CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Level

MARK SCHEME for the October/November 2012 series

9709 MATHEMATICS

9709/73 Paper 7, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2012 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

1	Normal with mean 28 Var = $0.12^2 \times 8$ = 0.115 (3 sfs)	B1 M1 A1	[3]	Both square & × by 8 or sd = 0.12 × √8 or sd = 0.339 (3 sfs) clearly stated var / sd
Total			**[3]**	
2 (i)	μ	B1		(as an expression)
	$\frac{\sigma^2}{n}$	B1	[2]	(as an expression) SC If B0B0 scored, N(μ, $\frac{\sigma^2}{n}$) scores B1
(ii)	$\frac{176-177.8}{\frac{6.1}{\sqrt{12}}}$ (= –1.022)	M1		Standardise with √ 12 Accept 'totals' method. No mixed methods. (2112 – 2133.6) / √ ($6.1^2 \times 12$)
	Φ('–1.022') = 1 – Φ ('1.022')	M1		Correct area (consistent with working)
	= 0.153 (3 sfs)	A1	[3]	
(iii)	No; X norm distr'd or pop norm distr'd Or hts norm distr'd Or original dist normal	B1	[1]	Need 'No' stated or implied AND correct reason NB 'No, because small sample' scores B0 NB 'it is normally distr`d' scores B0
Total			**[6]**	
3 (i)	$\left(\frac{5}{6}\right)^{25} + 25\left(\frac{5}{6}\right)^{24}\left(\frac{1}{6}\right)$	M1		Allow end errors, but just P(2) implies M0 Accept p/q mix
	= 0.0629 final answer	A1		
	Sig level = 6.29%	B1ft	[3]	ft their P($X \leq 1$) with Binomial used. Allow 6.3% or 6%
(ii)	Var (p) $\approx \frac{0.09 \times 0.91}{100}$ (= 0.000819)	M1		For pq /100 seen (any p/q) (must be probs)
	$z = 1.96$	B1		
	$0.09 \pm z\sqrt{\frac{0.09 \times 0.91}{100}}$	M1		For correct form of C.I. (any p/q) (must be probs)
	= 0.034 to 0.146 (3 dps)	A1	[4]	
Total			**[7]**	

4	Use of $X_1 - 2X_2$ or similar $E(X_1-2X_2) = 180 - 360$ ($= -180$)	B1		Or use of $\frac{1}{2} X_1 - X_2$ $E(2X_1-X_2) = 360 - 180$ ($= 180$) Or $E(\frac{1}{2} X_1 - X_2) = 90 - 180 = (-90)$
	$Var(X_1-2X_2) = 5\times1550$ or 7750	M1 A1		for $1550 + 4 \times 1550$ or $\frac{1}{4} \times 1550 + 1550$ 7750 or 1937.5
	$\frac{0-(-180)}{\sqrt{'7750'}}$ or $\frac{0-180}{\sqrt{'7750'}}$ $(= \pm 2.045)$	M1		Allow incorrect var (dep > 0 & ≠ 1550), no √ Standardising – no mixed methods Or $\pm (0 - -90)/\sqrt{1937.5}$
	$1 - \Phi('2.045')$ = 0.0205 or 0.0204	M1 A1		For finding correct area (consistent with working)
	Ans 0.041 (2 sf)	B1ft	[7]	Allow double their prob
Total			**[7]**	
5 (i)	Est(μ) = 2.3	B1		
	$Est(\sigma^2) = \frac{200}{199}\left(\frac{1636}{200} - \left(\frac{460}{200}\right)^2\right)$	M1		Allow $\sqrt{\frac{200}{199}\left(\frac{1636}{200} - \left(\frac{460}{200}\right)^2\right)}$ or 1.7043 for M1 Or $1/199\ (1636 - 460^2/200)$
	= 2.90 (3 sf) or 2.91 or 578/199	A1	[3]	
(ii)	H_0: Pop mean wt loss = 2 kg H_1: Pop mean wt loss > 2 kg	B1		Allow 'μ' but not just 'mean'
	$\frac{2.3-2}{\sqrt{\frac{'2.9045'}{200}}}$	M1		$\frac{2.3-2}{\sqrt{\frac{'1.7043'}{200}}}$ Stand'ise with √200. Accept sd/var mixes Or $x_{crit} = 2 + 2.326\sqrt{(2.9045/200)}$
	= 2.489 or ± 2.49 or 0.0064 / 0.9936 for area comparison or $x_{crit} = 2.28(03)$	A1		
	comp $z = 2.326$	M1		For valid comparison (z or area or x_{crit})
	Evidence that mean wt loss > 2 kg	A1ft		No contradictions Reject H_0 / accept H_1 only if H_0 / H_1 correctly defined If $\frac{200}{199}$ not used in **(i)**: var = 2.89, sd = 1.7,
			[5]	cr $z = 2.496$ can score all marks
Total			**[8]**	

6 (i)	$f(x) \geqslant 0$ for all x defined	B1		
	$\int_0^a \frac{2}{a^2} x \mathrm{d}x$	M1		Attempt $\int f(x)\mathrm{d}x$ with limits 0, a. Must be a.
	$\left(= \left[\frac{2x^2}{2a^2} \right]_0^a \right)$	A1		Or equivalent methods (e.g. by areas)
	$= 1$		[3]	
(ii)	$\int_0^a \frac{2}{a^2} x^2 \mathrm{d}x \ (= 8)$	M1		Attempt $\int x f(x)\mathrm{d}x$, ignore limits
	$\frac{2}{a^2}\left[\frac{x^3}{3} \right]_0^a \ (= 8)$	A1		Correct integrand and limits
	$\left(\frac{2a}{3} = 8 \right)$	A1		
	$a = 12$		[3]	
(iii)	$1 - \int_0^6 \frac{2}{144} x \mathrm{d}x$ or $\int_6^{12} \frac{2}{144} x \mathrm{d}x$	M1		Correct expr'n incl limits; ft their 'a'
	$= 1 - 1 - \frac{1}{72}\left[\frac{x^2}{2} \right]_0^6$ or	A1ft		Correct integrand and limits; ft their 'a'
	$\frac{1}{72}\left[\frac{x^2}{2} \right]_6^{12}$			
	$= \frac{3}{4}$	A1ft	[3]	ft their 'a', dep $0 <$ ans < 1
Total			**[9]**	

7 (i)	$n > 50$ $np = 0.8$, which is < 5	B1 B1	 [2]	Accept n large Accept p small
(ii)	$\lambda = 9.6$ $e^{-9.6}(\frac{9.6^3}{3!}+\frac{9.6^4}{4!}+\frac{9.6^5}{5!})$ $= 0.0800$ (3 sfs)	B1 M1 A1	 [3]	 Any λ Accept end errors. Allow 0.08
(iii)	H_0: Pop mean for 10 days = 8 H_1: Pop mean for 10 days < 8 $e^{-8}(1 + 8 + \frac{8^2}{2!})$ $= 0.0138$ or 0.0137 Compare 0.02 Evidence that mean number of absentees has decreased	 B1 M1 A1 M1 A1ft	 [5]	or Pop mean for 1 day = 0.8 Pop mean for 1 day < 0.8 Allow λ or μ but not just 'mean' Any λ. Accept end errors. NB P(2) only used scores M0M0 Accept CR method CR = 0, 1, 2 all working must be shown Valid comparison with 0.02 or CR No contradictions Reject H_0 / accept H_1 only if H_0 / H_1 correctly defined
Total			**[10]**	
	Total for paper		**[50]**	