1. Find the integral of $\frac{5}{8}e^{4t}(2t^2+t+3)$ with respect to t.

$$\bigcirc \frac{5}{16} e^{4t} t^2 + \frac{5}{16} e^{4t} t + \frac{15 e^{4t}}{32}$$
+ constant

$$\bigcirc \frac{25}{32} e^{4t} t + \frac{5 e^{4t}}{32} + \text{constant}$$

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$$\frac{5}{192} e^{4t} t (4 t^2 + 3 t + 18) + constant$$

2. Find the integral: $\int_{\frac{9}{2}}^{\frac{9}{2}} e^{-2x} (x^2 + x + 1)$ dx.

$$-\frac{9}{4} e^{-2x} X^2 - \frac{27}{4} e^{-2x} X - \frac{27 e^{-2x}}{4}$$
+ constant

$$-\frac{9}{4}e^{-2x}X^2 - \frac{9}{2}e^{-2x}X - \frac{9e^{-2x}}{2}$$
+constant

$$\bigcirc -\frac{9}{4}e^{-2x}X^2 + constant$$

$$\bigcirc -\frac{3}{8} e^{-2x} x \left(2 x^2 + 3 x + 6\right)$$
+ constant

Difficulty level: Intermediate

3. What is $\int_{\frac{3}{5}}^{\frac{3}{5}} (2t^2 + t + 4) \cos(2t) dt$?

- $\frac{3}{5}t^{2}\sin(2t) + \frac{3}{10}t\sin(2t) + \frac{3}{2}\sin(2t) \frac{3}{5}t\cos(2t) \frac{3}{20}\cos(2t) + \text{constant}$
- $\bigcirc \frac{1}{20} t (4 t^2 + 3 t + 24) \sin(2 t)$ + constant
- $\frac{3}{5}t^2\sin(2t) + \frac{3}{10}t\sin(2t) + \frac{9}{10}\sin(2t) + \frac{3}{5}t\cos(2t) + \frac{3}{20}\cos(2t) + \cosh 2t$

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$$\frac{6}{5}t\sin(2t) + \frac{3\cos^{2}(t)}{10} + \frac{3}{5}t\cos(2t) + constant$$

4. Integrate $\frac{4}{5} \left(2 t^2 + 2 t + 2\right) \sin(t)$ with respect to t.

$$-\frac{8}{5}t^2\cos(t) + \frac{16}{5}t\sin(t) + \frac{8\sin(t)}{5} - \frac{8}{5}t\cos(t) + \frac{8\cos(t)}{5} + \text{constant}$$

- $\bigcirc \frac{16}{5}t\sin(t) + \frac{8\sin(t)}{5} \frac{16}{5}t\cos(t) + \frac{8\cos(t)}{5} + \text{constant}$
- $\bigcirc -\frac{4}{15}t(2t^2+3t+6)\cos(t)$ +constant

 $-\frac{8}{5}t^{2}\cos(t) - \frac{16}{5}t\sin(t) - \frac{8\sin(t)}{5} - \frac{8}{5}t\cos(t) - \frac{24\cos(t)}{5} + \text{constant}$

ANSWER KEY

5. Find the integral of $\frac{5}{9} e^t \cos(2t)$ with respect to t.

- $\bigcirc \frac{5}{18} e^t \sin(2t) + \text{constant}$
- $\bigcirc \frac{1}{3} e^t \sin(2t) \frac{1}{9} e^t \cos(2t)$ + constant
- $\bigcirc \frac{1}{6} e^t \sin(2t) + \frac{2}{9} e^t \cos(2t)$ + constant

6. What is
$$\int_{2}^{1} e^{-2x} x^{3} dx$$
?

$$\bigcirc -\frac{9}{8} e^{-2x} X^2 - \frac{3}{8} e^{-2x} X - \frac{3 e^{-2x}}{16}$$
+ constant

$$-\frac{1}{4}e^{-2X}X^3 + \frac{3}{8}e^{-2X}X^2 + \frac{3}{8}e^{-2X}X + \frac{3}{16}e^{-2X}X + \frac{3}{16}$$

$$\bigcirc -\frac{1}{16} e^{-2X} X^4 + constant$$

$$-\frac{1}{4}e^{-2x}X^3 - \frac{3}{8}e^{-2x}X^2 - \frac{3}{8}e^{-2x}X - \frac{3}{16}e^{-2x} + \text{constant}$$

ANSWER KEY

- 7. What is $\int_{\frac{8}{7}}^{\frac{8}{7}} e^t \sin(2t) dt$?
 - - $\bigcirc -\frac{8}{35} e^t \sin(2t) \frac{24}{35} e^t \cos(2t)$ +constant
 - $\bigcirc \frac{16}{35} e^t \sin(2t) \frac{12}{35} e^t \cos(2t)$ + constant
 - $\bigcirc -\frac{4}{7} e^t \cos(2t) + \text{constant}$

- 8. Find the integral: $\int_{0}^{2} t^{3} \cos(t) dt$.
 - $\frac{2}{9}t^3\sin(t) + \frac{2}{3}t^2\cos(t) \frac{4}{3}t\sin(t) \frac{4\cos(t)}{3} + \text{constant}$
 - $\bigcirc \frac{1}{18} t^4 \sin(t) + \text{constant}$
 - $\bigcirc \frac{2}{3}t^2\sin(t) + \frac{2}{3}t^2\cos(t) \frac{4}{3}t\sin(t) \frac{4\cos(t)}{3} + \text{constant}$

- **9.** What is $\int_{3}^{2} t^{4} \sin(2t) dt$?
 - $\bigcirc -\frac{1}{15}t^5\cos(2t) + constant$

$$-\frac{1}{3}t^{4}\cos(2t) + \frac{2}{3}t^{3}\sin(2t) +$$

$$t^{2}\cos(2t) - t\sin(2t) -$$

$$\frac{1}{2}\cos(2t) + constant$$

- $-\frac{1}{3}t^{4}\cos(2t) \frac{2}{3}t^{3}\sin(2t) t^{2}\cos(2t) + t\sin(2t) + \frac{1}{2}\cos(2t) + constant$
- $-\frac{1}{3}t^{4}\cos(2t) + \frac{4}{3}t^{3}\sin(2t) + 2t^{2}\cos(2t) 2t\sin(2t) \cos(2t) + constant$

10. Find the integral: $\int_{\frac{7}{4}}^{7} (t^2 + 3t + 1) \sin(3t) dt$.

$$-\frac{7}{12}t^{2}\cos(3t) + \frac{7}{18}t\sin(3t) + \frac{7}{12}\sin(3t) - \frac{7}{4}t\cos(3t) - \frac{49}{108}\cos(3t) + \text{constant}$$

$$-\frac{7}{72}t(2t^2+9t+6)\cos(3t)$$

$$\frac{7}{18} t \sin(3t) + \frac{7}{12} \sin(3t) - \frac{7}{6} t \cos(3t) - \frac{175}{108} \cos(3t) + \text{constant}$$

$$-\frac{7}{12}t^{2}\cos(3t) - \frac{7}{18}t\sin(3t) - \frac{7}{12}\sin(3t) - \frac{7}{4}t\cos(3t) - \frac{77}{108}\cos(3t) + \cosh t$$

11. Find the integral of $\frac{5}{6}e^{x}\cos(x)$ with respect to x.

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$$\frac{5}{3} e^X \sin(x) - \frac{5}{6} e^X \cos(x) + \text{constant}$$

 $\bigcirc \quad \frac{5}{4} e^X \sin(X) - \frac{5}{12} e^X \cos(X)$

+constant

- $\bigcirc \frac{5}{6} e^X \sin(x) + \text{constant}$

12. Find the integral: $\int_{\frac{4}{9}}^{\frac{4}{9}} x^3 \sin(3x) dx$.

$$\bigcirc -\frac{1}{27} x^4 \cos(3 x) + \text{constant}$$

$$-\frac{4}{27} x^3 \cos(3 x) + \frac{4}{27} x^2$$

$$\sin(3 x) - \frac{8}{243} \sin(3 x) + \frac{8}{81} x \cos(3 x) + \text{constant}$$

$$\frac{4}{27} x^2 \sin(3 x) - \frac{4}{9} x^2 \cos(3 x) - \frac{8}{243} \sin(3 x) + \frac{8}{81} x \cos(3 x) + \text{constant}$$

ANSWER KEY

13. What is $\int_{-4}^{5} t \ln(2t) dt$?

- $\bigcirc \frac{5}{8} t^2 \ln(2 t) + \frac{5 t^2}{16} + constant$
- $\bigcirc \frac{5}{8}t^3(\log(2t)-1) + \text{constant}$
- $\frac{5}{8}t^2\ln(2t) \frac{5t^2}{16} + \text{constant}$
- \bigcirc $\frac{5}{8}t^2\ln(2t) \frac{5t^2}{8} + constant$

14. Find the integral: $\int \frac{8}{9} t^4 \cos(t) dt$.

$$\bigcirc \frac{8}{9} t^4 \sin(t) - \frac{32}{9} t^3 \cos(t) + \frac{32}{3} t^2 \sin(t) - \frac{64 \sin(t)}{3} + \frac{64}{3} t \cos(t) + \text{constant}$$

$$\frac{32}{9} t^3 \sin(t) +$$

$$\frac{32}{9} t^3 \cos(t) - \frac{32}{3} t^2 \sin(t) +$$

$$\frac{64 \sin(t)}{3} - \frac{64}{3} t \cos(t) + \text{constant}$$

$$\bigcirc \frac{8}{45} t^5 \sin(t) + \text{constant}$$

ANSWER KEY

15. Find the integral of $\frac{4}{7}(x^2 + 3x + 1)$ $\sin(4x)$ with respect to x.

$$\bigcirc -\frac{1}{42} x \left(2 x^2 + 9 x + 6\right) \cos(4 x)$$
+ constant

$$-\frac{1}{7}x^{2}\cos(4x) + \frac{1}{14}x\sin(4x) + \frac{3}{28}\sin(4x) - \frac{3}{7}x\cos(4x) - \frac{1}{8}\cos(4x) + constant$$

$$-\frac{1}{7}x^{2}\cos(4x) - \frac{1}{14}x\sin(4x) - \frac{3}{28}\sin(4x) - \frac{3}{7}x\cos(4x) - \frac{9}{56}\cos(4x) + \text{constant}$$

$$-\frac{1}{14} x \sin(4 x) - \frac{3}{28} \sin(4 x) - \frac{2}{7} x \cos(4 x) - \frac{25}{56} \cos(4 x) + \text{constant}$$

16. Find the integral: $\int_{\frac{2}{5}}^{2} e^{-x} (x^2 + 2x + 2) dx$.

$$\bigcirc \frac{4e^{-x}}{5} - \frac{2}{5}e^{-x}X^2 + constant$$

+constant

$$\bigcirc \frac{4e^{-x}}{5} + constant$$

 \bigcirc

$$-\frac{2}{15}e^{-x}x(x^2+3x+6)$$
 + constant

17. Find the integral of $\frac{5}{9} x^3 \sin(2 x)$ with respect to x.

$$-\frac{5}{18} x^3 \cos(2 x) +$$

$$\frac{5}{12} x^2 \sin(2 x) - \frac{5}{24} \sin(2 x) +$$

$$\frac{5}{12} x \cos(2 x) + \text{constant}$$

$$-\frac{5}{18}x^{3}\cos(2x) - \frac{5}{12}x^{2}\sin(2x) + \frac{5}{24}\sin(2x) - \frac{5}{12}x\cos(2x) + constant$$

$$\bigcirc -\frac{5}{72} x^4 \cos(2 x) + \text{constant}$$

18. Integrate $\frac{1}{2} e^{-3t} t^3$ with respect to t.

$$-\frac{1}{6}e^{-3t}t^3 - \frac{1}{6}e^{-3t}t^2 - \frac{1}{9}e^{-3t}t - \frac{e^{-3t}}{27} + constant$$

$$\bigcirc -\frac{1}{24}e^{-3t}t^4 + \text{constant}$$

$$-\frac{1}{6} e^{-3t} t^3 + \frac{1}{6} e^{-3t} t^2 + \frac{1}{9} e^{-3t} t + \frac{e^{-3t}}{27} + \text{constant}$$

ANSWER KEY

19. Integrate $\frac{2}{5} e^X \sin(x)$ with respect to x.

$$\bigcirc -\frac{2}{5} e^X \cos(X) + \text{constant}$$

$$\bigcirc -\frac{2}{5} e^{x} \sin(x) - \frac{4}{5} e^{x} \cos(x)$$

+constant

$$\bigcirc -\frac{1}{5} e^X \sin(X) - \frac{3}{5} e^X \cos(X)$$
+ constant

20. Integrate $\frac{5}{6}t^3 \ln(4t)$ with respect to t.

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$$\frac{5}{24} t^4 \ln(4 t) - \frac{5 t^4}{96} + \text{constant}$$

$$\bigcirc \frac{5}{24} t^4 \ln(4 t) + \frac{5 t^4}{96} + constant$$

$$\bigcirc \frac{5t^3}{24} - \frac{5t^4}{96} + constant$$

$$\bigcirc \frac{5}{24} t^5 (\log(4t) - 1) + \text{constant}$$