Subject: Machine Learning Lab

Experiment No.: 04

Title: Write a program to implement of logistic regression.

Objectives: To learn logistic regression

Theory:

Logistic regression is a method for classifying data into discrete outcomes. For example, we might use logistic regression to classify an email as spam or not spam. Logistic regression is a statistical model that in its basic form uses a logistic function to model a binary dependent variable, although many more complex extensions exist. In regression analysis, logistic regression (or logit regression) is estimating the parameters of a logistic model (a form of binary regression). Mathematically, a binary logistic model has a dependent variable with two possible values, such as pass/fail which is represented by an indicator variable, where the two values are labeled "0" and "1". In the logistic model, the log-odds (the logarithm of the odds) for the value labeled "1" is a linear combination of one or more independent variables ("predictors"); the independent variables can each be a binary variable (two classes, coded by an indicator variable) or a continuous variable (any real value). The corresponding probability of the value labeled "1" can vary between 0 (certainly the value "0") and 1 (certainly the value "1"), hence the labeling; the function that converts log-odds to probability is the logistic function, hence the name. The unit of measurement for the log-odds scale is called a logit, from logistic unit, hence the alternative names. Analogous models with a different sigmoid function instead of the logistic function can also be used, such as the probit model; the defining characteristic of the logistic model is that increasing one of the independent variables multiplicatively scales the odds of the given outcome at a constant rate, with each independent variable having its own parameter; for a binary dependent variable this generalizes the odds ratio.

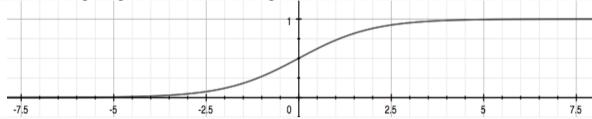
Hypothesis Representation

We could approach the classification problem ignoring the fact that y is discrete-valued, and use our old linear regression algorithm to try to predict y given x. However, it is easy to construct examples where this method performs very poorly. Intuitively, it also doesn't make sense for $h_{\theta}(x)$ to take values larger than 1 or smaller than 0 when we know that $y \in \{0, 1\}$. To fix this, let's change the form for our hypotheses $h_{\theta}(x)$ to satisfy $0 \le h_{\theta}(x) \le 1$. This is accomplished by plugging $\theta^T.x$ into the Logistic Function.

Our new form uses the "Sigmoid Function," also called the "Logistic Function":

$$h_{\theta}(\mathbf{x}) = \mathbf{g}(\theta^{T}.\mathbf{x})$$
$$\mathbf{z} = \theta^{T}.\mathbf{x}$$
$$g(\mathbf{z}) = \frac{1}{1 + e^{-\mathbf{z}}}$$

The following image shows us what the sigmoid function looks like:



The function g (z), shown here, maps any real number to the (0, 1) interval, making it useful for transforming an arbitrary-valued function into a function better suited for classification.

 $h_{\theta}(\mathbf{x})$ will give us the **probability** that our output is 1. For example $h_{\theta}(\mathbf{x}) = 0.7$ gives us a probability of 70% that our output is 1. Our probability that our prediction is 0 is just the complement of our probability that it is 1 (e.g. if probability that it is 1 is 70%, then the probability that it is 0 is 30%).

$$h_{\theta}(\mathbf{x}) = P(y=1|x;\theta) = 1 - P(y=0|x;\theta)$$

$$P(y=0 | x; \theta) + P(y=1|x; \theta) = 1$$

Hypothesis Function

- Hypothesis Function for Logistic regression is,
- $h_{\theta}(x) = g((\theta^T x))$

$$h_{\Theta}(x) = \frac{1}{1 + e^{-\Theta^{T}x}}$$

i.e.

Cost Function

• Cost Function for Logistic regression is

$$J(\theta) = -\frac{1}{m} \left[\sum_{i=1}^{m} y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log (1 - h_{\theta}(x^{(i)})) \right]$$

Gradient Descent

• Gradient Descent Function for logistic regression is

Repeat
$$\{$$

$$\theta_j := \theta_j - \alpha \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)}$$
 $\}$ (simultaneously update all θ_j)

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Algorithm-

- 1] Import all necessary libraries.
- 2] Read data set into pandas dataframe
- 3] Use train_test_split function to split dataset into training set and testing set.
- 4] Create logistic regression object using linear model
- 4] Train model using fit function
- 5] Use build model for prediction