

TUTORIAL ANSWERS WORK ENERGY POWER

Question 1

$$\begin{aligned}\text{Mechanical power} &= mgh / \text{time} = (400)(9.81)(1200) / (2 \times 60) \\ &= 39\,240 \text{ W}\end{aligned}$$

$$\text{Efficiency} = (P_{\text{output}} / P_{\text{input}}) \times 100\%$$

This case P_{out} is the mechanical power & P_{input} is the electrical power.

$$80\% = (39\,240 / P_{\text{input}}) \times 100\%$$

$$P_{\text{input}} = 49\,050 \text{ W} = \underline{50 \text{ kW}}$$

(Answer: D)

Question 2

Since mass M moved down a distance x , mass m has also moved up a distance x on the rough plane. Hence, work done against the frictional force is F_x . Thus, F_x is eventually the amount of heat generated by friction in this process. (Answer: A)

Question 3

By definitions power is also equals to Fv .

By using $F = ma$, total force applied to the body is

$$(F - mg \sin\theta) = ma$$

$$F = ma + mg \sin\theta$$

$$\text{Power} = Fv = (ma + mg \sin\theta)v = \underline{mav + mgv \sin\theta}$$

(Answer: C)

Question 4

Since air resistance is negligible, by conservation of energy, loss in K.E. is equal to the gain in G.P.E and vice versa. Thus answer is C

Question 5

Assume the body has mass m kg and the constant force applied is F N.

$$\text{Power} = Fv; \quad v = u + at; \quad v = at, \text{ since } u = 0.$$

$$\text{Power} = F(at); \quad a = F/m$$

$$\text{Power} = F(F/m)(t) = (F^2/m)t$$

Since F and m are constant, thus power is directly proportional to t . (Answer: E)

Question 6

Assuming air resistance is negligible, the gain in K.E. of system = loss in P.E. of system

$$\begin{aligned}\text{Gain in K.E. system} &= \text{Loss in P.E. of Y} - \text{Gain in P.E. of X} \\ &= (5 \times 9.81)(2.0) - (4 \times 9.81)(2.0 \sin 30^\circ) \\ &= 58.86 \text{ N} = \mathbf{59 \text{ N}} \quad (\text{Answer: B})\end{aligned}$$

Question 7

Total work done = $80 \times 10 = 800 \text{ J}$

Work done against friction = $60 \times 10 = \mathbf{600 \text{ J}}$ (thermal energy)

Work done converted to K.E = $800 - 600 = \mathbf{200 \text{ J}}$ (Answer: C)

Question 8

$$\text{K.E.} = \frac{1}{2} mv^2$$

Since object falling with constant speed,

$$mg = kv$$

$$v = mg / k$$

$$\text{K.E.} = \frac{1}{2} m(mg / k)^2 = \mathbf{m^3 g^2 / 2k^2} \quad (\text{Answer: D})$$

Question 9

K.E. will be constant and equal to $\frac{1}{2} mv^2$, since the velocity is constant.

P.E. will decrease at a rate of $= mg\Delta h / \Delta t$, and $v = (\Delta h / \Delta t)$

$$= mgv$$

So answer is A

Question 10

Power generated by the dynamo, at any instant, is given by the slope of the energy-time curve. From the graph, it is obvious that maximum power occurs during time interval from 2 to 3 seconds since the portion of graph (straight line) has the largest gradient.

$$\text{Max. power} = (0.4 - 0.1) / (3 - 2) = \mathbf{0.30 \text{ W}} \quad (\text{Answer: C})$$

Question 10

$$P_{\text{out}} / P_{\text{in}} \times 100\% = 40\%$$

$$1000 \text{ M} / P_{\text{in}} \times 100\% = 40\%$$

$$P_{\text{in}} = \mathbf{2500 \text{ MW}}$$

$$\text{Wasted power} = 2500 \text{ M} - 1000 \text{ M} = \mathbf{1500 \text{ MW}} \quad (\text{Answer: D})$$

Question 11

$$P_{\text{out}} / P_{\text{in}} \times 100\% = 40\%$$

$$1000 \text{ M} / P_{\text{in}} \times 100\% = 40\%$$

$$P_{\text{in}} = \mathbf{2500 \text{ MW}}$$

Question 12

$$\text{Power} = \text{Energy} / \text{time}$$

$$= mgs \sin\theta / t, v = s/t$$

$$= \mathbf{mgv \sin\theta \text{ (Answer: B)}}$$

Question 13

$$\text{Total force developed by motor} = (1000 + (1000 \times 9.81)) = 10\,810 \text{ N}$$

$$\text{Power} = Fv = (10\,810)(0.5) = 5\,405 \text{ W} = \mathbf{5.5 \text{ kW} \quad (\text{Answer: B})}$$