



**CAMBRIDGE A LEVEL PROGRAMME  
SEMESTER ONE EXAMINATION JUNE 2010**  
(March 2010 Intake)

Thursday

10 June 2010

8.15 am – 10.15 am

**MATHEMATICS**

**9709/1,6**

2 hours

Additional materials: Answer Paper  
List of formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your name and class on all the work you hand in.  
Write in dark blue or black pen on both sides of the paper.  
You may use a soft pencil for any diagrams or graphs.  
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.  
At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total marks for this paper is 80.

Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

This document consists of 5 printed pages.

## Section A: Pure Mathematics (P1)

- 1 Expand  $(1 - 2x - x^2)^6$  in ascending power of  $x$ , up to and including the term in  $x^3$ . [3]

- 2 Find the set of values of  $q$  for which

$$f(x) \equiv x^2 - 2qx + q + 2$$

is greater than zero for all real values of  $x$ . [4]

- 3 In an arithmetic progression, the first term is  $a$  and the common difference is  $d$ . Given that the sum of the first 8 terms is half the sum of the next four terms, express  $a$  in terms of  $d$ .

[4]

- 4 Prove the identity  $1 + \frac{\tan \theta \sin \theta}{\cos \theta} \equiv \frac{1}{\cos^2 \theta}$ . [2]

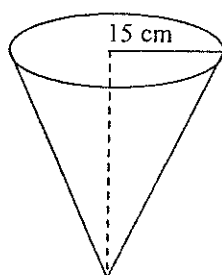
Hence solve the equation  $3 + \frac{3 \tan \theta \sin \theta}{\cos \theta} - 5 = 0$ , for  $0^\circ \leq \theta \leq 360^\circ$ . [4]

- 5 The curve  $y = \frac{1}{4}x^2 - 1$  and the line  $2y = x + 10$  intersect at the points  $A$  and  $B$ , and  $O$  is the origin.

(i) Calculate the coordinates of  $A$  and  $B$ . [3]

(ii) Hence show that  $OA$  and  $OB$  are perpendicular. [3]

6



The diagram shows a hollow right circular cone with a base radius of 15 cm and a height of 50 cm. It contains water which leaks through a small hole in the vertex at the rate of  $60 \text{ cm}^3 \text{ s}^{-1}$ . Find the exact rate at which the water level is falling when the height of the water in the cone is 25 cm from the vertex. [6]

- 7 Points  $A$ ,  $B$  and  $C$  have coordinates  $(4, 0, 4)$ ,  $(0, 6, 6)$  and  $(0, 0, c)$  respectively. The point  $O$  is the origin, and the mid-point of  $AB$  is  $M$ .

- (i) Given that  $c = 5$ , calculate the angle  $OMC$ . [5]  
 (ii) Find the value of  $c$  for which angle  $OMC$  is a right angle. [2]

- 8 Function  $f$ ,  $g$ , and  $h$  are defined by

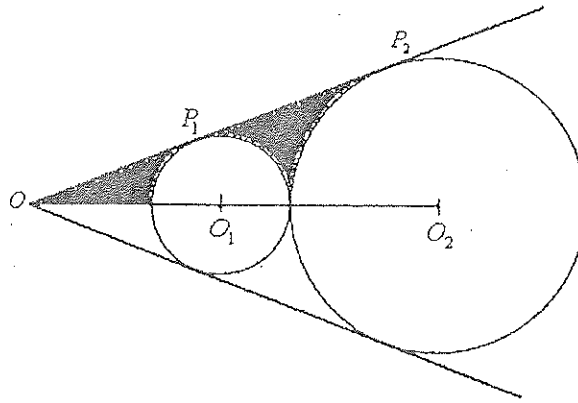
$$f: x \mapsto x + p \quad \text{for } x \in R, \text{ where } p \text{ is a constant,}$$

$$g: x \mapsto \frac{64}{4 - x} \quad \text{for } x \in R, x \neq 4$$

$$h: x \mapsto 12 + 8x - x^2 \quad \text{for } x \leq 4$$

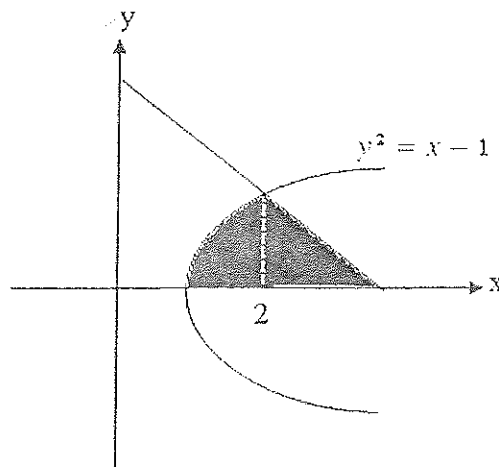
- (i) Find the values of  $p$  for which equation  $f(x) = g(x)$  has two equal roots. [4]  
 (ii) Solve the equation  $fg(x) = -20$  for the positive value of  $p$  in part (i). [2]  
 (iii) Express  $12 + 8x - x^2$  in the form  $a - (x + b)^2$ . [1]  
 (iv) Sketch, in a single diagram, the graph of  $y = h(x)$  and  $y = h^{-1}(x)$ , making clear the relationship between the two graphs. [3]

[Turn over]



- 9 In the diagram,  $OP_1P_2$  is a tangent to two circles with centres  $O_1$  and  $O_2$ . Given that  $OP_1 = 15$  cm and the radius of the circle centre  $O_1$  is 8 cm.
- Find the radius of circle centre  $O_2$ . [2]
  - Find the perimeter of the shaded region. [4]
  - Find the area of the shaded region. [4]

- 10 (a) Find  $\int \sqrt{x-1} \, dx$ . [2]



- (b) The diagram shows the curve  $y^2 = x - 1$  and the normal to the curve at the point  $(2, 1)$ .
- Find the equation of the normal at the point  $(2, 1)$ . [3]
  - Calculate the area of the shaded region. [6]

**Section B: Statistics (S1)**

- 11 For each of 50 plants, the height,  $h$  cm was measured and the value of  $(h-100)$  was recorded. The mean and standard deviation of  $(h-100)$  were found to be 20.2 cm and 3.8 cm respectively.

(i) Write down the mean and standard deviation of  $h$ . [2]

The mean of the heights of another 100 plants were found to be 112 cm.

(ii) Calculate the mean height of all 150 plants. [2]

- 12 The following data shows the marks obtained by 25 students in a Mathematics test.

47	53	62	79	36
66	34	85	46	35
82	87	42	59	65
75	40	31	64	44
41	67	54	88	68

- (i) Construct a stem plot. [3]
- (ii) Find the first quartile, median and third quartile of the above data. [3]
- (iii) Construct a box plot of the data. [3]