

Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

```
svn co https://github.com/gadepall/school/trunk/
control/codes
```

1 SIGNAL FLOW GRAPH

1.1 Mason's Gain Formula

1.2 Matrix Formula

2 BODE PLOT

2.1 Introduction

2.2 Example

3 SECOND ORDER SYSTEM

3.1 Damping

3.2 Example

3.3 Peak Overshoot

3.3.1. Find the peak overshoot for the second order control system given by:

$$G(S) = \frac{100}{s^2 + 10s + 100} \quad (3.3.1.1)$$

Solution: Peak overshoot (M_p) is defined as the deviation of the response at peak time from the final value of response.

$$\Rightarrow M_p = c(t_p) - c(\infty) \quad (3.3.1.2)$$

Given,

$$G(S) = \frac{C(s)}{R(s)} = \frac{100}{s^2 + 10s + 100} \quad (3.3.1.3)$$

To calculate the unit step response,

$$r(t) = 1 \Rightarrow R(s) = \frac{1}{s} \quad (3.3.1.4)$$

$$\Rightarrow C(S) = \frac{100}{(s)(s^2 + 10s + 100)} \quad (3.3.1.5)$$

$C(s)$ can be expanded as:

$$C(s) = \frac{1}{s} - \frac{s+5}{(s+5)^2 + 75} - \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{75}}{(s+5)^2 + 75} \quad (3.3.1.6)$$

In time domain,

$$c(t) = \mathcal{L}^{-1}C(s) \quad (3.3.1.7)$$

$$\Rightarrow c(t) = 1 - e^{-5t} \cos(\sqrt{75}t) - \frac{e^{-5t}}{\sqrt{3}} \sin(\sqrt{75}t) \quad (3.3.1.8)$$

From (3.3.1.8):

$$\lim_{t \rightarrow \infty} c(t) = 1 \quad (3.3.1.9)$$

At t_p , $c(t)$ is maximum:

$$\Rightarrow \frac{dc(t)}{d(t)} = 0 \quad (3.3.1.10)$$

Applying this condition on (3.3.1.8), we get:

$$t_p = \frac{\pi}{\sqrt{75}} \quad (3.3.1.11)$$

Substitute t_p in (3.3.1.8) to get $c(t_p)$:

$$c(t_p) = 1 + e^{\frac{-\pi}{\sqrt{3}}} \Rightarrow c(t_p) = 1.163 \quad (3.3.1.12)$$

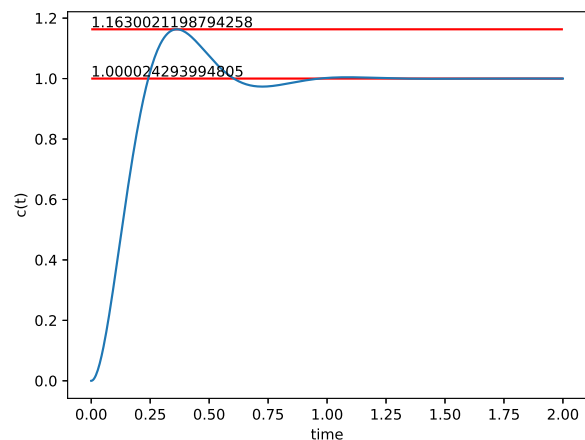
Substitute $c(t_p)$ and $c(\infty)$ in (3.3.1.2) to get peak overshoot:

$$M_p = 1.163 - 1 = 0.163 \quad (3.3.1.13)$$

3.3.2. Verify using a Python Plot

Solution:

```
codes/ee18btech11045.py
```



4 ROUTH HURWITZ CRITERION

4.1 *Routh Array*

4.2 *Marginal Stability*

4.3 *Stability*

4.4 *Example*

5 STATE-SPACE MODEL

5.1 *Controllability and Observability*

5.2 *Second Order System*

5.3 *Example*

5.4 *Example*

5.5 *Example*

6 NYQUIST PLOT

7 COMPENSATORS

7.1 *Phase Lead*

7.2 *Example*

8 GAIN MARGIN

8.1 *Introduction*

8.2 *Example*

9 PHASE MARGIN

10 OSCILLATOR

10.1 *Introduction*

10.2 *Example*