

**CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**GCE Advanced Subsidiary Level and GCE Advanced Level**

**MARK SCHEME for the May/June 2013 series**

**9709 MATHEMATICS**

**9709/41**

Paper 4, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

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### **Mark Scheme Notes**

Marks are of the following three types:

**M** Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\checkmark$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking  $g$  equal to 9.8 or 9.81 instead of 10.

|               |                                       |                 |              |
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The following abbreviations may be used in a mark scheme or used on the scripts:

|     |   |
|-----|---|
| AEF | Any Equivalent Form (of answer is equally acceptable)   |
| AG  | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)   |
| BOD | Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)  |
| CAO | Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)   |
| CWO | Correct Working Only – often written by a ‘fortuitous’ answer   |
| ISW | Ignore Subsequent Working   |
| MR  | Misread   |
| PA  | Premature Approximation (resulting in basically correct work that is insufficiently accurate)   |
| SOS | See Other Solution (the candidate makes a better attempt at the same question)  |
| SR  | Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance) |

### **Penalties**

|       |   |
|-------|---|
| MR –1 | A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through √” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting. |
| PA –1 | This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.   |

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|   |      |  |                |                |  |
|---|------|--|----------------|----------------|--|
| 1 | (i)  | Less than<br>$F = 1.25W$ so $W < F$                          | B1             |                |  |
|   | (ii) | $[P - 60 \times 1.25 = 6 \times 4]$<br>$P = 99$              | B1<br>M1<br>A1 | [2]<br><br>[2] | For applying Newton's second law.  |
| 2 |      | Increase in PE = $1250 \times 10 \times 600 \sin 2.5^\circ$  | B1             |                |  |
|   |      | Decrease in KE = $\frac{1}{2} 1250(30^2 - v_{\text{top}}^2)$ | B1             |                |  |
|   |      | WD against resistance = $400 \times 600$                     | B1             |                |  |
|   |      | $[562500 - 625v_{\text{top}}^2 = 327145 + 240000 - 450000]$  | M1             |                | For using WD by DF = Increase in PE – decrease in KE + WD against resistance |
|   |      | Speed is $26.7 \text{ ms}^{-1}$                              | A1             | [5]            |  |

**Special Ruling** for candidates who assume, without justification, that the driving force (DF) is constant (maximum mark 4).

|   |      |   |                        |            |  |
|---|------|---|------------------------|------------|--|
|   |      | [DF – Weight component – Resistance = Mass $\times$ Accel'n]<br>$750 - 545 - 400 = 1250a$<br>$v^2 = 30^2 + 2 \times (-0.156) \times 600$<br>Speed is $26.7 \text{ ms}^{-1}$ | M1<br>A1<br>B1ft<br>B1 |            | For applying Newton's second law.<br><br>ft value of a   |
| 3 | (i)  | $u^2 = 2 \times 10 \times 45$ ; speed is $30 \text{ ms}^{-1}$   | M1<br>A1               | [2]        | For using $0 = u^2 - 2gs$  |
|   | (ii) | $[40 = 30t - 5t^2 \rightarrow t = 2, 4]$<br>$[5 = \frac{1}{2} 10t^2 \rightarrow t = 1]$<br>Time above the ground is 2 s   | M1<br>A1ft             | [2]<br>[2] | For using $s = ut - \frac{1}{2} gt^2$ with $s = 40$ , $u = 30$ and $T = t_2 - t_1$ or $s = ut + \frac{1}{2} gt^2$ $s = 5$ , $u = 0$ and $T = 2t$ |

**Special Ruling** for candidates who assume, without justification, that the length of time required is that of the upward movement only. (maximum mark 1).

|  |       |  |                |     |                           |
|--|-------|--|----------------|-----|---------------------------|
|  | (ii)  | $5 = \frac{1}{2} 10t^2 \rightarrow t = 1$ , the length of time required is 1 s   | B1             | B1  |                           |
|  | (iii) | Max. height above top of cliff = $\frac{1}{2} g(17 \div 4)$ (= 21.25)<br>$[0 = V^2 - 2g(40 + 21.25)]$<br>Speed is $35 \text{ ms}^{-1}$ | B1<br>M1<br>A1 | [3] | For using $0 = u^2 - 2gs$ |

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## Alternative Marking Scheme for (iii)

|  |                               |   |  |  |  |
|--|-------------------------------|---|--|--|--|
| (iii)  |                               | M1  |  | For using $40 = Vt - 5t^2 \rightarrow$<br>$t_2 - t_1 =$<br>$\frac{1}{2} (V/5 + \sqrt{(V^2/25 - 32)}) - \frac{1}{2} (V/5 - \sqrt{(V^2/25 - 32)})$ |  |
|  | $17 = V^2/25 - 32$            | A1  |  |  |  |
|  | Speed is $35 \text{ ms}^{-1}$ | A1  | [3]  |  |  |
|  |                               |   |  |  |  |
| 4  | (i)                           | DF = $1500\,000/37.5$ (= 40 000)  | B1   | For using Newton's second law  |  |
|  |                               | [DF – R = ma]   | M1   |  |  |
|  |                               | DF – 30 000 = 400 000a  | A1   |  |  |
|  |                               | Acceleration is $0.025 \text{ ms}^{-2}$   | A1   |  |  |
|  | (ii)                          | [ $1500\,000/v - 30\,000 = 0$ ]   | M1   | For using Newton's 2 <sup>nd</sup> law with a = 0  |  |
|  |                               | Steady speed is $50 \text{ ms}^{-1}$  | A1   |  |  |
| 5  | (i)                           | R = $2.6 \times (12 \div 13)$ (= 2.4)   | B1   | For using $F = \mu R$<br><br>For applying Newton's 2 <sup>nd</sup> law to A or to B.   |  |
|  |                               | [ $F = 0.2 \times 2.4$ ]  | M1   |  |  |
|  |                               | [ $T - 2.6(5 \div 13) - F = 0.26a$ , $5.4 - T = 0.54a$ ]  | M1   |  |  |
|  |                               | For any two of $T - 1 - 0.48 = 0.26a$ , $5.4 - T = 0.54a$ or<br>( $5.4 - 1 - 0.48$ ) = ( $0.54 + 0.26$ )a | A1   |  |  |
|  |                               | Acceleration is $4.9 \text{ ms}^{-2}$   | B1   |  |  |
|  |                               | Tension is 2.75 N (2.754 exact)   | A1   |  |  |
|  | (ii)                          | [ $s = \frac{1}{2} 4.9 \times 0.4^2$ ]  | M1   | For using $s = \frac{1}{2} at^2$   |  |
|  |                               | Distance is 0.392 m   | A1   |  |  |
|  | 6                             | (i)   |  | M1   | For resolving forces in the x and y directions (or<br>for sketching a marked triangle of forces)<br><br>(= 3.4)<br><br>(= 1.7)<br><br>For using $F^2 = (F\cos\theta)^2 + (F\sin\theta)^2$ to find F or<br>$\tan\theta = F\sin\theta \div F\cos\theta$ to find $\theta$ |
|  |                               |   | $F\cos\theta = 2.5 \times 24 \div 25 + 2.6 \times 5 \div 13$ | A1   |  |
| $F\sin\theta = 2.6 \times 12 \div 13 - 2.5 \times 7 \div 25$ |                               |   | A1   |  |  |
|  |                               |   | M1   |  |  |
| For $F = 3.80 \text{ N}$ or $\tan\theta = 0.5$               |                               |   | A1   |  |  |
| For $\tan\theta = 0.5$ or $F = 3.80 \text{ N}$               |                               |   | B1   |  |  |
|  |                               |   | [6]  |  |  |

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|  |       |   |                                  |                |  |
|--|-------|---|----------------------------------|----------------|--|
|  | (ii)  | $[3.80 = 0.5a]$<br><br>Acceleration is $7.60 \text{ ms}^{-2}$<br><br>Direction is $26.6^\circ$ clockwise from +ve $x$ -axis.  | M1<br><br>A1ft<br><br>B1ft       | [3]<br><br>[3] | For using Newton's 2 <sup>nd</sup> law with the magnitude of the resultant force equal to the value of $F$ found.<br><br>ft value of $F$ found in (i)<br><br>ft value of $\tan\theta$ found in (i) |
|  | 7 (i) | $[0.0000117(1200t^2 - 12t^3) = 0]$<br><br>$1200t^2 = 12t^3 \rightarrow t = 0, 100$<br><br>Distance AB = 1170 m  | M1<br><br>A1<br><br>A1           | [3]<br><br>[3] | For differentiating and solving $ds/dt = 0$<br><br>Accept just $t = 100$ , if it is used to find distance AB.  |
|  | (ii)  | $2400t - 36t^2 = 0 \rightarrow t = 0, 200/3$<br><br>$[v_{\max} = 0.0000117\{1200(200/3)^2 - 12(200/3)^3\}]$<br><br>Maximum speed is $20.8 \text{ ms}^{-1}$  | M1<br><br>A1<br><br>M1<br><br>A1 | [4]<br><br>[4] | For differentiating again and solving $d^2s/dt^2 = 0$<br><br>Accept just $t = 200/3$ , if it is used to find $v_{\max}$ .<br><br>For substituting into $v(t)$                                      |
|  | (iii) | At A $a(t) = 0$<br><br>At B $a(t) = 0.0000117(2400 \times 100 - 36 \times 100^2) = -1.40 \text{ ms}^{-2}$ ( $-1.404$ exact)   | B1<br><br>B1                     | [2]<br><br>[2] |  |
|  | (iv)  | Sketch has $v$ increasing<br><br>from 0 to maximum and decreasing to 0, with maximum closer to $t = 100$ than $t = 0$ .<br><br>Sketch has zero gradient at $t = 0$ and inflexion closer to $t = 0$ than $t = 100$ . | B1<br><br>B1                     | [2]<br><br>[2] |  |