{r+1} = qu_r$
- (j) $u_1 = \frac{a^3}{h^2}, u_{r+1} = \frac{bu_r}{a}$
- (k) $u_1 = x^3, u_{r+1} = \frac{5u_r}{}$
- (1) $u_1 = 1, u_{r+1} = (1+x)u_r$
- 3 (a) $5, 7, 9, 11, 13; u_1 = 5, u_{r+1} = u_r + 2$
 - (b) $1, 4, 9, 16, 25; u_1 = 1, u_{r+1} = u_r + 2r + 1$
 - (c) $1, 3, 6, 10, 15; u_1 = 1, u_{n+1} = u_r + r + 1$
 - (d) $1, 5, 14, 30, 55; u_1 = 1, u_{n+1} = u_r + (r+1)^2$
 - (e) $6,18,54,162,486; u_1 = 6, u_{r+1} = 3u_r$
 - (f) $3,15,75,375,1875; u_1 = 3, u_{r+1} = 5u_r$
- **4** (a) $u_r = 10 r$ (b) $u_r = 2 \times 3^r$

 - (c) $u_r = r^2 + 3$ (d) $u_r = 2r(r+1)$
 - (e) $u_r = \frac{2r-1}{r+3}$ (f) $u_n = \frac{r^2+1}{2^r}$

Exercise 8B (page 119)

- **2** (a) r (c) $1^3 = t_1^2 t_0^2$, $2^3 = t_2^2 t_1^2$, $3^3 = t_3^2 - t_2^2, \dots, n^3 = t_n^2 - t_{n-1}^2$
- **3** (a) 5040
- (b) 6720
- (c) 35

- **4** (a)
- (b) 12!
- (n+1)!(d) (n-2)!
- (e) $\frac{(n+3)!}{(n-1)!}$
- (f) $\frac{(n+6)!}{(n+6)!}$ (n+3)!
- (g) 8! (h) n!
- (b) $22 \times 22!$ **5** (a) 12
 - (c) n+1
- (d) $n \times n!$
- 7 (a) 1,5,10,10,5,1,0,0,...
 - (b) $1, 6, 15, 20, 15, 6, 1, 0, 0, \dots$
 - (c) $1, 8, 28, 56, 70, 56, 28, 8, 1, 0, 0, \dots$
- 11! **8** (a) $4! \times 7!$
- (b) $\frac{11!}{7! \times 4!}$
- 5!×5!
- (e) $\frac{12!}{9! \times 3!}$
- 11 The sum of the terms in the sequence is 2^n .

Exercise 8C (page 124)

- 1 (a), (d), (f), (h); 3, -2, q, x respectively
- **2** (a) 12,2r
- (b) 32,14+3r
- (c) -10.8-3r
- (d) 3.3, 0.9 + 0.4r
- (e) $3\frac{1}{2}, \frac{1}{2} + \frac{1}{2}r$
- (f) 43,79-6r
- (g) x+10, x-2+2r
- (h) 1+4x, 1-2x+xr
- **3** (a) 14
- (b) 88
- (c) 36 (f) 11
- (d) 11 16 (g)
- (e) 11
- (h) 28

- 4 60
- **5** (-6,125)
- **6** $y = -\frac{3}{4}x \frac{5}{4}$
- 7 y = -3x + 48

Exercise 12C (page 179)

- 1 (a) $30(5x+3)^5$
- (b) $\frac{5}{2}(5x+3)^{-\frac{1}{2}}$

- 2 (a) $-20(1-4x)^4$ (b) $12(1-4x)^{-4}$ (c) $\frac{-2}{\sqrt{1-4x}}$
- 3 (a) $15x^2(1+x^3)^4$ (b) $-12x^2(1+x^3)^{-5}$
- 4 (a) $24x(2x^2+3)^5$ (b) $\frac{-4x}{(2x^2+3)^2}$ (c) $\frac{2}{\sqrt{(2x^2+3)^3}}$
- 5 $24x^3(3x^4+2)$
- **6** (a) $72x^8 + 72x^5 + 18x^2$ (b) $18x^2(2x^3 + 1)^2$
- 7 (a) $20x^4(x^5+1)^3$ (b) $48x^2(2x^3-1)^7$

 - (c) $\frac{5}{2\sqrt{x}}(\sqrt{x}-1)^4$
- **8** (a) $8x(x^2+6)^3$

- (a) $8x(x^2+6)^3$ (b) $45x^2(5x^3+4)^2$ (c) $28x^3(x^4-8)^6$ (d) $-45x^8(2-x^9)^4$
- 9 (a) $\frac{2}{\sqrt{(4x+3)}}$ (b) $12x(x^2+4)^5$

 - (c) $-36x^2(6x^3-5)^{-3}$ (d) $3x^2(5-x^3)^{-2}$
- **10** (a) $-\frac{4}{25}$ (b) 0
- 11 $\frac{3}{8}$
- 12 (a) $6(x^2+3x+1)^5(2x+3)$ (b) $\frac{-3(2x+5)}{(x^2+5x)^4}$
- 13 y = 12x 25
- 14 x + 4y = 8
- 15 x + 6y = 23
- **16** $6x(x^2-1)^{-\frac{1}{2}}(\sqrt{x^2-1}+1)^5$
- 17 $\frac{1}{\sqrt{(4x+3)(1+\sqrt{4x+3})}}$
- **18** (0,3); minimum

Exercise 12D (page 182)

- 1 4500 per hour
- 2 0.622 °C per minute
- 3 (a) 4.8 cm s^{-1}
- (b) $24 \text{ cm}^2 \text{ s}^{-1}$ (b) $2400 \text{ mm}^3 \text{ s}^{-1}$
- (a) $240 \text{ mm}^2 \text{ s}^{-1}$
- $942\; mm^2\; s^{-1}$
- 0.25 m min^{-1}
- 0.0076 m s^{-1}
- $0.011 \, m \, s^{-1}$
- 0.0040 cm s^{-1}

Miscellaneous exercise 12 (page 184)

- 1 $80(4x-1)^{19}$
- 3 $40x^3(x^4+3)^4$
- **4** 24x + y = 49
- 7 y = 20x + 11
- **8** $(0,\frac{1}{4})$
- 9 3x + 4y = 18
- 10 $0.377 \text{ cm}^2 \text{ s}^{-1}$
- 11 (a) $\frac{10}{\sqrt{\pi}}$ cm (b) $\frac{1}{4\sqrt{\pi}}$ cm s⁻¹
- 12 8x + 5y 34 = 0
- **13** (2,-4); (0,0), (4,0)
 - $(0,16),(4,-16);(2,0),(2\pm2\sqrt{3},0),(0,16)$
- 14 $\frac{(1-1/x^2)}{2\sqrt{(x+1/x)}}$
- 15 $4 \text{ m}^2 \text{ s}^{-1}$
- 16 y = 2x 3
- 17 $\frac{-12t}{\left(3t^2+5\right)^3}$
- **18** (a) $\frac{2-x}{\sqrt{4x-x^2}}$, (2,2)
- 19 (a) Minimum
- **20** $\frac{3}{20\pi}$ cm s⁻¹
- **21** 0.052 m s^{-1}
- **22** $(-\sqrt{3}, -4)$, minimum; (-1,0), maximum; (0,-4), minimum; (1,0), maximum; $(\sqrt{3},-4)$, minimum