Marking scheme: Worksheet (A2) 26

1
$$F = EQ = 5.0 \times 10^5 \times 3.2 \times 10^{-19}$$

$$F = 1.6 \times 10^{-13} \,\mathrm{N}$$

2 **a**
$$E = \frac{V}{d} = \frac{600}{3.0 \times 10^{-2}}$$
 [1]

$$E = 2.0 \times 10^4 \,\mathrm{V m^{-1}}$$

The electric field is at right angles to the plate.

electric

Since the droplet is stationary, the electric force on the droplet must be equal and opposite to its weight. [1] The electric force must act upwards, so the charge on the droplet must be negative. [1]

ii
$$E = \frac{r}{Q}$$

c

$$Q = \frac{F}{E} = \frac{6.4 \times 10^{-15}}{2.0 \times 10^4}$$
 [1]

$$Q = 3.2 \times 10^{-19} \,\mathrm{C}$$
 [1]

$$\mathbf{3} \quad F = BQv \tag{1}$$

$$F = 0.18 \times 1.6 \times 10^{-19} \times 4.0 \times 10^{6}$$
 [1]

$$F = 1.15 \times 10^{-13} \text{ N} \approx 1.2 \times 10^{-13} \text{ N}$$
 [1]

$$\mathbf{4} \quad \mathbf{a} \quad F = BQv \tag{1}$$

$$F = 0.004 \times 1.6 \times 10^{-19} \times 8.0 \times 10^{6}$$
 [1]

$$F = 5.12 \times 10^{-15} \,\mathrm{N} \approx 5.1 \times 10^{-15} \,\mathrm{N}$$
 [1]

$$\mathbf{b} \quad a = \frac{F}{m} = \frac{5.12 \times 10^{-15}}{9.11 \times 10^{-31}}$$
 [1]

$$a = 5.63 \times 10^{15} \text{ m s}^{-2} \approx 5.6 \times 10^{15} \text{ m s}^{-2}$$
 [1]

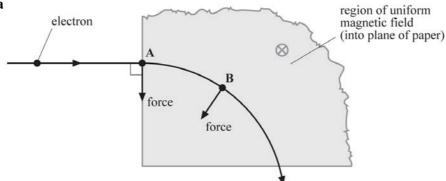
c From circular motion, the centripetal acceleration *a* is given by:

$$a = \frac{v^2}{r}$$

$$r = \frac{v^2}{a} = \frac{(8.0 \times 10^6)^2}{5.63 \times 10^{15}}$$
 [1]

$$r = 1.14 \times 10^{-2} \text{ m} \approx 1.1 \times 10^{-2} \text{ m} (1.1 \text{ cm})$$
 [1]

5 a



Both arrows at **A** and **B** are towards the centre of the circle. [1]

- **b** The force on the electron is at 90° to the velocity. Hence the path described by the electron is a circle. [1]
- **c** The magnetic force provides the centripetal force. [1]

Therefore:
$$BQv = \frac{mv^2}{r}$$
 [1]

$$BQ = \frac{mv}{r} \text{ or } v = \frac{BQr}{m}$$
 [1]

$$v = \frac{2.0 \times 10^{-3} \times 1.6 \times 10^{-19} \times 5.0 \times 10^{-2}}{9.1 \times 10^{-31}}$$
 [1]

$$v = 1.76 \times 10^7 \,\mathrm{m \, s^{-1}} \approx 1.8 \times 10^7 \,\mathrm{m \, s^{-1}}$$
 [1]

d
$$v = \frac{BQr}{m}$$
, so the speed v is directly proportional to the radius r . [1]

Radius is halved, so
$$v = \frac{1.76 \times 10^7}{2} = 8.8 \times 10^6 \,\text{m s}^{-1}$$
 [1]

6 **a**
$$E_k = 15 \times 10^3 \times 1.6 \times 10^{-19} = 2.4 \times 10^{-15} \text{ J (1 eV} = 1.6 \times 10^{-19} \text{ J)}$$
 [1]
$$\frac{1}{2} mv^2 = 2.4 \times 10^{-15}$$

$$v = \sqrt{\frac{2 \times 2.4 \times 10^{-15}}{1.7 \times 10^{-27}}}$$
 [1]

$$v = 1.68 \times 10^6 \text{ m s}^{-1} \approx 1.7 \times 10^6 \text{ m s}^{-1}$$
 [1]

$$\mathbf{b} \quad F = ma = \frac{mv^2}{r} \tag{1}$$

$$F = \frac{1.7 \times 10^{-27} \times (1.68 \times 10^6)^2}{0.05}$$
 [1]

$$F = 9.60 \times 10^{-14} \,\mathrm{N} \approx 9.6 \times 10^{-14} \,\mathrm{N}$$
 [1]

$$\mathbf{c} \quad F = BQv \tag{1}$$

$$B = \frac{F}{Ov} = \frac{9.60 \times 10^{-14}}{1.6 \times 10^{-19} \times 1.68 \times 10^{6}}$$
 [1]

$$B \approx 0.36 \text{ T}$$

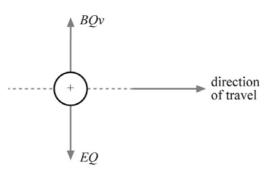
d speed = $\frac{\text{distance}}{\text{time}}$

time =
$$\frac{\text{circumference}}{\text{speed}} = \frac{2\pi \times 0.05}{1.68 \times 10^6}$$
 [1]

time =
$$1.87 \times 10^{-7} \text{ s} \approx 1.9 \times 10^{-7} \text{ s}$$
 [1]

[1]

7 a In order for the positively charged ions to emerge from the slit, the net force perpendicular to the velocity must be zero.



electrical force on ion = magnetic force on ion [1]

$$EQ = BQv ag{1}$$

The charge *Q* cancels.

$$[1]$$

The electric field strength is $E = \frac{V}{d}$. Therefore, the magnetic flux density is:

$$B = \frac{E}{v} = \frac{V/d}{v} = \frac{(5.0 \times 10^3)/0.024}{6.0 \times 10^6}$$
 [1]

$$B = 3.47 \times 10^{-2} \text{ T} \approx 35 \text{ mT}$$
 [1]

$$\mathbf{b} \quad v = \frac{BQr}{m} \quad \text{so} \quad r = \frac{mv}{BQ}$$

$$\Delta r = \frac{(m_1 - m_2) v}{BQ} \tag{1}$$

8 a The centripetal force is provided by the magnetic force. [1]

Therefore:
$$Bev = \frac{mv^2}{r}$$
 [1]

$$Be = \frac{mv}{r}$$
 or $v = \frac{Ber}{m}$ [1]

$$T = \frac{r}{\text{circumference}} = \frac{m}{Ber/m}$$
 [1]

The radius r of the orbit cancels. Hence: $T = \frac{2\pi m}{Be}$

The time
$$T$$
 is independent of both the radius of the orbit r and the speed v . [1]

b The faster electron travels in a circle of larger radius. [1]