



UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
General Certificate of Education  
Advanced Subsidiary Level and Advanced Level

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**MATHEMATICS**

**9709/12**

Paper 1 Pure Mathematics 1 (P1)

**May/June 2013**

**1 hour 45 minutes**

Additional Materials:      Answer Booklet/Paper  
   Graph Paper  
   List of Formulae (MF9)

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**READ THESE INSTRUCTIONS FIRST**

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

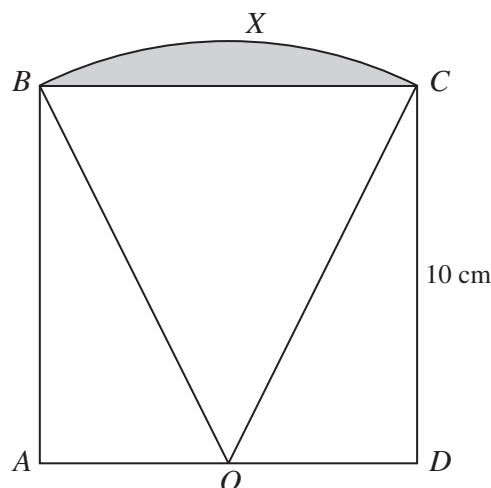
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This document consists of **4** printed pages.



- 1 A curve is such that  $\frac{dy}{dx} = \frac{6}{x^2}$  and  $(2, 9)$  is a point on the curve. Find the equation of the curve. [3]
- 2 Find the coefficient of  $x^2$  in the expansion of
- (i)  $\left(2x - \frac{1}{2x}\right)^6$ , [2]
- (ii)  $(1 + x^2)\left(2x - \frac{1}{2x}\right)^6$ . [3]
- 3 The straight line  $y = mx + 14$  is a tangent to the curve  $y = \frac{12}{x} + 2$  at the point  $P$ . Find the value of the constant  $m$  and the coordinates of  $P$ . [5]

4



The diagram shows a square  $ABCD$  of side 10 cm. The mid-point of  $AD$  is  $O$  and  $BXC$  is an arc of a circle with centre  $O$ .

- (i) Show that angle  $BOC$  is 0.9273 radians, correct to 4 decimal places. [2]
- (ii) Find the perimeter of the shaded region. [3]
- (iii) Find the area of the shaded region. [2]
- 5 It is given that  $a = \sin \theta - 3 \cos \theta$  and  $b = 3 \sin \theta + \cos \theta$ , where  $0^\circ \leq \theta \leq 360^\circ$ .
- (i) Show that  $a^2 + b^2$  has a constant value for all values of  $\theta$ . [3]
- (ii) Find the values of  $\theta$  for which  $2a = b$ . [4]

- 6 Relative to an origin  $O$ , the position vectors of points  $A$  and  $B$  are given by

$$\overrightarrow{OA} = \mathbf{i} - 2\mathbf{j} + 2\mathbf{k} \quad \text{and} \quad \overrightarrow{OB} = 3\mathbf{i} + p\mathbf{j} + q\mathbf{k},$$

where  $p$  and  $q$  are constants.

- (i) State the values of  $p$  and  $q$  for which  $\overrightarrow{OA}$  is parallel to  $\overrightarrow{OB}$ . [2]

- (ii) In the case where  $q = 2p$ , find the value of  $p$  for which angle  $BOA$  is  $90^\circ$ . [2]

- (iii) In the case where  $p = 1$  and  $q = 8$ , find the unit vector in the direction of  $\overrightarrow{AB}$ . [3]

- 7 The point  $R$  is the reflection of the point  $(-1, 3)$  in the line  $3y + 2x = 33$ . Find by calculation the coordinates of  $R$ . [7]

- 8 The volume of a solid circular cylinder of radius  $r$  cm is  $250\pi$  cm<sup>3</sup>.

- (i) Show that the total surface area,  $S$  cm<sup>2</sup>, of the cylinder is given by

$$S = 2\pi r^2 + \frac{500\pi}{r}. \quad [2]$$

- (ii) Given that  $r$  can vary, find the stationary value of  $S$ . [4]

- (iii) Determine the nature of this stationary value. [2]

- 9 A function  $f$  is defined by  $f(x) = \frac{5}{1-3x}$ , for  $x \geq 1$ .

- (i) Find an expression for  $f'(x)$ . [2]

- (ii) Determine, with a reason, whether  $f$  is an increasing function, a decreasing function or neither. [1]

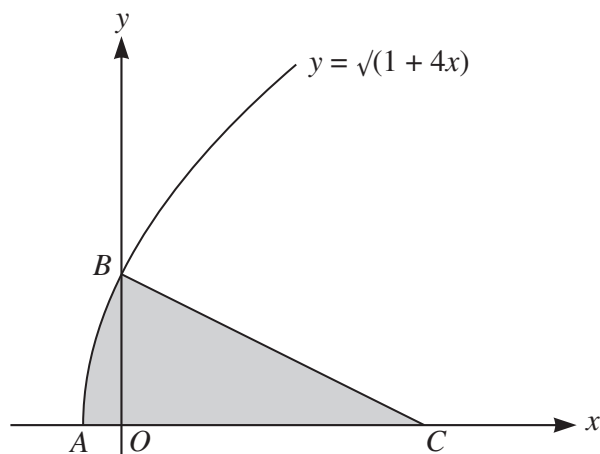
- (iii) Find an expression for  $f^{-1}(x)$ , and state the domain and range of  $f^{-1}$ . [5]

- 10 (a) The first and last terms of an arithmetic progression are 12 and 48 respectively. The sum of the first four terms is 57. Find the number of terms in the progression. [4]

- (b) The third term of a geometric progression is four times the first term. The sum of the first six terms is  $k$  times the first term. Find the possible values of  $k$ . [4]

[Question 11 is printed on the next page.]

11



The diagram shows the curve  $y = \sqrt{1 + 4x}$ , which intersects the  $x$ -axis at  $A$  and the  $y$ -axis at  $B$ . The normal to the curve at  $B$  meets the  $x$ -axis at  $C$ . Find

- (i) the equation of  $BC$ , [5]
- (ii) the area of the shaded region. [5]