

## **NOVEMBER 2002**

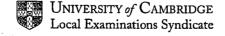
## GCE Advanced Subsidiary Level Advanced International Certificate of Education

## MARK SCHEME

**MAXIMUM MARK: 50** 

SYLLABUS/COMPONENT: 9709 /6, 0390 /6

MATHEMATICS (Probability and Statistics 1)





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|  |            |    | • •   |
|--|------------|----|---|
| 1 (i) $a+b=0.45$   | B1         | 1  | Accept unsimplified equation  |
| (ii) $0.3 + 3a + 5b + 7 \times 0.25 = 4$   | M1         |    | For an equation involving $\sum x_i p_i = 4$ must be  |
|  | M1         |    | correct unsimplified version, seen anywhere For sensible attempt to solve the two equations ie                              |
| a = 0.15 $b = 0.3$   | A1         | 3  | eliminating one letter For correct a and b.   |
| 2 (i) options (122), (212), (221), (113), (131), (311)                             | M1         |    | For an option involving $(1,2,2)$ and an option involving $(1,1,3)$   |
| prob = 6 /216 (AG)   | A1<br>A1   | 3  | For all six correct options For legitimately obtaining answer given   |
| (ii) (133)×3, (223)×3, (115)×3,  | M1         | ,  | For listing 3 or 4 different correct options or tree  |
| (124)×6  |            | nd | diagram  For multiplying 4 prob options by a relevant number or listing ≥ 12 correct options                                |
| prob = 15 / 216 (= 5/72)   | A1         | 3  | For correct answer  |
| 3 (i) $z = \pm \frac{40 - 35.0}{11.6} = \pm 0.431$                                 | M1         |    | For standardising ( $\sqrt{11.6}$ in denom M1, ccM0 $11.6^2$ M0)  |
| 11.0   | M1         |    | For subtracting two relevant probabilities or   |
| $\Phi(0.431) - \{1 - \Phi(0.431)\} = 0.334$  | A1         | 3  | equivalent For correct answer   |
| (ii) $z = \pm 1.282$ or $\pm 1.281$ only   | Bi         |    | For stating z   |
| $1.282 = \frac{x - 35.0}{11.6}$  | M1         |    | For solving an equation for x with some z value   |
| x = 49.9  or  49.8  on  z = 1.28   | Al         | 3  | from tables, allow cc, $\sqrt{11.6}$ , 35-x, not 11.6 <sup>2</sup><br>For correct answer                                    |
| 4 (i) ${}_{8}C_{2} = 28$ or $7+6+5+4+3+2+1$  | B1         | 1  | For <sub>8</sub> C <sub>2</sub>   |
| (ii) ${}_{8}C_{1} + {}_{8}C_{2} + {}_{8}C_{3} + {}_{8}C_{4}$<br>= 8 + 28 + 56 + 70 | M1         |    | For listing 4 Combination options (can be added or multiplied here)   |
|  | A1         |    | For ${}_{8}C_{1} + {}_{8}C_{2} + {}_{8}C_{3} + {}_{8}C_{4}$   |
|  | <b>A</b> 1 |    | For at least 3 correct numbers, can be implied by seeing 878080 (mult)  |
| = 162  | A1         | 4  | For correct answer $SR_8C_1+_8C_2++_8C_8$ M1 only $SR_8C_3\times_8C_3\times_8C_1\times_8C_2$ M1 only                        |
| (iii) $(162)^4$<br>= 688 747 536 or 3s   | M1<br>A1ft | 2  | For (their (ii)) <sup>4</sup> or ${}_{8}C_{3}+{}_{8}C_{3}+{}_{8}C_{1} \times {}_{8}C_{2}$<br>For correct answer in any form |
|  | 1          |    |   |



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| 5 (i) P(W <sub>1</sub>   L <sub>2</sub> ) = $\frac{0.6 \times 0.3}{0.6 \times 0.3 + 0.4 \times 0.6}$ | B1      |   | For 0.6×0.3 seen anywhere in isolation                                |
|--|---------|---|---|
| $0.6 \times 0.3 + 0.4 \times 0.6$  | B1      |   | For correct numerator   |
| $=\frac{0.18}{0.42}=0.429$   |         |   | For summing two 2 factor products in denom                            |
| $\frac{1}{0.42} = 0.42$  | A1      |   | For correct denominator unsimplified                                  |
|  | A1      | 5 | For correct answer  |
| (ii) $P(W_1W_2L_3) = 0.6 \times 0.7 \times 0.3 = 0.126$  | M1      |   | For summing three probability options                                 |
| $P(W_1L_2W_3) = 0.6 \times 0.3 \times 0.4 = 0.072$   | B1      |   | For one correct probability option                                    |
| $P(L_1W_2W_3) = 0.4 \times 0.4 \times 0.7 = 0.112$   | B1      |   | For two correct probability options                                   |
| Probability = 0.31   | A1      | 4 | For correct answer  |
|  |         |   |   |
| 6 (i) P(equal) = $(0.25)^5 \times (0.75)^5 \times_{10} C_5$  | M1      |   | For $(0.25)^5 \times (0.75)^5$ must be 0.25, 0.75                     |
| = 0.0584   | Al      | 2 | For correct answer. A0 if subsequently doubled                        |
| - 0.0364   | AI      |   | Por correct answer. As it subsequently doubled                        |
| (ii) $(0.0584)^1 \times (0.9416)^7 \times {}_{8}C_1$   | M1      |   | For $(\text{their}(a))^1 \times (1 - \text{their}(a))^7 \times_8 C_1$ |
| = 0.307  | Alft    | 2 | For correct answer from their ans to (i)                              |
| •  |         |   | Accept anything from 0.304 to 0.307 for the ft if                     |
|  |         |   | they have lost the A1 in (i) from PA                                  |
| (iii) $\mu = 120 \times 0.25 = 30$ , $\sigma^2 = 30 \times 0.75 = 22.5$                              | Н<br>М1 |   | For both mean and variance correct from any                           |
| (III) $\mu = 120 \times 0.23 = 30$ , $0 = 30 \times 0.73 = 22.3$                                     | IVII    |   | sensible p  |
|  | M1      |   | For correct standardisation with or without cc                        |
| (24.5. 20)   | IVII    |   | For correct standardisation with or without ce                        |
| $P(X < 35) = \Phi\left(\frac{34.5 - 30}{\sqrt{22.5}}\right) = \Phi(0.949)$                           | B1      |   | For correct use of continuity correction 34.5                         |
|  |         |   |   |
|  | M1      |   | For use of tables based on their z value either                       |
| = 0.829  |         |   | end NB can't get if z is too large or too small                       |
|  | A1      | 5 | For correct answer  |
| 7 (i) LQ = 72, or 73 or 71.5 only  | B1      |   | Accept Q <sub>1</sub> , Q <sub>2</sub> , Q <sub>3</sub>               |
| median = 78,   | B1      |   | LQ UQ muddle scores B1 B0 and possibly B1 for                         |
| UQ = 88 or 87.75 only  | B1      | 3 | median  |
| (ii)   | B1      |   | For only one numbered linear scale                                    |
| $\stackrel{\smile}{P}$   | BI      |   | For country P all correct on linear scale                             |
| -  | Blft    |   | For Q all correct on linear scale                                     |
| Q  | Bl      | 4 | For P and Q labelled, weights or kg shown                             |
|  |         | - | SR non linear scale max B0 B0 B0 B1                                   |
| 50 60 70 80 90 100 110 wts   |         |   | Or max B0 B1 B0 B1 if one error in a                                  |
|  |         |   | otherwise linear scale  |
|  | 1       |   | NB No outliers  |
| (iii) people heavier in P than in Q  |         |   | Or equivalent statement   |
| weights more spread out in $Q$   |         | _ | Or equivalent statement   |
|  |         | 2 | l -   |
|  |         |   | Cannot have two statements saying the                                 |
|  |         |   | equivalent of the same category (wts, spread                          |
|  |         |   | skewness). Must have the same statemen                                |
|  | J       |   | relating to P and to Q.   |

