UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

MARK SCHEME for the October/November 2010 question paper for the guidance of teachers

9709 MATHEMATICS

9709/43 Paper 4, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

- CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the October/November 2010 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

1	$a = g\sin30^o$	B1		
	[**(i)** $v_1^2 = 2(g\sin30^o)0.9$ or ½ $mv_1^2 = mg(0.9\sin30^o)$ or **(ii)** $v_2 = (g\sin30^o)0.8$]	M1		For using $v^2 = 2as$ or $1/2\ mv^2 = mgh$ or $v = at$
	(i) Speed is 3 ms^{-1} or **(ii)** Speed is 4ms^{-1}	A1		
	(ii) Speed is 4ms^{-1} or **(i)** Speed is 3 ms^{-1}	B1	**[4]**	
2	**(i)** [½ $v^2 = 10x1.8$]	M1		For using ½ $mv^2 = mgh$
	Speed is 6 ms^{-1}	A1	**[2]**	
	(ii) [WD = ½x0.5($6^2 - 5^2$) or 0.5x10x1.8 = ½x0.5x5^2]	M1		For using WD = loss of KE or $KE_A + PE_A - WD = KE_C + PE_C$
	Work done is 2.75 J	A1	**[2]**	
3	**(i)** [2T $\cos30^o = 3\sqrt{3}$	M1		For expressing resultant in terms of T and equating with value
	or $T/\sin30^o = 3\sqrt{3}/\sin120^o$			or for using sine rule
	or $T^2 = T^2 + (3\sqrt{3})^2 - 2T(3\sqrt{3})\cos30^o$			or for using cosine rule
	or $\sqrt{\{(T\cos30^o)^2 + (T + T\cos60^o)^2\}} = 3\sqrt{3}$]			or for finding Rx and Ry and equating resultant to $3\sqrt{3}$
	Tension is 3 N	A1	**[2]**	AG
	(ii) [T = F + mg sin30]	M1		For resolving forces on Q parallel to AC
	R = mg cos30	B1		
		M1		For using $F = \mu R$
	$3 = 0.75(10\cos30^o)m + 10m \sin 30^o$	A1		
	Mass is 0.261 kg	A1	**[5]**	
4	**(i)** v(4) = 0.75x4	B1		
	v(54) = v(4) and v(60) = v(54) – 0.5(60 – 54)	B1		
	Velocity is 3 ms^{-1} when t = 4 and 0 when t = 60	B1		
		M1		Graph consists of 3 straight line segments with 1st and 3rd having +ve and –ve slopes respectively; v is single valued and continuous throughout, and v(0) = 0.
	2nd segment has zero slope; end points of segments are seen to be correct{(0,0), (4,3), (54,3), (60,0)}	A1ft	**[5]**	ft incorrect value(s) for v(4) and v(60)
	(ii) [XY = ½ (60 + 50)x3 or XY = ½ x0.75x4^2 + 3x50 – ½ x0.5x6^2]	M1		For using area property for distance or $s_1 = ½\ a_1t_1^2$, $s_2 = u_2t_2$, $s_3 = ½\ a_3t_3^2$ and $XY = s_1 + s_2 - s_3$
	Distance is 165 m	A1	**[2]**	

5	**(i)**	$[F^2 = 27.5^2 + (-24)^2]$	M1		For using $F^2 = X^2 + Y^2$ (may be scored in **(ii)**)
		$F = 36.5$	A1		
		$[\tan\alpha^\circ = -(-24/27.5)]$	M1		For using $\tan\alpha^\circ = -Y/X$
		$\alpha = 41.1$	A1	**[4]**	
	(ii)	$R = 94.9$	B1		
		$[\alpha^\circ + \theta^\circ = \tan^{-1}(87.6/36.5)$; or $(\alpha^\circ + \theta^\circ) = \cos^{-1}(36.5/94.9)$ or $\theta^\circ = \tan^{-1}(87.6\sin 48.9^\circ - 24)/(27.5 + 87.6\cos 48.9^\circ)]$	M1		For using $\tan(\alpha^\circ + \theta^\circ) = 87.6/F$ or $\cos(\alpha^\circ + \theta^\circ) = F/R$ or $\tan\theta^\circ = Y/X$
		$\theta = 26.3$	A1ft	**[3]**	ft 67.4 – incorrect α
6	**(i)**		M1		For using $a(t) = \dot{v}(t)$
		$a_1(t) = 1.44t - 0.288t^2$, $a_2(t) = 2.4 - 0.48t$	A1		
		$[a_1 = 1.44x5 - 0.288x25$, $a_2 = 2.4 - 0.48x5]$	M1		For evaluating $a_1(5)$ and $a_2(5)$
		$a_1 = a_2 (= 0)$ ➔ no instantaneous change	A1	**[4]**	
	(ii)		M1		For using $s = \int v dt$
		$s_1 = 0.24t^3 - 0.024t^4$, $s_2 = 1.2t^2 - 0.08t^3$	A1		
		$[\{(0.24x5^3 - 0.024x5^4) - (0 - 0)\} + \{(1.2x10^2 - 0.08x10^3) - (1.2x5^2 - 0.08x5^3)\}]$	M1		For using limits 0 to 5 and 5 to 10 or equivalent
		Distance is 35 m	A1	**[4]**	
7	**(i)**	$DF = 24000/20$	B1		
		$[DF - R = 1250x0.32]$	M1		For using Newton's second law (3 terms)
		$R = 800$	A1	**[3]**	
	(ii)	$24000/29.9 - 800 = 1250a$	B1		
		Acceleration is $0.002\,ms^{-2}$	B1	**[2]**	
	(iii)	$[a = (24000/30 - 800)/1250$ $24000/v - 800 > 0$ ➔ $v < 30]$	M1		For finding a when $v = 30$ or for using $a > 0$ to obtain an inequality for v
		Car not accelerating when $v = 30$ or Speed cannot reach $30\,ms^{-1}$	A1	**[2]**	AG
	(iv)	$29.9 \le v < 30$ ➔ speed approximately constant	B1	**[1]**	
	(v)	$30\,ms^{-1}$ (max error 0.1) or $29.95\,ms^{-1}$ (max error 0.05) or $29.9\,ms^{-1}$ (max error 0.1)	B1	**[1]**	
	(vi)	**(a)** $[24 = 1200/T]$	M1		For using $P = \Delta WD/\Delta t$
		Time taken is 50 s	A1		
		(b) $[s = 30x50$ or $29.95x50$ or $29.9x50]$	M1		For using $s = vt$
		Distance BC is 1500 m or 1500 m or 1495 m	A1	**[4]**	

ALTERNATIVE FOR PART **(vi)**

(b)	[1200 000 = 800d]	M1	For using 'no change in KE' ➔ WD by car's engine = WD against resistance' (may be implied)
	Distance BC is 1500 m	A1	
(a)	[t = 1500/30 or 1500/29.95 or 1500/29.9]	M1	For using t = s/v
	Time taken is 50 s or 50.1 s or 50.2 s	A1	