Oxford Physics Aptitude Test (PAT) 2008 Solutions

Maths

$$\frac{1}{1}$$
 $1+2+3+...+99+100 = \frac{n}{2}(n+1) = \frac{100}{2}(101) = \frac{5050}{2}$

$$\frac{2}{2}(0.25)^{-1/2} = \left(\frac{1}{4}\right)^{-1/2} = (4)^{1/2} = 2$$

$$(0.09)^{3/2} = (0.3)^3 = 0.027$$

$$\frac{3}{3}\left(1+x\right)^{m+1}\left(1-2x\right)^{m} \approx \left[1+(m+1)x+\frac{(m+1)(m)x^{2}}{2}\right]\left[1-2mx+\frac{1+m(m-1)x^{2}}{2}\right]$$

$$=1+(m+1-2m)x+\left(2m^{2}-2m-2m^{2}-2m+\frac{m^{2}}{2}+\frac{m}{2}\right)x^{2}$$

$$=1+\left(1-m\right)x+\left(\frac{m^{2}-2m}{2}\right)x^{2}$$

5) i)
$$\log_2 q = \frac{\log_4 q}{\log_4 2} = \frac{1}{2}$$

11)
$$\log_{3} 3 = \frac{\log_{3} 3}{\log_{3} 8} = \frac{1/2}{\log_{3}(2)^{3}} = \frac{1}{2} \cdot \frac{1}{3\log_{3} 2} = \frac{1}{62}$$

$$(2x+1)(x-1)=0$$

$$x = -\frac{1}{2}$$
 or 1

$$\frac{7}{7}$$
 $y = x + \frac{x^2}{2} + \frac{x^3}{3} + \cdots$

$$x^{2} + \cdots \qquad m = a$$

When
$$x = 0$$
, $\frac{dy}{dx} = 1 \implies \alpha = 1$

$$\frac{1}{\sqrt{2}} = \frac{1}{1 - 1/4} = \frac{4}{3} \implies a = \frac{4}{3}$$

8) Centre = mid-point =
$$\left(\frac{S-3}{2}, \frac{8+2}{2}\right) = (1, 5)$$

Radius,
$$r = \sqrt{(5-1)^2 + (2-5)^2}$$

$$r^2 = 25$$

$$\Rightarrow$$
 $(x-1)^2 + (y-5)^2 = 25$

$$P(2) = \frac{1}{9}, P(3) = \frac{1}{9}, P(4) = \frac{1}{9}, P(5) = \frac{3}{9}, P(6) = \frac{3}{9}$$
i) $\frac{1}{9}$

$$P(S)(0) = P(4,6) + P(S,S) + P(S,6) + P(6,4) + P(6,5) + P(6,6)$$

$$= \left(\frac{1}{9} \times \frac{3}{9}\right) + \left(\frac{3}{9} \times \frac{3}{9}\right) + \left(\frac{3}{9}$$

$$r^{2} = a^{2} + a^{2} = 2a^{2}$$

$$d^{2} = a^{2} + r^{2} = 3a^{2}$$

$$d^{3} = \sqrt{3}a$$

1) 1)
$$\int_{-1}^{1} (x + x^3 + x^5 + x^7) dx = \left[\frac{x^2}{2} + \frac{x^4}{4} + \frac{x^6}{6} + \frac{z^8}{8} \right]_{-1}^{1}$$

$$\frac{11}{11} \int_{0}^{1} \frac{x^{9} + x^{99}}{11} dx = \frac{1}{11} \left[\frac{x^{10}}{10} + \frac{x^{100}}{100} \right]_{0}^{1} = \frac{0 - 11}{11}$$

A ABC =
$$\frac{1}{2}x^2 \sin 60 = \frac{\sqrt{3}}{4}x^2$$

Sin $60 = \frac{x}{2} \cdot \frac{1}{5}$

The second cycle, $A_1 = 1$

A real of smill cycle, $A_1 = 1$

Area of small circle,
$$A_1 = \Pi r_1^2 = \frac{\Pi x^2}{3}$$

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Area of big circle,
$$A_{2} = \Pi \left(x + r_{1} \right)^{2} = \Pi x^{2} \pm \frac{x^{2} \Pi}{3} + \frac{2 x^{2} \Pi}{\sqrt{3}}$$

$$= 2 \pi x^{2} \left(\frac{2 + \sqrt{3}}{3} \right)$$

$$PE A_{ADEC} = \frac{240}{360} \left(A_2 - A_1 \right)$$

$$= \frac{2}{3} \left(2\pi x^2 \left(\frac{2+\sqrt{3}}{3} \right) - \frac{\pi x^2}{3} \right)$$

$$= \frac{2\pi x^2}{9} \left(4 + 2\sqrt{3} - 1 \right) = \frac{2\pi x^2}{9} \left(3 + 2\sqrt{3} \right)$$

$$\frac{A_{ABC}}{A_{ABC}} = \frac{2\pi x^{2}}{9} \left(3 + 2\sqrt{3}\right) \div \frac{\sqrt{3}}{4} x^{2}$$

$$= \frac{8\pi (3 + 2\sqrt{3})}{9\sqrt{3}} = \frac{8\pi (\sqrt{3} + 2)}{9}$$

Physics

13)
$$\frac{1.5m}{20g} \propto \frac{20g(1.5) = 30g \times 20g(1.5)}{20g} \times \frac{30g}{20g} \times \frac{1.5m}{20g} \times \frac{30g}{20g} \times \frac{1.5m}{20g} \times \frac{30g}{20g} \times \frac{1.5m}{20g} \times \frac{30g}{20g} \times \frac{1.5m}{20g} \times \frac{30g}{20g} \times \frac{30g}{20g}$$

$$z = 1m$$

Ans: D

... She must sit 1-5+1=2.5 many

- It Energy released comes from the decrease mass. Ans: B
- 15) M = 2 x 1030 x 2 50 x 109 x 400 x 109 x 21 = 20x104x21x1048 = 4,2x1034kg Ans: D
- 16) Moon between the Earth and the sun. Ans: A

17)
$$g = \frac{m}{\sqrt{2}} = \frac{m}{\sqrt{2}$$

$$W = \frac{2^2}{2C} = \frac{C^2V^2}{2C} = \frac{CV^2}{2} = \frac{PAV^2}{2d}$$

For
$$\rho = 2 \times 10^{-11} \text{ Fm}^{-1}$$
, $\beta = 2 \times 10^{3} \text{ Vm}^{-1}$, $D = 10000 \text{ kg}^{-1} \text{ milky}$;

$$|E_{\text{max}}| = \frac{|X \times 2 \times 10^{3}| \times (2 \times 10^{3})^{2}}{2 \times 1000} = \text{Lt} \text{ J}$$

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$$|E_{\text{max}}| = \frac{|X \times 10^{3}| \times (2 \times 10^{3})^{2}}{2 \times 10$$

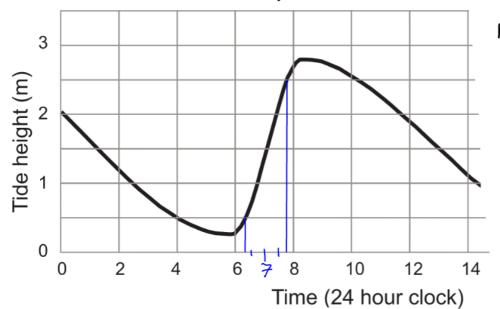
(3) in (1):
$$r = 2(1-2i)-c = 2-5c$$

In (2): $c^2 + (1-2i)^2 = (2-5c)^2$
 $c^2 + 1 - 4c + 4c^2 = 4 - 20c + 25c^2$
 $0 = 20c^2 - 16c + 3$
 $= (10c - 3)(2c - 1)$
 $c = \frac{3}{10}$ or $\frac{1}{2}$

From (3), c cannot be $\frac{1}{2}$, as this would give 5=0

c = 0.3m, S = 0.4m, r = 0.5m

26) most rapid change is when the gradient is the steepest >> Zam



$$m = \frac{\Delta h}{\Delta t} = \frac{250 - 50}{105 - 15}$$

= 2.2 cm/min

$$27$$
 $\frac{18m}{2}$
 2π
 $18m$
 $2 = 18m$

$$+ \alpha 45 = \frac{2}{18}$$

$$2 = 18$$

a) 5=20m, u=0, v=x, a=lom5-2, t=? thre 5=ut + = at2 20= 5t2 t = 2s

b)
$$V^2 = u^2 + 2as$$

 $V = \sqrt{2 \times 10 \times 20} = 28 \text{ ms}^{-1}$

c)
$$\frac{1}{2}$$
 mu² = Fd
 $F = \frac{0.5 \times 0.02 \times 20^{2}}{1 \times 10^{-3}} = 4 \text{ kN}$

$$ft = mv - mu$$

 $t = 8.02(0-20) = \frac{1}{200} = 5ms$

9)
$$E_{min} \times efficiency = mc \Delta T$$

 $efficiency = \frac{0.02 \times 4 \times 10^3 \times 80}{2 \times 10^4} = 32 \times 10^{-2}$
 $= 32\%$